

Handbook on special functions

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§1. Elementary functions and some constants

Absolute value $|x|$ and **sign** function $\operatorname{sgn} x$.

Interpolation between linear and exponential function $[x]_q = \frac{q^x - 1}{q - 1}$, where $q \geq 1$, so that $[x]_1 = x$.