Stochastic Signal Processing

Lesson 2 – Experiment: changing a simulation system

Weize Sun

Problem of codes (this year)

- There are some problems of the submitted program:
 - data format error

```
无法执行赋值,因为左侧和右侧的元素数目不同。
出错 Run_Strategies (第 13 行)
   Strategies_one_trade(12) = id12(counterparty_list(12));
出错 main (第 34 行)
   Strategies_one_trade = Run_Strategies(counterparty_list)
 function [your_strategy] = id12(counterparty_id)
       load infor_id12.mat;
       load storage_id12.mat;
       if counterparty_action==0
           your_strategy=round(rand); %this means th
       else
           your_strategy=round(rand(0, 10));
           if your_strategy<3
               your_strategy=0; %this means that you
           end
       end
       Trade_no=Trade_no+1;
       save('storage_id12', 'Trade_no', 'vour_id');
```

```
load infor_id12.mat;
load storage_id12.mat;

if counterparty_action==0
    your_strategy=round(rand); %this means that you
else
    your_strategy=randi([0, 9]);
    if your_strategy<3
        your_strategy=0; %this means that you will }
    end
end
Trade_no=Trade_no+1;</pre>
```

save('storage_id12', 'Trade_no', 'vour_id');

function [your_strategy] = id12(counterparty_id)

Problem of codes (this year)

- There are some problems of the submitted program:
 - Wrong parameter name

```
无法识别的字段名称 "counterpart_action"。
 出错 id20 (第 13 行)
     counterpart_action = inforData.counterpart_action;
 出错 Run_Strategies (第 21 行)
     Strategies_one_trade(20) = id20(counterparty_list(20));
 出错 main (第 34 行)
 Strategies one trade = Rum Strategies(counternarty list);
% this time
function [strategy_id20] = id20(counterparty_id)
     X = 4:
     Y = 5:
     your strategy = 1; % this strategy means that you w
     inforData = load("infor_id20.mat");
     counterparty id = inforData.counterparty id;
     counterpart_action = inforData.counterpart_action
     storageData = load("storage_id20.mat");
     Trade_on = storageData.Trade_on;
     vour_id = storageData.your_id;
     if counterpart_action == 1
             Trade_on = Trade_on - Y;
     elseif counterpart action == 0
             Trade_on = Trade_on + 2*X;
     save("storage_id20.mat", 'Trade_on', '-append'
     strategy id20 = counterparty id;
```

First is the error in the variable names: counterparty action

Trade_no

Second, the code is difficult to understand, recommended to provide comments, which makes the code easier to understand



Problem of codes (this year)

- There are some problems of the submitted program:
 - Saving strange things

```
出错 <u>id29</u> (<u>第 21 行</u>)
save('storage_id29', 'Trade_no', '29')
出错 <u>Run_Strategies</u> (<u>第 30 行</u>)
Strategies_one_trade(29) = id29(counterparty_list(29));
出错 <u>main</u> (<u>第 34 行</u>)
Strategies_one_trade = Run_Strategies(counterparty_list);
```

```
## Now we begins

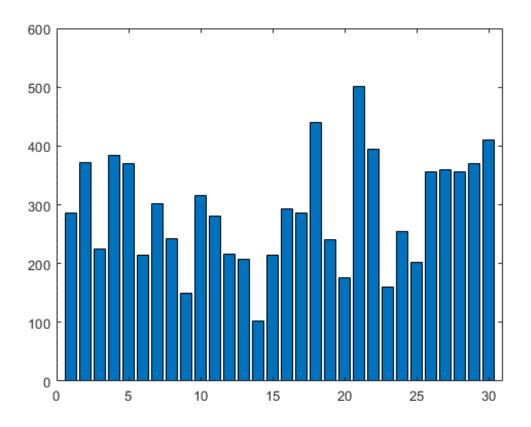
[] function [your_strategy] = id29(counterparty_id)

| load storage_id29.mat |
| if mod(Trade_no, 2) == 0 |
| your_strategy = 0; % this means that you will trust delse |
| your_strategy = 1; % this means that you will betray end |
| Trade_no = Trade_no + 1; |
| save('storage_id29', 'Trade_no', '29') |
| % your strategy will trush one person and then betray one |
| % ONLY save your data in the file storage_id21.mat, |
| % otherwise you will be treated as 'homework not submitted end
```



```
function [your_strategy] = id29(counterparty_id)
    load storage_id29.mat
    if mod(Trade_no, 2) == 0
        your_strategy = 0; % this means that you will trus
    else
        your_strategy = 1; % this means that you will betr
    end
    Trade_no = Trade_no + 1;
    save('storage_id29', 'Trade_no', 'your_id')
    % your strategy will trush one person and then betray of
% ONLY save your data in the file storage_id21.mat,
% otherwise you will be treated as 'homework not submit-end
```

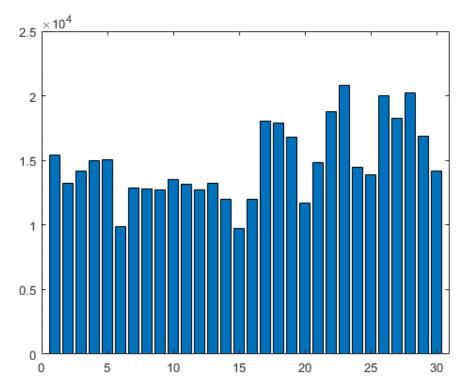
- Run 100 times among 30 persons
 - Note that the result will be different every time, as 100 trades is a small number



- Run 5000 times among 30 persons
 - If you run this again, you will see very similar result
 - This is the origin of the so called 'Monte Carlo' Simulation: test your model with an extremely long time (here, it means trade a large number of times), and give the average performance
 - However, a person cannot trade with others 5000 times in real life, that is

unrealistic

```
PLATE TO STORY THE PLATE THE PLATE
```



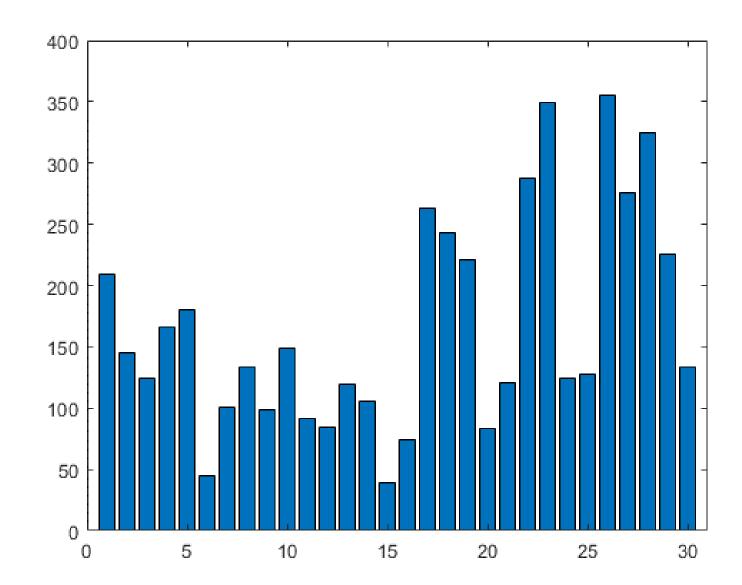
Then how to be realistic?

- In each game, there are totally 20 trades. That is more realistic as one person cannot perform 5000 'important' trades in his whole life
- In each game, take the top 5 person with highest value as winners, and record them with '+1'
- Repeat the game 1000 times.
 - This is the basic idea of 'Statistics', and also exactly the idea of 'Monte Carlo' Simulation: repeat an experiment a large number of times, and output the average result
 - It means: if you can repeat your life 1000 times, what is the total numbers you can win, or
 - The average performance of your strategy in 1000 parallel worlds

```
clear;
clc;
% the above two commands clear all the previous record in the Memory
Repeated_trails = 1000;
                              % repeat the game Repeated_trails times
N_{trades} = 20;
                 % trade N trades times
N_persons = 30;
               % totally N_persons persons
X_betray_trust_point = 4;
Y_betray_betray_point = 5;
Winning_numbers_in_one_game = 5; % assume that the first 5 persons win in this game
ranking_result_total = zeros(N_persons, 1); % store the result of all the games
```

```
end
    [Return_total_list, Return_total_index] = sort(Return_total, 'descend');
   ranking_result = zeros(N_persons, 1);
   ranking_result(Return_total_index(1:Winning_numbers_in_one_game)) = 1;
   ranking_result_total = ranking_result_total + ranking_result;
end
% bar(Return_total)
bar(ranking_result_total)
x1im([0, 31])
```

- Highest 5:
 - ID22
 - ID23
 - ID26
 - ID27
 - ID28



```
% this time
 %% Now we begins
function [your strategy] = id26(counterparty id)
                                                       %% Now we begins
      load storage_id21.mat
                                                     function [your_strategy] = id28(counterparty_id)
      load infor_id21.mat
                                                           load infor id28.mat
      if mod(Trade no, 2) == 0
                                                           load storage_id28.mat
          your strategy = 0; % this means that you
      else
                                                           your strategy = 0; % this means that you will trust this pe
          your strategy = 1; % this means that you
                                                           Trade no = Trade no + 1;
      end
                                                           save ('storage id28', 'Trade no', 'your id')
      Trade no = Trade no + 1:
                                                           % your strategy will trust this person all the time
      save('storage_id21', 'Trade_no', 'your_id')
                                                           % ONLY save your data in the file storage id28.mat,
      % your strategy will trush one person and the
                                                           % otherwise you will be treated as 'homework not submitted'
      % ONLY save your data in the file storage id2
                                                       end
      % otherwise you will be treated as 'homework
  end
```

- Interesting conclusion:
 - In fact, winners will trust a lot, you can test the program yourself
 - Luck is very important, although some other IDs are exactly the same, the results are slightly different
 - But it might be not real for real world, therefore, we need to modify the game!

- The deficiencies of the 'ranking' index:
 - In 1000 games, if one strategy win 800 times with final value 10, but loss 200 times with final value -50, it will be given a high score in this 'ranking' index
 - But this strategy is very stupid: the expectation is 800*10-50*200=-2000!
 - We can use the 'average return' and the 'ranking' to evaluate the strategy comprehensively!
 - You can re-write this program by yourself.

- Now consider this updated game:
 - 1. There are N=2K persons in the game
 - 2. In each time, two person (K pairs) will trade with each other
 - 3. You and your counterparties both have three options:
 - Trade, or says, trust
 - Cheat, or says, betray
 - Reject, or says, refuse to trade

Once both persons choose his/her options, calculate the points he/she get as the table

		A					
		Trust	Betray	Reject			
В	Trust	A: +10; B: +10	A: +2X; B: -X	A&B: +0			
	Betray	A: -X; B: +2X	A: -Y; B: -Y	A&B: +0			
	Reject	A&B: +0	A&B: +0	A&B: +0			

- Now, you are not the participant only, you are the game designer!
- You need to consider two parts:
 - Technique part: how to change the system so that the 'Reject' can be added?
 - strategy part: how to design X and Y so that the 'Reject' is useful?
- The Technique part is easy:
 - In previous system, we design '0' = 'Trade' and 'not 0' = 'Betray'
 - Quick question: why not assign '0' = 'Trade' and '1' = 'Betray'?
 - Because, in that case, one might give a strategy '2', or 'A', and the system will fails.
 - Therefore, we must define at least one option of the system as 'others'
 - For example:
 - '0' = 'Trade' and '>0' = 'Betray'
 - 'others' = 'Reject'

```
'0' = 'Trade' and '>0' = 'Betray'
if Strategy_this==0
                                   'others' = 'Reject'
   if Strategy counterparty==0
       Return_one_trade(person_id) = 10; % both trust, add 10 points
    elseif Strategy_counterparty>0
       Return_one_trade(person_id) = -X_betray_trust_point; % self trust, counterparty betray, -X = -
    else
       Return_one_trade(person_id) = 0; % self trust, counterparty reject, 0 points
    end
elseif Strategy this>0
   if Strategy_counterparty==0
       Return_one_trade(person_id) = 2*X_betray_trust_point; | % self betray, counterparty trust, + 2 >
    elseif Strategy_counterparty>0
       Return_one_trade(person_id) = -Y_betray_betray_point; % self betray, counterparty betray, -Y
    else
       Return_one_trade(person_id) = 0; % self betray, counterparty reject, 0 points
    end
       % self reject, always 0 points, no matter what counterparty action is
   Return_one_trade(person_id) = 0;
end
```

- Before we goes on, let's see some bugs, or the unsatisfying parts of the previous system, and change them first.
- Let's take the previous default id21.m as an example

```
% Print your student ID and Name here, for example
 % 000000
             Weize Sun
 %%
 % your strategy returns your strategy of the trade this time
 % your strategy = 0 means that you want to trust the counterparty this time
 % your_strategy not equal to 0 means that you want to betray the
 % counterparty this time
 % counterparty id is the ID of the counterparty you are going to trade with
 % this time
 %% Now we begins
function [your_strategy] = id21(counterparty_id
     load storage id21. mat
     if mod(Trade no, 2) == 0
         your_strategy = 0; % this means that you will trust this person
     else
         your_strategy = 1; % this means that you will betray this person
     end
     Trade_no = Trade_no + 1;
     save('storage_id21', 'Trade_no', 'your_id')
     % your strategy will trush one person and then betray one and goes on
     % ONLY save your data in the file storage_id21.mat,
     % otherwise you will be treated as 'homework not submitted'
```

Here, it load the 'storage_id21.mat' at default, and use the 'Trade_no' to decide his strategy. It will leads to the following problems:

- 1. If there is no 'storage_id21.mat', the system will fails.
- 2. The 'storage_id21.mat' might give a default value of 'Trade_no' randomly, making the strategy very unstable
- For a game participant, he should care about the 2nd problem majorly (also, he should care about the 1st problem in order to avoid failure of his program);
- But, for the game designer, he should care about the 1st problem seriously!

- Before we goes on, let's see some bugs, or the unsatisfying parts of the previous system, and change them first.
- Let's take the previous default id21.m as an example

```
% Print your student ID and Name here, for example
 % 000000
             Weize Sun
 %%
 % your strategy returns your strategy of the trade this time
 % your_strategy = 0 means that you want to trust the counterparty this time
 % your_strategy not equal to 0 means that you want to betray the
 % counterparty this time
 % counterparty id is the ID of the counterparty you are going to trade with
 % this time
 %% Now we begins
function [your_strategy] = id21(counterparty_id)
     load storage_id21.mat
     if mod(Trade no, 2) == 0
         your_strategy = 0; % this means that you will trust this person
     else
         your_strategy = 1; % this means that you will betray this person
     end
     Trade_no = Trade_no + 1;
     save('storage_id21', 'Trade_no', 'your_id')
     % your strategy will trush one person and then betray one and goes on
     % ONLY save your data in the file storage_id21.mat,
     % otherwise you will be treated as 'homework not submitted'
```

Therefore, in the main program, we should add some codes to generate a default 'storage_idXX.mat' with a parameter 'Trade_no', then the system will be of less possibility to fail.

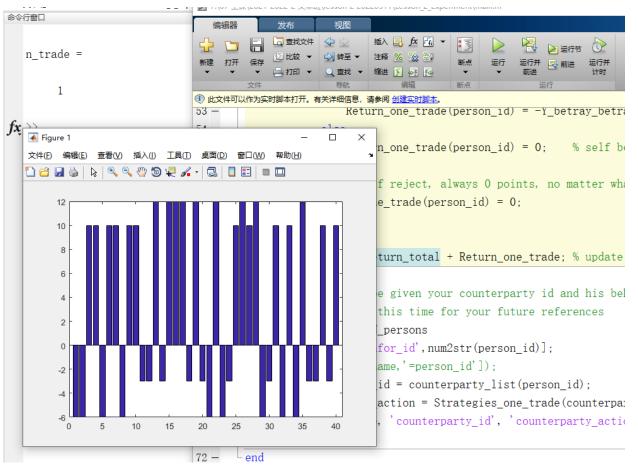
• That is:

- 这段程序的作用为:在主程序中,在游戏开始时,给所有的storage_idXX.mat文件里面创造了一个Trade_no=0,这等于给了一个约束和指示:
 - 约束: 使每次游戏开始时, 有一个统一的标准数字
 - 指示:作为游戏的参与者(IDXX),参与者不能调用主程序的数据,但是可以看到自己的storage_idXX.mat文件中的Trade_no;当它为0的时候,说明游戏刚开始。而这个Trade_no可以在每次游戏后+1,指示游戏的进度。

- Similarly, you are also required to take care of the 'infor_idXX.mat', as its generation code is placed in the end of the main loop.
- If there are no 'infor_idXX.mat', for example, 'infor_id31.mat', in the very beginning, the system will fail!

• Try to modify this system by yourself

For example: there is 'infor_idXX.mat'



For example: no 'infor_idXX.mat'

```
    ▼ I/fE

☑ F:\07 上课\2021-2022-2 文华班\lesson 2 20220311\Lesson_2_Experiment\main.m

   n_trade =
   错误使用 load
   无法读取文件 'infor_id31. mat'。没有此类文件或目录。
                                                                     53 -
                                                                                             Return_one_trade(person_id) = -Y_betray_betray_point;
                                                                     54 -
                                                                                         else
                                                                     55 -
                                                                                             Return_one_trade(person_id) = 0; % self betray, co
   出错 id31 (line 12)
                                                                     56 -
                                                                                         end
       load infor id31. mat
                                                                     57 -
                                                                                             % self reject, always 0 points, no matter what counter
                                                                                         Return_one_trade(person_id) = 0;
                                                                     58 -
   出错 Run Strategies (line 32)
                                                                     59 -
                                                                                     end
       Strategies_one_trade(31) = id31(counterparty_list(31));
                                                                     60 -
                                                                                 end
                                                                                 Return_total = Return_total + Return_one_trade; % update the retu
                                                                     61 -
   出错 main (line 36)
                                                                     62
       Strategies_one_trade = Run_Strategies(counterparty_list);
                                                                                % here you will be given your counterparty id and his behaviour
                                                                     63
                                                                     64
                                                                                 % information of this time for your future references
|fx>>
                                                                     65 -
                                                                                for person_id=1:N_persons
                                                                                     filename=['infor id', num2str(person id)];
                                                                     66 -
                                                                                       eval([filename, '=person_id']);
                                                                     67
                                                                                     counterparty id = counterparty list(person id);
                                                                     68 -
                                                                     69 -
                                                                                     counterparty_action = Strategies_one_trade(counterparty_id);
                                                                                     save(filename, 'counterparty_id', 'counterparty_action');
                                                                     70 -
                                                                     71 -
                                                                                 end
```

• Try to modify this system by yourself

• Now there comes another problem. Using the ID12 from last year as example:

```
function [your_strategy] = id12(counterparty_id)

load infor_id12.mat

load storage_id12.mat

if counterparty_action == 0

Trust_no = Trust_no + 1; % count the total number you've been trusted

else

Betray_no = Betray_no + 1; % count the total number you've been betrayedend
```

if 'Trust_no' / 'Betray_no' does not exists, it will fails

However, as the 'infor_idXX.mat' are new generated, 'Trust_no' / 'Betray_no' does not exists

• How to modify?

- Now there comes another problem. Using the ID12 from last year as example: if 'Trust_no' / 'Betray_no' does not exists, it will fails
- However, as the 'infor_idXX.mat' are new generated, 'Trust_no' / 'Betray_no' does not exists
- How to modify?
- 这段程序的作用为:在主程序中,在游戏开始时,给所有的storage_idXX.mat文件里面创造了一个Trade_no=0,这等于给了一个约束和指示:
 - 约束: 使每次游戏开始时, 有一个统一的标准数字
 - 指示:作为游戏的参与者(IDXX),参与者不能调用主程序的数据,但是可以看到自己的storage_idXX.mat文件中的Trade_no;当它为0的时候,说明游戏刚开始。而这个Trade_no可以在每次游戏后+1,指示游戏的进度。

• Now there comes another problem. Using the ID12 from last year as

example:

```
/0 UII3 UIIIE
function [your_strategy] = id12(counterparty_id)
    load infor_id12.mat
    load storage_id12.mat
    if Trade_no == 0
      Trust_no = randn(1);
      Betray no = randn(1);
    end
    if counterparty_action == 0
      Trust_no = Trust_no + 1; % count the total number you've been trusted
    else
      Betray_no = Betray_no + 1; % count the total number you've been betrayed
    end
    save('storage_id12', 'Trust_no', 'Betray_no', 'Trade_no')
    if Trust_no > Betray_no
      your_strategy = 0; % this means that you will trust this person
    else
      your_strategy = 1; % this means that you will betray this person
    end
```

Modify your program accordingly

- Now we go back to the strategy problem: how to design X and Y so that the 'Reject' is useful?
- Generally speaking, it is a 'strategy' or 'Sociology(社会学)' problem
 - Different person can give different ideology, thus leading to different X and Y
- But, this is a math programming course!
- Therefore, I will simply introduce a 'programming' method to decide the X and Y.

Experiment: changing a simulation system – the programming method

- We begin with the following assumptions:
 - The previous default 30 strategies, i.e., id1 to id30, are appropriate
 - 10 always trade; 10 always betray; 10 trade once and then betray once and then go on
 - There are 10 more strategies for us to test the 'reject' option
 - Of course, you can use more, for example, you can set 'N_persons = 300' and test 270 strategies to see how 'reject' works, but that is another story.
 - For these 10 strategies, if the 'reject' option is not chosen, randomly trade or betray
 - Other strategies can be set, but this 'randomly trade or betray' can make the system more robust to the general case: there are always trade, and betray

Experiment: changing a simulation system – the programming method

- How to design?
 - 10 strategies, with 'reject' probability 10% to 100%
 - trade 1000 times
 - Test several pairs of X and Y values, and see which pair make the strategy that 'reject' with probability 30% wins
 - Choose this X and Y

- Note: this is just one idea, you can use your idea to do the design
- Your are encourage to try this test, but it is not a homework
- Here I will show one 'reject after being betrayed' strategy

Experiment: the reject after being betrayed strategy

```
function [your_strategy] = id40(counterparty_id)
    counterparty_now = counterparty_id;
    % as loading the infor id40.mat will give a variable named
    % counterparty_id, therefore here, we store the counterparty_id from
    % the input to counterparty now first!
    % In fact, this problem can be solved by a good design of the system,
    % you can modify the system by yourself, however, when submitting your
    % homework, your are suggested to use this commend!
    load infor_id40.mat
    load storage_id40.mat
    if Trade no==0
      list betray = ∏;
    end
    if counterparty action > 0
      list betray = [list betray; counterparty id];
    end
    [m]=find(list_betray==counterparty_now);
    % if m is 'empty 0*0 double', then the counterparty_now had not been
    % betrayed you; otherwise, the counterparty_now had betrayed you at
    % least once
    if isempty(m)
      your strategy = 0; % if not been betrayed before, trade with this person
    else
      your strategy = -1; % otherwise, reject to trade
    end
    Trade_no = Trade_no + 1;
    save storage id40.mat Trade no your id list betray
  end
```

Experiment: the reject after being betrayed strategy

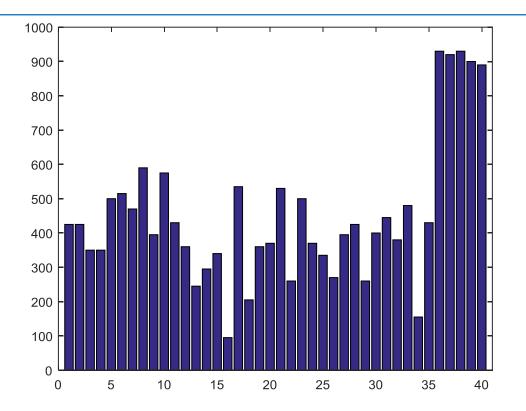
```
load infor_id40.mat
   load storage_id40.mat
   if Trade no==0
     list_betray = [];
   end
   if counterparty_action > 0
     list_betray = [list_betray; counterparty_id];
   end
   [m]=find(list_betray==counterparty_now);
   % if m is 'empty 0*0 double', then the counterparty_now had not been
   % betrayed you; otherwise, the counterparty_now had betrayed you at
   % least once
   if isempty(m)
     your strategy = 0; % if not been betrayed before, trade with this person
   else
     your_strategy = -1; % otherwise, reject to trade
   end
   Trade_no = Trade_no + 1;
   save storage id40.mat Trade no your id list betray
- end
```

Experiment: the result

- The settings
 - The setting now: {X=5 and Y=5}, and {Repeated_trails=1, N_trades=200}
 - 10 more default strategies given: 5 'betray always' and 5 'reject after being betrayed', named as id31-35 and 36-40
 - for id1-30, we use default in as previous lesson
 - Therefore, there are now 40 persons

```
Repeated_trails = 1;
N_trades = 1000;
N_persons = 40;
N_persons_pairs = round(N_persons/2);

X_betray_trust_point = 5;
Y_betray_betray_point = 5;
```



- It is not strange that id36-40 wins, as I design the 'reject after being betrayed' strategy based on the fact that many players betray a lot
- I hope that you can beat my 'reject after being betrayed' strategy under $\{X=5 \text{ and } Y=5\}$ and $\{X=8 \text{ and } Y=5\}$, in this homework
- Note that, a strategy always trade will not as good as enough (but usable) this time

Experiment: homework

- Programming homework today
 - The setting now: ${X=5 \text{ and } Y=5}/{X=8 \text{ and } Y=5}$, and ${Repeated_trails=1}$, $N_{trades=1000}$
 - Default strategies: 5 'betray always' and 5 'reject after being betrayed'
 - Add the option 'reject'
 - You can redesign your strategy, and submit it before 03.15 (Fir.) 23:59:59, to 译哲's email box
 - The problems listed today must not happen again!
 - The first two homework (last week and this week) will be attached as attachments of mini project / experimental report 1, with approx. 20-30 points
 - Homework submitted in time, and **runnable**, will get all these points

ID列表

- 请严格按照本列表,交自己ID号的程序
- 23:59:59, 15/03前直接email交给刘译哲

交程序的ID号	学号	姓名	交程序的ID号	学号	姓名	交程序的ID号	学号	姓名
1	2022040399	张桂嘉	11	2022280179	李梓琦	21	2022280450	孙浩然
2	2022090123	徐雷	12	2022280247	林茵茵	22	2022280453	陈奇峰
3	2022110131	廖祖颐	13	2022280297	陈应权	23	2022280485	贾苏健
4	2022270054	詹兴足	14	2022280307	叶朗钊	24	2022280546	张梓荣
5	2022280039	郭瑞煜	15	2022280327	古炜	25	2022280553	林凡超
6	2022280069	曾颖岚	16	2022280365	郭展鹏	26	2022280562	陈柯瑜
7	2022280105	郑志锰	17	2022280380	杨烨	27	2022280573	王梓为
8	2022280142	崔殷霖	18	2022280419	薛玉龙	28	2022280574	马海洲
9	2022280160	姚宇铭	19	2022280432	彭佳	29	2022300013	卫宏林
10	2022280162	曾源原	20	2022280445	何雨璇			