

Deep learning

Episode 2, 2025

Deep learning whereabouts

A catch-all lecture in philosophy,
tricks and frameworks

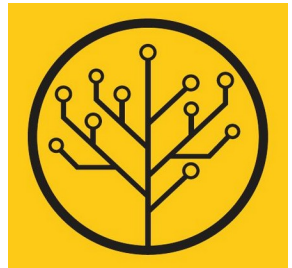


Yandex
Data Factory

LAMBDA

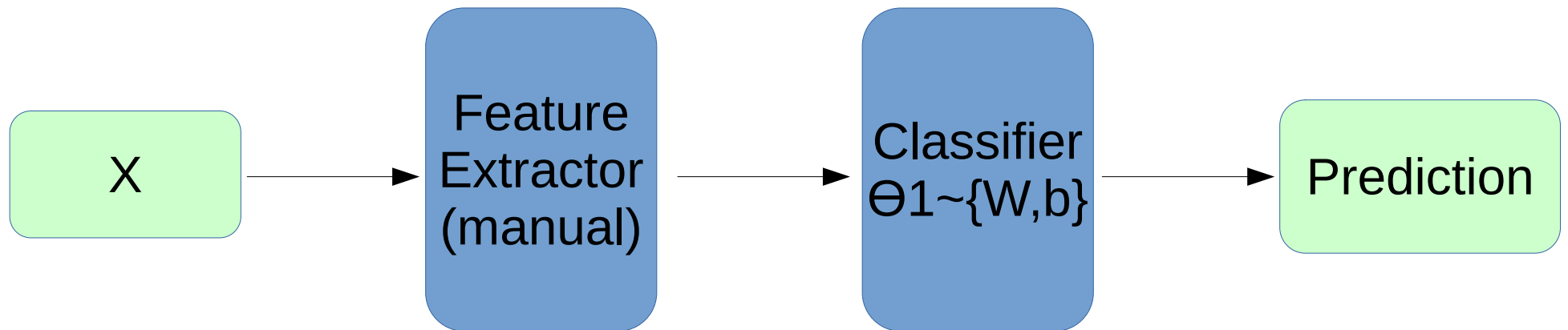


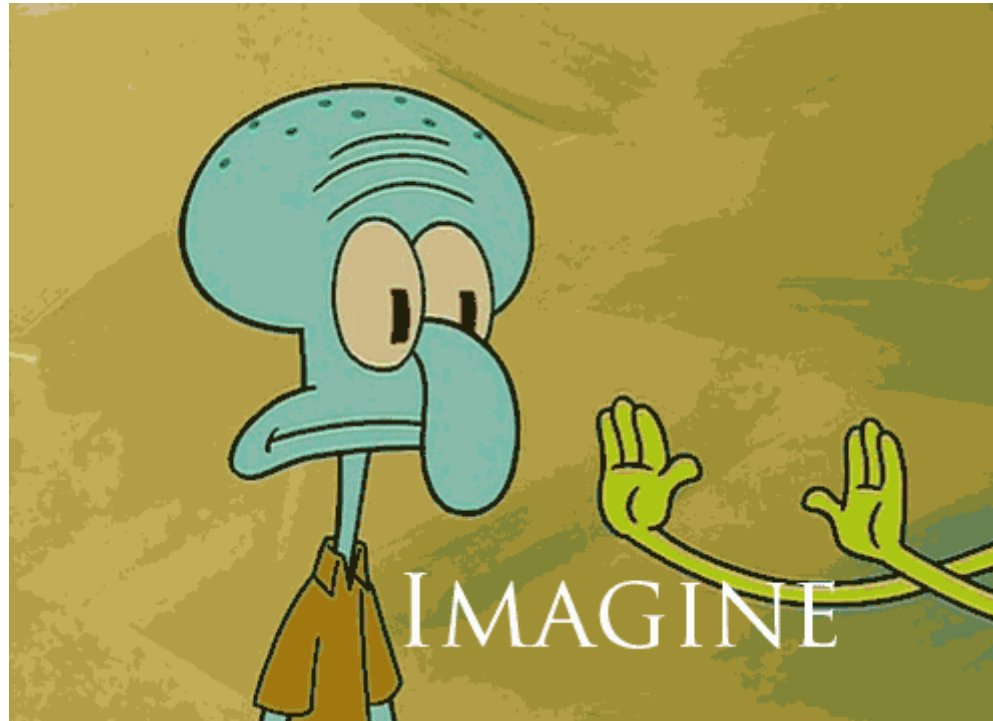
British Hedgehog
Preservation Society



Previously on deep learning...

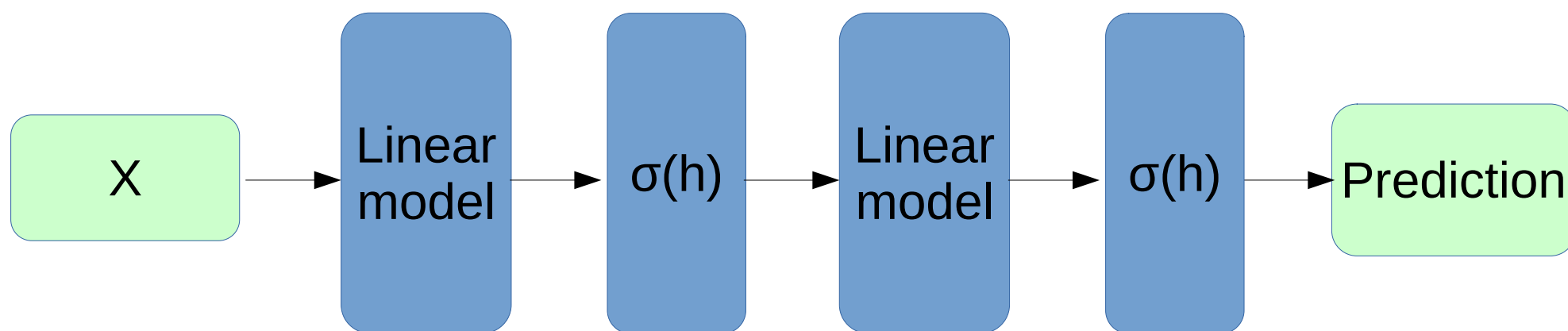
Feature extraction





Features would tune to your problem automatically!

Simple neural network



Trains with stochastic gradient descent!
or momentum/rmsprop/adam/...

Connectionist phrasebook

- Layer – a building block for NNs :
 - “Dense layer”: $f(x) = Wx+b$
 - “Nonlinearity layer”: $f(x) = \sigma(x)$
 - Input layer, output layer
 - A few more we gonna cover later
- Activation – layer output
 - i.e. some intermediate signal in the NN
- Backpropagation – a fancy word for “chain rule”

Backpropagation

TL;DR: backprop = chain rule*

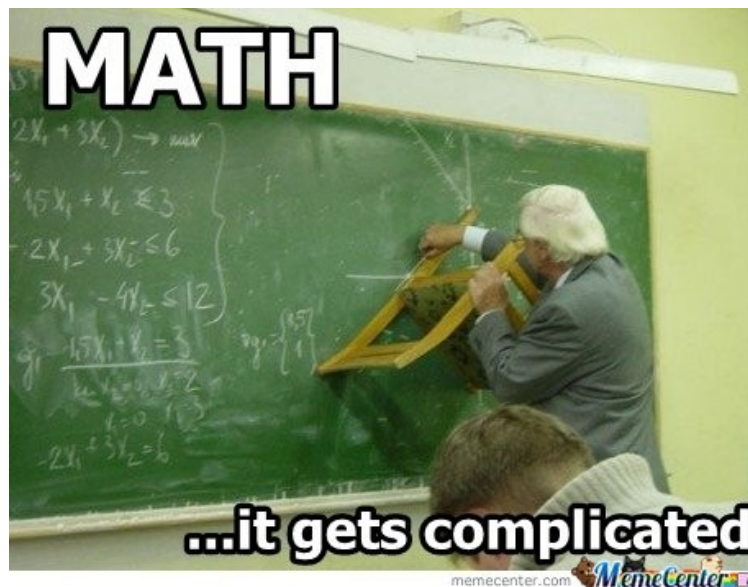
$$\frac{\partial f(g(x))}{\partial x} = \frac{\partial f(g(x))}{\partial g(x)} \cdot \frac{\partial g(x)}{\partial x}$$

Backpropagation

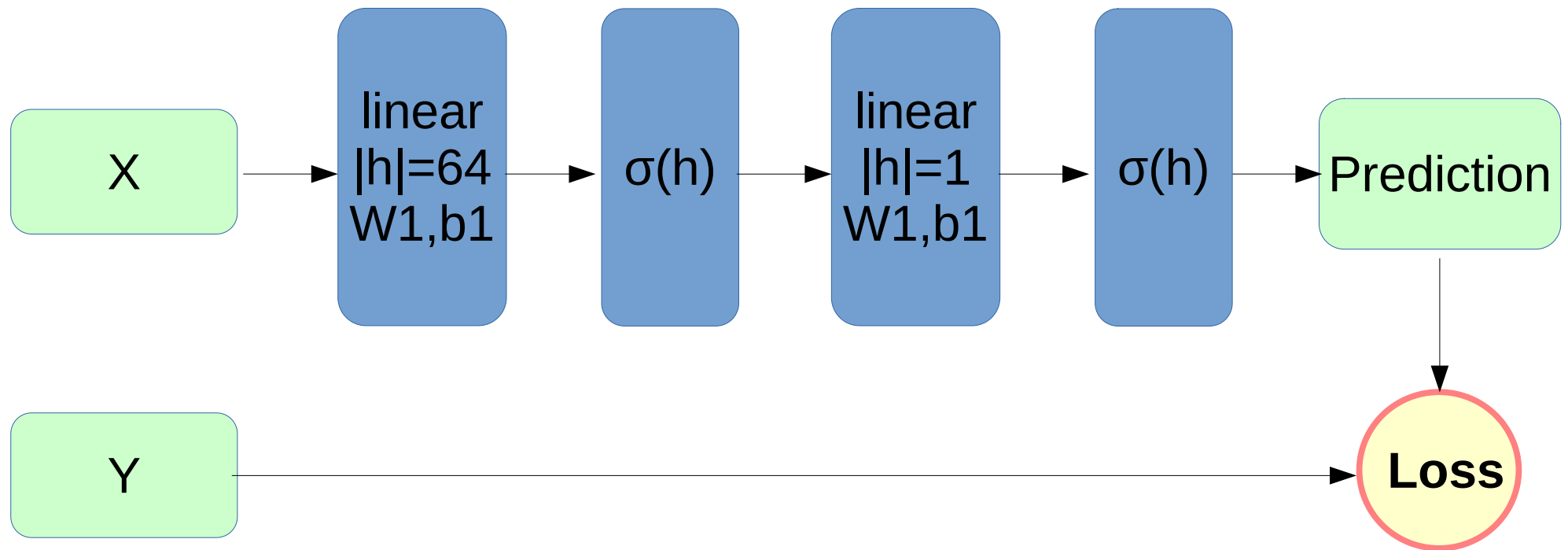
TL;DR: backprop = chain rule*

$$\frac{\partial f(g(x))}{\partial x} = \frac{\partial f(g(x))}{\partial g(x)} \cdot \frac{\partial g(x)}{\partial x}$$

* g and x can be vectors/vectors/tensors

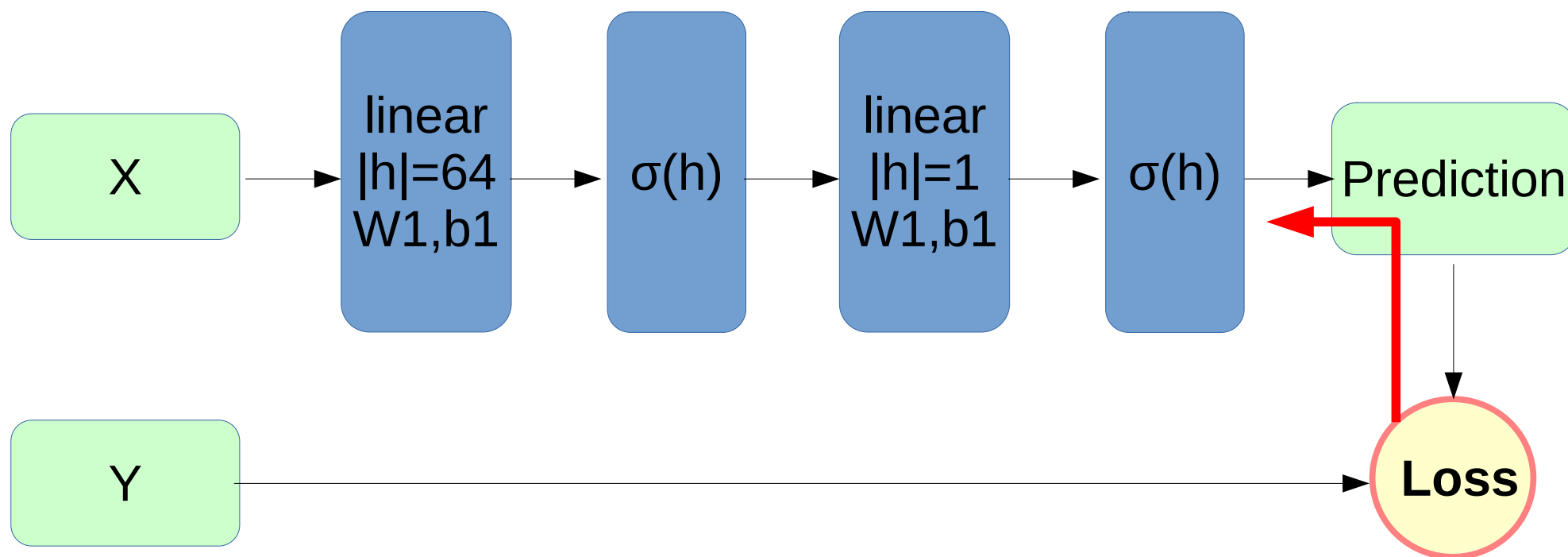


Backpropagation



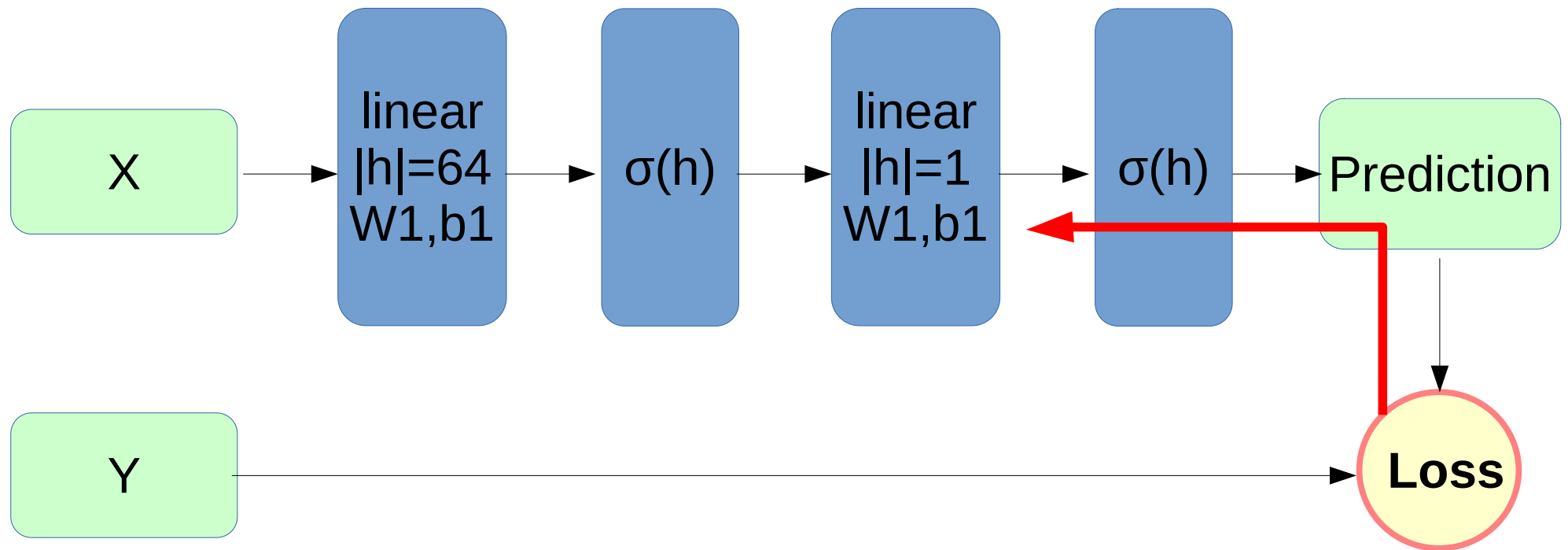
$$\frac{\partial L(\sigma(\text{linear}_{w_2, b_2}(\sigma(\text{linear}_{w_1, b_1}(x)))))}{\partial w_1} = \dots$$

Backpropagation



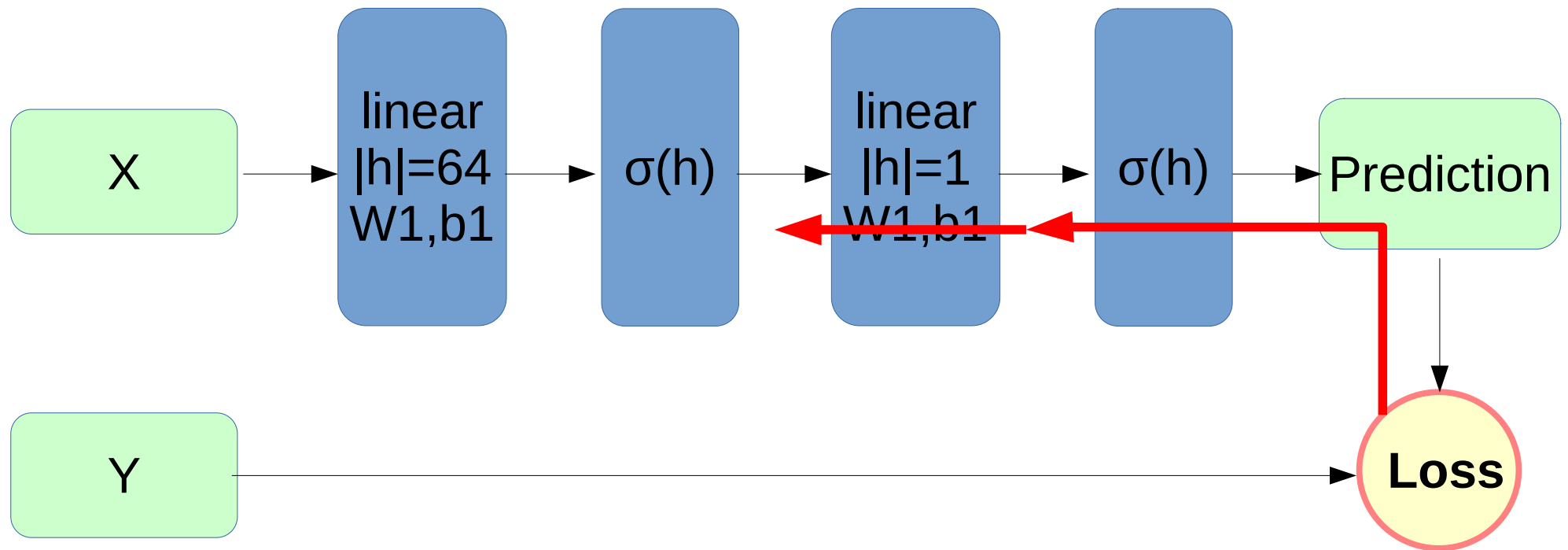
$$\frac{\partial L}{\partial w1} = \frac{\partial L}{\partial \sigma}.$$

Backpropagation



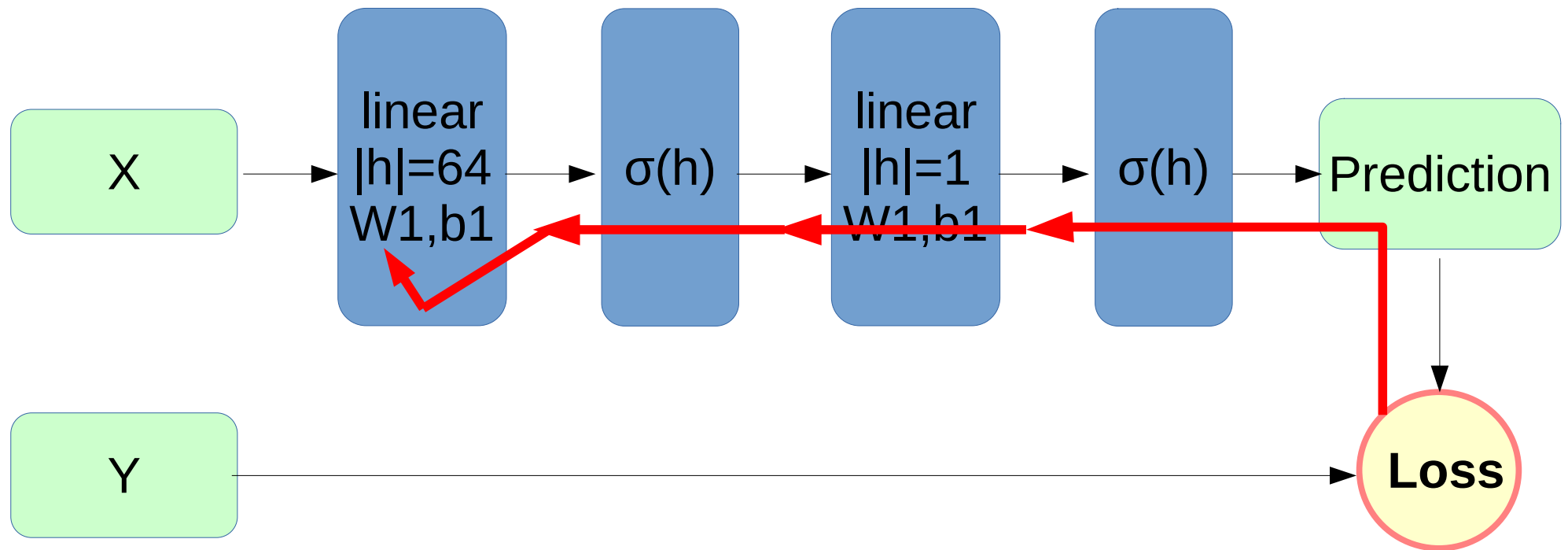
$$\frac{\partial L}{\partial w1} = \frac{\partial L}{\partial \sigma} \cdot \frac{\partial \sigma}{\partial \text{linear}_{w2,b2}}.$$

Backpropagation



$$\frac{\partial L}{\partial w1} = \frac{\partial L}{\partial \sigma} \cdot \frac{\partial \sigma}{\partial linear_{w2, b2}} \cdot \frac{\partial linear_{w2, b2}}{\partial \sigma}.$$

Backpropagation



$$\frac{\partial L}{\partial w1} = \frac{\partial L}{\partial \sigma} \cdot \frac{\partial \sigma}{\partial linear_{w2,b2}} \cdot \frac{\partial linear_{w2,b2}}{\partial \sigma} \cdot \frac{\partial \sigma}{\partial linear_{w1,b1}} \cdot \frac{\partial linear_{w1,b1}}{\partial w1}$$

Matrix derivatives we used

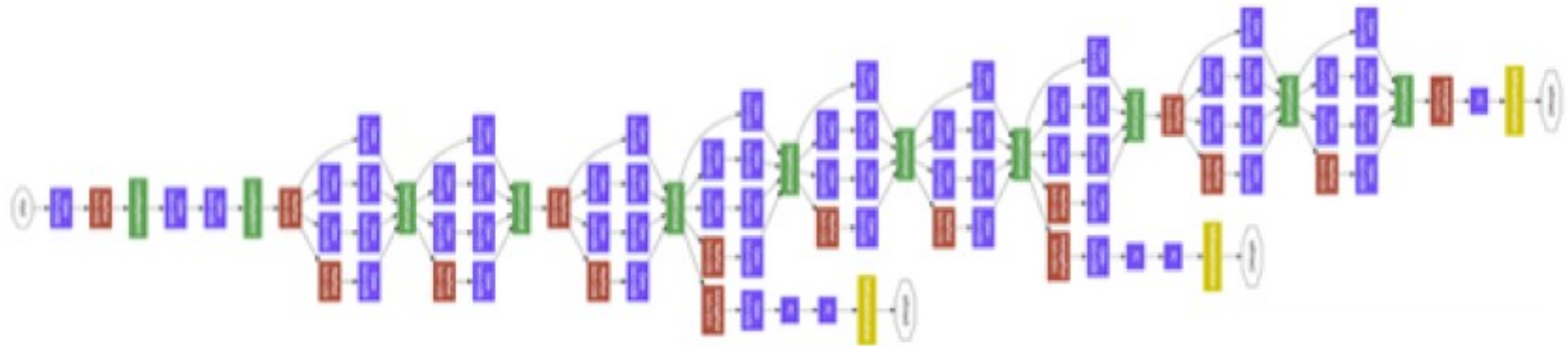
$$\text{sigmoid} : \frac{\partial L}{\partial \sigma(x)} \cdot [\sigma(x) \cdot (1 - \sigma(x))]$$

Works for any kind of x
(scalar, vector, matrix, tensor)

$$\text{linear over } X : \frac{\partial L}{\partial W \times X + b} \times W^T$$

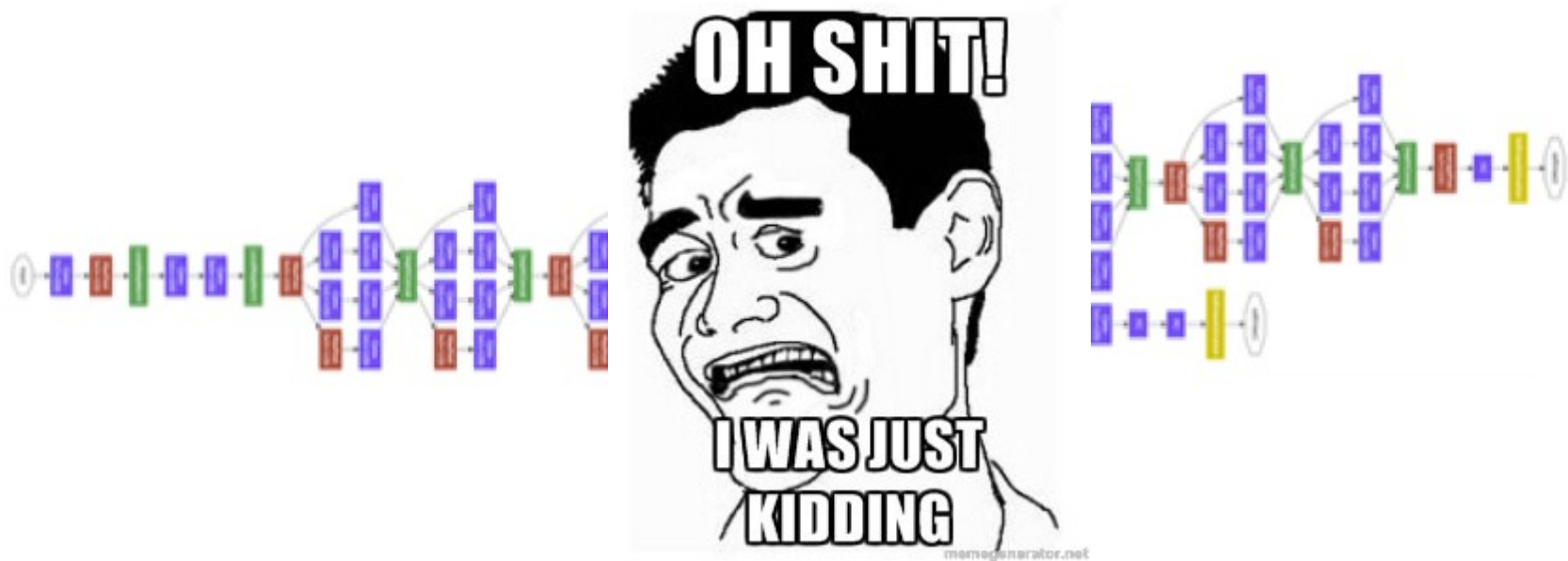
$$\text{linear over } W : \frac{1}{\|X\|} \cdot X^T \times \frac{\partial L}{\partial [X \times W + b]}$$

And now let's differentiate



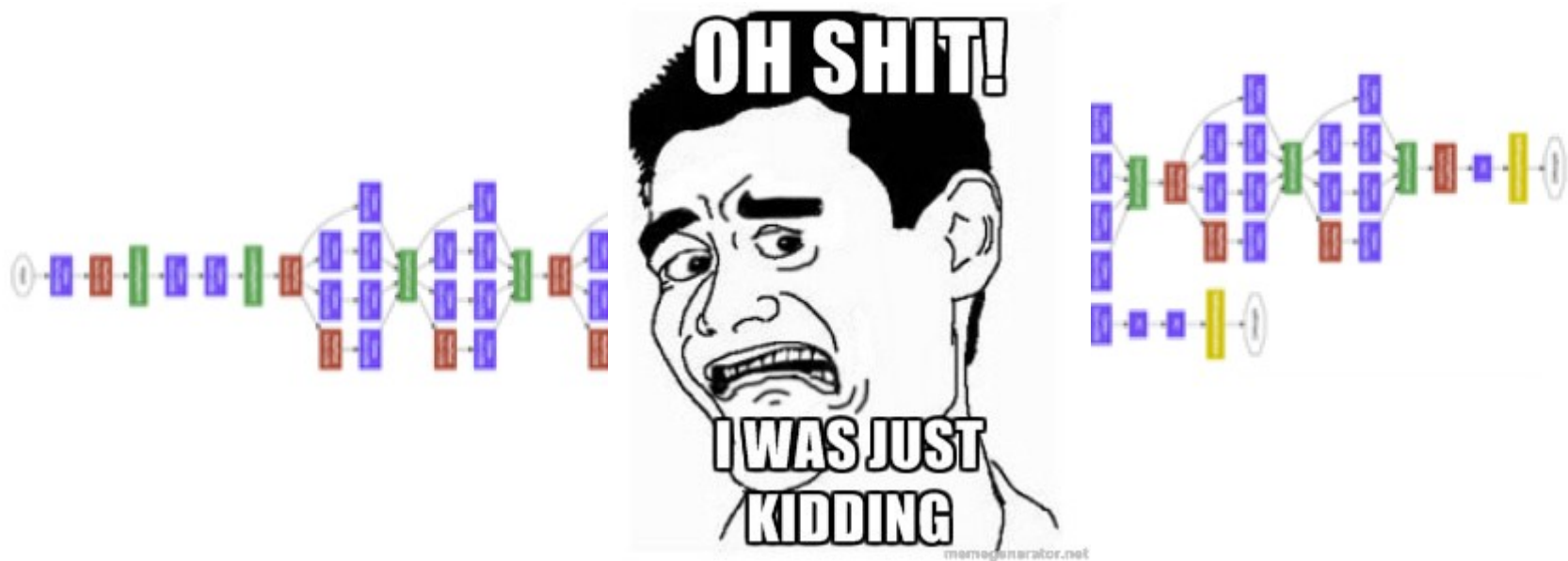
- 5+ types of layers
- each with different dimensions
- parallel branches with independent losses
- several nonlinearities

And now let's differentiate



- 5+ types of layers
- each with different dimensions
- parallel branches with independent losses
- several nonlinearities

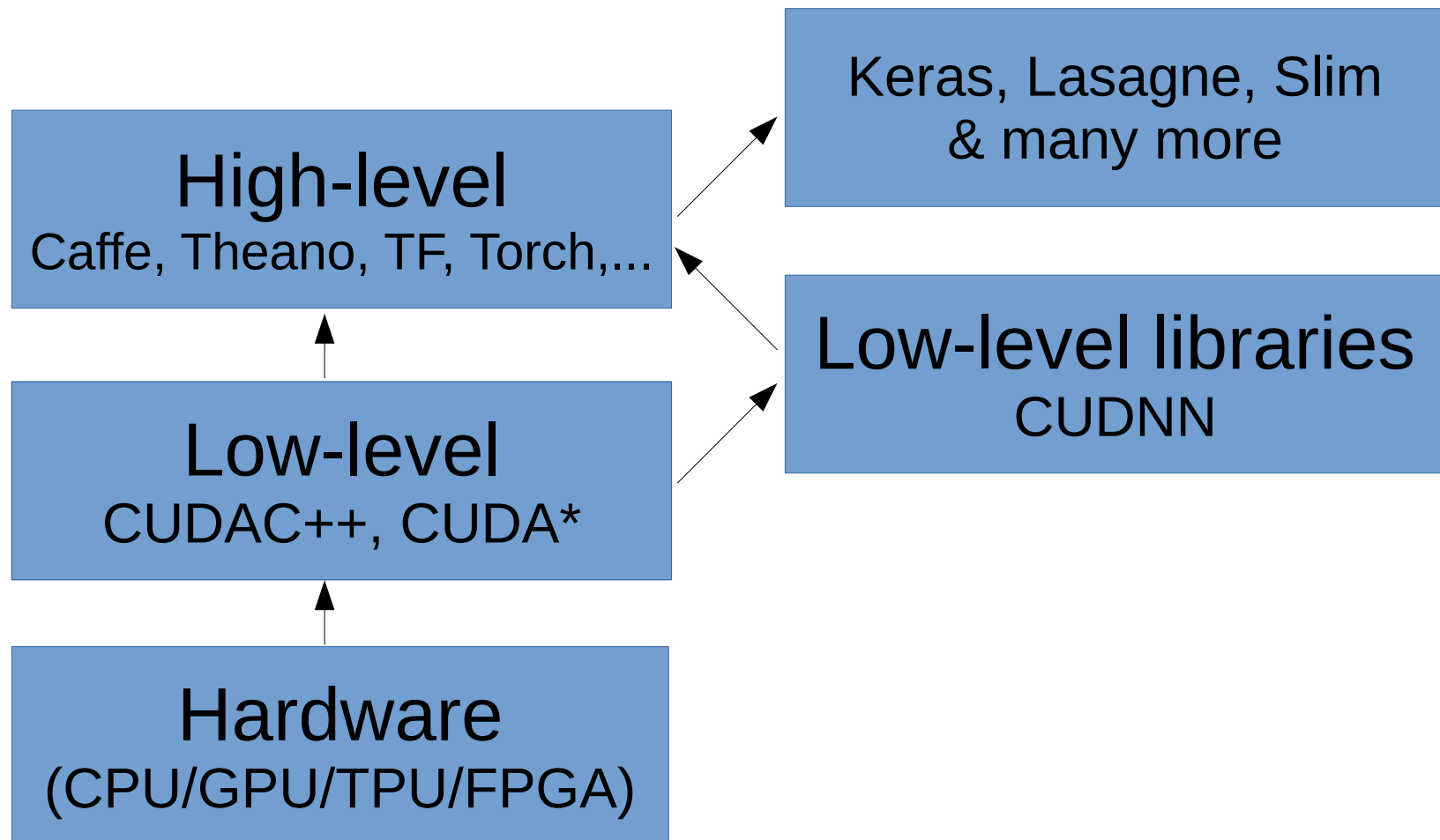
Deep learning frameworks



- 5+ types of layers
- each with different dimensions
- parallel branches with independent losses
- several nonlinearities

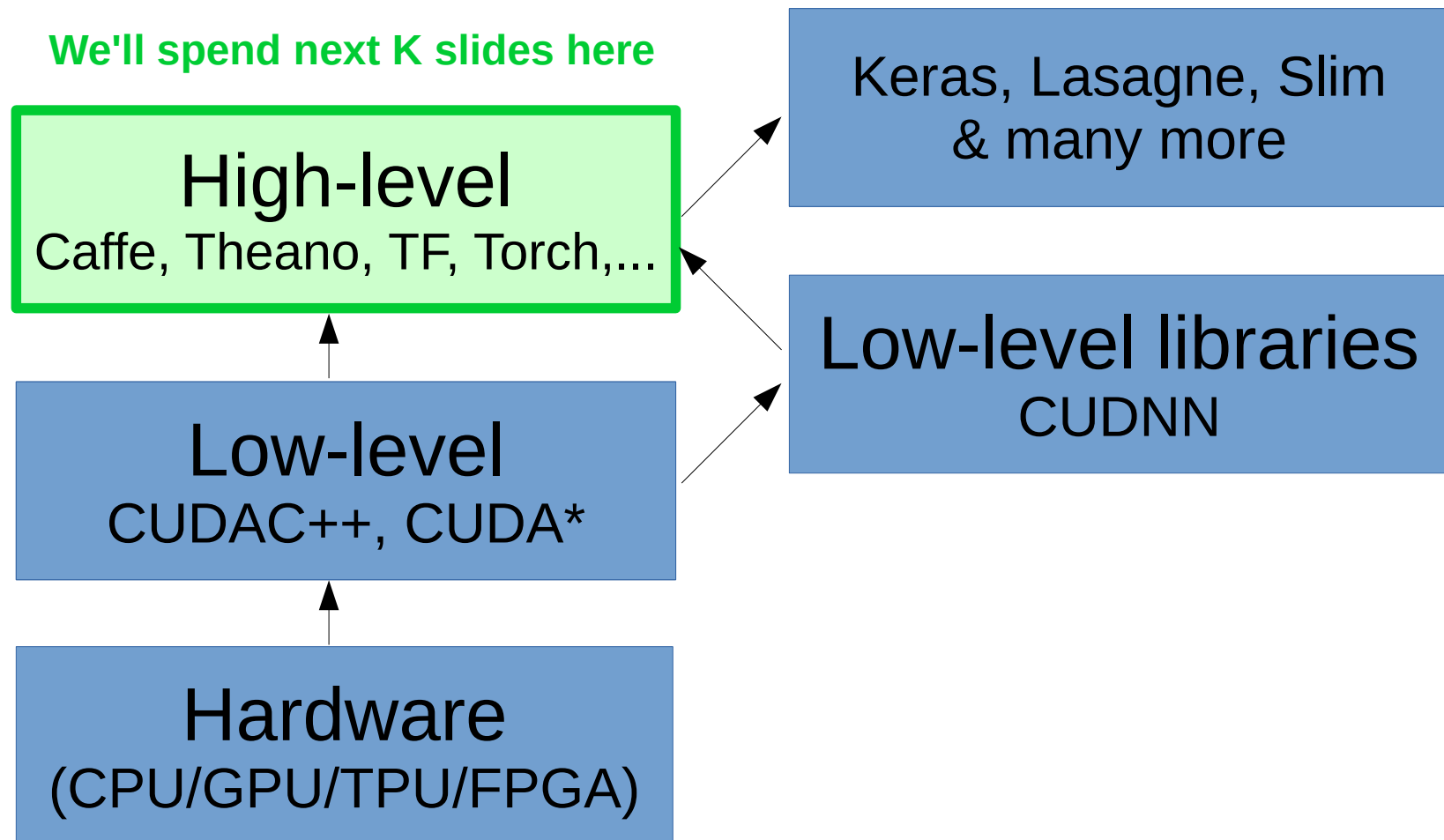
Deep learning frameworks

- Core idea: helps you define and train neural nets



Deep learning frameworks

- Core idea: helps you define and train neural nets



Deep learning frameworks

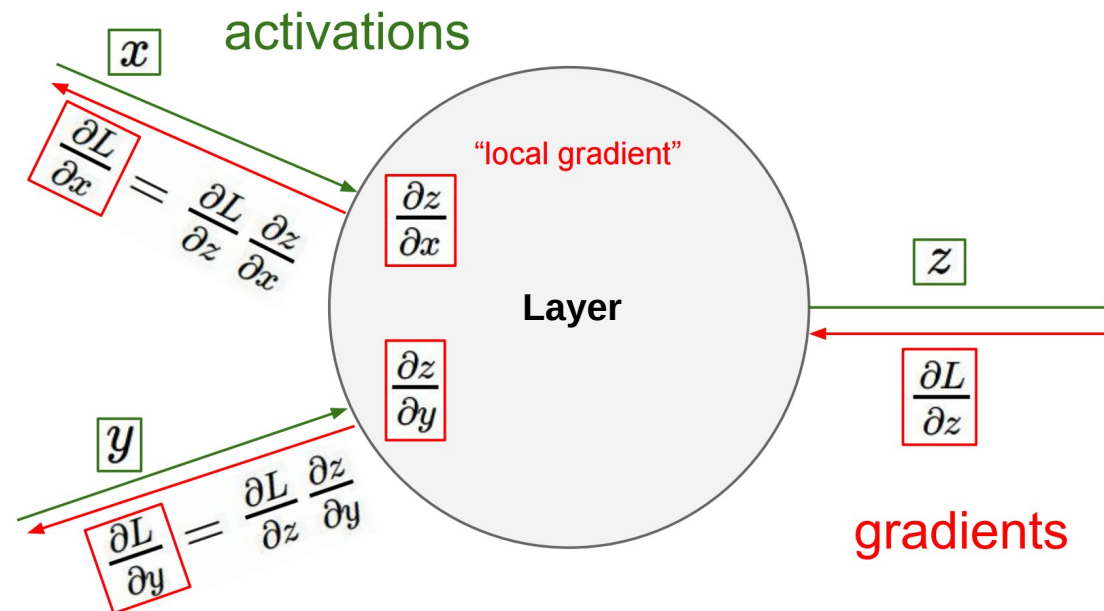
Layer-based frameworks:

Same idea as in our hand-made neural net

Deep learning frameworks

Layer-based frameworks:

Same idea as in our hand-made neural net
this one - <http://bit.ly/2w9kAHm>



Deep learning frameworks

Caffe

```
name: "LeNet"
layer {
  name: "conv1"
  type: "Convolution"
  bottom: "data"
  top: "conv1"
  param {lr_mult: 1}
  param {lr_mult: 2}
  convolution_param {
    num_output: 20
    kernel_size: 5
    stride: 1
    weight_filler {
      type: "xavier"
    }
  }
}
```

....

130 lines

You define model in config file
by stacking layers.

Then train like this:

```
caffe train -solver
examples/mnist/lenet_solve
r.prototxt
```

Deep learning frameworks

Caffe

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name: "LeNet"
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}
```

....

130 lines

- + Easy to deploy (C++)
- + A lot of pre-trained models (model zoo)
- Model as protobuf
- Hard to build new layers
- Hard to debug

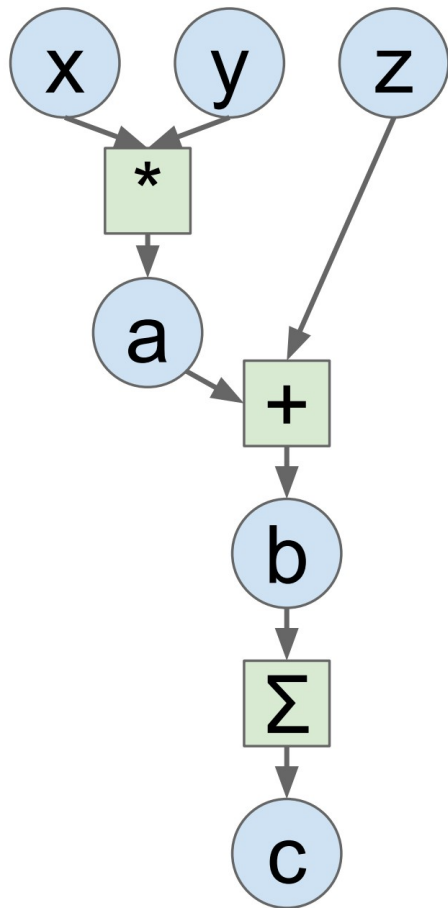
Still used in some
legacy codebases

Symbolic graphs

What will your CPU do
when you write this?

```
a = x * y  
b = a + z  
c = np.sum(b)
```


Symbolic graphs



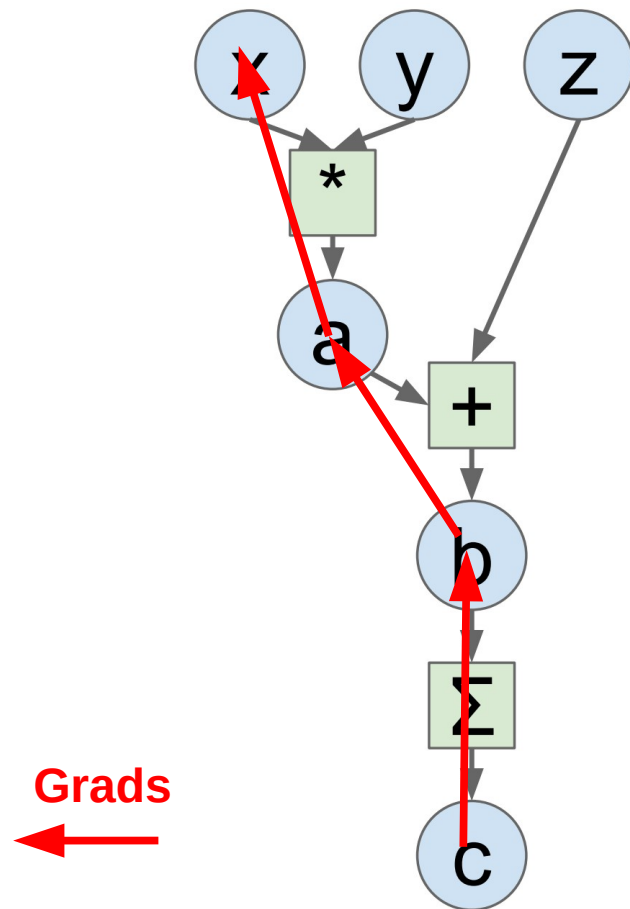
`a = x * y`

`b = a + z`

`c = np.sum(b)`

Idea: let's define
this graph explicitly!

Symbolic graphs



```
a = x * y
b = a + z
c = np.sum(b)
```

- + Automatic gradients!
- + Easy to build new layers
- + We can optimize the Graph
- Graph is static during training
- Need time to compile/optimize
- Hard to debug

Symbolic graphs

Static graph frameworks

- Purely static is legacy

Theano (deprecated)

TensorFlow (before 2.0)

- Static in modern frameworks
`torch.jit.trace/script`, `compile`
`jax.jit` / `tensorflow.function`

The Theano logo, consisting of the word "theano" in a lowercase, blue, sans-serif font.

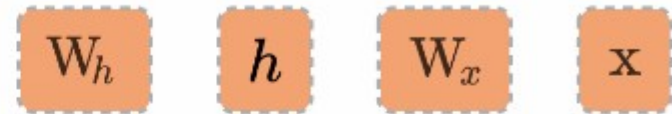
Dynamic graphs

Chainer, DyNet, Pytorch

A graph is created on the fly

```
from torch.autograd import Variable

x = Variable(torch.randn(1, 10))
prev_h = Variable(torch.randn(1, 20))
W_h = Variable(torch.randn(20, 20))
W_x = Variable(torch.randn(20, 10))
```



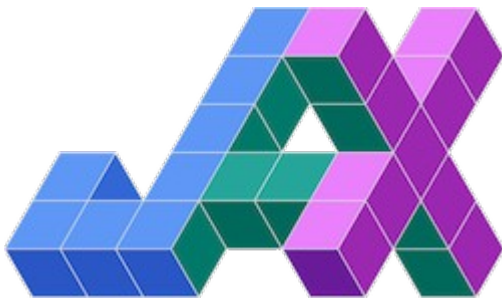
Dynamic graphs

Chainer, DyNet, Pytorch

PYTORCH



Chainer



- + Can change graph on the fly
- + Can get value of any tensor at any time (easy debugging)
- Hard to optimize graphs (especially large graphs)
- Still early development

Researchers love them!

Dynamic graphs



Andrej Karpathy ✓
@karpathy

Following



I've been using PyTorch a few months now and I've never felt better. I have more energy. My skin is clearer. My eye sight has improved.

Researchers love them!

Advanced: GPU kernels w/o CUDA

<https://openai.com/index/triton/>

Python

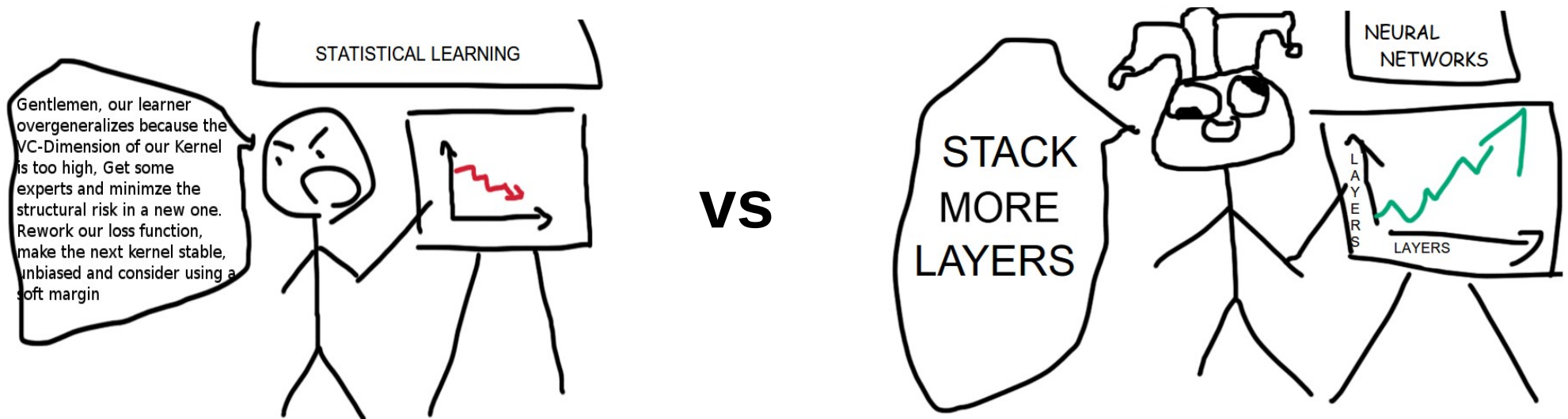


```
1 @triton.jit
2 def matmul(A, B, C, M, N, K, stride_am, stride_ak,
3           stride_bk, stride_bn, stride_cm, stride_cn,
4           **META):
5     # extract metaparameters
6     BLOCK_M, GROUP_M = META['BLOCK_M'], META['GROUP_M']
7     BLOCK_N = META['BLOCK_N']
8     BLOCK_K = META['BLOCK_K']
9     # programs are grouped together to improve L2 hit rate
10    _pid_m = tl.program_id(0)
11    _pid_n = tl.program_id(1)
12    pid_m = _pid_m // GROUP_M
13    pid_n = (_pid_n * GROUP_M) + (_pid_m % GROUP_M)
14    # rm (resp. rn) denotes a range of indices
15    # for rows (resp. col) of C
16    rm = pid_m * BLOCK_M + tl.arange(0, BLOCK_M)
17    rn = pid_n * BLOCK_N + tl.arange(0, BLOCK_N)
18    # rk denotes a range of indices for columns
19    # (resp. rows) of A (resp. B)
20    rk = tl.arange(0, BLOCK_K)
21    # the memory addresses of elements in the first block of
22    # A and B can be computed using numpy-style broadcasting
23    A = A + (rm[:, None] * stride_am + rk[None, :] * stride_ak)
24    B = B + (rk[:, None] * stride_bk + rn[None, :] * stride_bn)
25    # initialize and iteratively update accumulator
26    acc = tl.zeros((BLOCK_M, BLOCK_N), dtype=tl.float32)
```

[Short break, then practice, then the rest of the class]

Not magic!

Don't expect deep learning to solve all your problems for free. For it won't.



Not magic

Book of grudges

- No core theory
 - Relies on intuitive reasoning

Not magic

Book of grudges

- No core theory
 - Relies on intuitive reasoning
- Needs tons of data
 - You need either large dataset or heavy wizardry

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 - Running on mobiles/embedded is a challenge

Not magic

Book of grudges

- No core theory
 - Relies on intuitive reasoning
- Needs tons of data
 - You need either large dataset or heavy wizardry
- Computationally heavy
 - Running on mobiles/embedded is a challenge
- Pathologically overhyped
 - People expect of it to make wonders

Deep learning is a language

Deep learning is a language

in which you can hint your model
on what you want it to learn

Deep learning is a language

Say, you train classifier on two sets of features



Raw
features

The diagram consists of three rectangular boxes. On the left side, there are two blue boxes stacked vertically. The top blue box contains the text 'Raw features' and the bottom blue box contains the text 'High-level features'. On the right side, there is a single yellow box containing the text 'Target'. There are no arrows or other graphical elements connecting these boxes.

High-level
features

Target

Deep learning is a language

Say, you train classifier on two sets of features

Raw
features

Car photo
(image pixels)

High-level
features

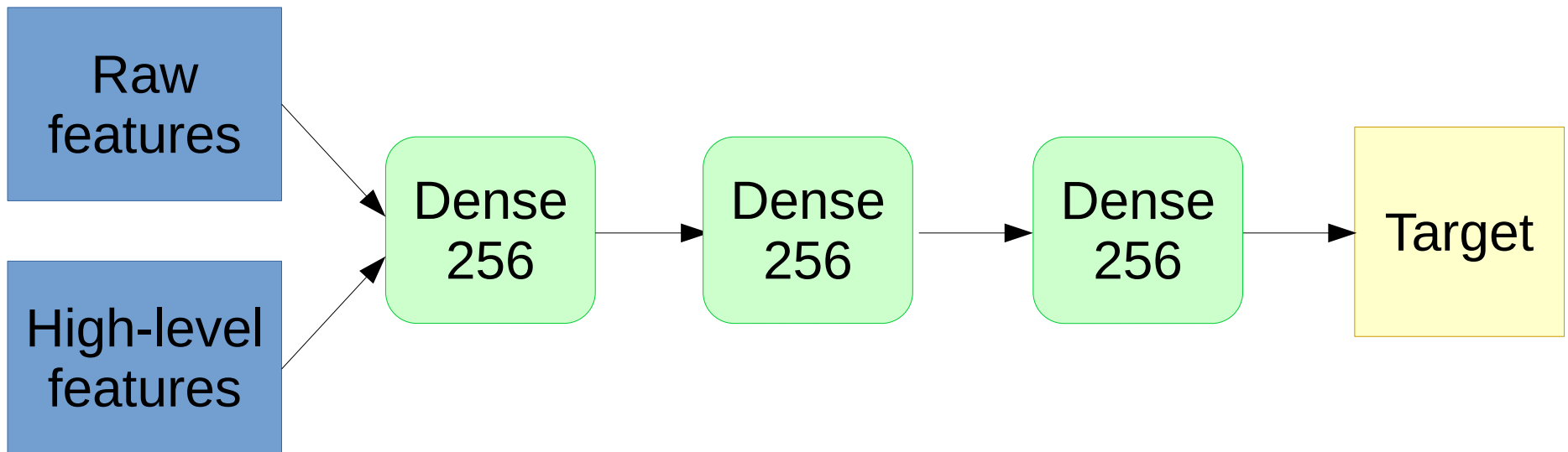
Car brand,
model, age,
blemishes

Car
price

Target

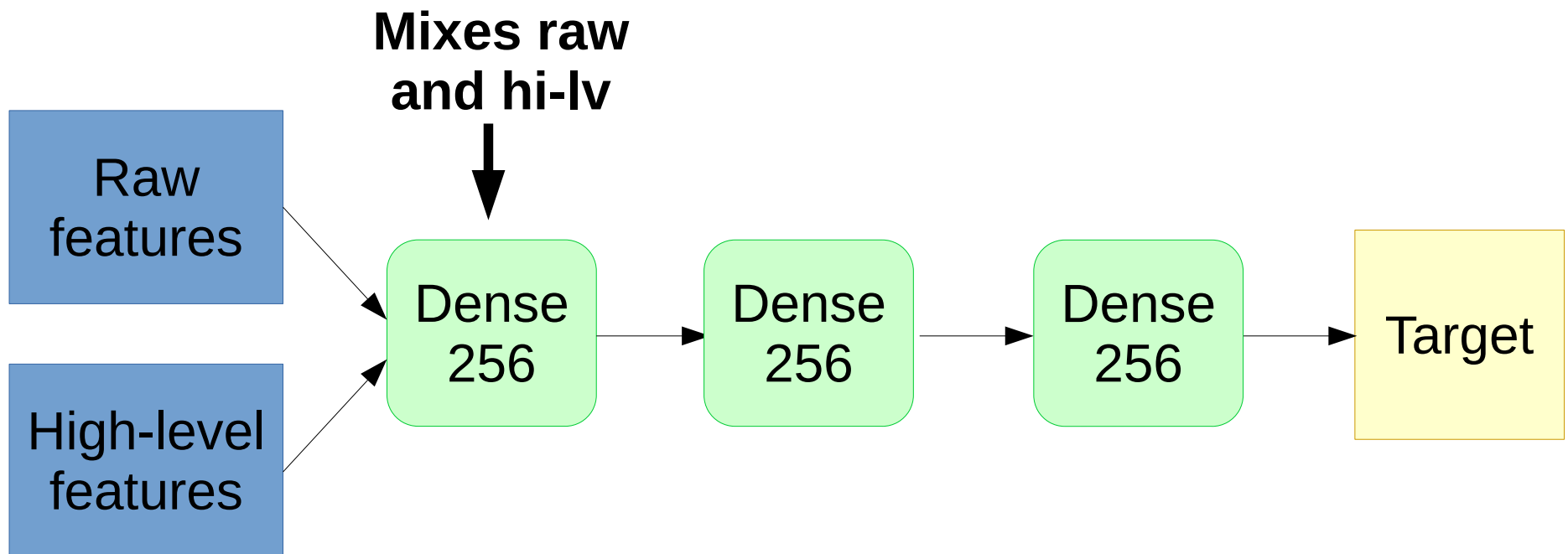
Deep learning is a language

Naive approach



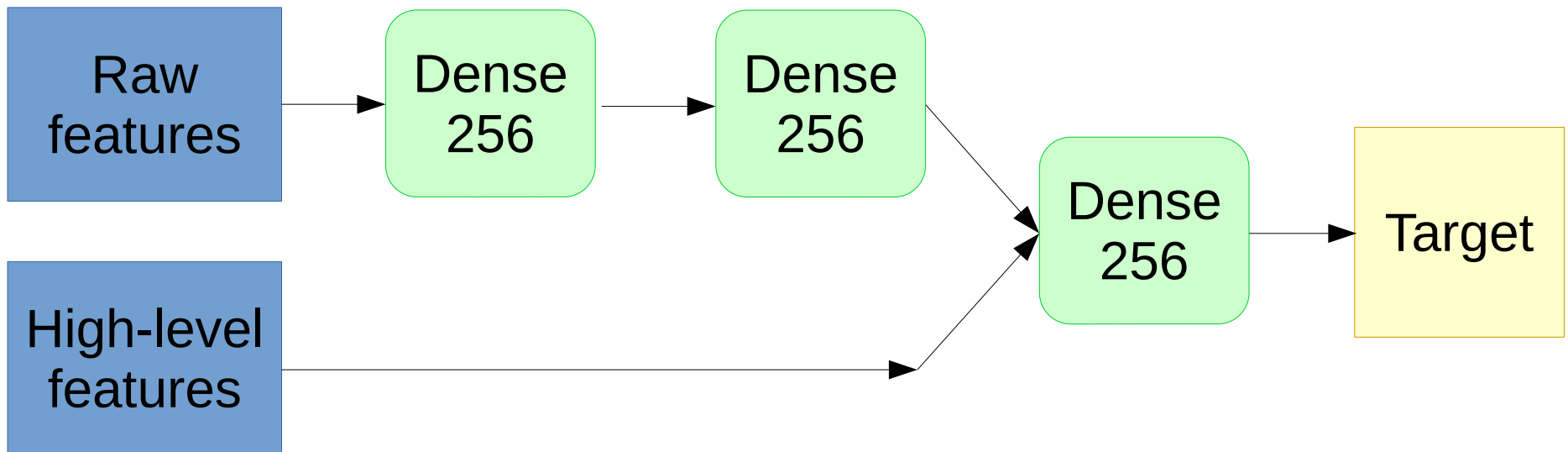
Deep learning is a language

Naive approach



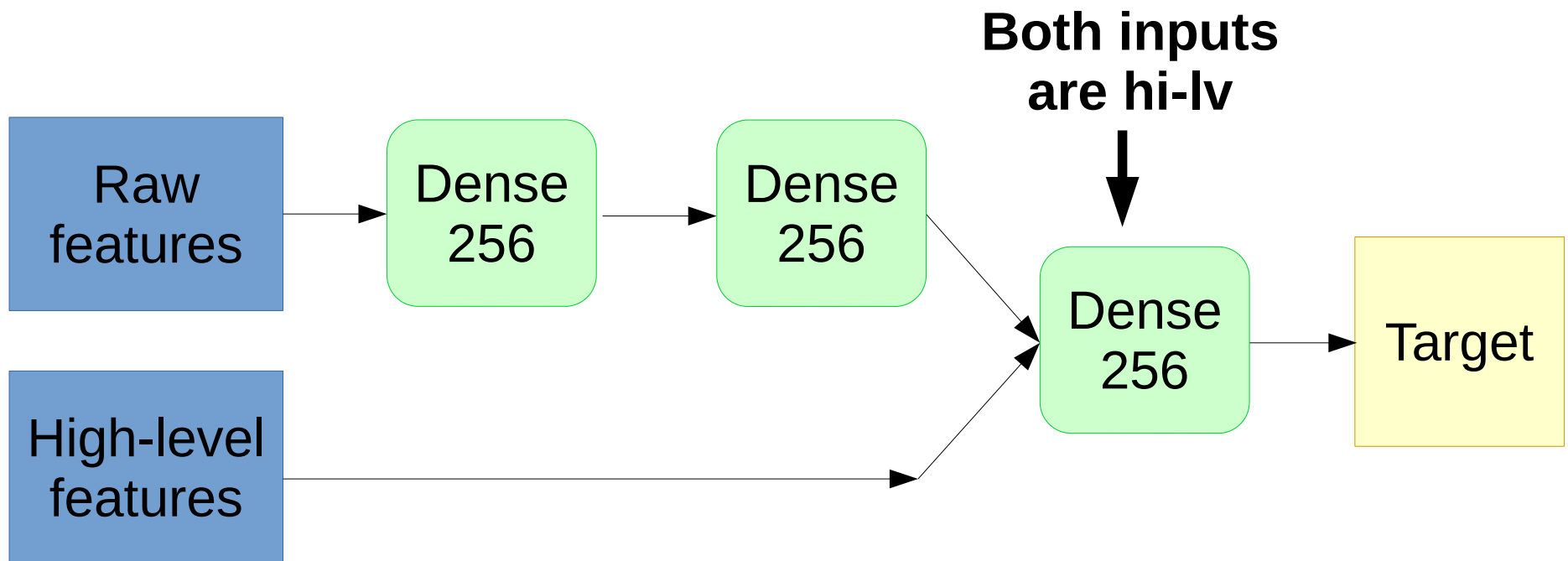
Deep learning is a language

Less naïve approach



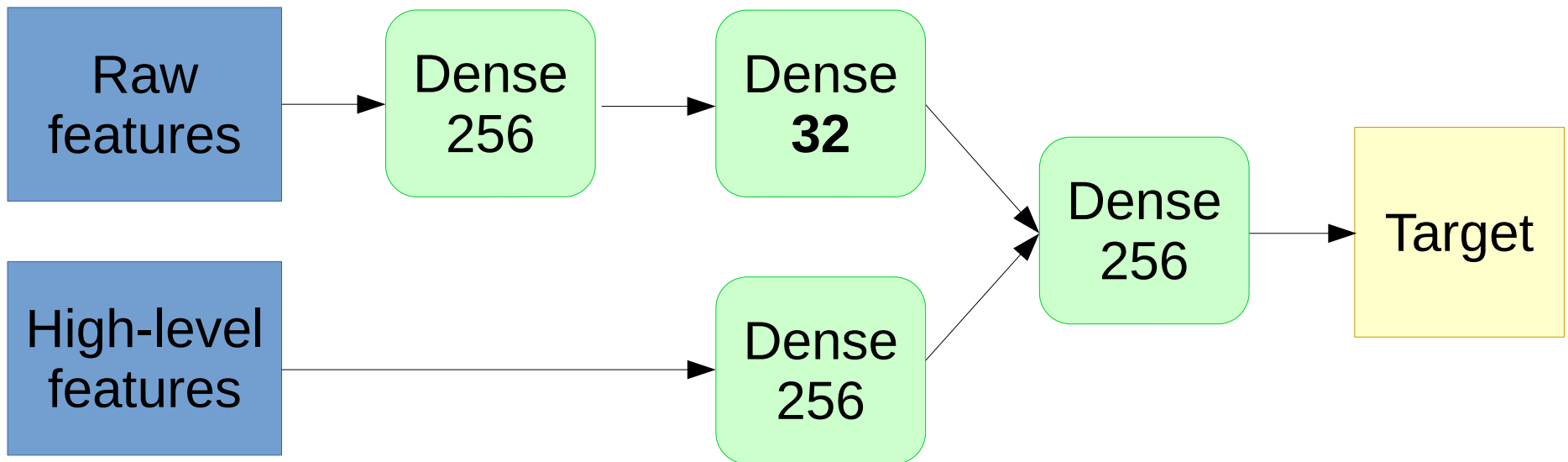
Deep learning is a language

Less naïve approach



Deep learning is a language

“Image features should be less important”
if that's what you want to say



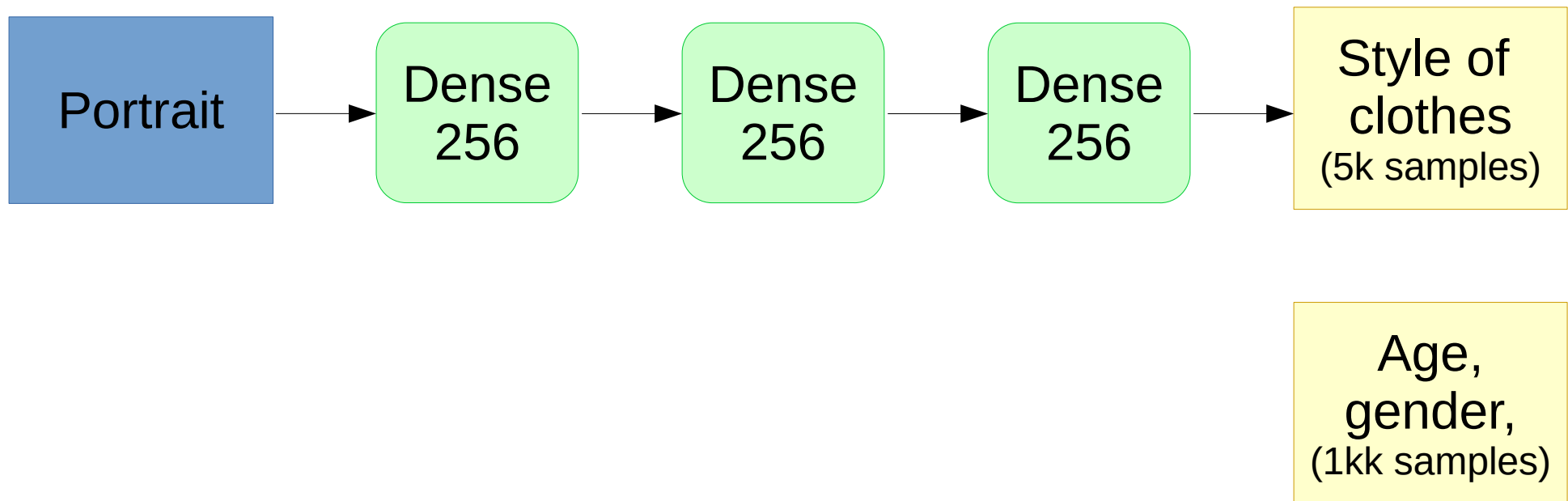
Deep learning is a language

You have a small dataset



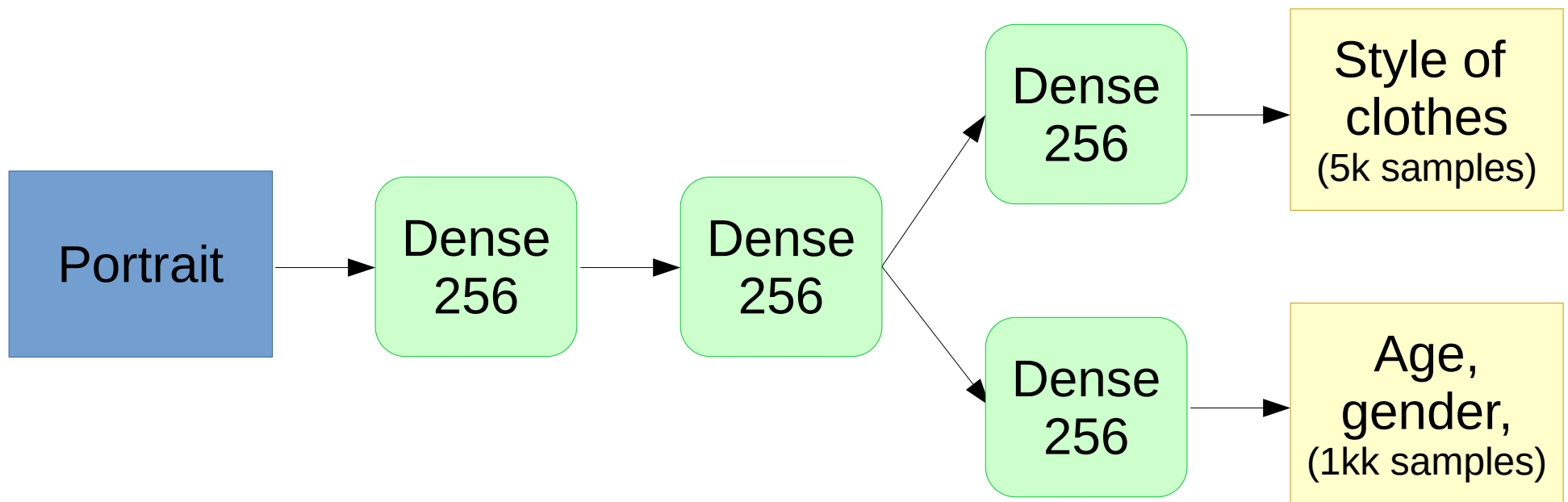
Deep learning is a language

You have a small dataset
and a larger dataset with similar task



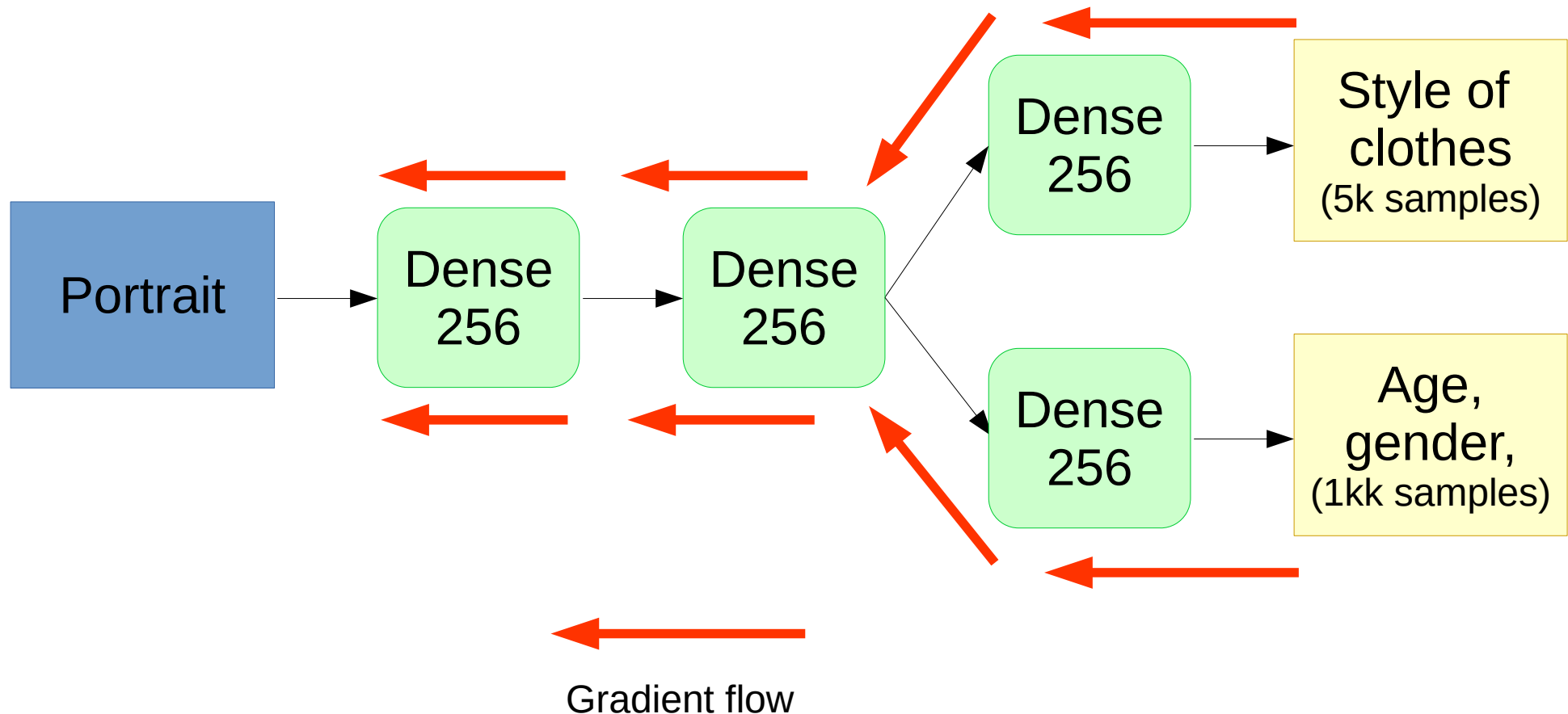
Deep learning is a language

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Deep learning is a language

I want to learn features for style classification that also help determine age & gender



Deep learning is a language

For images:

- “I want to classify cats regardless where they are”
- “A cat shifted by 3 pixels is still a cat”

For texts:

- “People read and write texts left to right”

In general:

- “I don't want model to trust single feature too much”
- “I want my features to be sparse”

Let's see a few more “words”

Regularization

- Neural networks overfit like nothing else.

Gotta regularize!

- We can use L1/L2 like usual, but there's more!

Regularization

- Dropout:

“I don't my network to trust any single neuron too much”

- Idea:

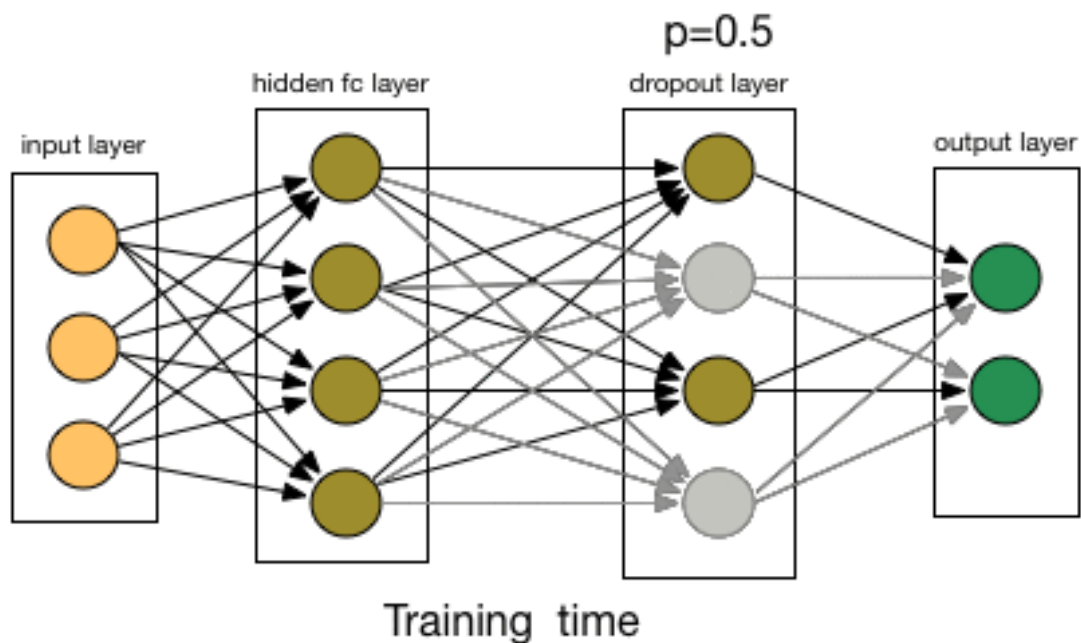
At training time, with probability p
multiply neurons by zero!

- Scale up the remaining neurons to keep average the same

Regularization

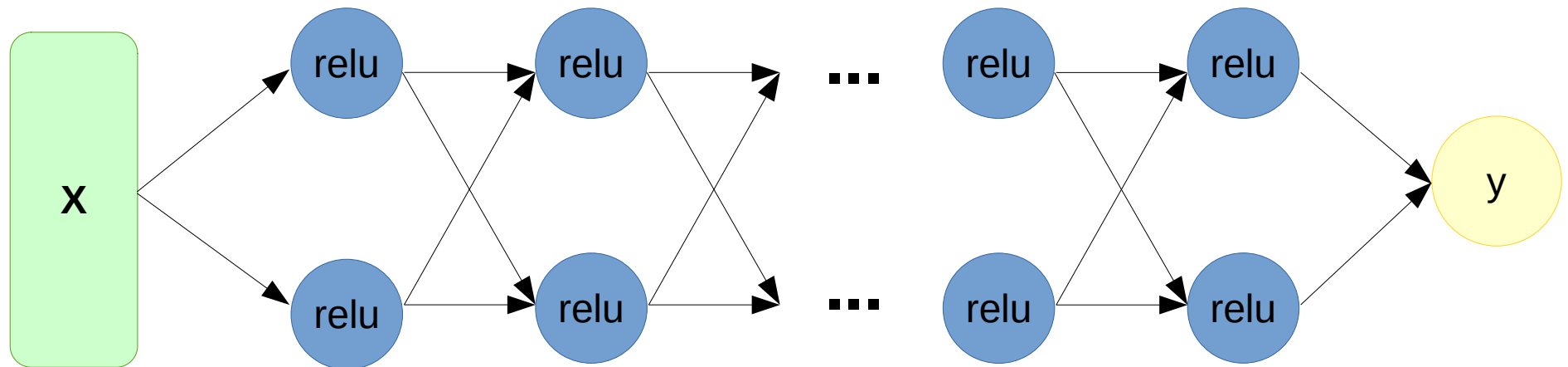
- Dropout:

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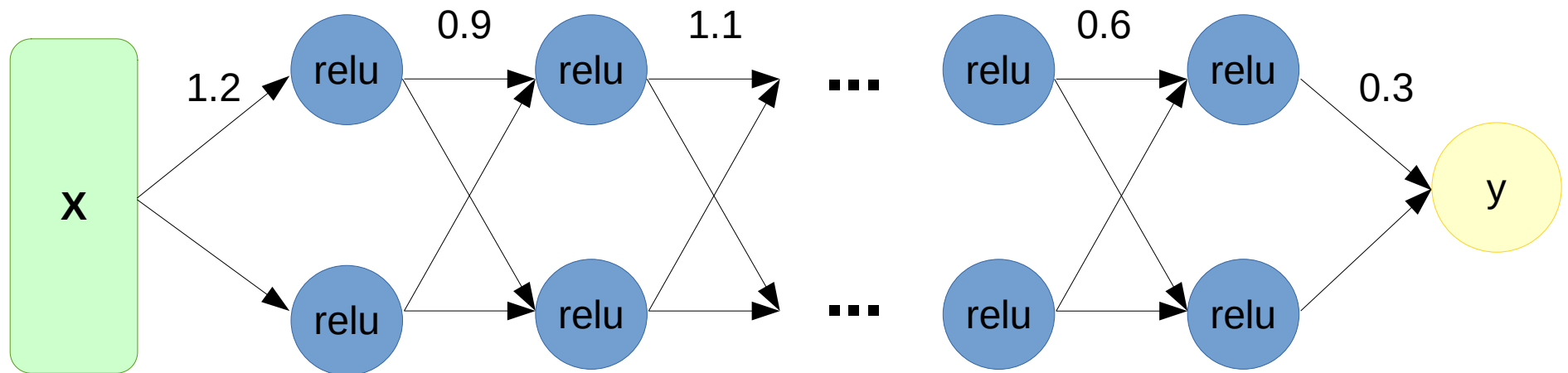
The problem with deep networks

- Imagine a 100-layer network with ReLU



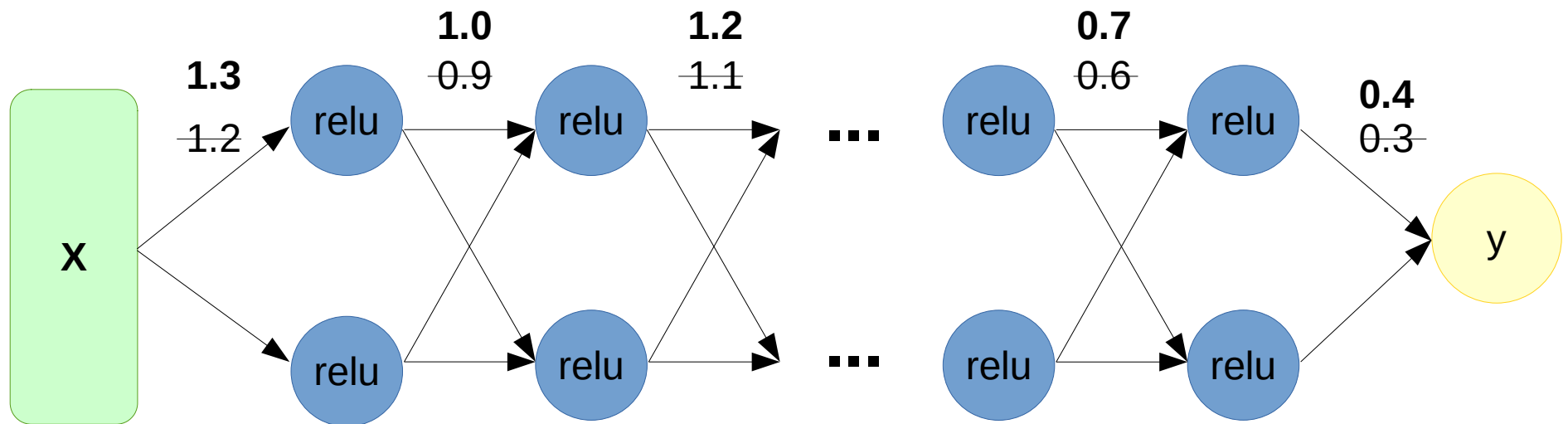
The problem with deep networks

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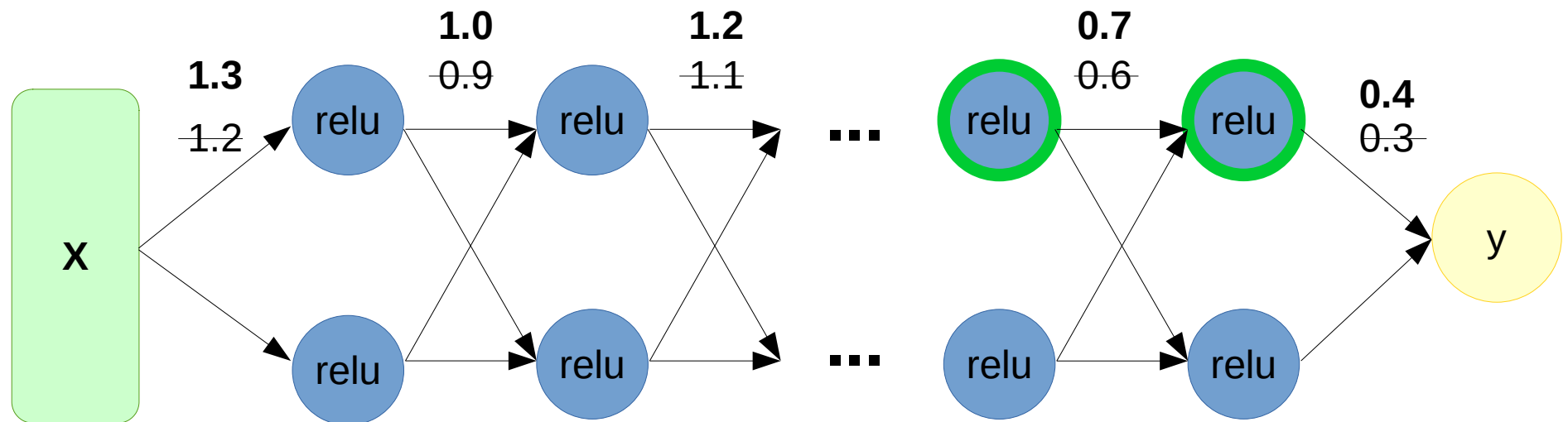
The problem with deep networks

- Imagine a 100-layer network with ReLU
- Single gradient step...



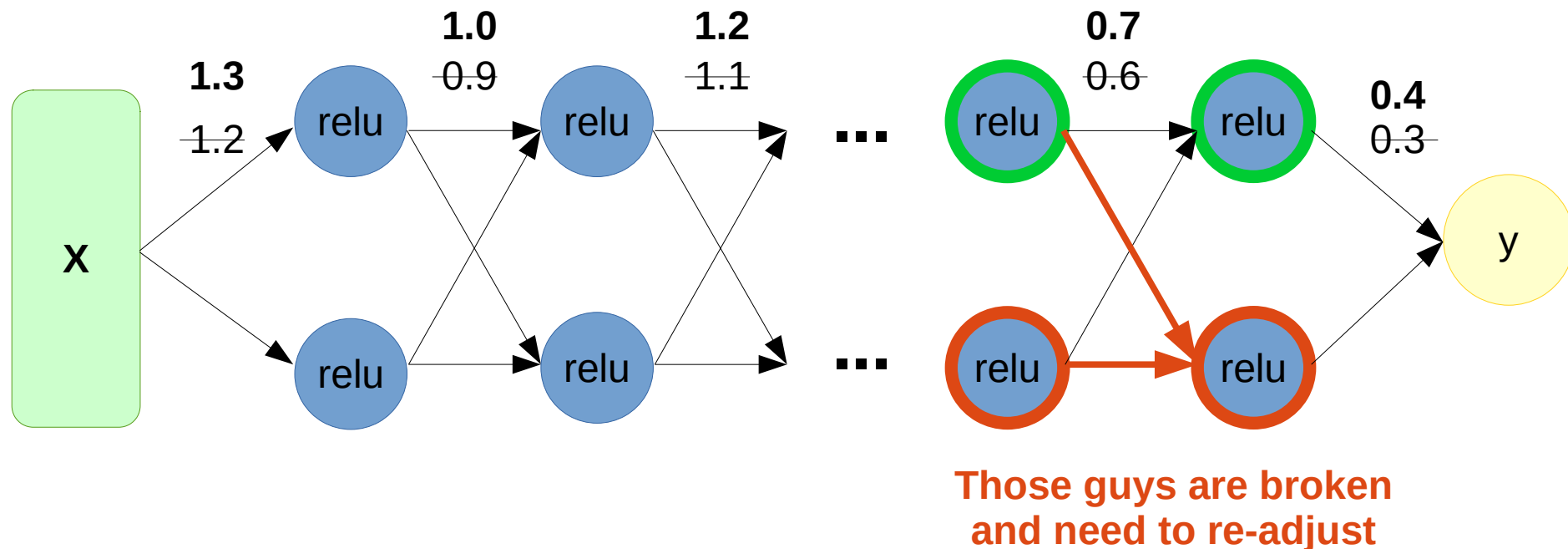
The problem with deep networks

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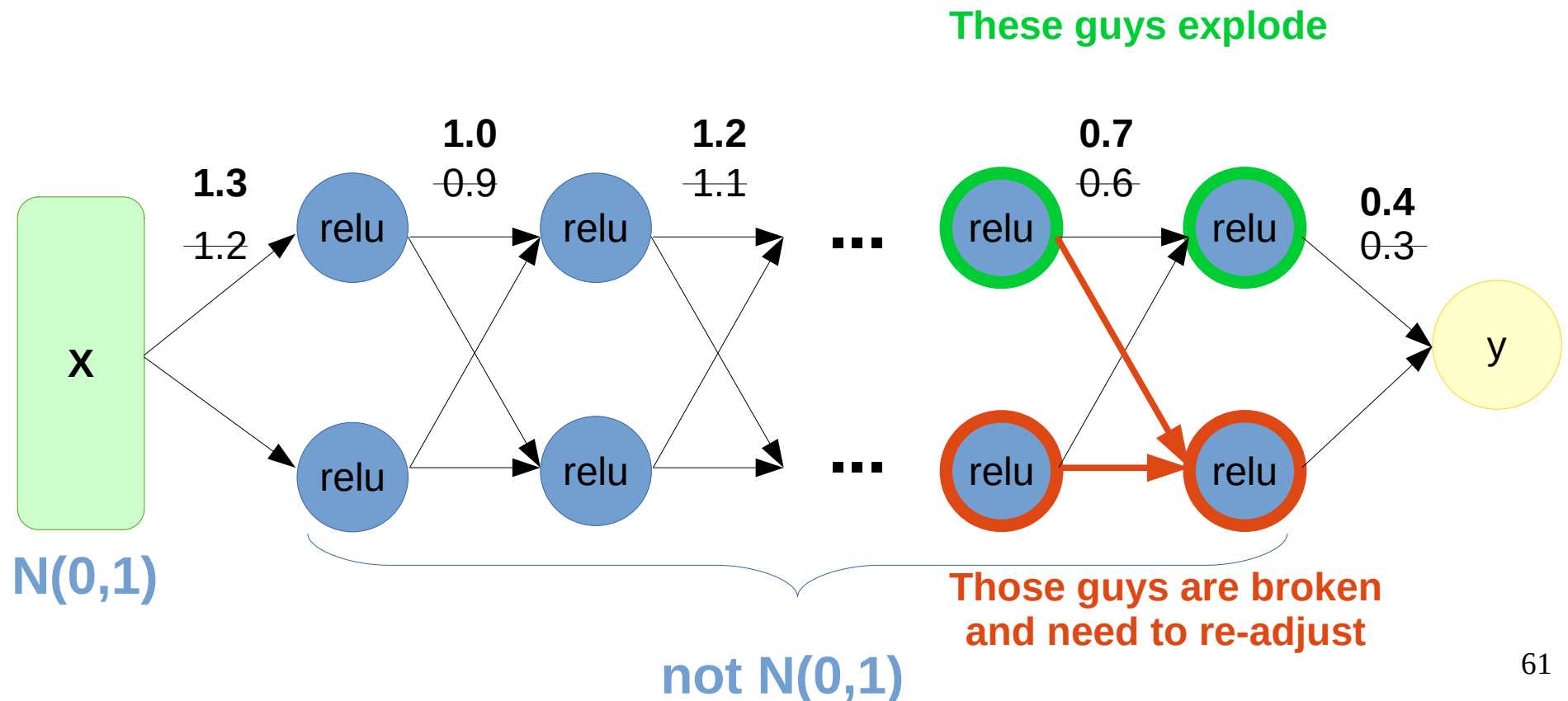
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The problem with deep networks

- Imagine a 100-layer network with ReLU
- Single gradient step...



Batch normalization

TL;DR:

- It's usually a good idea to normalize linear model inputs

(c) Every machine learning lecturer, ever

Batch normalization

Idea:

- We normalize activation of a hidden layer
(zero mean unit variance)

$$h_i = \frac{h_i - \mu_i}{\sqrt{\sigma_i^2}}$$

- Update μ_i, σ_i^2 with moving average while training

$$\mu_i := \alpha \cdot \text{mean}_{batch} + (1 - \alpha) \cdot \mu_i$$

$$\sigma_i^2 := \alpha \cdot \text{variance}_{batch} + (1 - \alpha) \cdot \sigma_i^2$$

Batch normalization

Idea:

- We normalize activation of a hidden layer
(zero mean unit variance)

$$h_i = \frac{h_i - \mu_i}{\sqrt{\sigma_i^2}}$$

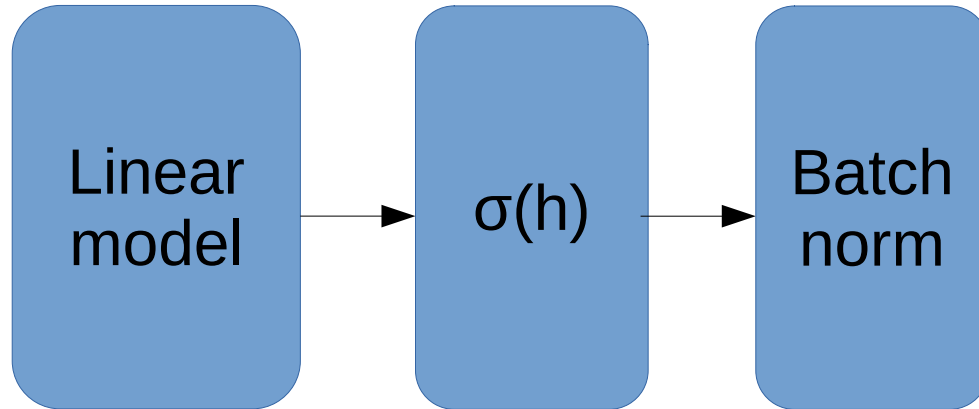
i stands for i-th neuron

- Update μ_i, σ_i^2 with moving average while training

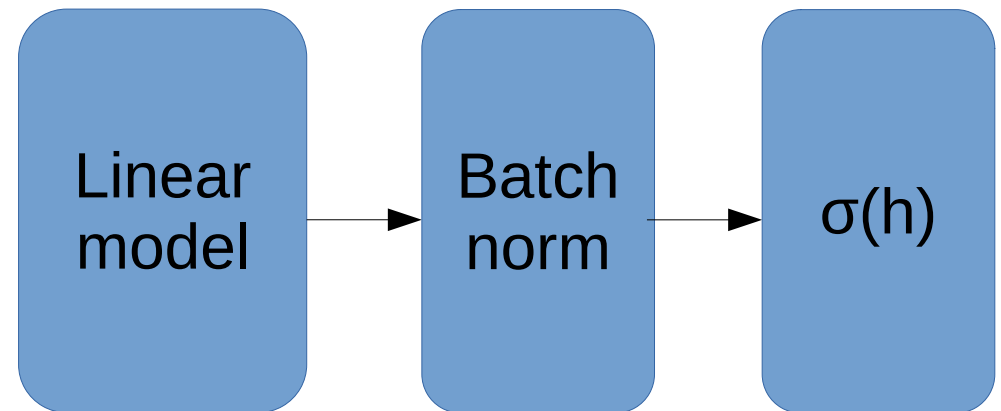
$$\mu_i := \alpha \cdot \text{mean}_{\text{batch}} + (1 - \alpha) \cdot \mu_i$$

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Batch normalization



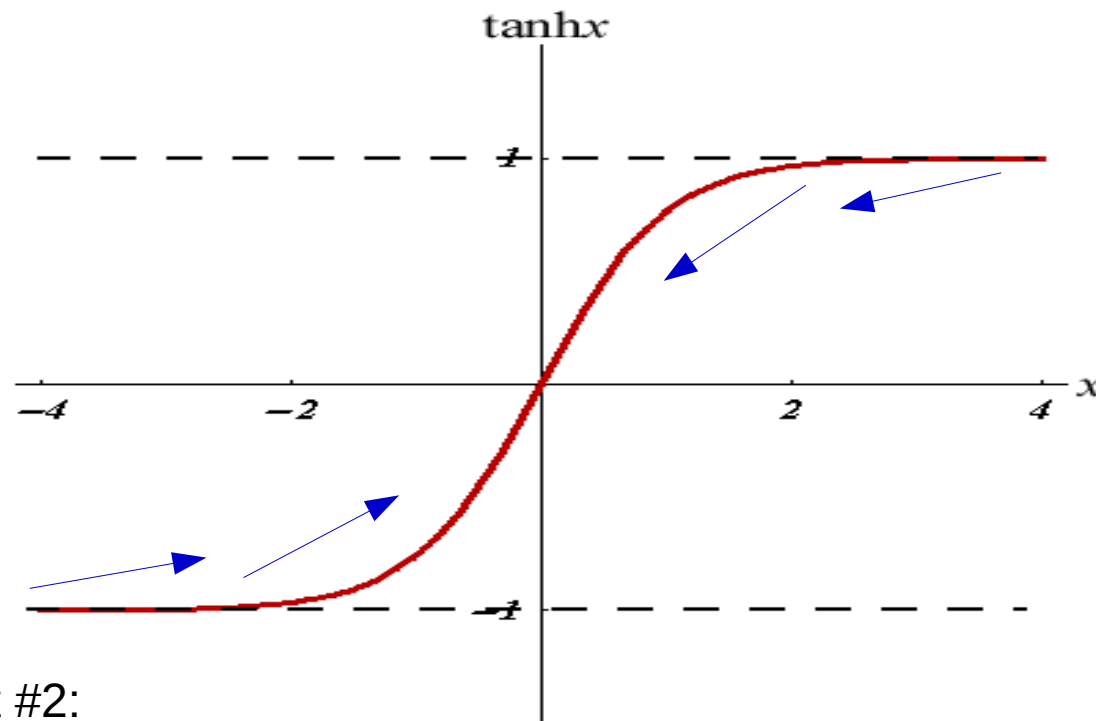
VS



Batch normalization

Good side effect #1:

- Vanishing gradient less a problem for sigmoid-like nonlinearities



Good side effect #2:

- We no longer need to train bias (+b term in $Wx+b$)

Weight normalization

Same problem, different solution

- Learn separate “direction” w and “length” l

$$\hat{w} \stackrel{\text{def}}{=} \frac{w}{\|w\|} \cdot l$$

- Much simpler, but requires good init

More normalization

Layer/Instance normalization

- Like batchnorm, but normalizes over different axes

Normprop

- A special training algorithm

Self-normalizing neural networks (SELU)

More normalization

Layer/Instance normalization

- Like batchnorm, but normalizes over different axes

Normprop

- A special training algorithm

Self-normalizing neural networks (SELU)

Architectures: residual network

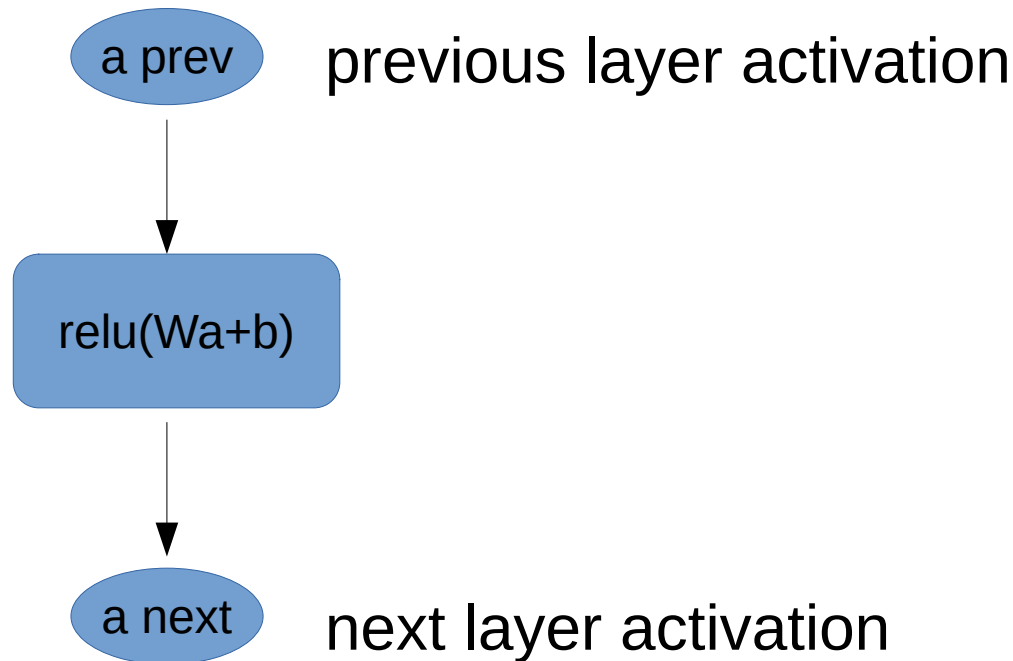
Problem: very deep networks are hard to train

Gradients w.r.t. first layers are volative

Architectures: residual network

Idea: let's create a shortcut for gradients

Normal layer

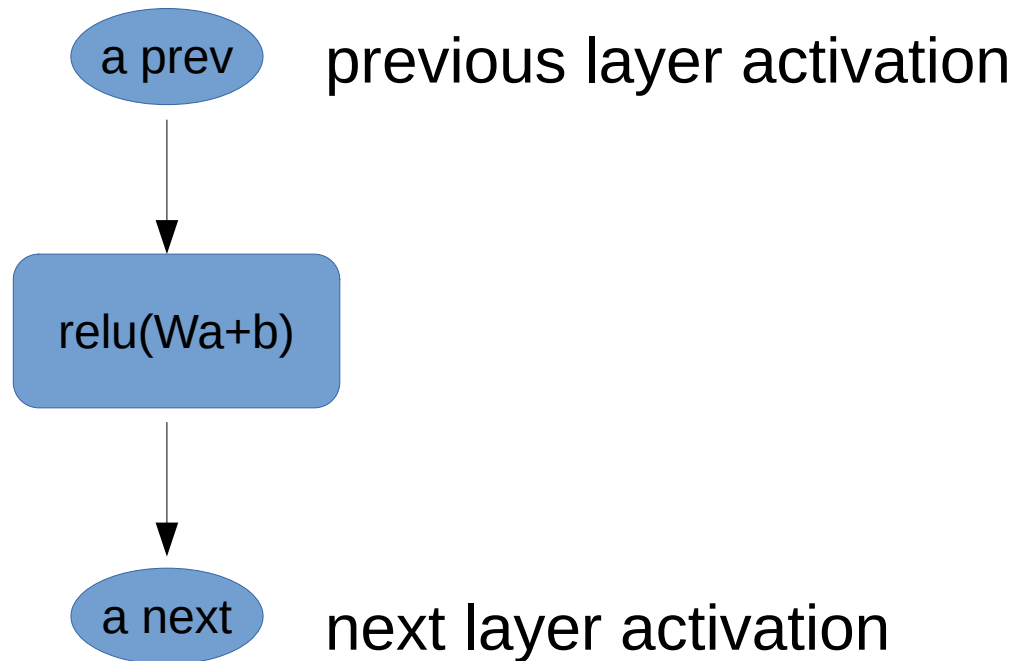


$$f_{w,b}(x) = \text{relu}(W \cdot a + b)$$

Architectures: residual network

Idea: let's create a shortcut for gradients

Normal layer



$$f_{w,b}(x) = \text{relu}(W \cdot a + b)$$

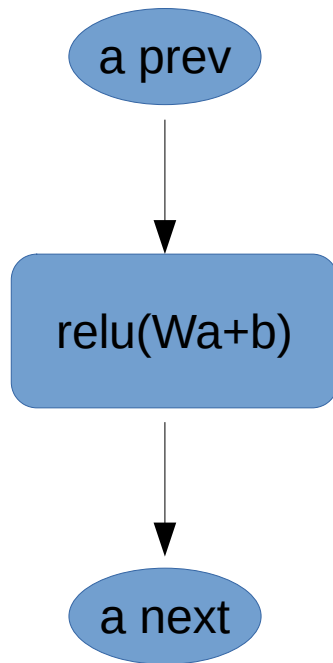
$$\nabla f_{w,b}(x) = \underline{\nabla \text{relu}(W \cdot a + b)}$$

Gradients can vanish if relu < 0

Architectures: residual network

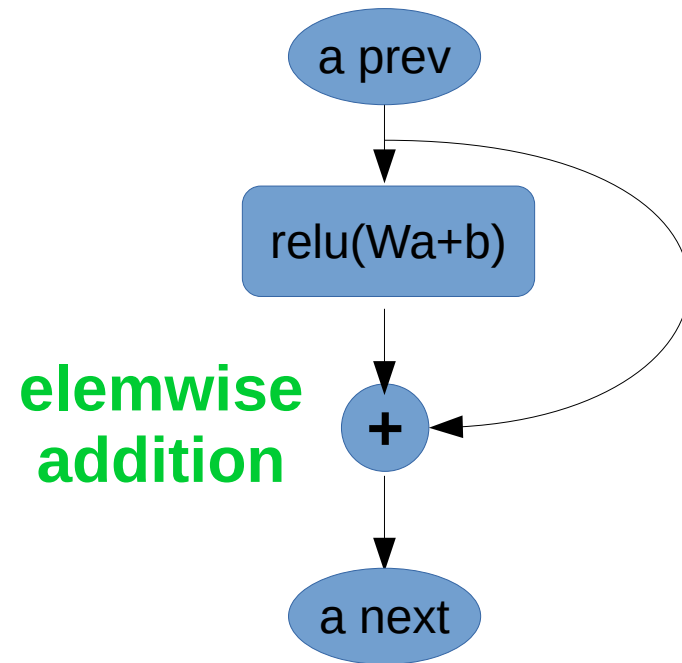
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Normal layer



$$f_{w,b}(x) = \text{relu}(W \cdot a + b)$$

Residual layer

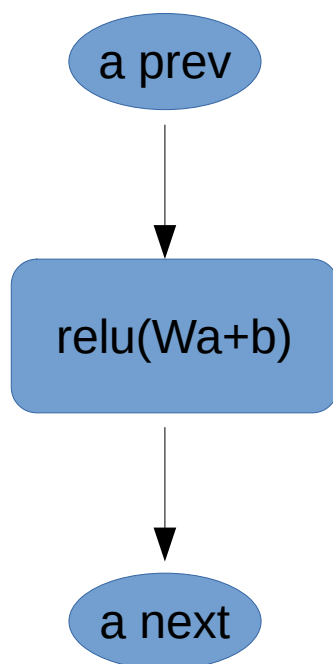


$$f_{w,b}(x) = \text{relu}(W \cdot a + b) + X$$

Architectures: residual network

Idea: let's create a shortcut for gradients

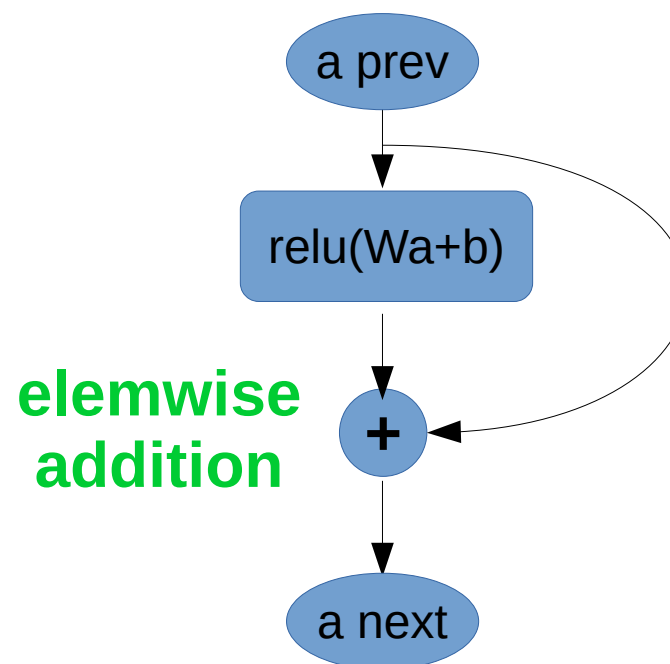
Normal layer



$$f_{w,b}(x) = \text{relu}(W \cdot a + b)$$

$$\nabla f_{w,b}(x) = \nabla \text{relu}(W \cdot a + b)$$

Residual layer



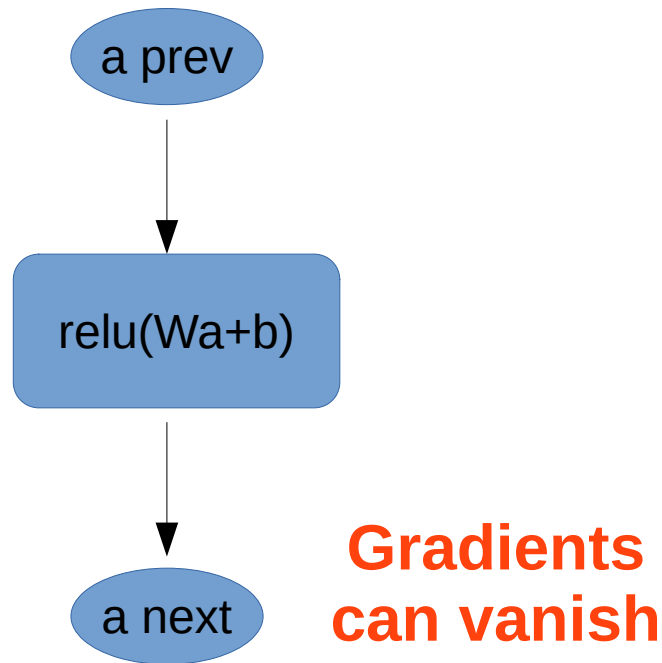
$$f_{w,b}(x) = \text{relu}(W \cdot a + b) + X$$

???

Architectures: residual network

Idea: let's create a shortcut for gradients

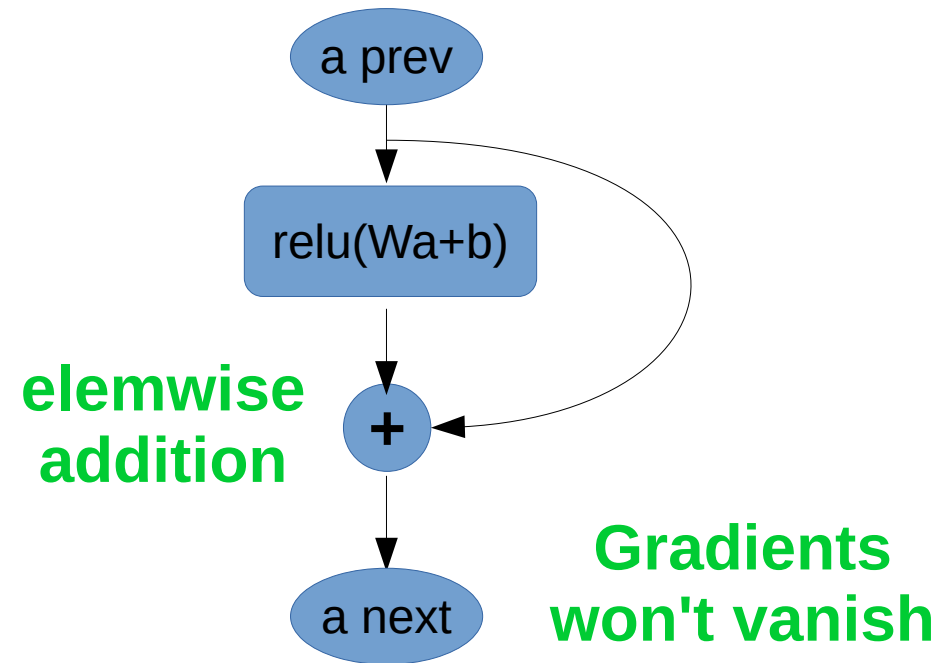
Normal layer



$$f_{w,b}(x) = \text{relu}(W \cdot a + b)$$

$$\nabla f_{w,b}(x) = \underline{\nabla \text{relu}(W \cdot a + b)}$$

Residual layer

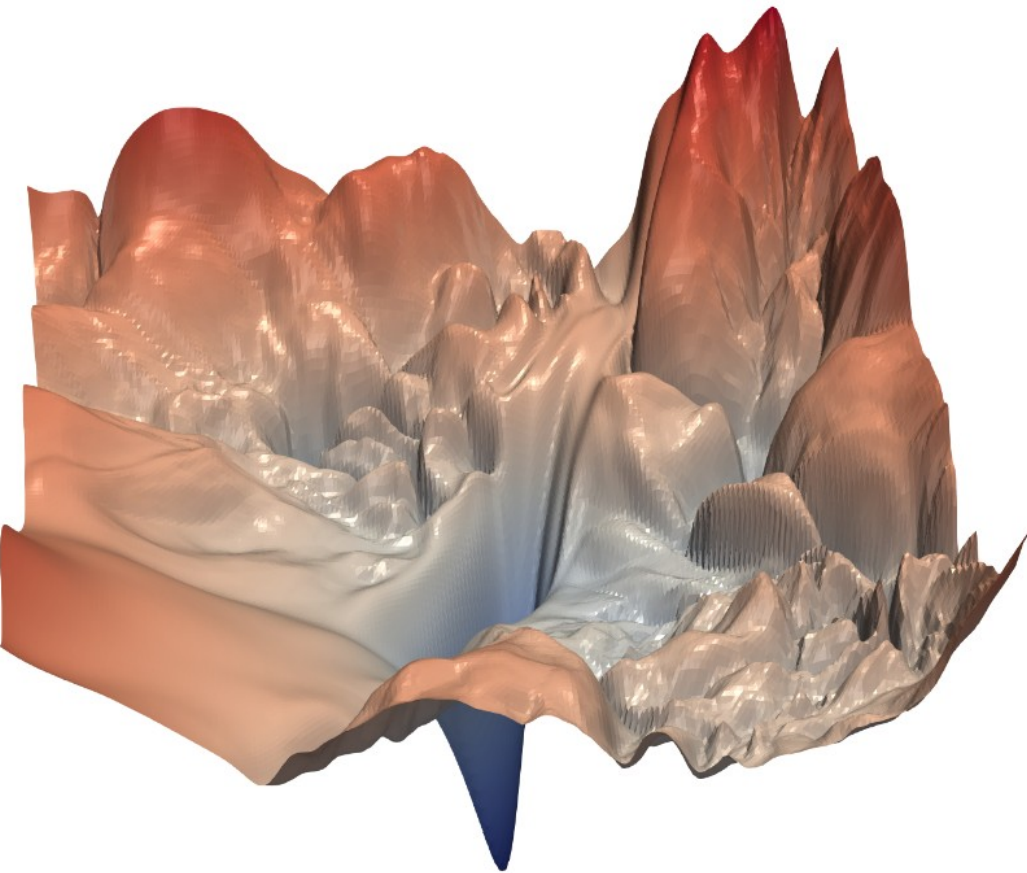


$$f_{w,b}(x) = \text{relu}(W \cdot a + b) + X$$

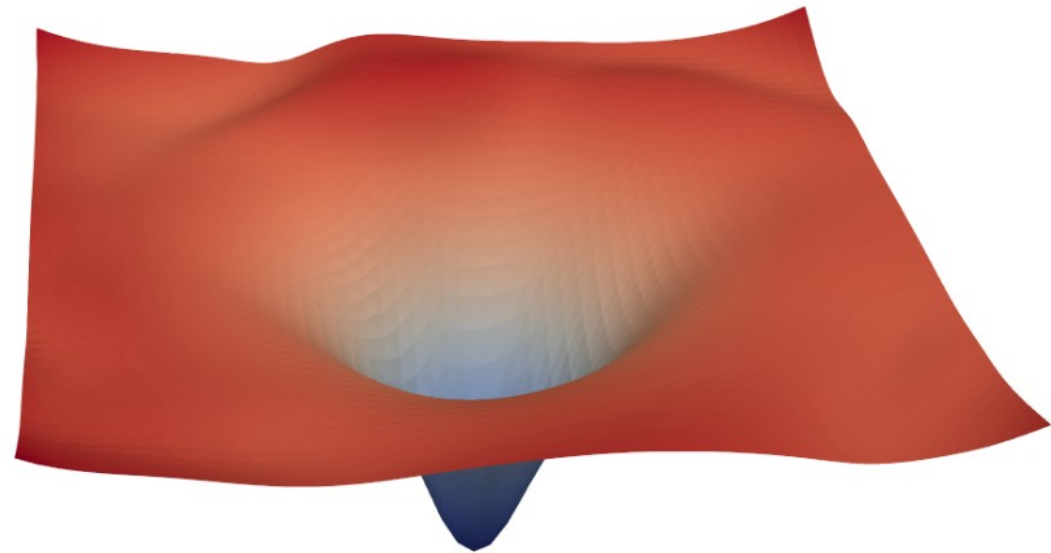
$$\nabla f_{w,b}(x) = \underline{\nabla \text{relu}(W \cdot a + b)} + \underline{\vec{1}}$$

Loss Surfaces

Idea: <https://arxiv.org/abs/1712.09913>



(a) without skip connections



(b) with skip connections

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BatchNorm, Residual connections

Nuff

Coding time!

