

# <sup>1</sup> Beam Position Reconstruction for the g2p Experiment <sup>2</sup> in Hall A at Jefferson Lab

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## **14 Abstract**

Beam-line equipment was upgraded for experiment E08-027 (g2p) in Hall A at Jefferson Lab. Two beam position monitors (BPMs) were necessary to measure the beam position and angle at the target. A new BPM receiver was designed and built to handle the low beam currents (50-100 nA) used for this experiment. Two new super-harps were installed for calibrating the BPMs. In addition to the existing fast raster system, a slow raster system was installed. Before and during the experiment, these new devices were tested and debugged, and their performance was also evaluated. In order to achieve the required accuracy (1-2 mm in position and 1-2 mrad in angle at the target location), new methods were developed for analyzing the data of the BPMs and harps, as well as reconstructing the beam position and angle event by event at the target location. The calculated beam position will be used in the data analysis to accurately determine the kinematics for each event.

<sup>15</sup> *Keywords:* g2p; BPM; raster; beam position

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16     **1. Introduction**

17     A polarized ammonia ( $NH_3$ ) target was used for the first time in Hall A for  
18     the g2p experiment [1]. It operated at a low temperature of 1K and a strong  
19     transverse magnetic field of either 5 T or 2.5 T. A high electron beam current  
20     would cause significant target polarization drop due to target temperature rising  
21     and ionization radiation to the target material [2]. To minimize depolarization,  
22     the beam current was limited to below 100 nA and a raster system was used  
23     to spread the beam spot out to a larger area. The transverse magnetic field  
24     in the target region would cause the beam to be deflected downward when the  
25     beam enters the target region. To compensate for this, two chicane magnets  
26     were placed in front of the target to pre-bend the beam upwards. Due to the  
27     low beam current and tight space limitations after the chicane magnets, the  
28     experimental accuracy goals for the position (1-2 mm) and angle (1-2 mrad) at  
29     the target were challenging to achieve. New beam-line devices and an associated  
30     readout electronics system were designed for the g2p experiment to accomplish  
31     these goals. Design details and the performance of the beam-line devices will  
32     be described in the following sections along with a discussion of a new analysis  
method determine the beam position and direction.

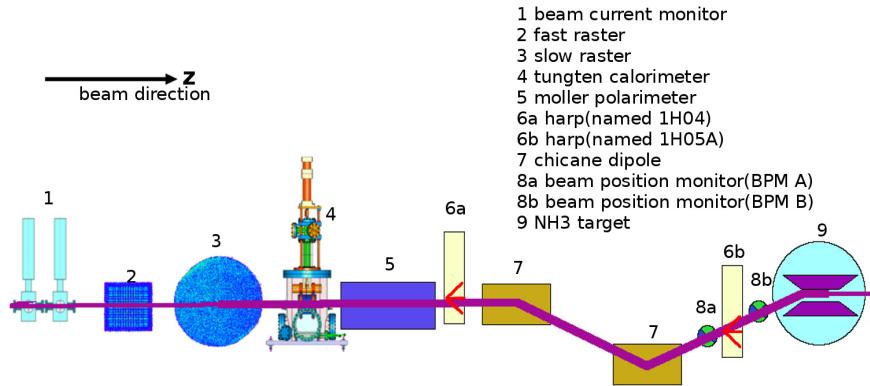


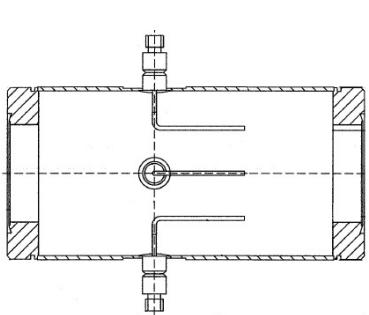
Figure 1: Schematic of beamline components for g2p experiment

34    **2. Beam-line Instrumentation**

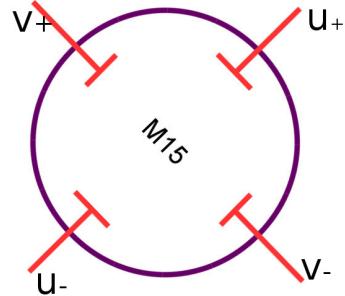
35    *2.1. Beam position monitor (BPM)*

36    The scattering angle of the outgoing lepton in deep inelastic scattering, which  
37    is defined with respect to the direction of the incident beam, is an important  
38    variable for obtaining meaningful physics results. Therefore, the position and  
39    direction of the beam, after being bent by the chicane magnetic field and spread  
40    out by the rasters, must be measured precisely. Two BPMs and two harps were  
41    installed for relative and absolute measurements of beam position and direction  
42    near the target, respectively.

43    The BPM consists of four open-ended antennas for detecting the beam po-  
44    sition; the measurement is non-invasive to the beam. The BPM chambers  
45    shown in Fig.2 are part of the beam pipe. The four antennas are attached  
46    to feedthroughs on the interior wall of the pipe at  $90^\circ$  intervals. The BPM



(a) BPM design diagram, from JLab in-  
strumentation group



(b) BPM chamber which contains 4 an-  
tennas

Figure 2: BPM chamber

46  
47    chambers are inclined  $45^\circ$  with the global Hall coordinate. In order not to con-  
48    fuse with the direction in the Hall coordinate, two antennas are marked as  $u_+$   
49    and  $u_-$ , which are used to determine the beam position in  $u$  direction. An-  
50    other two are marked as  $v_+$  and  $v_-$ . When the beam passes through the BPM  
51    chamber, each antenna receives an induced signal. The BPM front-end receiver

52 collects and sends the signal to the regular Hall A DAQ system and another  
53 DAQ system designed for parity violation experiments, the HAPPEX system  
54 [3]. The new BPM receiver was designed by the JLab instrumentation group  
55 [4] in order to achieve the required precision at a level of 0.1 mm with a beam  
56 current as low as 50 nA. The regular DAQ system was connected to a 13-bit  
57 fastbus ADC (Lecroy ADC 1881) with an integration time of 50 ns, which was  
58 triggered by a scattered electron event. The HAPPEX system was connected  
59 to an 18-bit ADC with an integration time of 875  $\mu$ s, which was triggered by a  
60 beam helicity signal at 1 kHz. The amplitude,  $A$ , recorded in the ADC has the  
61 following relation with the BPM signal,  $\phi$ :

$$A \propto \phi \cdot 10^{g/20}, \quad (1)$$

62 where  $g$  is the gain of the receiver.

63 The BPM receiver generates a large time delay for the output signals. The  
64 digital filter used in the receiver contributes 1/175 s delay time, which was the  
65 inverse of the bandwidth setting chosen for the filter. There is a  $\sim 4 \mu$ s delay  
66 as a result of finite processing times. The BPM can not provide event by event  
67 position because of this time delay, due to the 25 kHz fast raster system.

68 Because of the space limitation between the second chicane magnet and the  
69 target, the two BPMs were placed close to each other. One was placed 95.5 cm  
70 upstream of the target while the other was placed 69 cm upstream, making the  
71 distance between them only 26.5 cm. The short distance magnified the position  
72 uncertainty from the BPMs to target.

73 *2.2. Super harp*

74 Two super harps were designed and installed in the beam-line, as shown in  
75 Fig.1 (label 6a - 1H04 and 6b - 1H05A), to provide an absolute measurement  
76 of the beam position for calibration of the BPMs. The new harps were able to  
77 work in pulsed beam (1% duty factor) with a current of several  $\mu$ A. A diagram  
78 for the harp is shown in Fig.3,

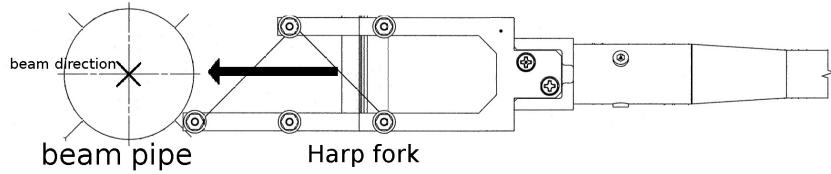


Figure 3: Harp diagram

79 which consists of three wires with a thickness of  $50 \mu\text{m}$ , a fork and a controller  
 80 chassis. The harp chamber is perpendicular to the beam pipe and connected  
 81 to the beam pipe as part of the vacuum chamber of the beamline. The two  
 82 harps have different configurations of three wires: vertical(|), bank left(\), and  
 83 bank right(/) for 1H04, and /, |, \ for 1H05. The angle of the / or \ wires is  
 84  $45^\circ$  relative to the wire dock frame. The wires are arranged in a fork (Fig.3)  
 85 controlled by a step motor [5] which can be moved in and out of the beam-line.  
 86 The harps must be moved out of the beam-line when production data is being  
 87 taken because they are invasive to the beam. The original position of the wires  
 88 was surveyed before the experiment at a precision level of  $0.1 \text{ mm}$ . As the motor  
 89 driver moved the fork through the beam, each wire received a signal, which was  
 90 recorded for further analysis. The signals received from the wire and the step-  
 91 counters from the motor driver were then sent to an amplifier and the DAQ.  
 92 The amplification and the speed of the motor were adjustable for the purpose  
 93 of optimizing the signals of each scan. Recorded data combined with the survey  
 94 data was used to calculate the absolute beam position.

95 The signal from the | wire ( $\text{peak}_{|}$ ) was used for getting the  $x$  position ( $x_{\text{harp}}$ )  
 96 of the beam , and the signals from the /, \ wires ( $\text{peak}_{/}$  and  $\text{peak}_{\backslash}$ ) were used  
 97 for getting the  $y$  position ( $y_{\text{harp}}$ ):

$$\begin{aligned}
 x_{\text{harp}} &= \text{survey}_{|} - \text{peak}_{|} \\
 y_{\text{harp}} &= \frac{1}{2}[(\text{survey}_{\backslash} - \text{survey}_{/}) - (\text{peak}_{\backslash} - \text{peak}_{/})]
 \end{aligned} \tag{2}$$

98      *2.3. Raster system*

99      In order to minimize the depolarization, avoid damage to the target material  
100     from radiation, and reduce systematic error for the polarization measurement  
101     by NMR (The polarization of the  $NH_3$  target was measured by a NMR coil  
102     which installed inside the target cell [6]. The non-uniformity of depolarization  
103     could reduce the precision of the NMR measurement due to the measurement  
104     being an average over the target), two raster systems were installed at  $\sim 17$  m  
105     upstream of the target, as shown in Fig.1 (labels 2 and 3 for fast and slow rasters,  
106     respectively). Both the fast and slow rasters consist of two dipole magnets. The  
107     same triangular waveforms with frequency of 25 kHz were used to drive the  
108     magnet coils of the fast raster to move the beam in x and y directions, forming  
109     a rectangular pattern of  $2\text{ mm} \times 2\text{ mm}$ , as shown in Fig.4.

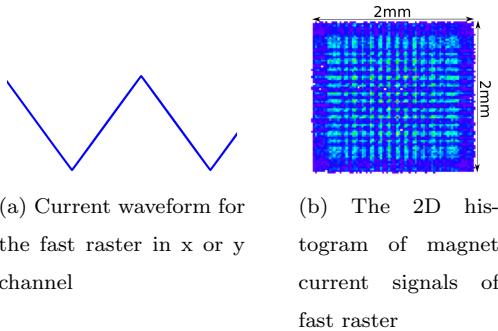


Figure 4: Fast raster pattern

109  
110     A dual-channel function-generator<sup>1</sup> was used to generate two independent  
111     waveforms to drive the magnet coils of the slow raster. The waveforms for the  
112      $x$  and  $y$  directions are:

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<sup>1</sup>agilent 33522A function generator, <http://www.home.agilent.com/en/pd-1871286-pn-33522A/function-arbitrary-waveform-generator-30-mhz>

$$\begin{aligned} x &= A_x t^{1/2} \sin(\omega t), \\ y &= A_y (t + t_0)^{1/2} \sin(\omega t + \phi), \end{aligned} \quad (3)$$

113 where the  $A_x$  and  $A_y$  are the maximum amplitude,  $t_0$  and  $\phi$  are the AM and  
sin phase difference between  $x$  and  $y$  waveform, respectively. Both of them

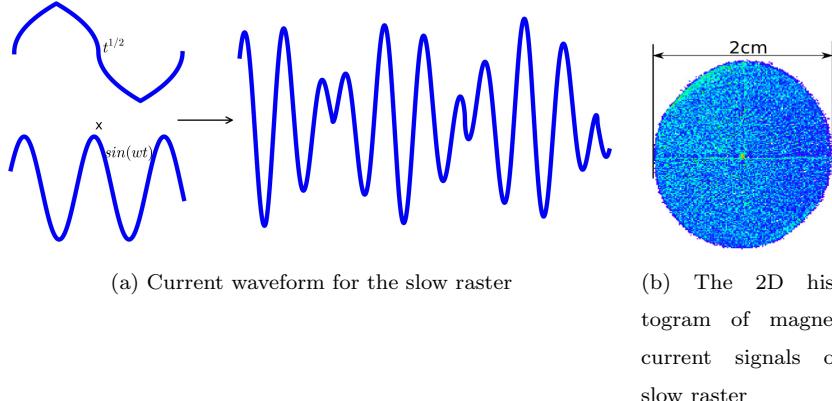
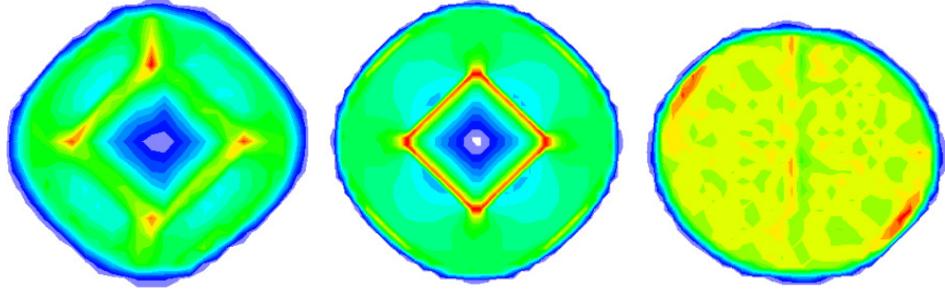


Figure 5: Slow raster pattern

114  
115 are sine functions modulated by a function  $t^{1/2}$  in order to generate a uniform  
116 circular pattern [7], as shown in Fig.5. The frequency of the  $x$  and  $y$  waveforms  
117 kept same:  $\omega = 99.412$  Hz. In order to cycle the amplitude modulation (AM)  
118 function, four piece-wise functions are combined together. The first term is  $t^{1/2}$ ,  
119 and the second term is  $period - t^{1/2}$ , and so on for the third and fourth terms.  
120 The cycled function has the frequency of 30 Hz.

121 The  $\phi$  was locked to  $\frac{\pi}{2}$  by the function generator, while the  $t_0$  was manually  
122 adjusted to 0. Non-zero  $t_0$  could cause a non-uniformity pattern, as shown in  
123 Fig.6(a), which would cause non-uniformity beam distribution. A simulation  
124 was reproduced the non-uniformity by setting the  $t_0$  to non-zero, as shown  
125 in Fig.6(b). The  $t_0$  was carefully adjusted and minimized before production  
126 data taking to avoid the non-uniformity. The pattern of the spread beam was  
127 relatively uniform after this adjustment during the experiment, as shown in  
128 Fig.6(c).



(a) Raster pattern with  $t_0 \neq 0$  (b) Simulated raster pattern, (c) Manually adjust  $t_0$  to 0 with  $t_0 \neq 0$

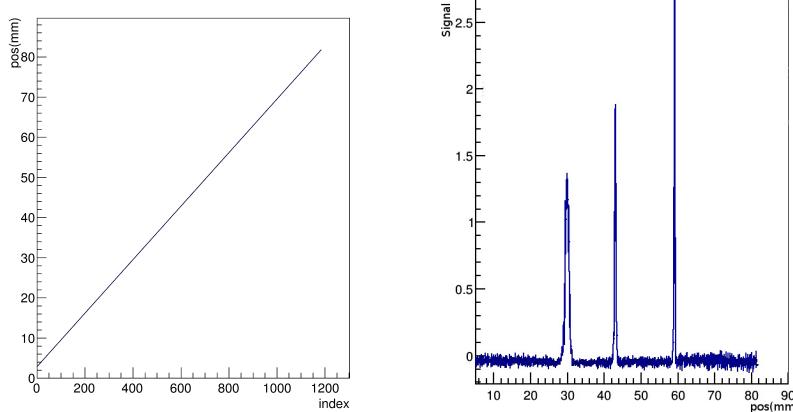
Figure 6: None-zero  $t_0$  caused slow raster non-uniformity, (a) and (c) are from the data, (b) is simulated.

### 129 3. Data analysis

#### 130 3.1. Harp scans for measuring absolute beam position

131 An example of a harp scan result is shown in Fig.7. There are three groups of  
 132 recorded data for each harp scan, which are “index”, “position”, and “signal”.  
 133 The index is related to the moving steps of the fork during the scan. Each  
 134 step of the index increases by 0.008-0.07 mm depending on the speed of the  
 135 motor driver [5]. The position is the wire location for each index. The testing  
 136 results show a good linear relation between the position and the index as shown  
 137 in Fig.7(a), because the motor speed is uniform. The line is the fitted result  
 138 with  $pos = a * index + b$ . According to this linear relation, interpolation or  
 139 extrapolation can be applied when a few data points are missing, in some cases.  
 140 The strength of signal vs. position is plotted in Fig.7(b). Each peak represents  
 141 the location when one of the three wires passed through the beam.

142 The positions measured by the two harps were used for calibrating the beam  
 143 positions in the two BPMs. When the chicane magnets were on, beam did not  
 144 pass straight through from the first harp to the second harp. BPM calibrations  
 145 using two harps were only possible when the chicane magnets were off, i.e. in the  
 146 straight-through settings. Since the BPM was calibrated in the local coordinate



(a) position vs index for harp scan, used for extending position record

(b) Signal vs position for harp,  $x$  axis is position,  $y$  axis is the strength of signal. The unit of signal strength is the ADC unit.

Figure 7: 1H05A harp scan data

147 system, the calibration constants were independent from the settings of other  
 148 instruments. To make sure that the calibration constants for the BPMs were  
 149 still valid during the non-straight-through settings, the settings for the BPM  
 150 receiver were kept the same as in the straight-through settings during production  
 151 running.

152 The scan data from the harps was not reliable when the current of CW beam  
 153 (100% duty factor) was lower than 100 nA due to the low signal-to-noise ratio.  
 154 The harp scans were taken in pulsed mode at a current of a few  $\mu$ A, while the  
 155 BPMs were used for production data taking in CW mode at a beam current  
 156 of 50-100 nA. For a BPM calibration run, a harp scan was done first in pulsed  
 157 mode, then a DAQ run was taken immediately to record the ADC value in CW  
 158 mode without changing the beam position. The harp scan was then taken again  
 159 in the pulsed mode to double check the beam position. The harp scan data was  
 160 discarded and the scan was taken again if the beam position changed.

161    3.2. BPM data analysis and calibration

162    The traditional difference-over-sum (diff/sum) method to calculate the beam  
 163    position has the non-linearity effect in the position far away from the center of  
 164    the beam pipe [8]. It is necessary to correct the equation of diff/sum since we  
 165    have a slow raster. The signal from each antenna excited by the beam can be  
 166    calculated via image charge method (Fig. 8) [9, 10] :

$$\phi_i = \phi_0 I \frac{R^2 - \rho^2}{R^2 + \rho^2 - 2R\rho\cos(\theta_i - \theta_0)}, \quad (4)$$

167    where  $\phi_i$  is the signal received in the antenna, and  $i$  is  $u_+$ ,  $u_-$ ,  $v_+$  and  $v_-$ ,  
 168    respectively,  $\phi_0$  is a constant related to the geometry of the BPM-chamber and  
 169    the output resistance,  $I$  is the beam current,  $R$  is the radius of the BPM vacuum  
 170    chamber,  $\rho$  is the radial position of the beam, and  $\theta_i - \theta_0$  is the angle difference  
 between the antenna and the beam in the polar coordinate .

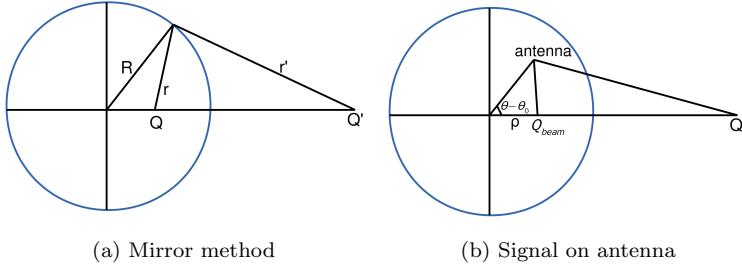


Figure 8: Signal for each antenna of BPM

171  
 172    In order to extract the beam position information, and eliminate the de-  
 173    pendence on the beam current in equation (4), the diff/sum method is used as  
 174    follows:

$$D_U = \frac{\phi_{U+} - \phi_{U-}}{\phi_{U+} + \phi_{U-}}, \quad (5)$$

175    where  $U$  is  $u$  and  $v$ , respectively. Substituting equation (4) into equation (5),  
 176    they can be rewritten as follows:

$$D_U = \frac{\phi_{U+} - \phi_{U-}}{\phi_{U+} + \phi_{U-}} = \frac{2}{R} \frac{\rho\cos(\theta - \theta_0)}{1 + \frac{\rho^2}{R^2}} = \frac{2}{R} \frac{U}{1 + \frac{\rho^2}{R^2}}, \quad (6)$$

177 where  $\rho^2 = u^2 + v^2$ . When  $u^2 + v^2 \ll R^2$ , equations (6) can be simplified as:

$$U \approx \frac{R}{2} D_U = \frac{R}{2} \frac{\phi_{U+} - \phi_{U-}}{\phi_{U+} + \phi_{U-}}. \quad (7)$$

178 Equation (7) can be used in the simple case when the beam is near the center  
 179 of the beam pipe. When the beam is far from the center, equation (7) is no  
 180 longer valid. For the g2p experiment, the beam was rastered to have a diameter  
 181 of about 2 cm at the target. From equation (6) the beam position can be  
 182 calculated as:

$$U = RD_U \left( \frac{1}{D_u^2 + D_v^2} - \frac{1}{\sqrt{D_u^2 + D_v^2}} \sqrt{\frac{1}{D_u^2 + D_v^2} - 1} \right). \quad (8)$$

183 To verify this corrected equation, a simulation was performed. First, a set  
 184 of position data was generated (Fig.9(a)), and the designed radius for the BPM  
 185 chamber was used for  $R$ . Using equation (4) to get the signal for each antenna,  
 186 and setting  $\phi_0$  and  $I$  to be equal to 1, equations (8) and (7) were used to  
 187 calculate the beam position for comparison. The results are shown in Fig.9(b)  
 and 9(c), respectively.

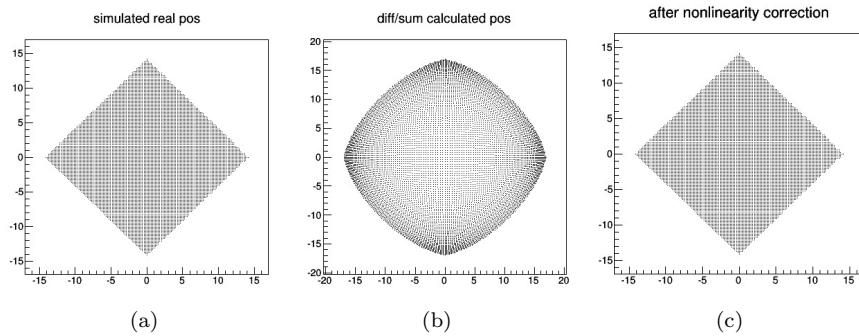


Figure 9: Comparing the calculated results using equation (7) and (8) with simulated position.  
 (a) Simulated position; (b) The calculated result with equation (7), (c) The calculated result with equation (8).

188  
 189 The corrected equation is also tested by using the experiment data and  
 190 the benchmark test data. Fig.10(a) shows the difference between the position  
 191 calculated from the corrected equation (8) and the one from the diff/sum equa-  
 192 tion (6). Fig.10(b) shows the comparison with the real beam position from the

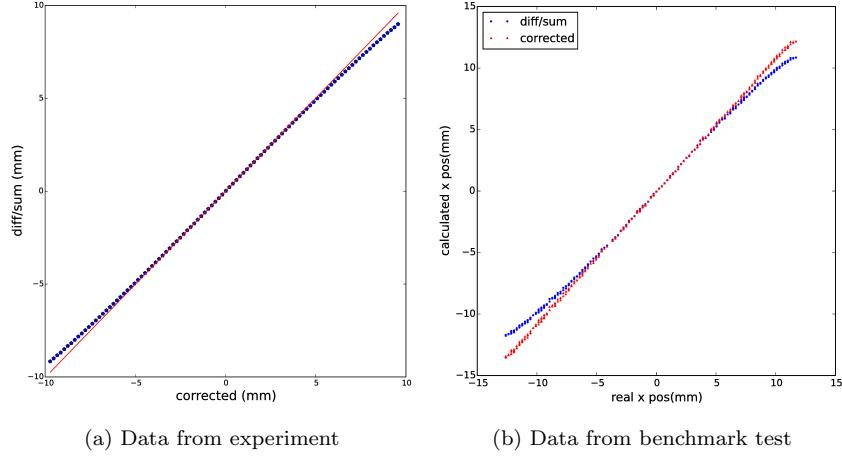


Figure 10: BPM non-linearity correction. (a) Relationship between the position calculated from diff/sum equation (6) (y axis) and the one from corrected equation (8) (x axis). Red solid line is a reference line came from linear fit for the center points . Data is collected from experiment. (b) Comparison between the diff/sum equation (6) and the corrected equation (8) using the benchmark test data. The x axis is the real beam position. The red triangles are the positions calculated from corrected equation (8). The blue circles are the positions calculated from diff/sum equation (6) .

193 benchmark test data. In this way the method using equation (8) can correct the  
 194 non-linearity effect caused by the diff/sum method. The handling of the BPM  
 195 information which only used for the center beam position (discussed in chapter  
 196 3.4) also reduced this non-linearity effect.

197 The final information recorded in the data-stream was designed to have a  
 198 linear response with the raw signal in the 50-100nA current range. The  $\phi_i$  in  
 199 equation (6) can be rewritten as:

$$\phi_i = a_i(A_i - A_{i,ped} + b_i), \quad (9)$$

200 where  $A_i$  and  $A_{i,ped}$  are the recorded ADC value and pedestal value, and  $a_i$  and  
 201  $b_i$  are the slope and intercept of the relationship between  $\phi_i$  and  $A_i - A_{i,ped}$ .  
 202 Equation (7) can be rewritten as:

$$D_U = \frac{(A_{U+} - A_{U+ped} + b_{U+}) - h_u(A_{U-} - A_{U-ped} + b_{U-})}{(A_{U+} - A_{U+ped} + b_{U+}) + h_u(A_{U-} - A_{U-ped} + b_{U-})}, \quad (10)$$

203 where  $h_u = a_{U-}/a_{U+}$ , and is related to the ratio of the signals for the  $U_+$  and  
204  $U_-$  antennas and the gain settings of the two channels.

205 Combining the equation (9) and (4), the calibration constant  $b_i$  was obtained  
206 by taking the linear fit between the ADC values of BPM and the beam current  
207 with a group of runs with the same beam position but different values of beam  
current:  $I \propto (A_i - A_{i-ped} + b_i)$ . Figure 11 shows the  $A_i - A_{i-ped}$  versus the beam

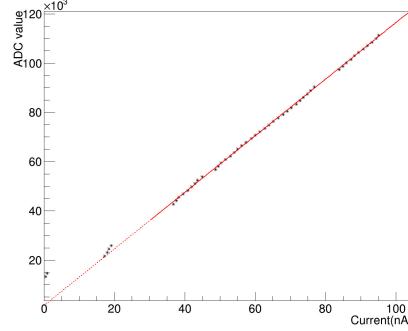


Figure 11: ADC value of BPM raw signal ( $A - A_{ped}$ ) V.S. current

208  
209 current. It can be seen that the ADC values were linear with beam current in  
210 the considering current range of 50-100 nA. The intercept from the linear fit of  
211 Fig.11 is the value  $b_i$ .

212 By transporting the position  $x_{harp}$  and  $y_{harp}$  in equation (2) from two harps  
213 to the BPM local coordinate  $u_{harp}$  and  $v_{harp}$ , a fit between the BPM data  $U$   
214 and the harp data  $U_{harp}$  determined three calibration constants  $c_0$ ,  $c_1$  and  $c_2$ :

$$U_{harp} = U_c = c_0 + c_1 u + c_2 v, \quad (11)$$

215 where  $U_c$  is the calibrated BPM position. It was converted to Hall coordinate  $X_c$   
216 for further transporting to the target location. An calibration example is shown  
217 in Fig. 12. The asterisks in Fig. 12 represent  $U_{harp}$ , and the dots represent  $U$ .

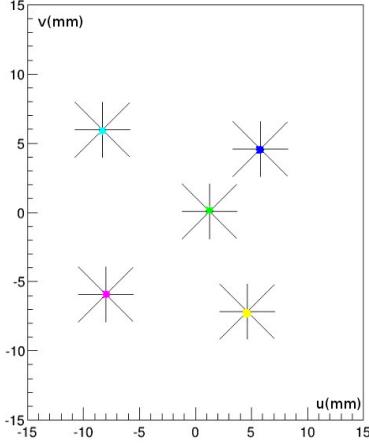


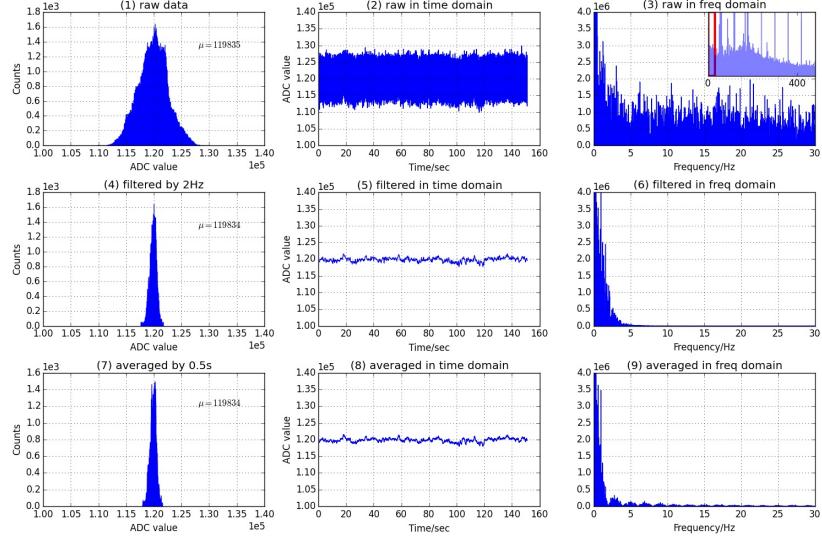
Figure 12: Harp scan data combined with BPM data, the asterisks are the positions from harp, while the dots are from BPM.

218     In order to reduce the noise and improve the resolution during data analysis,  
 219     a software filter was applied. Since the 18 bit ADC was triggered by the helicity  
 220     signal with a fixed frequency, it could be regarded as a sampling ADC. Fig.13  
 221     shows the signal dealt with a 2 Hz low pass filter. The bottom 3 plots in Fig. 13  
 222     (a,b) are the averaged signal for comparing with the filtered signal. The average  
 223     procedure lead to the same result as the filter. The filter also erases the beam  
 224     displacement caused by the rasters, which is necessary to extract the position  
 225     of the beam center.

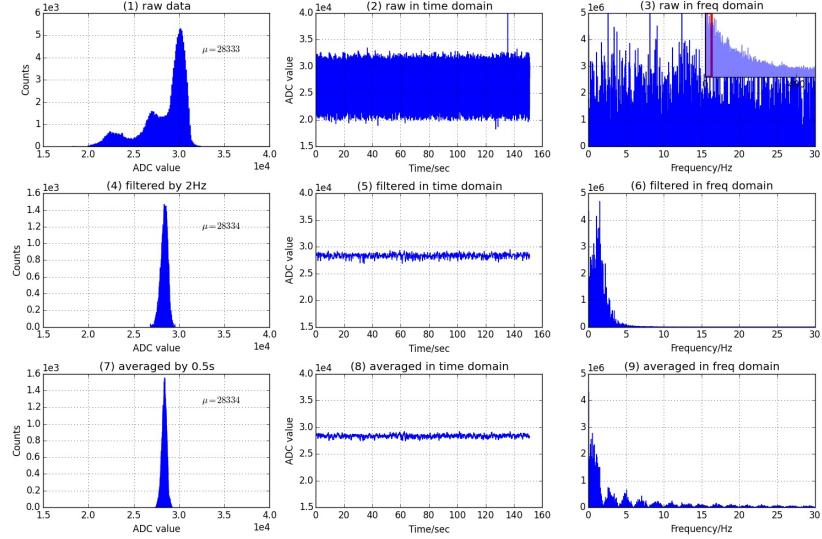
226     *3.3. Beam position reconstruction at the target*

227     It is easy to transport the position from the BPMs to the target by using a  
 228     linear transportation method for the straight through setting. For the settings  
 229     with a transverse magnetic field at the target, the linear transportation method  
 230     can not be used since the beam is bent near the target. A simulation package  
 231     was constructed to simulate the behavior of the beam. Polynomial curve fittings  
 232     were used for simulated data to generate the transport functions in order to  
 233     transport the beam from the two BPMs to the target (Fig.14).

234     A target magnet field map [11] was generated from the TOSCA model. To



(a) Normal run with beam



(b) Pedestal run without beam

Figure 13: Software filter applied to BPM signal. (a) is the signal with beam, (b) is the pedestal signal without beam. (1,2,3) in (a,b) are the raw signal without applying the filter, (4,5,6) are applied a 2Hz finite-impulse-response filter with 4th order. (7,8,9) are averaged with 0.5 s. (1,4,7) are the signal's 1-D histogram, (2,5,8) are the signal in time domain, (3,6,9) are in frequency domain. Note all of the plots in (a) is for a single signal, same as in (b).

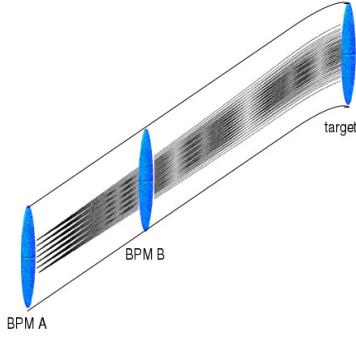


Figure 14: Transporting beam position from BPM to target with transverse target magnet field

235 test the accuracy of the TOSCA model, the target magnet field was measured  
 236 before the experiment [12, 13]. The generated field map was used in the simula-  
 237 tion. An event generator generated thousands of electrons with different initial  
 238 positions and angles, with the energy of the electrons set to the same values as  
 239 in the experiment. The Runge-Kutta method<sup>2</sup> with 0.02 mm step length was  
 240 used to generate the trajectories from BPM A to the target by using the field  
 241 map. Data extracted from the simulation was used as input for the polynomial  
 242 fitting:

$$\begin{bmatrix} x_{tgt} \\ y_{tgt} \\ \theta_{tgt} \\ \phi_{tgt} \end{bmatrix} = F\left(\begin{bmatrix} x_{BPMA} \\ y_{BPMA} \\ x_{BPMB} \\ y_{BPMB} \end{bmatrix}\right), \quad (12)$$

243 where  $F$  is the fitted polynomial transport function. The positions at the BPMs:  
 244  $x_{BPMA}$ ,  $y_{BPMA}$ ,  $x_{BPMB}$ ,  $y_{BPMB}$ , and the position and angle at the target:  
 245  $x_{tgt}$ ,  $y_{tgt}$ ,  $\theta_{tgt}$ ,  $\phi_{tgt}$ , are extracted from the simulated trajectory. In total, 24  
 246 different fits were taken for 4 different target positions and 6 configurations  
 247 with different target magnetic field and beam energy settings. The validity

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<sup>2</sup>[http://en.wikipedia.org/wiki/Runge-Kutta\\_methods](http://en.wikipedia.org/wiki/Runge-Kutta_methods)

248 of the transport functions was explored in the simulation using a new set of  
249 random trajectories generated in the same manner as those used in the fitting.  
250 The deviation between the fitted transport function and the simulation was less  
251 than 0.1%.

252 The transport functions were only used to transport the beam center position  
253 from the two BPMs to the target by applying the 2 Hz filter, which filtered out  
254 the fast raster and slow raster motion to keep only the beam center position.  
255 The transported position were expressed as  $X_{center}$ .

256 *3.4. Determining the beam position event-by-event*

257 The readout of the magnet current for the two rasters was connected to  
258 a series of ADCs. Two scintillator planes in the HRS form a DAQ trigger.  
259 This pulse signal triggered the ADC to record the raster magnet current for  
260 each event. The information from the rasters and the BPMs was combined  
261 to provide the beam position event-by-event. The position at the target was  
262 determined as:

$$X = X_{center} + X_{fstraster} + X_{slraster}, \quad (13)$$

263 where  $X_{fstraster}$  and  $X_{slraster}$  were the position displaced by the fast raster  
264 and slow raster, respectively, which were converted from the current values of  
265 the two raster magnets. The calibration of the conversion factors between the  
266 magnet current of the rasters and the displaced position will be discussed in the  
267 next subsection. An example of reconstructed beam position is shown in Fig.  
268 15.

269 *3.4.1. Conversion factor for the slow raster*

270 Two methods were used to calibrate the conversion factor for the slow raster.  
271 The first method used the calibrated BPM information, i.e., comparing the  
272 raster magnet current with the beam shape shown in the ADC of the BPMs.  
273 Several calibrations were taken during different run periods at a beam current of

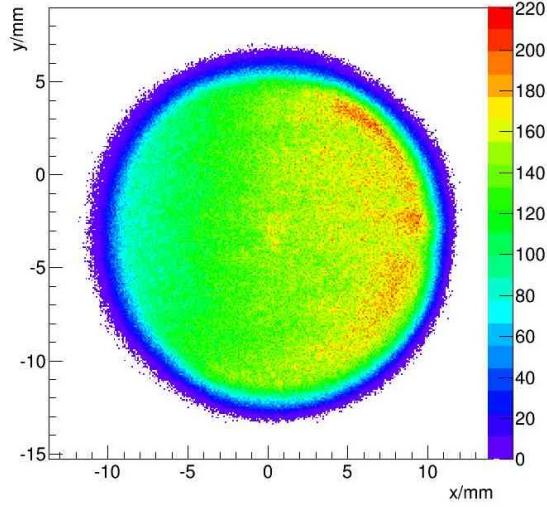


Figure 15: Reconstructed beam position at the target

274 100nA using different values of the raster magnet current, as shown in Fig.16(a).

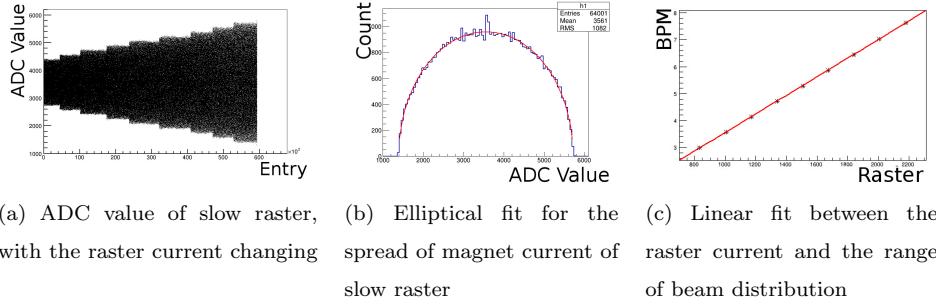


Figure 16: Converting the raster current to beam position shift

275

276 The range of the beam distribution at the target was calculated from the  
277 ranges at the two BPMs without applying the filter, using the transport func-  
278 tions fitted previously. The range of the beam distribution at the two BPMs  
279 and the amplitude of the raster current was calculated from an elliptical fit,  
280 an example is shown in Fig.16(b). Figure 16(c) shows a linear fit between the  
281 raster current and the range of the beam distribution at the target. The x axis

<sup>282</sup> in Fig.16(c) is the magnet current of the raster, and the y axis is the range of  
<sup>283</sup> the beam distribution obtained from the BPMs.

<sup>284</sup> The second method for calibrating the conversion factor used a target called  
“carbon hole” as shown in Fig.17(a).

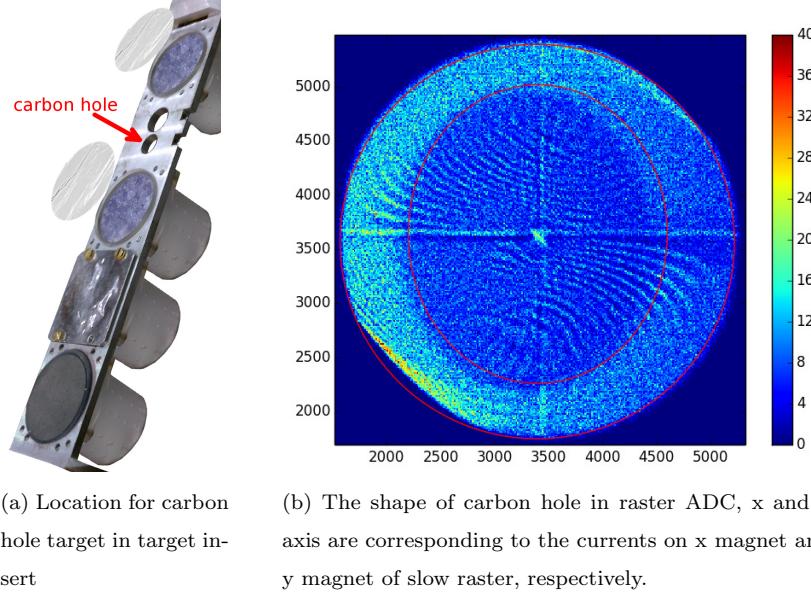


Figure 17: Carbon hole method to calibrate raster

<sup>285</sup>

<sup>286</sup> Scattered electrons were used as the trigger for recording the raster magnet  
<sup>287</sup> current. Since the density of the target frame was much higher than that of the  
<sup>288</sup> “hole”, which was submerged in liquid helium, the density of events triggered  
<sup>289</sup> from the target frame was much higher than that of the hole itself. Recorded  
<sup>290</sup> values reveal a hole shape as shown in Fig.17(b). The size of the carbon hole  
<sup>291</sup> was surveyed before the experiment, and a fit program was used to extract the  
<sup>292</sup> radius of the recorded hole shape for that raster current. The conversion factor  
<sup>293</sup>  $F$  was then calculated as the ratio of the size of the carbon hole  $S_{hole}$  and the  
<sup>294</sup> radius of the hole shape  $R_{hole}$  in the ADC:

$$F = \frac{S_{hole}}{2 * R_{hole}}. \quad (14)$$

295     3.4.2. *Conversion factor for the fast raster*

296     The conversion for the fast raster was the same as for the slow raster. The  
297     low pass filter for the BPM was set to a higher value than the frequency of the  
298     fast raster to see the beam shape at the BPM formed by the fast raster. For a  
299     higher frequency filter, a larger beam current was needed to get a clear pattern.  
300     The beam current chosen for calibrating the fast raster was near 300 nA, which  
301     was the safety limit for the target. The beam shape formed by the fast raster  
is shown in Fig.18.

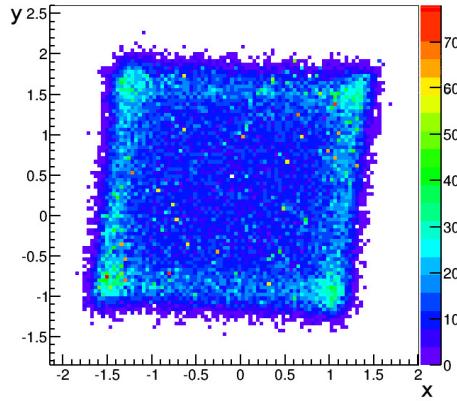


Figure 18: Beam shape formed by the fast raster at the BPM A location, the unit is millimeter

302

303     **4. Uncertainty**

304     The uncertainty of the final beam position at the target for each event con-  
305     tains several contributions:

- 306       • The first part comes from the uncertainty of the calibration constant. It  
307        includes the BPM resolution for the DAQ runs used for the calibration,  
308        the uncertainty of the harp data corresponding to each calibration, and  
309        the survey uncertainties for the BPMs and harps. It contributes about 0.7  
310        mm for the uncertainty of the position and 0.7 mrad for the uncertainty  
311        of the angle.

- The uncertainty on the pedestal is the largest uncertainty for the beam position measurement, contributing about 0.7~1.5 mm to the uncertainty of the position and 0.7~1.5 mrad to the uncertainty of the angle.
  - The uncertainties from the BPM survey need to be included, since the production data and the calibration data were taken at different beamline settings when the equipment was moved. They contribute 0.5 mm to the uncertainty of the position.
  - The uncertainty from the magnetic field map of the target was considered for the settings with the target magnet field.
  - The uncertainties due to the size conversion of the rasters were also included.
- The position uncertainty was magnified by a factor of 5 at the target because of the short distance between the two BPMs. For example, in the straight through setting, if the uncertainty at BPM A is 0.2 mm, and at BPM B is 0.27 mm, the uncertainty at the target is 1.1 mm for position and 1.3 mrad for angle. The uncertainty for the position at the target was around 1~2 mm, while the uncertainty for the angle was 1~2 mrad.

## 5. Summary

JLab g2p experiment used a transversely polarized  $NH_3$  target for the first time in Hall A. It put a limit of below 100 nA on the electron beam current and required a slow raster to spread beam to a large area. Two chicane magnets were used to compensate the strong transverse magnetic field. Beam-line equipment, including the BPMs, harps and associated readout system, were upgraded to allow precision measurements of the beam position at low current (50-100 nA). A software filter was used to reduce noise in the BPMs. A corrected equation was used to compensate the non-linearity caused by the diff/sum equation. The harp data and the linear fit between the bpm signal and the beam current were used to extract the calibration constant of the BPM. To account for the strong

340 target magnetic field effect, transport functions were generated to transport the  
341 beam position from the BPMs to the target. The beam position in the x-y plane  
342 and the angle at the target location are extracted event-by-event by combining  
343 information from the BPMs and the signals from the rasters. The performance  
344 of the new devices (BPMs, harps and slow rasters) were presented along with  
345 an analysis of systematic uncertainties.

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