



# Shadow

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Most of slides are from Graphics & Geometry Computing  
Group of Tsinghua University

# Why is shadow important ?

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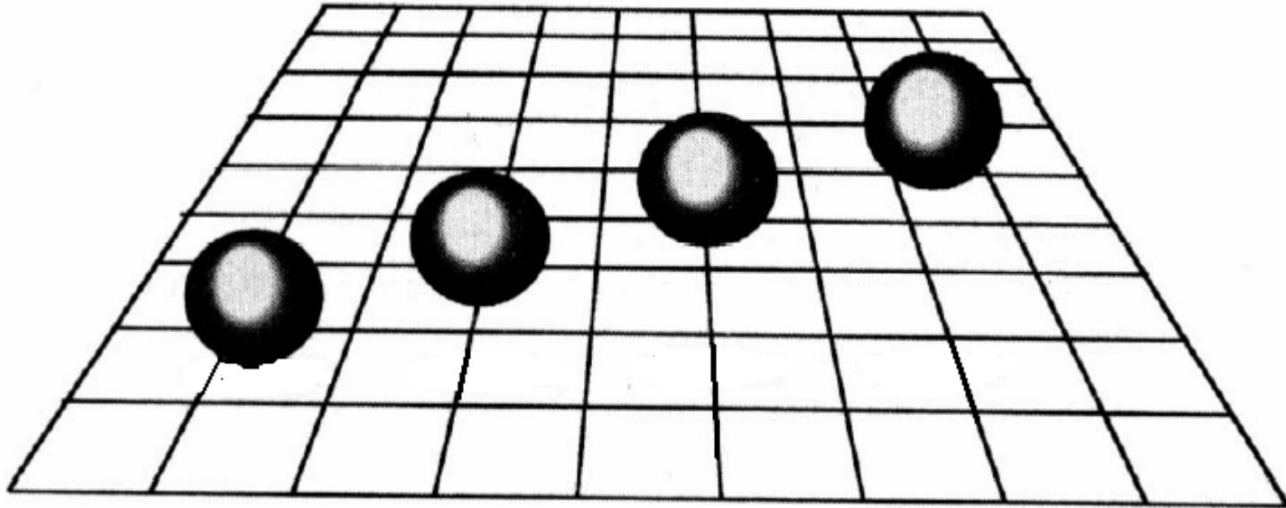
- Shadow generation is a fundamental problem in Computer Graphics.
- Why shadow is so important?
  - Lets see an example.



# Why is shadow important ?

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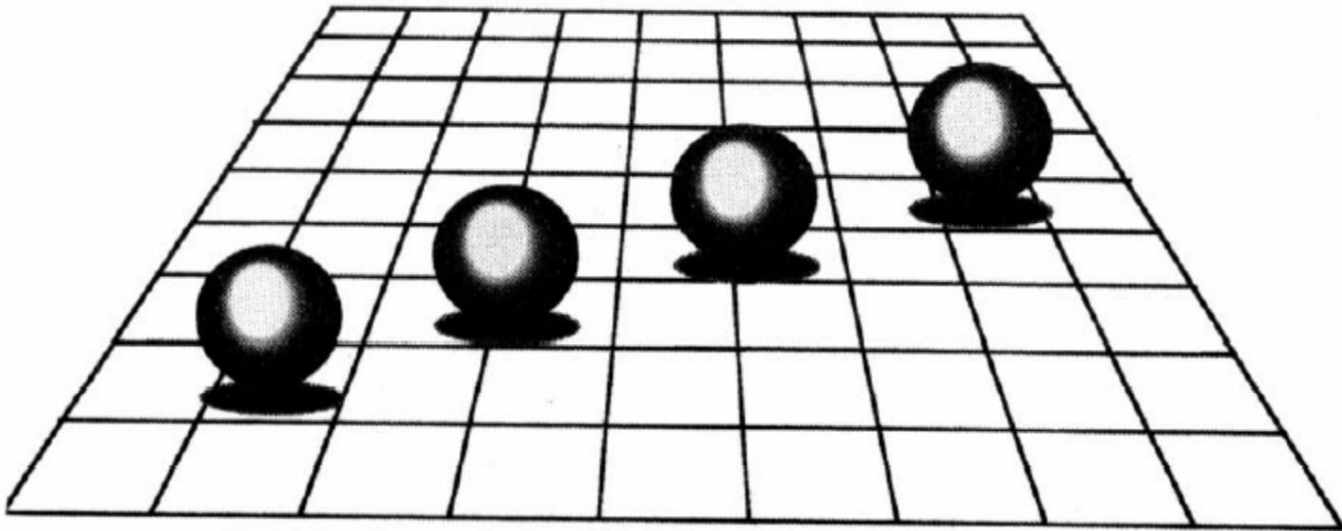
- **Do you know where are the balls located?  
(Without shadows)**
- **It is hard to determine the actual position**



# Why is shadow important ?

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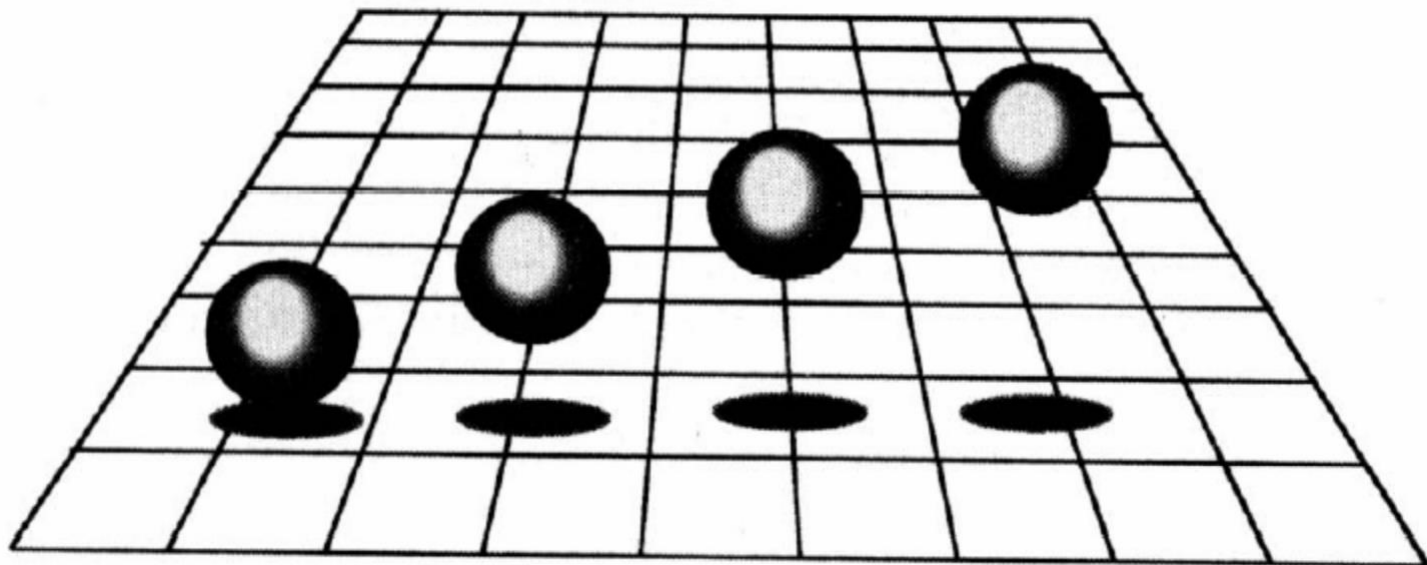
- **We know where the balls located are  
(With shadows)**



# Why is shadow important ?

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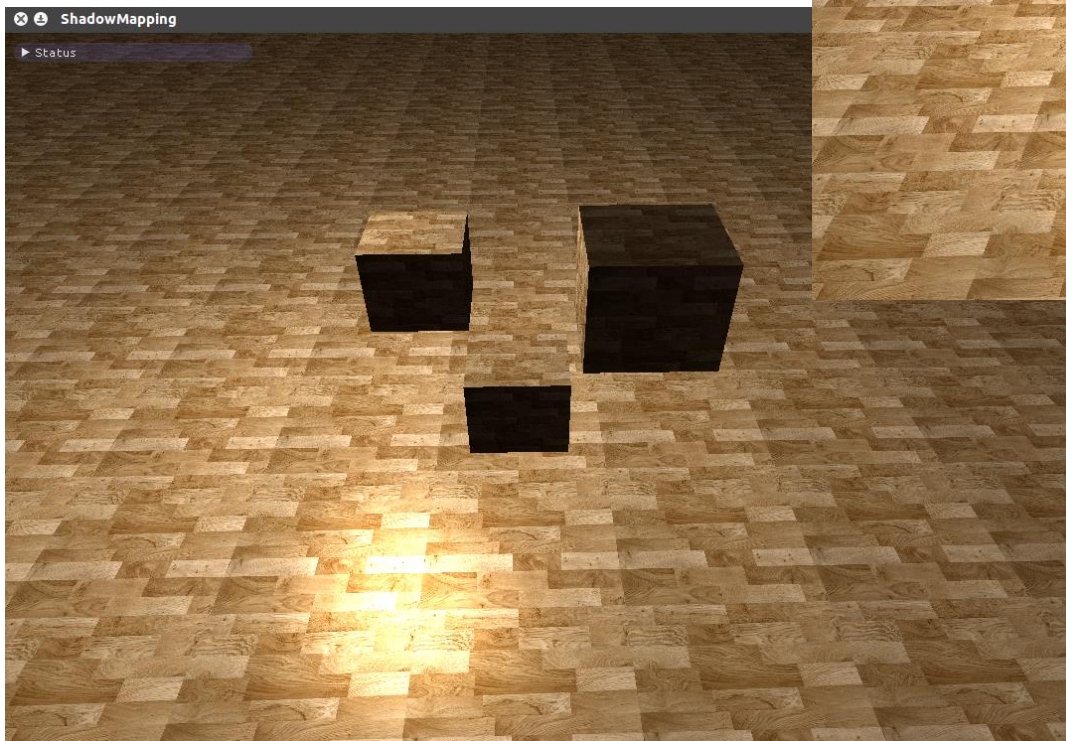
- **Different shadows implies different balls location**



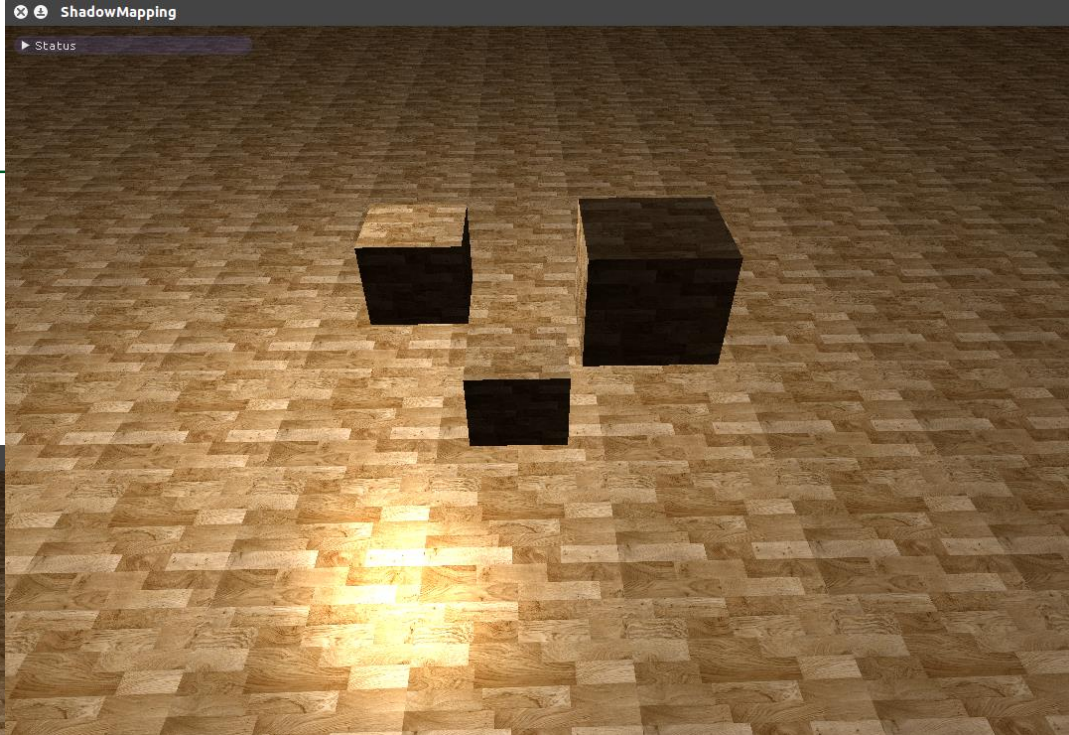


# More Examples

- without shadow



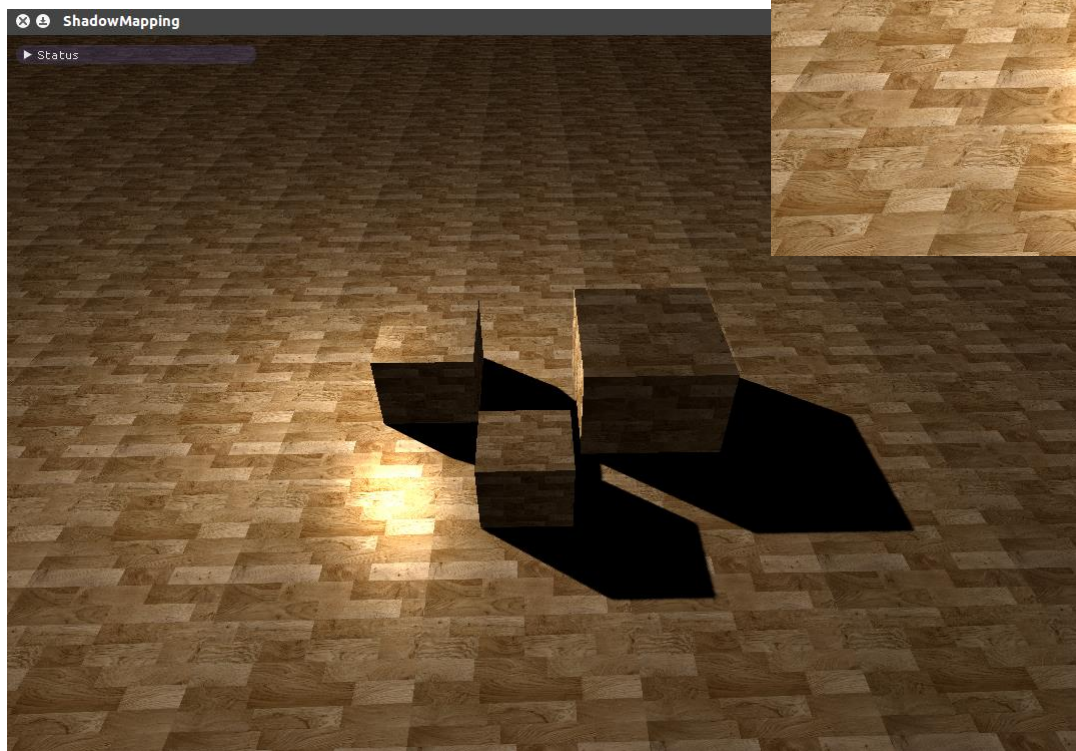
Scene B



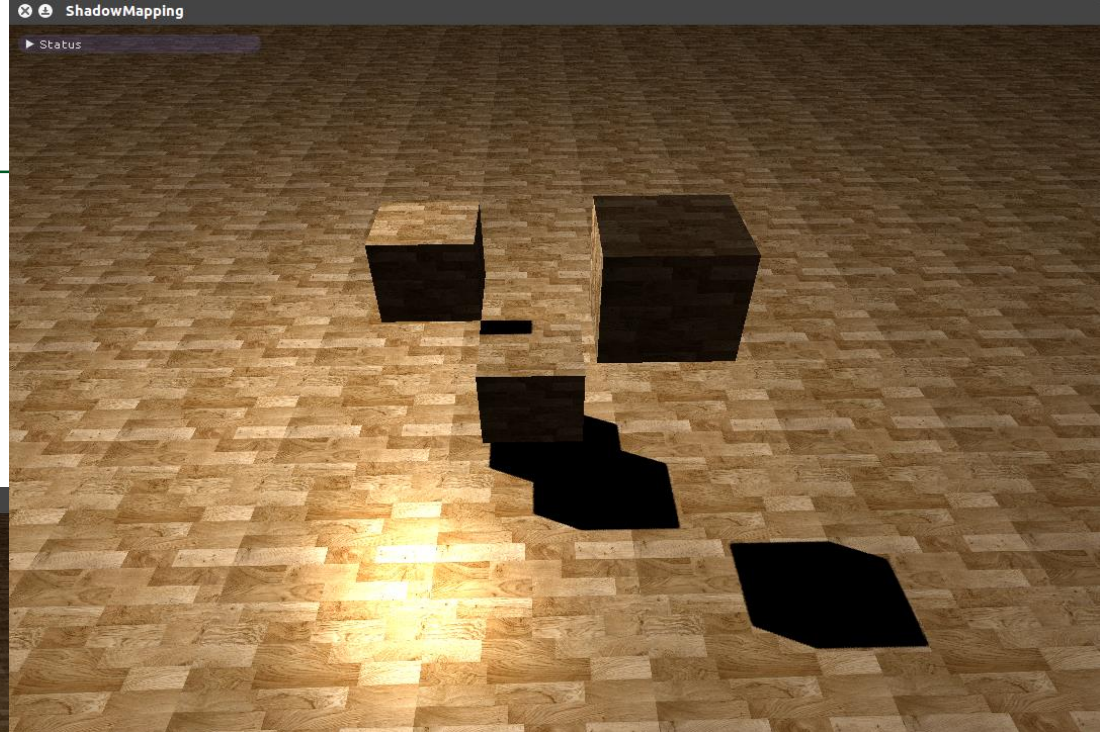
Scene A

# More Examples

- withshadow



Scene B



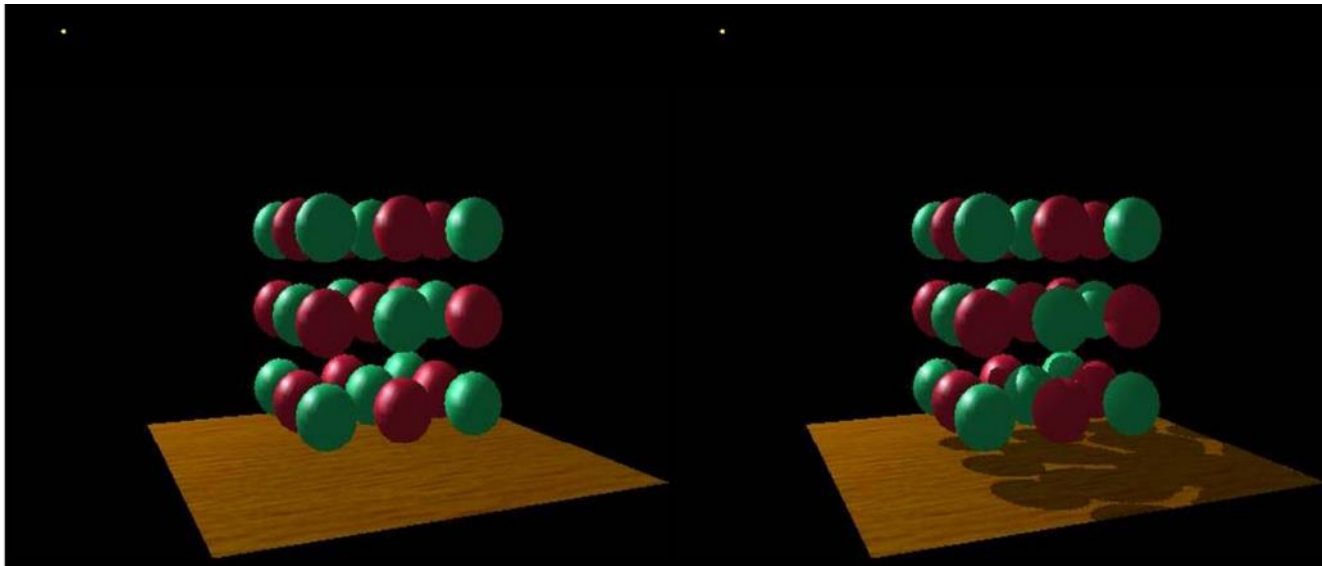
Scene A



# Why is shadow important ?

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- From these examples, we could conclude that:
  - Shadows give an important visual cue of object position.
  - Same images with different shadows implies different object positions.
- So, shadow is important.





# What is shadow?

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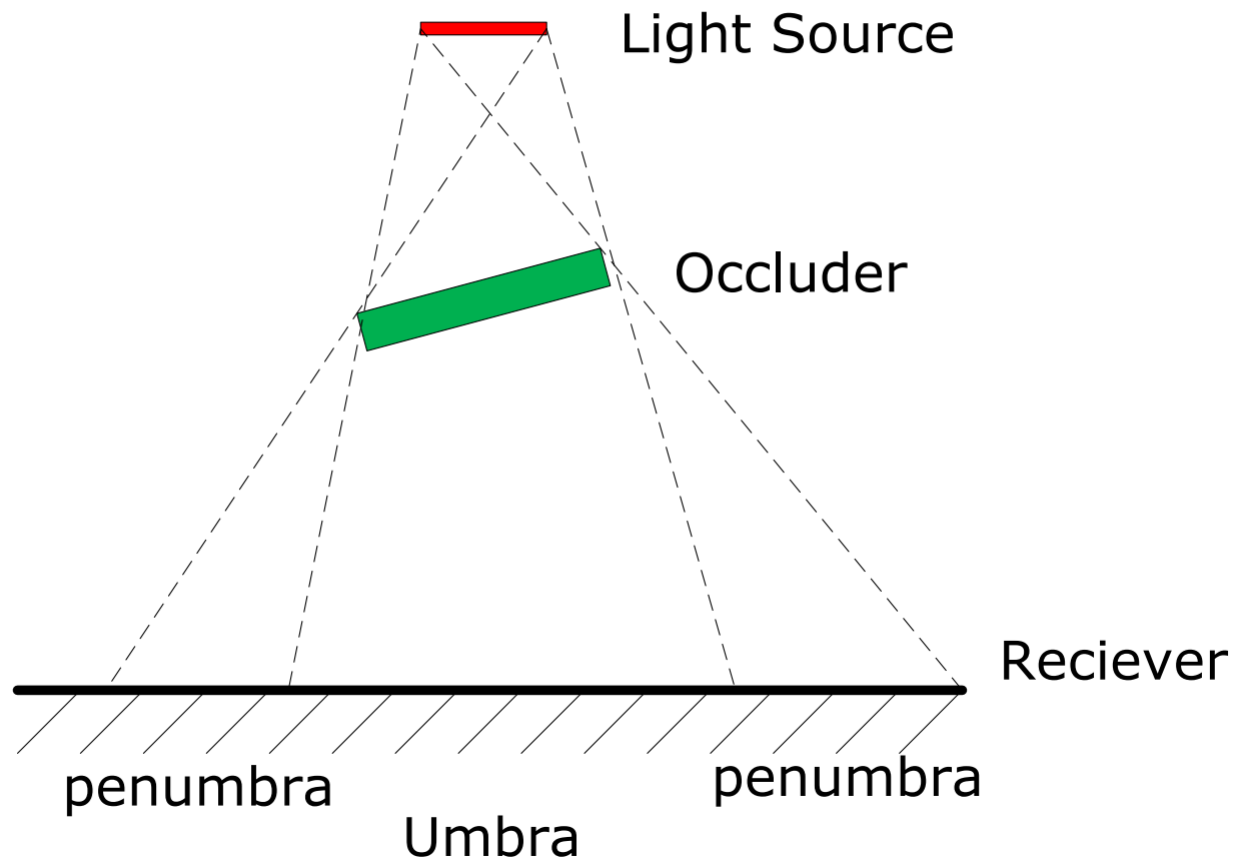
- Definition and Terminations

- Consider a **light source L** illuminating a scene:
- **Receivers** are objects of the scene that are potentially illuminated by L.
- A point P of the scene is considered to be in the umbra(本影) if it can not see any part of light source L.
- If P can see a part of the light source, it is in the penumbra(半影).
- Shadow is the **union** of the **umbra** and **penumbra**, is the region of space for which at least one point of the light source is occluded.
- Objects that hide a point from the light source are called **occluders**(遮挡物).



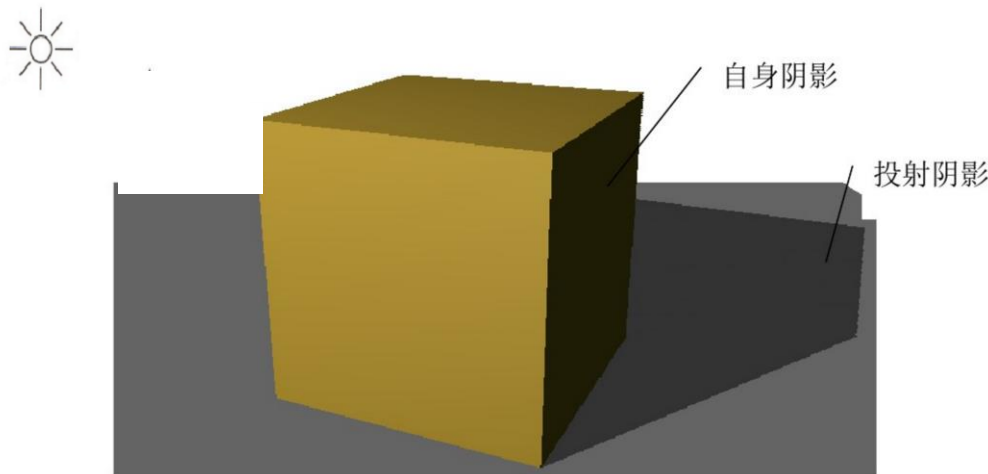
# What is shadow?

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# Types of Shadows

- **Cast shadows**: occurring when a shadow falls on an object whose normal is facing toward the light source ( 投射阴影 ).
- **Attached shadows**: occurring when the normal of the receiver is facing away from the light source ( 自身阴影或附着阴影 );
- **Self-shadows**: are a specific case of cast shadows that occur when the shadow of an object is projected onto itself, i.e. the occlude and the receiver are the same ( 自阴影 ).



自阴影



# Importance of Shadow

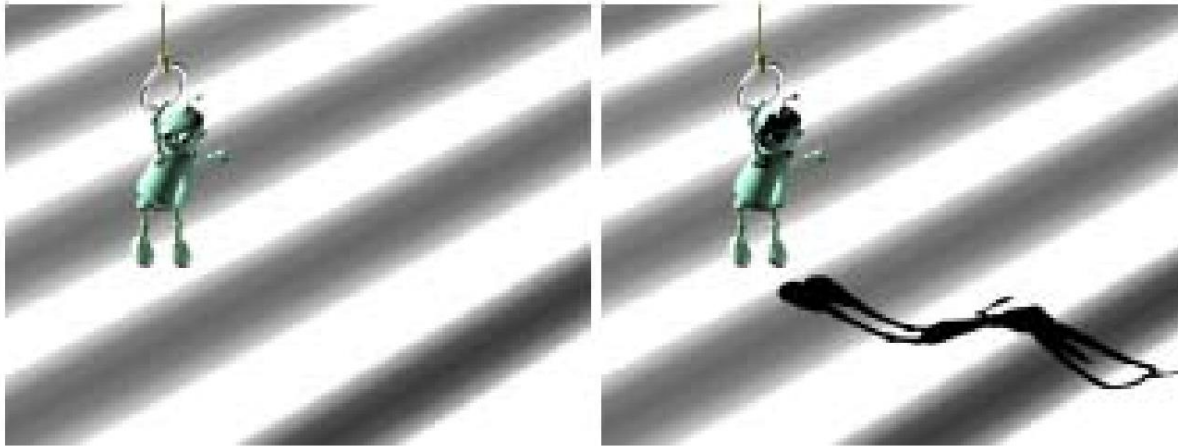
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- Shadows help to understand relative object position and size in a scene.
- Shadows can also help us understanding the geometry of a complex receiver.
- Shadows provide useful visual cues that help in understanding the geometry of a complex occluder.





- **Importance of Shadow**



Shadow helps to determine the geometry of receiver

- **Importance of Shadow**

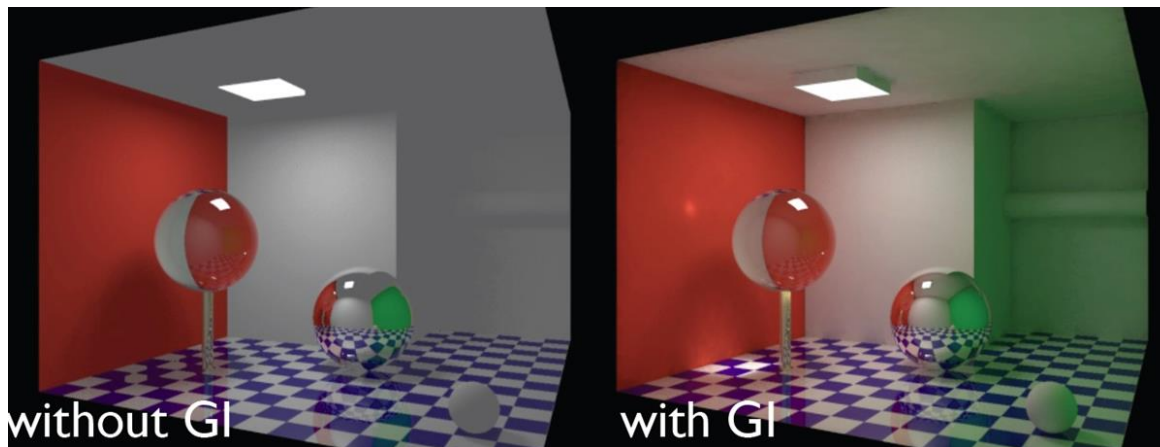


Shadow helps to determine the geometry of occluder

# Hard Shadow vs Soft Shadow

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- The common-sense notion of shadow is a binary status, i.e. a point is either “in shadow” or not. This corresponds to hard shadows, as produced by point light sources.
- However, point light sources do not exist in practice and hard shadows give a rather unrealistic feeling to images. Note that even the sun, the most common light source in our daily life, has a significant angular extent and does not create hard shadows.



# Hard Shadow vs Soft Shadow

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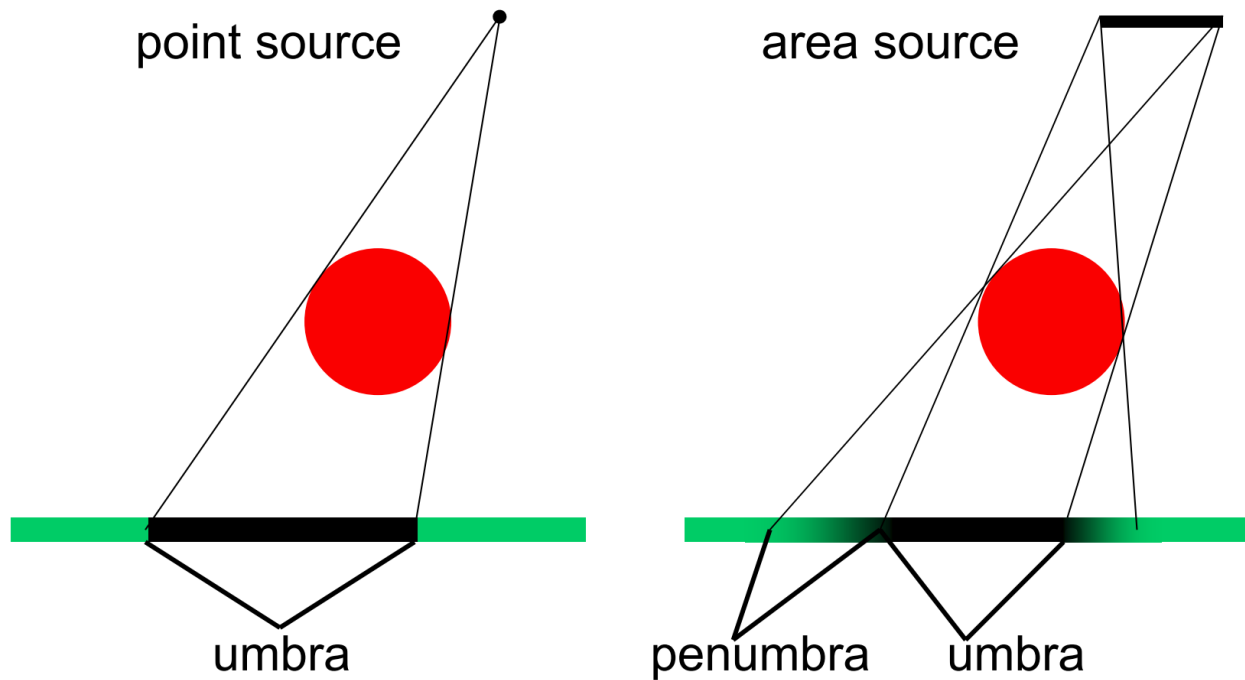
- Point light sources are easy to model in computer graphics and we shall see that several algorithms let us compute hard shadows in real time.
- For a light source with finite extent (actually an area source), the determination of the umbra and penumbra is a difficult task in general, as it amounts to solving visibility relationships in 3D, a notoriously hard problem.





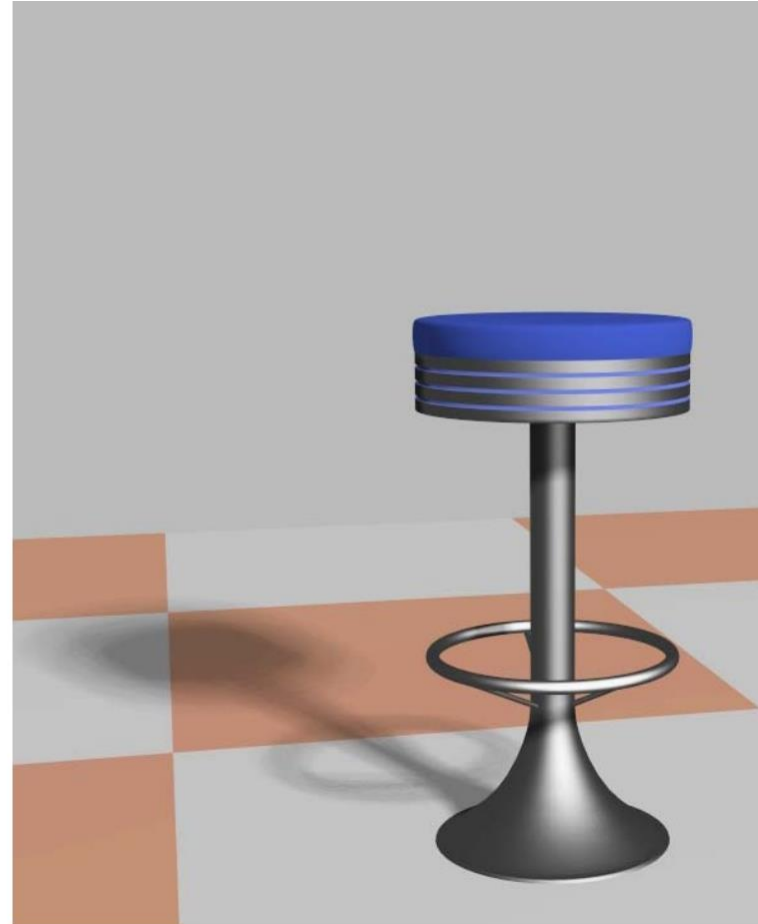
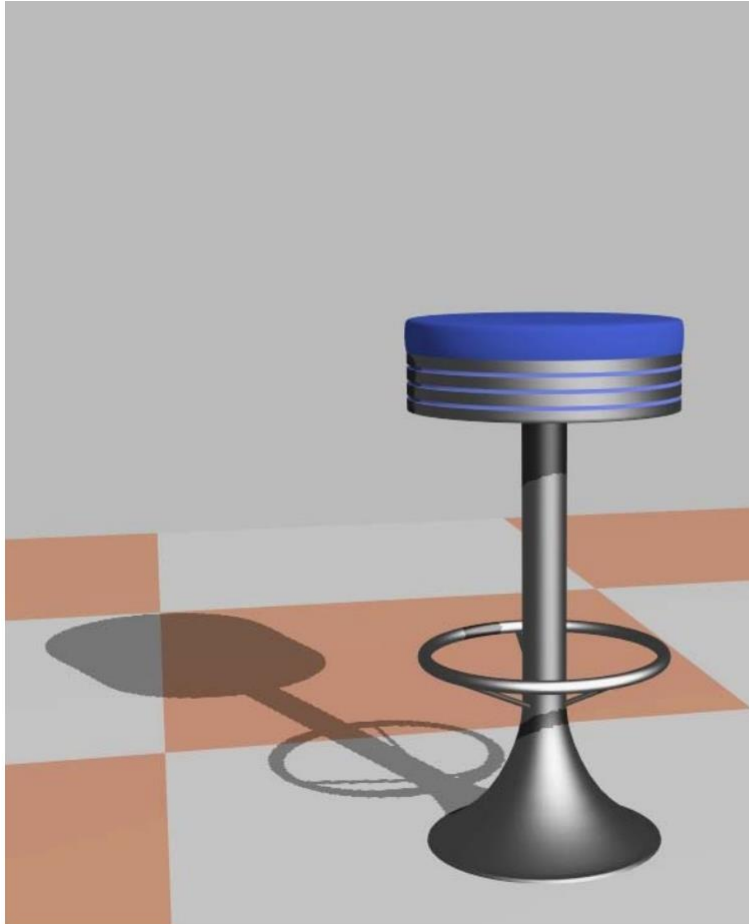
# Hard Shadow vs Soft Shadow

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# Hard Shadow vs Soft Shadow

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# Planar shadow

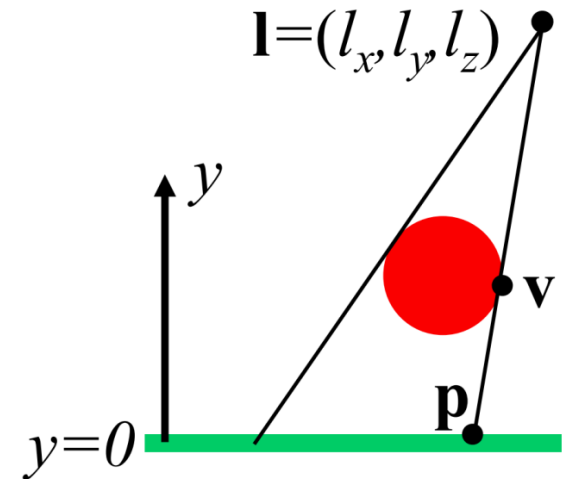
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- What is planar shadow?
  - A simple case of shadow when objects cast shadows on planar surface.



# Planar shadow

- Projection Shadow
  - In this case, the three-dimensional objects is rendered **second** times. A matrix could be derived that projects the vertices of an object onto a plane. Consider the situation in the figure, where the light source is located at  $l$ , the vertex to be projected is at  $v$ , and the projected vertex is at  $p$ .
  - Further suppose the receiver plane is  $y=0$  (this could also be generalized to work with any planes)

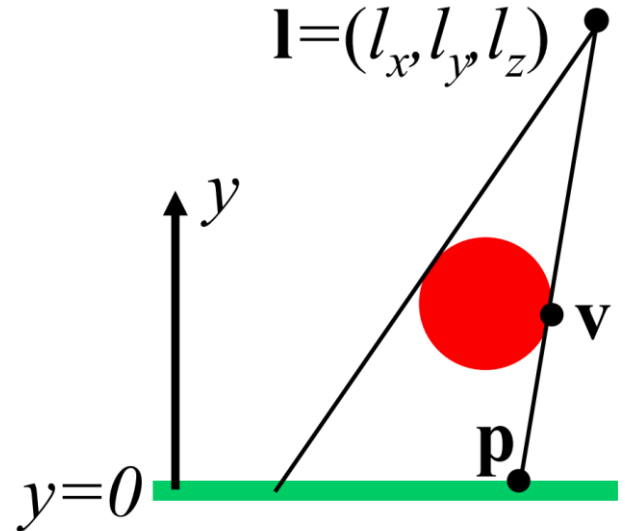




# Planar shadow

- Projection Shadow
  - By deriving the projection of x-coordinated. From similar triangles, the following equation could be obtained

$$\frac{p_x - l_x}{v_x - l_x} = \frac{l_y}{l_y - v_y}$$
$$\Rightarrow p_x = \frac{l_y v_x - l_x v_y}{l_y - v_y}$$



# Planar shadow

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- Projection Shadow
  - The z-coordinate could be obtained in the same way.

$$p_z = \frac{l_y v_z - l_z v_y}{l_y - v_y}$$

- These equations can be converted into a projection matrix M.



# Planar shadow

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- Projection Shadow
  - Projection Matrix

$$\mathbf{M} = \begin{pmatrix} l_y & -l_x & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & -l_z & l_y & 0 \\ 0 & -1 & 0 & l_y \end{pmatrix}$$

- It is easy to verify that:  $\mathbf{M}\mathbf{V} = \mathbf{P}$ .



# Planar shadow

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- Projection Shadow

- In the general case, the plane onto which the shadows should be cast is not the plane  $y = 0$ . But instead a plane  $n \cdot x + d = 0$ .
- Similar to the  $y = 0$  plane case, the projected point  $p$  could be described as:

$$p = l - \frac{d + n \cdot l}{n \cdot (v - l)} (v - l)$$





# Planar shadow

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- Projection Shadow
  - The equation can also be converted into a projection matrix, which satisfy  $Mv = p$ .

$$M = \begin{pmatrix} \mathbf{n} \cdot \mathbf{l} + d - l_x n_x & -l_x n_y & -l_x n_z & -l_x d \\ -l_y n_x & \mathbf{n} \cdot \mathbf{l} + d - l_y n_y & -l_y n_z & -l_y d \\ -l_z n_x & -l_z n_y & \mathbf{n} \cdot \mathbf{l} + d - l_z n_z & -l_z d \\ -n_x & -n_y & -n_z & \mathbf{n} \cdot \mathbf{l} \end{pmatrix}$$

- As expected, this matrix turns into the matrix in previous page if the plane is  $y = 0$  ( $n = (0, 1, 0)$  and  $d = 0$ )



# Planar shadow

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- Projection Shadow
  - To render the shadow, simply apply this matrix to the objects that should cast shadows on the plane. And render this projected object with a dark color and no illumination ( 只绘制环境光，不绘制漫反射和镜面反射 ) .
  - Limitation of the projection shadow method:
    - The receiver must be planar
    - The shadow has to be rendered for each frame, even though the shadow may not change.

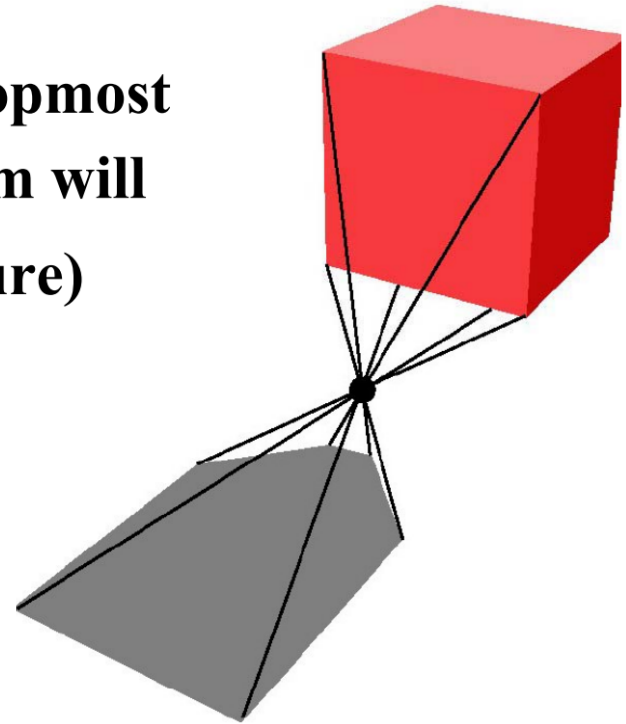


# Planar shadow

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- **Failure cases**
  - *false shadow*

**If the light source is below the topmost point on the object, the algorithm will produce false shadow (right figure)**



# Shadow Generation Methods

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- Shadow Volume
- Shadow Mapping



# Shadow Volume

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- A method proposed by Crow, which can cast shadows onto arbitrary objects.
- This technique is also sometimes called volumetric shadows.

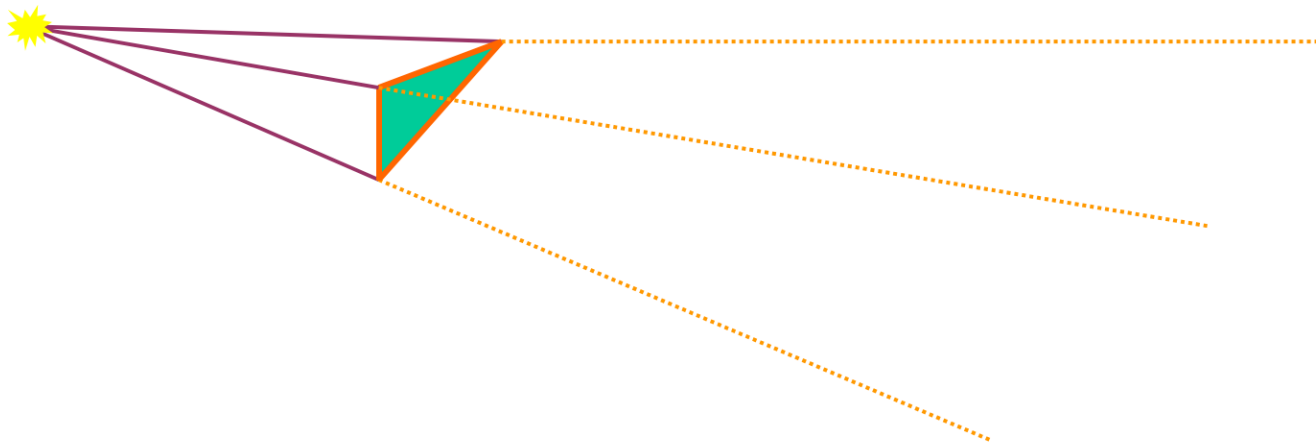


# Shadow Volume

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- To begin, imagine a point and a triangle.

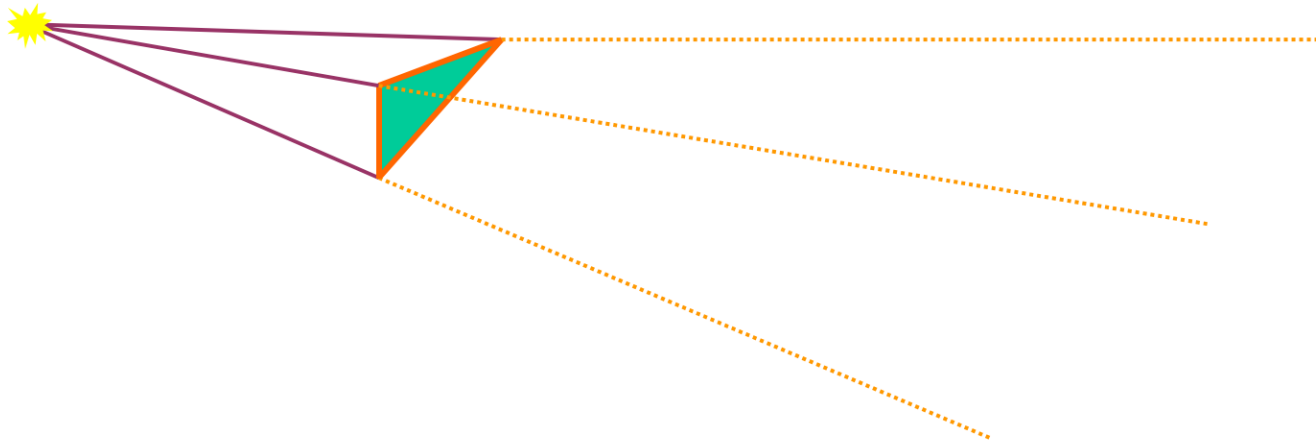
Extending the lines from the point through the vertices of the triangle to infinity yields an infinite pyramid.



# Shadow Volume

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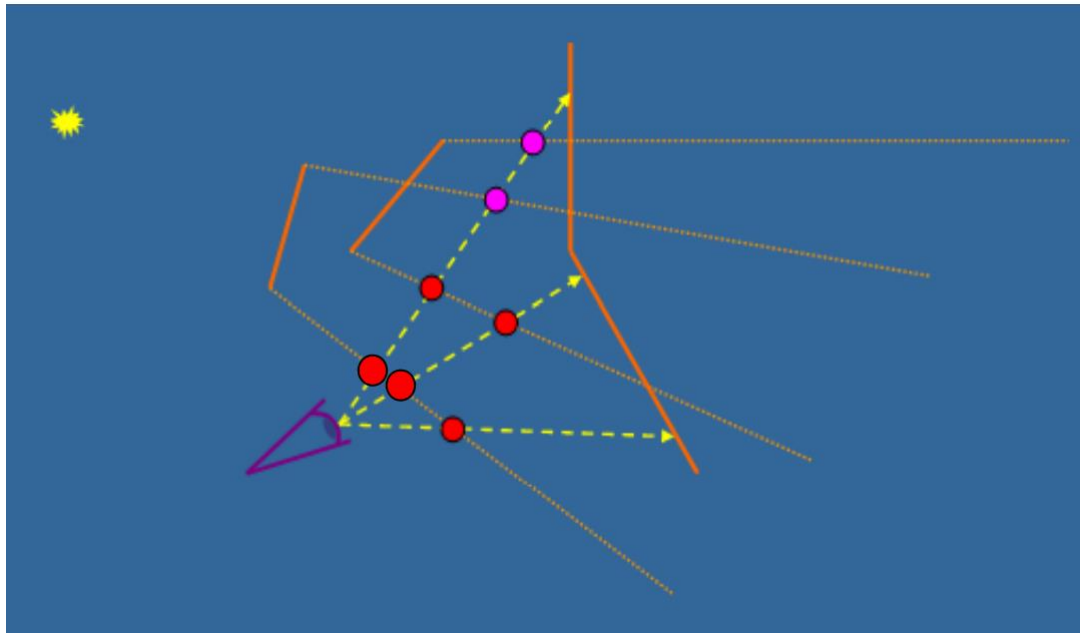
- Now, imagine the point is actually a point light source. Then any part of an object which is inside the volume of the truncated pyramid (under the triangle) is in shadow. This volume is called shadow volume.





# Shadow Volume

- Suppose we cast a ray through a pixel until the ray hits an object in the scene. Now we need to determine whether or not the pixel is in shadow.
- What we need to do is to determine whether the point is in a shadow volume.



# Shadow Volume

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- While the ray is on its way to the object, we increment a counter each time when it crosses a face of the shadow volume that is front-facing, thus the counter is incremented each time the ray goes into shadow.
- In the same manner, we decrement the same counter each time the ray crosses a back-facing face.
- Thus, finally, if the counter is greater than zero, then that pixel is in shadow; otherwise it is not.



# Shadow Volume

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- Using Stencil Buffer
  - Certainly, doing this geometrically is tedious and time-consuming. But there is a much smarter solution: using hardware's stencil buffer do the counting
  - A stencil buffer is a buffer which stores integer numbers in each pixel while Z-buffer stores depth value in real number.



# Shadow Volume

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- Using Stencil Buffer
  - **First**, clear the stencil buffer
  - **Second**, the whole scene is drawn into the frame buffer with only ambient component, in order to get these lighting components in the color buffer and the depth information into z-buffer.
  - **Third**, z-buffer updates and writing to the color buffer are turned off, and then the front faces of shadow volumes are drawn.
    - In this process, a stencil operation is set to increase the values in the stencil buffer wherever a poly gon is drawn(+1 each time).
  - **Fourth**, another pass is done by drawing the back-facing polygons. For this pass, the stencil operation is set to decrements(-1 each time)
  - **Finally**, the whole scene is rendered again, with diffuse and specular components, where the value in the stencil buffer is 0.



# Shadow Volume

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- Advantages

- First, it can be used on general-purpose **graphics hardware**. The only requirement is a stencil buffer.
- Second, since it is not image based method (unlike the shadow map method described later), it does not have sampling problems, and thus produces correct sharp shadows everywhere.

- Disadvantages

- The performance problem.
- This algorithm burns frame rate, as the number of shadow volume polygons is often large, and shadow volume polygons often cover many pixels, and so the **rasterizer becomes a bottleneck**



# Shadow Volume



# Shadow map

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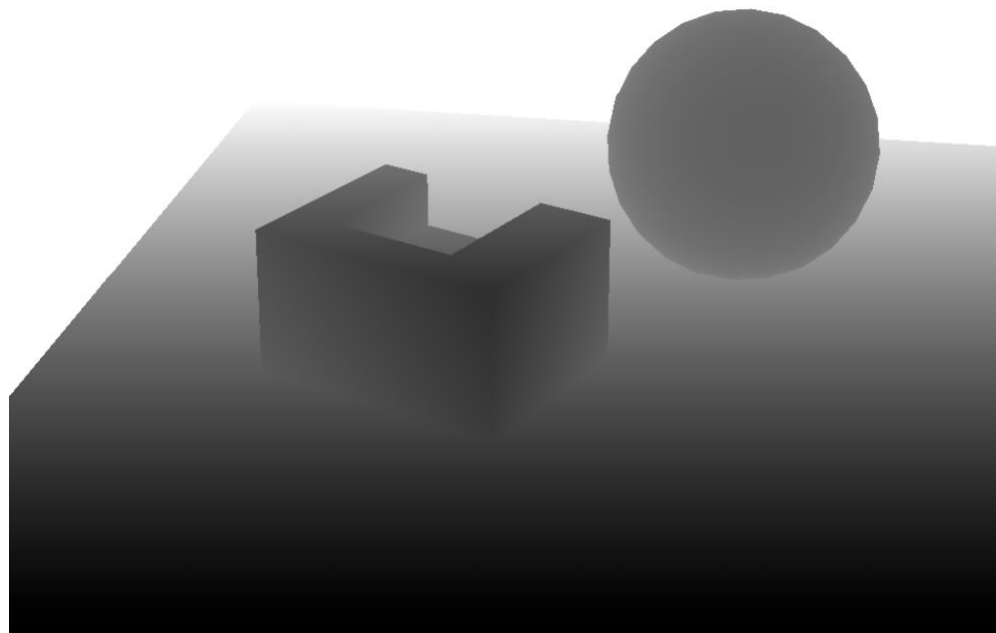
- In 1978, Williams proposed a common z-buffer based algorithm to generate shadows quickly on arbitrary objects.
- The idea is to render the scene, using the Z-buffer algorithm, from the position of the light source.



# Shadow map

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- By using **z-buffer**, the captured image from light's view records the distance to the object closest to the light.
- We call this entire content of the depth image “shadow map”.





# Shadow map

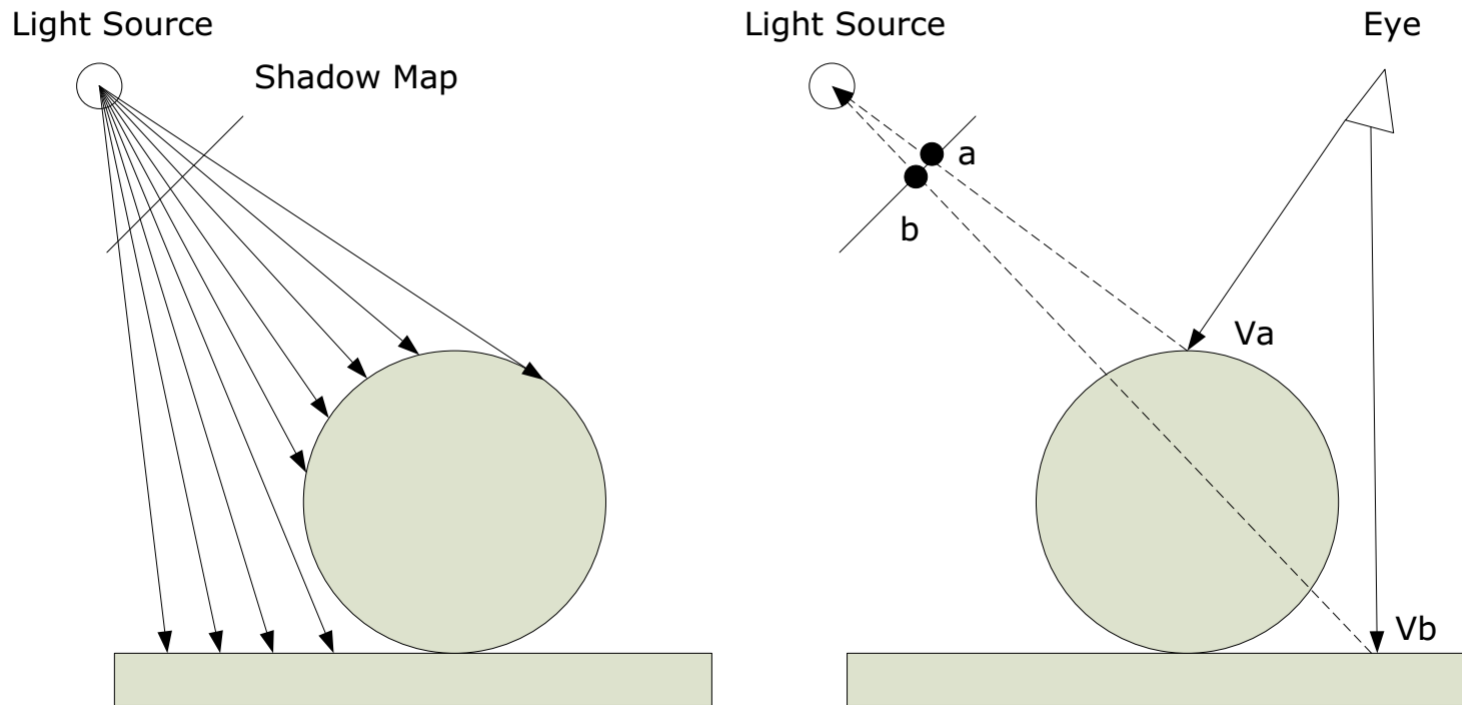
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- To use the shadow map, the scene is rendered a second time, but this time from the viewer's view.
- Now, when each primitive is being rendered, its location is compared to the shadow map:
  - If a rendered point from the light source is farther away than the value in the shadow map, then that point is in shadow;
  - Otherwise it is not.



# Shadow map

## Illustration



# Shadow map

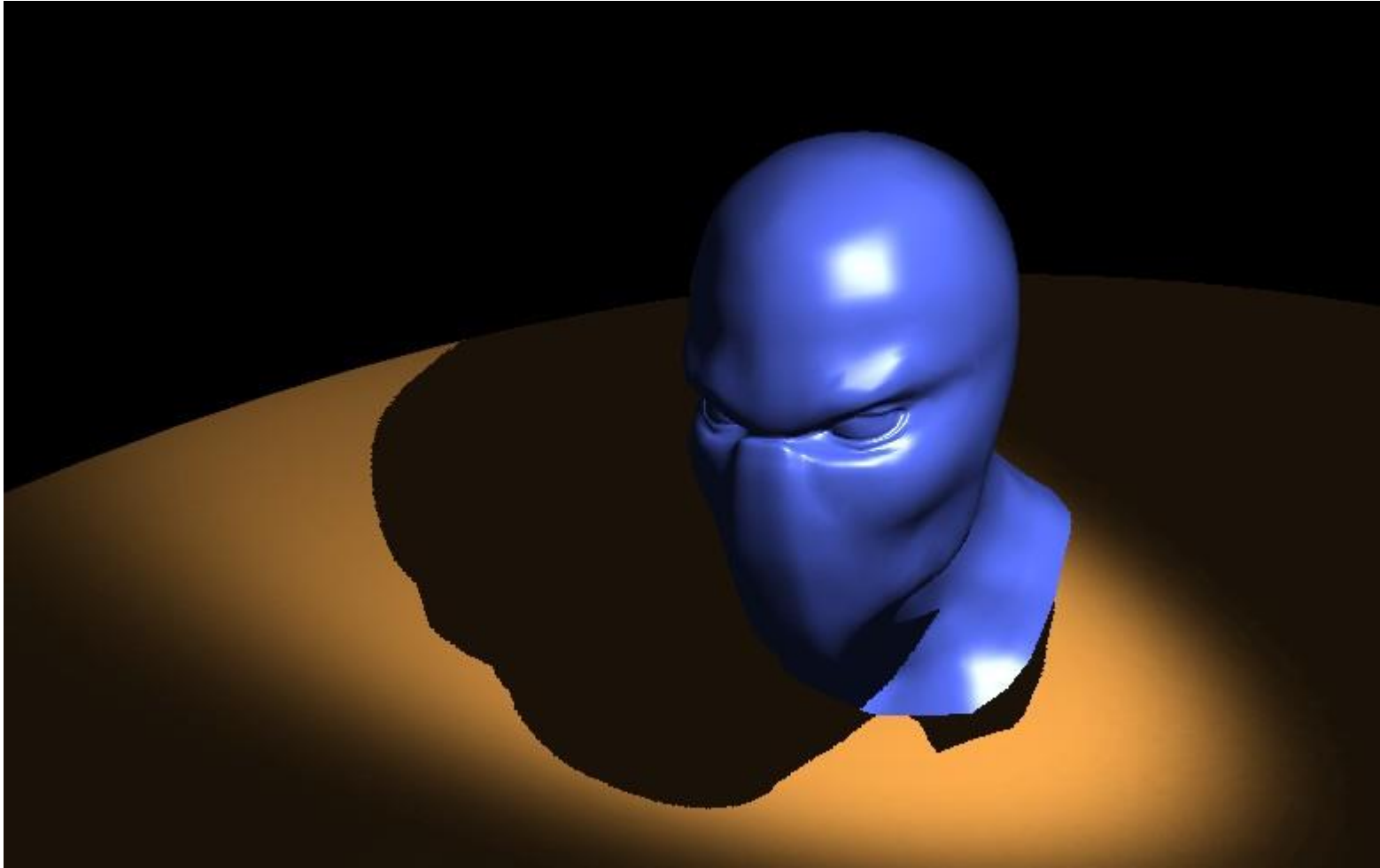
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- For the Picture, a shadow map is formed by storing the depths to the surface; on the right, the eye is shown looking at two locations.
  - The sphere is hit at point  $Va$ , and this point is found to be located at texture position  $a$  on the shadow map. The depth stored in  $a$  is not less than point  $Va$  is from light, so the point is not in shadow;
  - For point  $Vb$  distance from point light is farther than stored in shadow map, so the point is in shadow.



# Shadow map

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# Shadow map

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- Advantages

- Most hardwares directly support shadow map, and it can be used to render arbitrary geometry.
- It is fast. The cost of building the shadow map is linear to the number of rendered primitives and access time is constant.

- Disadvantages

- Because shadow map is image-based, so the quality depends on the resolution of the shadow map, and the numerical precision of the Z-buffer.



# Shadow map

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- Shadow map Problems

- If the epsilon value for comparison is low, it produces a pattern on object's surfaces ( see Fig a ) .
- If the epsilon value is set too high, we will see shadow “creeps” from under the block object(see Fig b).

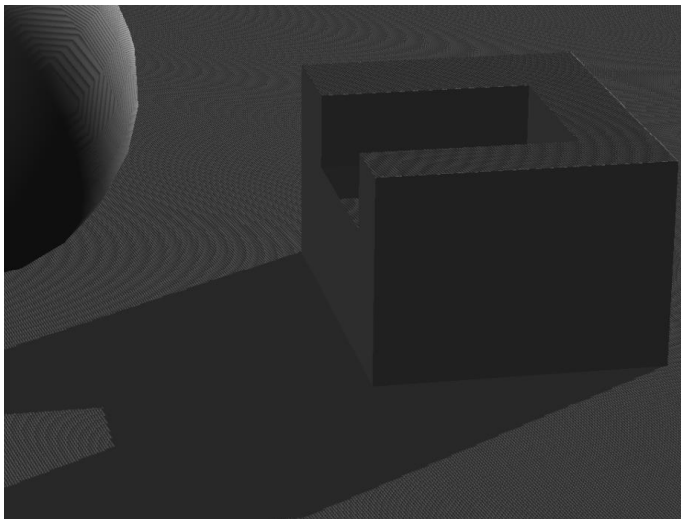


Fig a

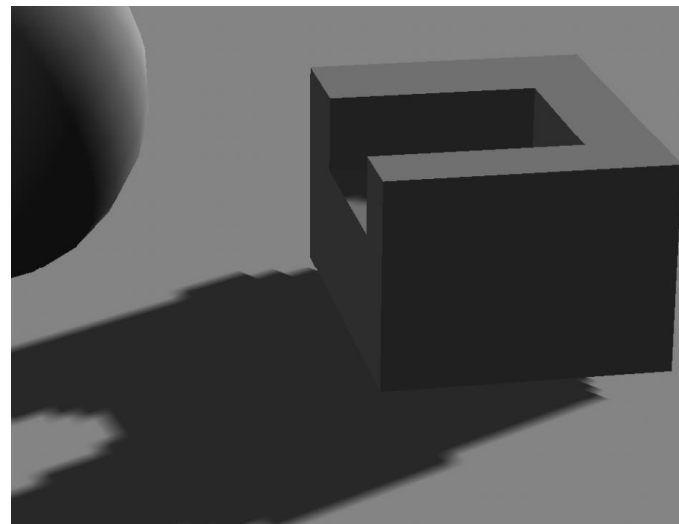
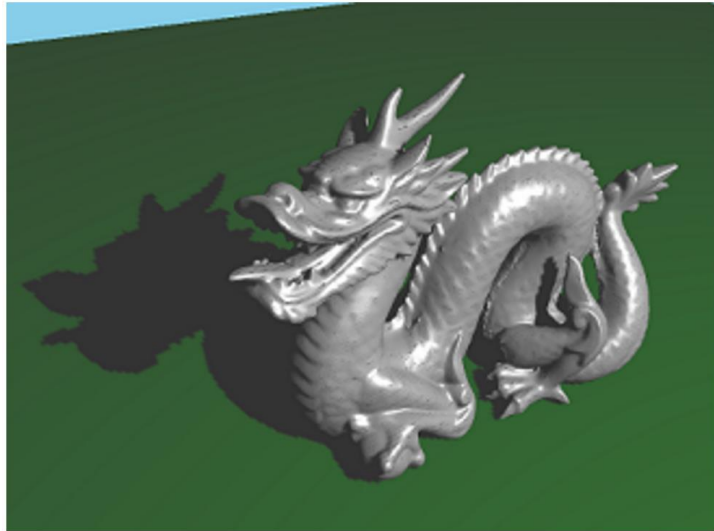


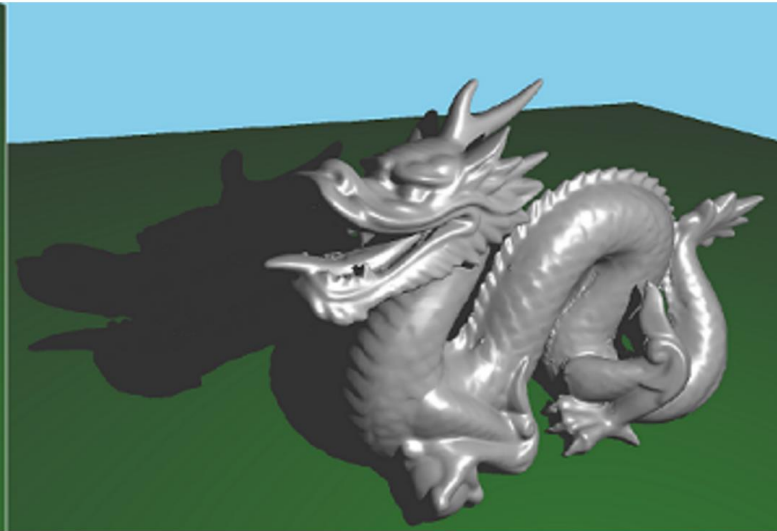
Fig b

# Shadow map & Shadow Volume

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Shadow map



Shadow Volume

# Shadow map

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- Some conclusion

- Shadow map and shadow volume are the most widely used shadow generation methods(especially, shadow map is used more).
- There are various extensions for these 2 techniques.
- For more information:
  - nVidia/ATI websites
  - <http://www.realtimerendering.com>
  - SIGGRAPH , SIGGRAPH Asia and Eurographics websites





# Reference

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- [http://courses.csail.mit.edu/6.837/F06-www/lectures/22\\_shadows.pdf](http://courses.csail.mit.edu/6.837/F06-www/lectures/22_shadows.pdf)
- *J.-M. Hasenfratz, M. Lapierre, N. Holzschuch, F.X. Sillion* [A survey of Real-Time Soft Shadows Algorithms](#)
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- *Xiao-Hua Cai, Yun-Tao Jia, Xi Wang, Shi-Min Hu and Ralph R. Martin* [Rendering Soft Shadows using Multi-layered Shadow Fins](#)
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- Ren Ng, Ravi Ramamoorthi and Pat Hanrahan [All-Frequency Shadows Using Non-linear Wavelet Lighting Approximation](#)
- *Kun Xu, Yun-Tao Jia, Hongbo Fu, Shi-Min Hu and Chiew-Lan Tai* [Spherical Piecewise Constant Basis Functions for All-Frequency Precomputed Radiance Transfer](#)



# Reference

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- <http://www.realtimerendering.com>
- <http://www.nvidia.com/page/home.html>
- <http://ati.amd.com/products/index.html>
- <http://www.siggraph.org>
- <https://www.eg.org/>
- [http://developer.nvidia.com/object/shadow\\_mapping.html](http://developer.nvidia.com/object/shadow_mapping.html)
- Lance Williams [Casting curved shadows on curved surfaces](#)
- [http://developer.nvidia.com/object/doc\\_shadows.html](http://developer.nvidia.com/object/doc_shadows.html)

