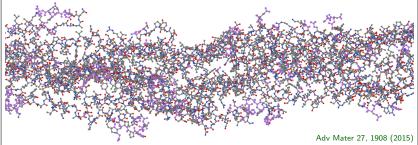
Electronic Coarse-Graining (ECG) in examples

- When do we need ECG? When system is too complex for use of conventional electronic structure methods (e.g. polymers)
- What is the "price" for ECG? Only frontier orbitals are calculated (enough for majority of electronic phenomena)
- ECG example 1/4: biopolymers (localized states ⇒ trivial ECG)



10k non-H atoms \implies 50k valence molecular orbitals (MOs) or 1M AOs but frontier MOs are localized on a small fraction of AOs (violet color)

ECG: more precise formulation





All-electron density

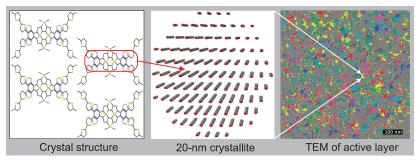
CG density (2 MOs)

ECG idea/goal: Get minimal basis providing accurate description of a particular electronic property under molecular fluctuations (large-scale/low-energy electronic phenomena: UV-Vis spectra, transport)

Requirements:

- Robustness of CG basis wrt molecular fluctuations
- Robustness and scalability of CG algorithm
- Quality control of CG basis and matrix elements
- Accurate extrapolation to infinite system (if needed)

ECG example 2/4: electronic transport in a molecular solid



- Coarse grain electrons to one site per molecule
- Simplify molecular motions to harmonic vibrations
- Linearize coupling between electrons and molecular motions

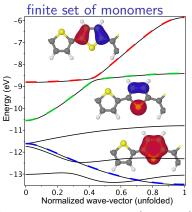
$$\implies \sum_{ij} \textbf{\textit{H}}^{1p}_{ij} c^{\dagger}_{i} c_{j} + \sum_{\alpha} \hbar \omega_{\alpha} \left(b^{\dagger}_{\alpha} b_{\alpha} + \frac{1}{2} \right) + \sum_{ij\alpha} \hbar \omega_{\alpha} \textbf{\textit{g}}_{ij\alpha} \left(b^{\dagger}_{\alpha} + b_{\alpha} \right) c^{\dagger}_{i} c_{j}$$

Then solve this Hamiltonian (e.g. in small polaron hopping approximation)

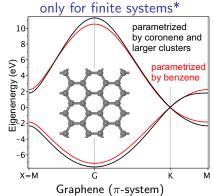
Annu Rev Phys Chem 66, 305 (2015) first review - Chem Rev 104, 4971 (2004)

ECG in examples 3/4: less trivial coarse-graining

Combinatorial screening of polymers and oligomers from a



Electronic structure of infinite systems with methods available



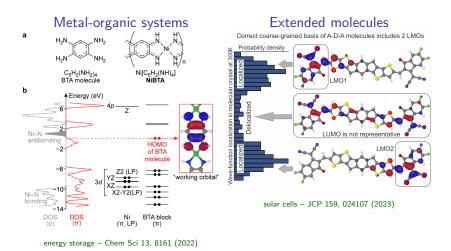
polarons in phosphorene - JPCL 12, 4674 (2021)

Single polythiophene chain $(\pi$ -system)

rational design - Chem Sci 8, 1146 (2017), Solar Energy 198, 605 (2020)

^{*}e.g. PBE-D3 is good for crystal structure but bad for e-properties JCTC 19, 8481 (2023)

ECG in examples 4/4: nontrivial coarse-graining (and applications)



... and other structurally complex systems