

We have  $2020 = 2^2 \cdot 5 \cdot 101$ . There are 4 ways to choose which of a,b,c, and d have each of the common factors, for a total of 256 solutions.