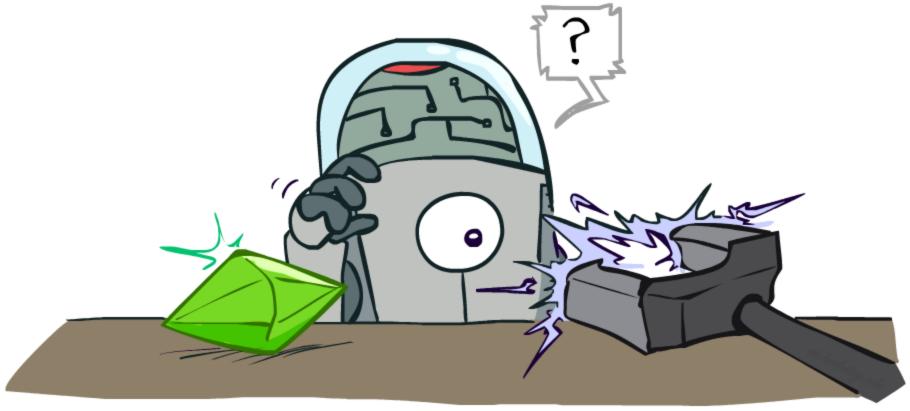
CS 188: Artificial Intelligence

Reinforcement Learning

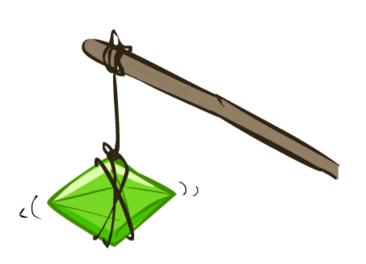


Instructors: Davis Foote and Jacob Andreas

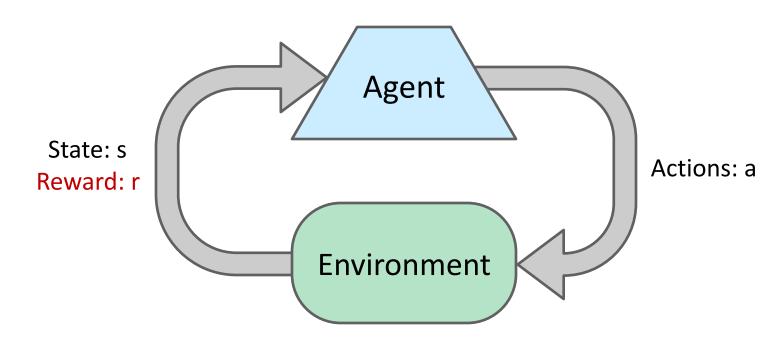
University of California, Berkeley

[Slides by Dan Klein, Pieter Abbeel, Anca Dragan, Davis Foote, Jacob Andreas. http://ai.berkeley.edu.]









Basic idea:

- Receive feedback in the form of rewards
- Agent's utility is defined by the reward function
- Must (learn to) act so as to maximize expected rewards
- All learning is based on observed samples of outcomes!

- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model T(s,a,s')
 - A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$







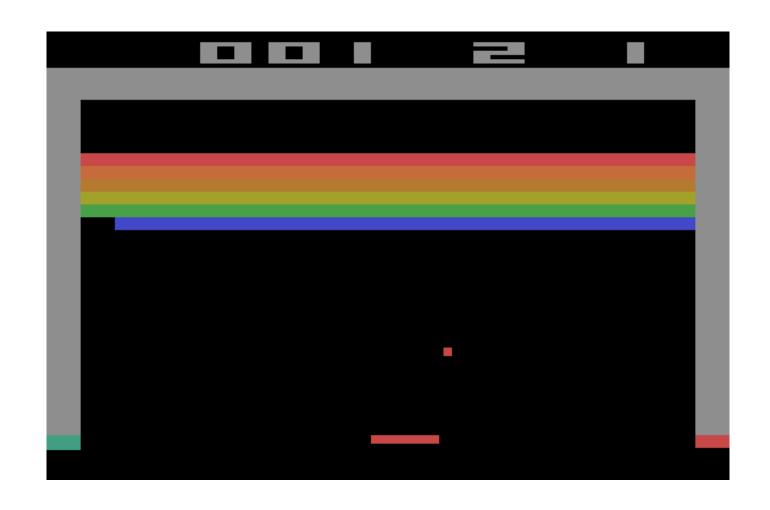
- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try actions and states out to learn

Example: Toddler Robot

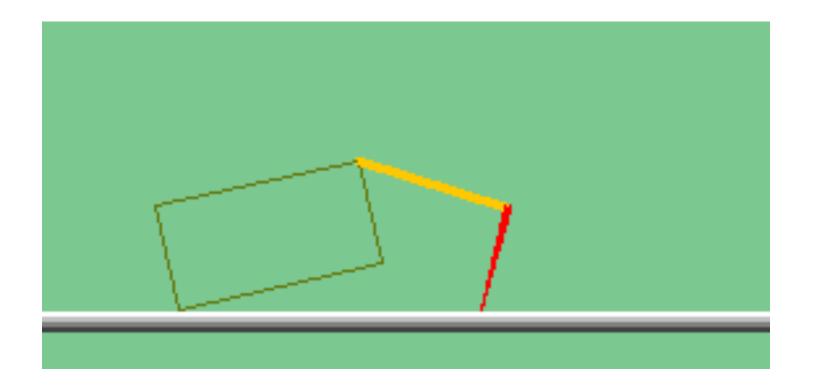


[Tedrake, Zhang and Seung, 2005]

Example: Learning to Play Breakout



The Crawler!



- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model T(s,a,s')
 - A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$

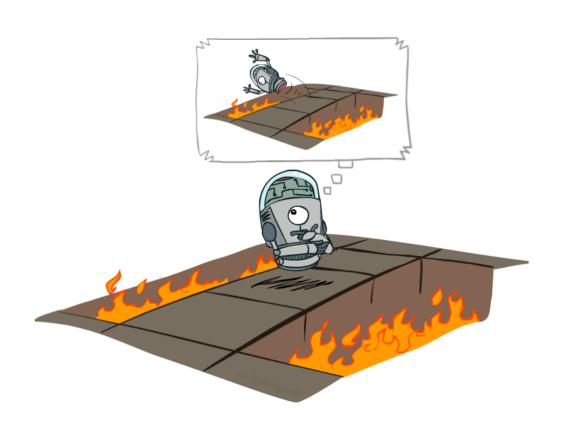






- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try actions and states out to learn

Offline (MDPs) vs. Online (RL)

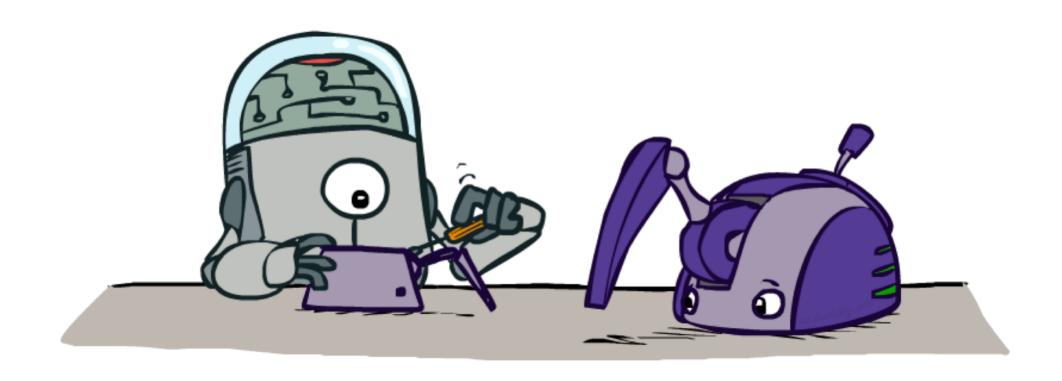




Offline Solution

Online Learning

Model-Based Learning



Model-Based Learning

Model-Based Idea:

- Learn an approximate model based on experiences
- Solve for values as if the learned model were correct



- Count outcomes s' for each s, a
- Normalize to give an estimate of $\widehat{T}(s, a, s')$ Discover each $\widehat{R}(s, a, s')$ when we experience (s, a, s')



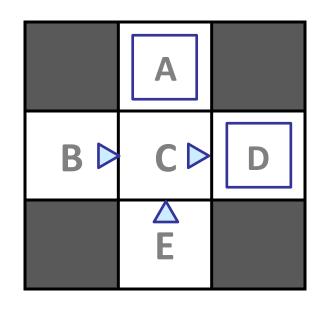
For example, use value iteration, as before





Example: Model-Based Learning

Input Policy π



Assume: $\gamma = 1$

Observed Episodes (Training)

Episode 1

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 2

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Learned Model

$$\widehat{T}(s,a,s')$$

T(B, east, C) = 1.00 T(C, east, D) = 0.75 T(C, east, A) = 0.25

Episode 3

E, north, C, -1 C, east, D, -1 D, exit, x, +10

Episode 4

E, north, C, -1 C, east, A, -1 A, exit, x, -10

$$\hat{R}(s, a, s')$$

R(B, east, C) = -1 R(C, east, D) = -1 R(D, exit, x) = +10 ...

Example: Expected Age

Goal: Compute expected age of cs188 students

Known P(A)

$$E[A] = \sum_{a} P(a) \cdot a = 0.35 \times 20 + \dots$$

Without P(A), instead collect samples [a₁, a₂, ... a_N]

Unknown P(A): "Model Based"

Why does this work? Because eventually you learn the right model.

$$\hat{P}(a) = \frac{\text{num}(a)}{N}$$

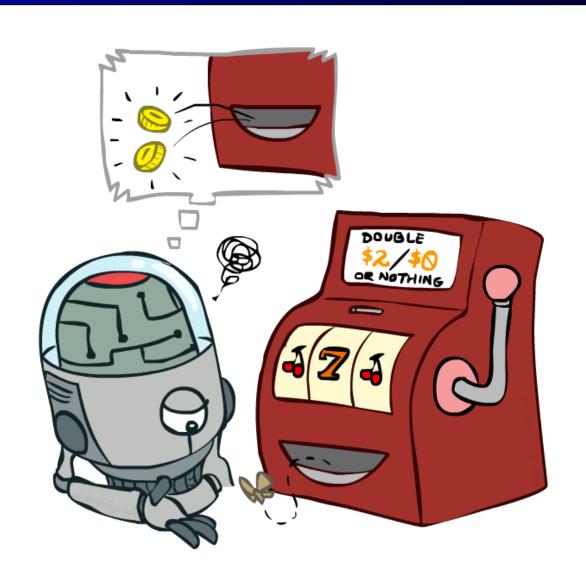
$$E[A] \approx \sum_{a} \hat{P}(a) \cdot a$$

Unknown P(A): "Model Free"

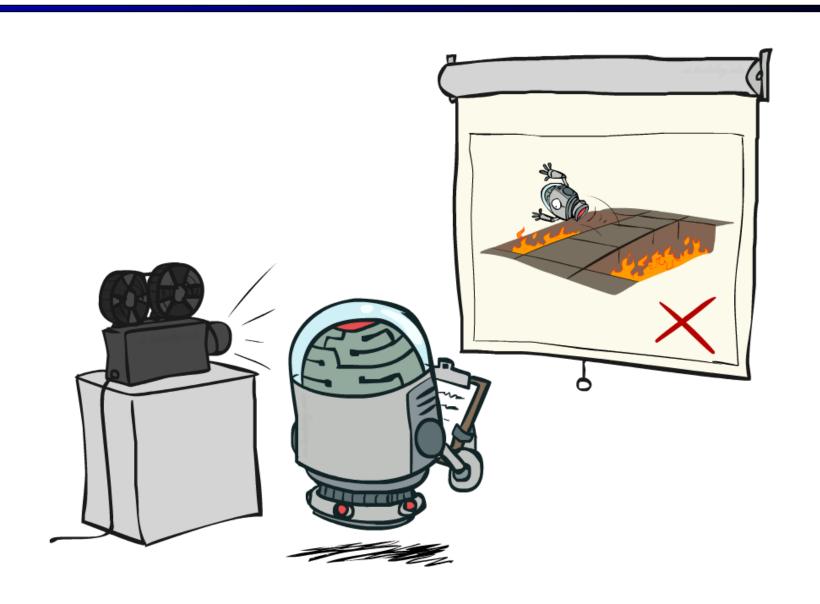
$$E[A] \approx \frac{1}{N} \sum_{i} a_{i}$$

Why does this work? Because samples appear with the right frequencies.

Model-Free Learning



Passive Reinforcement Learning



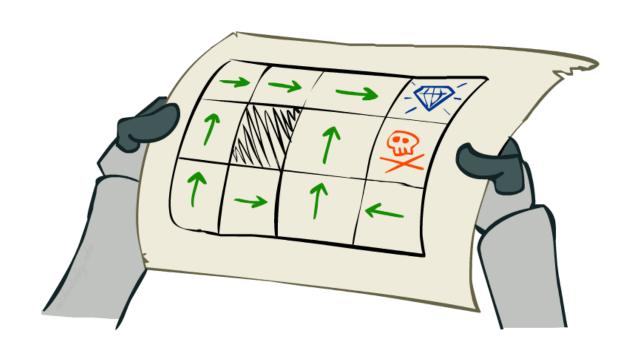
Passive Reinforcement Learning

Simplified task: policy evaluation

- Input: a fixed policy $\pi(s)$
- You don't know the transitions T(s,a,s')
- You don't know the rewards R(s,a,s')
- Goal: learn the state values

In this case:

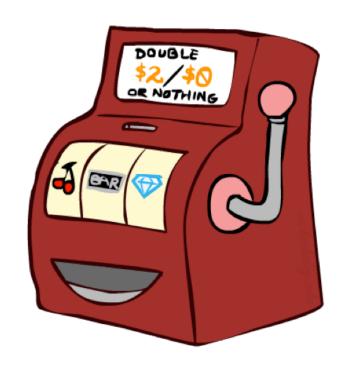
- Learner is "along for the ride"
- No choice about what actions to take
- Just execute the policy and learn from experience
- This is NOT offline planning! You actually take actions in the world.



Direct Evaluation

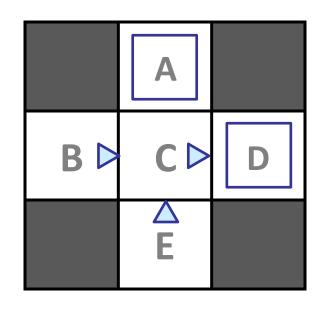
- Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be
 - Average those samples





Example: Direct Evaluation

Input Policy π



Assume: $\gamma = 1$

Observed Episodes (Training)

Episode 1

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 3

E, north, C, -1 C, east, D, -1 D, exit, x, +10

Episode 2

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 4

E, north, C, -1 C, east, A, -1 A, exit, x, -10

Output Values

	A -10	
+8 B	C +4	+10 D
	E -2	

Problems with Direct Evaluation

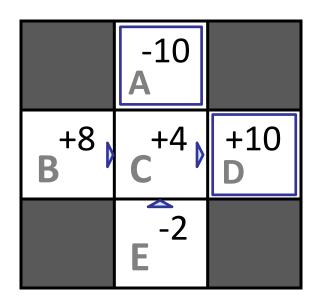
What's good about direct evaluation?

- It's easy to understand
- It doesn't require any knowledge of T, R
- It eventually computes the correct average values, using just sample transitions

What bad about it?

- It wastes information about state connections
- Each state must be learned separately
- So, it takes a long time to learn

Output Values



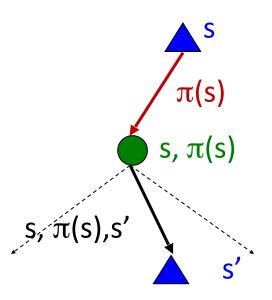
If B and E both go to C under this policy, how can their values be different?

Why Not Use Policy Evaluation?

- Simplified Bellman updates calculate V for a fixed policy:
 - Each round, replace V with a one-step-look-ahead layer over V

$$V_0^{\pi}(s) = 0$$

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$
 s, $\pi(s)$, s'



- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
 - In other words, how to we take a weighted average without knowing the weights?

Sample-Based Policy Evaluation?

We want to improve our estimate of V by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

Idea: Take samples of outcomes s' (by doing the action!) and average

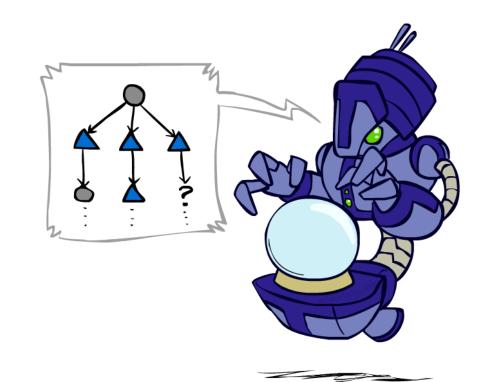
$$sample_1 = R(s, \pi(s), s'_1) + \gamma V_k^{\pi}(s'_1)$$

$$sample_2 = R(s, \pi(s), s'_2) + \gamma V_k^{\pi}(s'_2)$$

$$\dots$$

$$sample_n = R(s, \pi(s), s'_n) + \gamma V_k^{\pi}(s'_n)$$

$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_{i} sample_i$$



Temporal Difference Learning

- Big idea: learn from every experience!
 - Update V(s) each time we experience a transition (s, a, s', r)
 - Likely outcomes s' will contribute updates more often

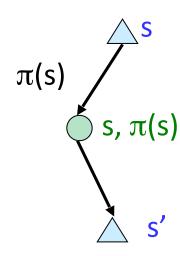


- Policy still fixed, still doing evaluation!
- Move values toward value of whatever successor occurs: running average



Update to V(s): $V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + (\alpha)sample$

Same update: $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$



Exponential Moving Average

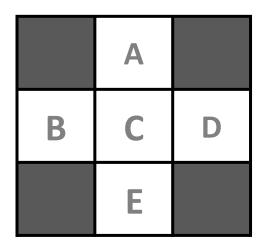
- Exponential moving average
 - The running interpolation update: $\bar{x}_n = (1-\alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$
 - Makes recent samples more important

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \cdots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \cdots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages

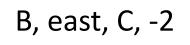
Example: Temporal Difference Learning

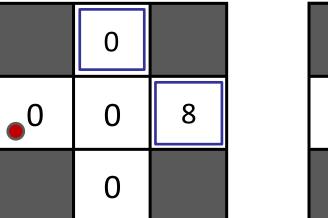
States

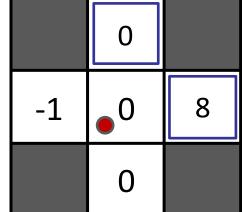


Assume: $\gamma = 1$, $\alpha = 1/2$

Observed Transitions







$$V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + \alpha \left[R(s, \pi(s), s') + \gamma V^{\pi}(s') \right]$$

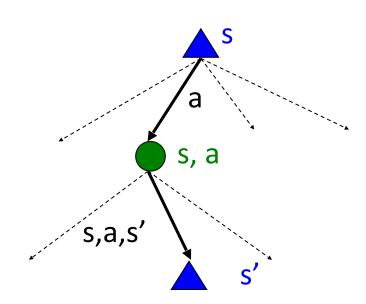
Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

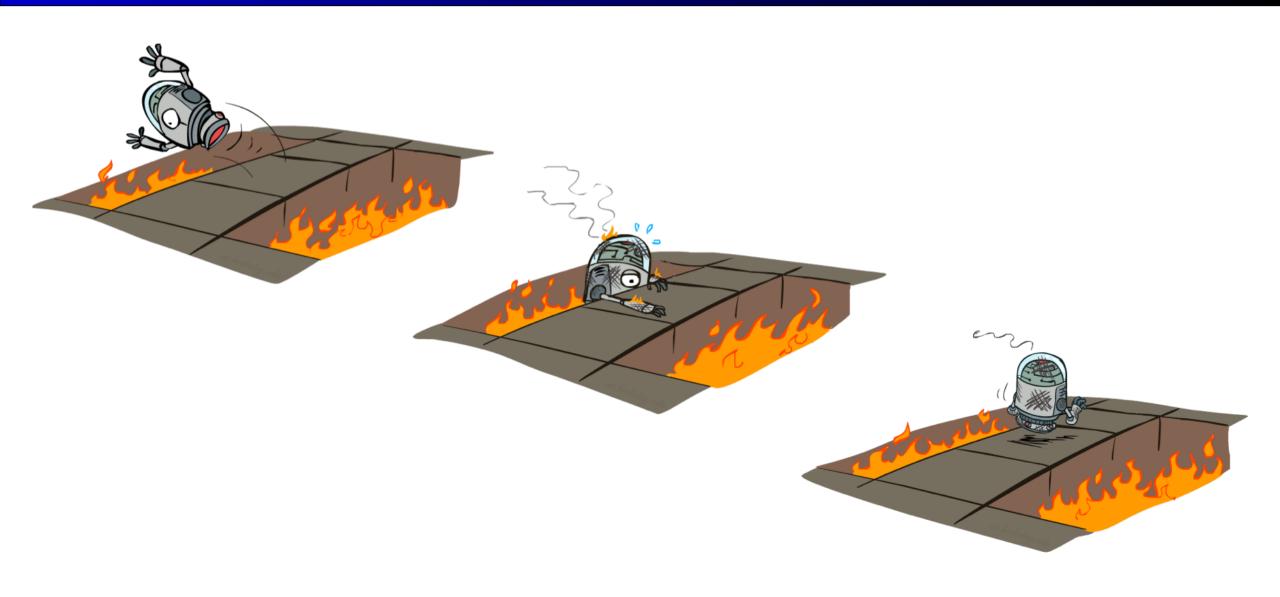
$$\pi(s) = \arg\max_{a} Q(s, a)$$

$$Q(s,a) = \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma V(s') \right]$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!

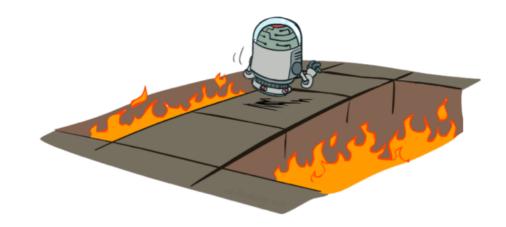


Active Reinforcement Learning



Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - You choose the actions now
 - Goal: learn the optimal policy / values



In this case:

- Learner makes choices!
- Fundamental tradeoff: exploration vs. exploitation
- This is NOT offline planning! You actually take actions in the world and find out what happens...

Detour: Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 - Start with $V_0(s) = 0$, which we know is right
 - Given V_k , calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
 - Start with $Q_0(s,a) = 0$, which we know is right
 - Given Q_k , calculate the depth k+1 q-values for all q-states:

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

Q-Learning

Q-Learning: sample-based Q-value iteration

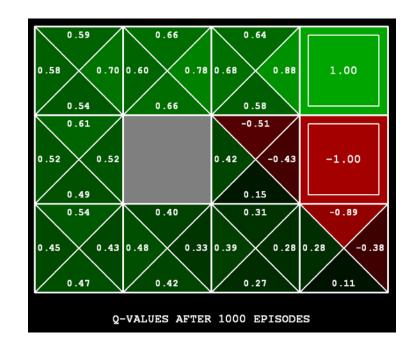
$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

- Learn Q(s,a) values as you go
 - Receive a sample (s,a,s',r)
 - Consider your old estimate: Q(s, a)
 - Consider your new sample estimate:

$$sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$$

• Incorporate the new estimate into a running average:

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + (\alpha) [sample]$$

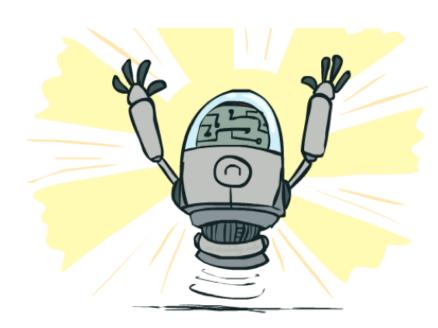


[Demo: Q-learning – gridworld (L10D2)]

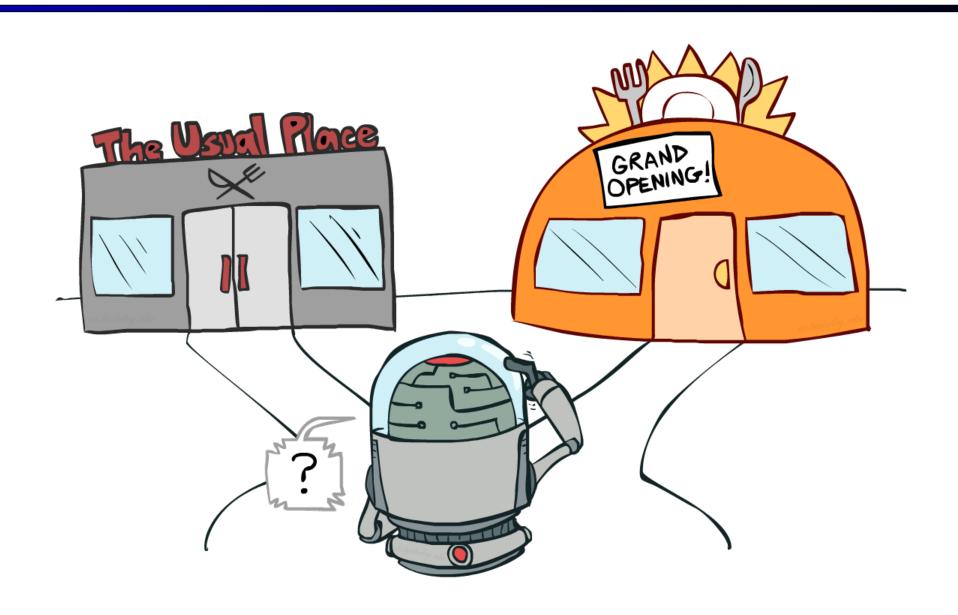
[Demo: O-learning - crawler (L10D3)]

Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
 - You have to explore enough
 - You have to eventually make the learning rate small enough
 - ... but not decrease it too quickly
 - Basically, in the limit, it doesn't matter how you select actions (!)



Exploration vs. Exploitation



How to Explore?

- Several schemes for forcing exploration
 - Simplest: random actions (ε-greedy)
 - Every time step, flip a coin
 - With (small) probability ε, act randomly
 - With (large) probability 1- ε , act on current policy
 - Problems with random actions?
 - You do eventually explore the space, but keep thrashing around once learning is done
 - One solution: lower ε over time
 - Another solution: exploration functions



Exploration Functions

When to explore?

- Random actions: explore a fixed amount
- Better idea: explore areas whose badness is not (yet) established, eventually stop exploring

Exploration function

■ Takes a value estimate u and a visit count n, and returns an optimistic utility, e.g. f(u,n) = u + k/n



Regular Q-Update: $Q(s, a) \leftarrow_{\alpha} R(s, a, s') + \gamma \max_{a'} Q(s', a')$

Modified Q-Update: $Q(s, a) \leftarrow_{\alpha} R(s, a, s') + \gamma \max_{a'} f(Q(s', a'), N(s', a'))$

■ Note: this propagates the "bonus" back to states that lead to unknown states as well!

The Story So Far: MDPs and RL

Known MDP: Offline Solution

Goal Technique

Compute V*, Q*, π * Value / policy iteration

Evaluate a fixed policy π Policy evaluation

Unknown MDP: Model-Based

Goal Technique

Compute V*, Q*, π * VI/PI on approx. MDP

Evaluate a fixed policy π PE on approx. MDP

Unknown MDP: Model-Free

Goal Technique

Compute V*, Q*, π * Q-learning

Evaluate a fixed policy π Value Learning