

We have $2020 = 2^3 \cdot 5 \cdot 101$. There are 4 ways to choose which of a, b, c, and d have each of the common factors, for a total of 256 solutions.