NYCU Pattern Recognition, Homework 3

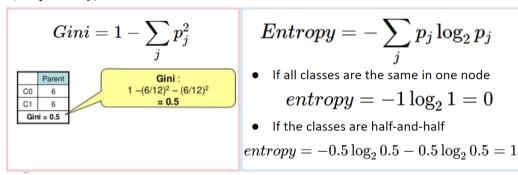
Deadline: May 4, 23:59

Part. 1, Coding (80%):

In this coding assignment, you need to implement the Decision Tree, AdaBoost and Random Fores t algorithm by using only NumPy, then train your implemented model by the provided dataset and test the performance with testing data. Find the sample code and data on the GitHub page https://github.com/NCTU-VRDL/CS AT0828/tree/main/HW3

Please note that only <u>NumPy</u> can be used to implement your model, you will get no points by sim ply calling sklearn.tree.DecsionTreeClassifier.

1. (5%) Gini Index or Entropy is often used for measuring the "best" splitting of the data. Please compute the Entropy and Gini Index of this array np.array([1,2,1,1,1,1,2,2,1,1,2]) by the for mula below. (More details on page 5 of the hw3 slides, 1 and 2 represent class1 and class 2, respectively)



2. (10%) Implement the Decision Tree algorithm (CART, Classification and Regression Tree s) and train the model by the given arguments, and print the accuracy score on the test dat a. You should implement two arguments for the Decision Tree algorithm, 1) Criterion: The function to measure the quality of a split. Your model should support "gini" for the Gin

i impurity and "entropy" for the information gain.

- 2) **Max_depth**: The maximum depth of the tree. If Max_depth=None, then nodes are expan ded until all leaves are pure. Max_depth=1 equals split data once
- **2.1.** Using Criterion= 'gini', showing the accuracy score of test data by Max_depth= 3 and Max_depth=10, respectively.
- **2.2.** Using Max_depth=3, showing the accuracy score of test data by Criterion= 'gin i' and Criterion=' entropy', respectively.

Note: Your decisition tree scores should over 0.7. It may suffer from overfitting, if so, you can tune the hyperparameter such as `max depth`

Note: You should get the same results when re-building the model with the same arguments, no need to prune the trees

Note: You can find the best split threshold by both methods. First one: 1) Try N-1 threshold values, where the i-th threshold is the average of the i-th and (i+1)-th sorted values. Second one: Use the unique sorted value of the feature as the threshold to split Hint: You can use the recursive method to build the nodes

- 3. (5%) Plot the <u>feature importance</u> of your Decision Tree model. You can use the model fro m Question 2.1, max_depth=10. (You can use simply counting to get the feature importance instead of the formula in the reference, more details on the sample code. **Matplotlib** is all owed to be used)
- 4. (15%) Implement the AdaBoost algorithm by using the CART you just implemented from question 2. You should implement one argument for the AdaBoost.
 - 1) **N_estimators**: The number of trees in the forest.
 - **4.1.** Showing the accuracy score of test data by n_estimators=10 and n_estimators=100, respectively.
- 5. (15%) Implement the Random Forest algorithm by using the CART you just implemented from question 2. You should implement three arguments for the Random Forest.
 - 1) **N_estimators**: The number of trees in the forest.
 - 2) Max features: The number of features to consider when looking for the best split
 - 3) Bootstrap: Whether bootstrap samples are used when building trees
 - **5.1.** Using Criterion= 'gini', Max_depth=None, Max_features=sqrt(n_features), Boo tstrap=True, showing the accuracy score of test data by n_estimators=10 and n_est imators=100, respectively.
 - **5.2.** Using Criterion= 'gini', Max_depth=None, N_estimators=10, Bootstrap=True, showing the accuracy score of test data by Max_features=sqrt(n_features) and Max_features=n_features, respectively.

Note: Use majority votes to get the final prediction, you may get different results when re-building the random forest model

6. (30%) Tune the hyperparameter, perform feature engineering or implement more po werful ensemble methods to get a higher accuracy score. Screenshot your tests scor e on the report. Please note that only the ensemble method can be used. The neural network method is not allowed.

Accuracy	Your scores
acc > 0.85	30 points
0.8 < acc <= 0.85	25 points
0.7 < acc <= 0.8	20 points

acc < 0.7	0 points

Part. 2, Questions (20%):

- (10%) Consider a data set comprising 400 data points from class C₁ and 400 data points from class C₂. Suppose that a tree model A splits these into (300, 100) at the first leaf node a nd (100, 300) at the second leaf node, where (n, m) denotes that n points are assigned to C₁ and m points are assigned to C₂. Similarly, suppose that a second tree model B splits them into (200, 400) and (200, 0). Evaluate the misclassification rates for the two trees and hence e show that they are equal. Similarly, evaluate the cross-entropy Entropy = -∑^K_{k=1} p_k log₂ p_k and Gini index Gini = 1 ∑^K_{k=1} p_k for the two trees and show that they are both lower for tree B than for tree A. Define p_k to be the proportion of data points in region R assigned to class k, where k = 1, ..., K
- 2. (10%) By making a variational minimization of the expected exponential error function given by (1) with respect to all possible functions y(x), show that the minimizing function is given by (2). Define t is target variable $\in \{-1, 1\}$, x is input vector.

$$E_{x,t} [e^{-ty(x)}] = \sum_{t} \int e^{-ty(x)} p(t|x) p(x) dx$$
 (1)
$$y(x) = \frac{1}{2} ln \frac{p(t-1|x)}{p(t-1|x)}$$
 (2)