Problem 1. (Sine Function) Implement the function sin() in sin.py that calculates the sine of the argument x in radians, using the formula:

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \cdots$$

Hint: In order to avoid the inaccuracies caused by computing with huge numbers, follow the approach described on page 97 of the IPP text for computing the function e^x .

```
$ python3 sin.py 60
0.8660254037844385
0.8660254037844386
```

Problem 2. (Euclidean Distance) Implement the function distance() in distance.py that returns the Euclidean distance between the vectors x and y represented as one-dimensional lists of floats. The Euclidean distance is calculated as the square root of the sums of the squares of the differences between the corresponding entries. You may assume that x and y have the same length.

```
$ python3 distance.py 5
-9 1 10 -1 1
-5 9 6 7 4
13.0
```

Problem 3. (*Palindrome*) Implement the function is_palindrome() in palindrome.py that returns true if the argument s is a palindrome (ie, reads the same forwards and backwards), and False otherwise. You may assume that s is all lower case and that it doesn't have any whitespace characters.

```
$ python3 palindrome.py bolton
False
$ python3 palindrome.py amanaplanacanalpanama
True
```

Problem 4. (*Reverse*) Implement the function reverse() in reverse.py that reverses the one-dimensional list a in place, ie, without creating a new list.

```
$ python3 reverse.py
to be or not to be that is the question
<ctrl-d>
question the is that be to not or be to
```

Problem 5. (*Transpose*) Implement the function transpose() in transpose.py that creates and returns a new matrix that is the transpose of the matrix represented by the argument a. Note that a need not have the same number rows and columns. Recall that the transpose of an m-by-n matrix A is an n-by-m matrix B such that $B_{ij} = A_{ji}$, where $1 \le i \le n$ and $1 \le j \le m$.

```
$ python3 transpose.py
2 3
1 2 3
4 5 6
1.0 4.0
2.0 5.0
3.0 6.0
```

Files to Submit

- 1. sin.py
- 2. distance.py
- 3. palindrome.py

- 4. reverse.py
- 5. transpose.py

Before you submit:

• Make sure your programs meet the input and output specifications by running the following command on the terminal:

```
$ python3 run_tests.py -v [problems>]
```

where the optional argument cproblems> lists the problems (Problem1, Problem2, etc.) you want to test, separated by spaces; all the problems are tested if no argument is given.

• Make sure your programs meet the style requirements by running the following command on the terminal:

```
$ pycodestyle codestyle
```

where cprogram> is the .py file whose style you want to check.