

# CV hw3

Zheyao Zhu

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## Q1.1

1.  $\frac{\delta W(x;p)}{\delta p^T}$  is the jacobian of the image evaluated at (x;p)

2.  $A = \nabla I \frac{\delta W}{\delta p}$  ,  $b = T(x) - I(W(x, p))$

3.  $A^T A$  needs to be full rank

## Q1.3



Frame 1

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Frame 100

:



Frame 200

:



Frame 300

:



Frame 400

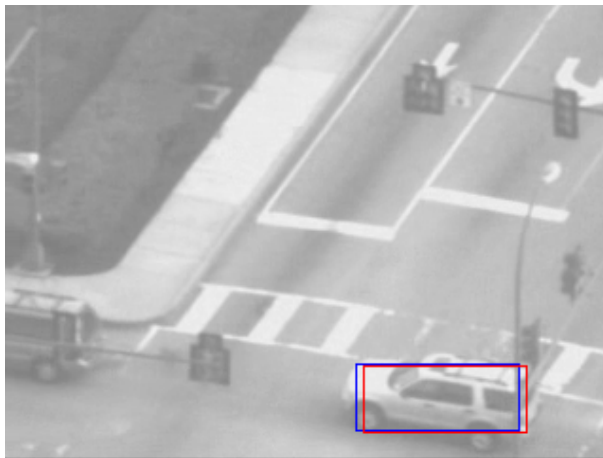
:

Q1.4



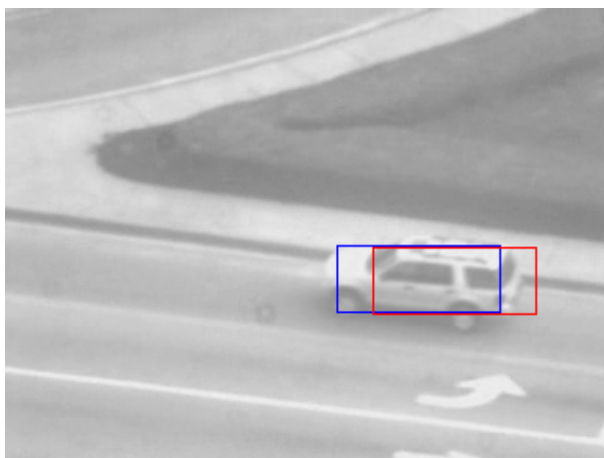
Frame 1

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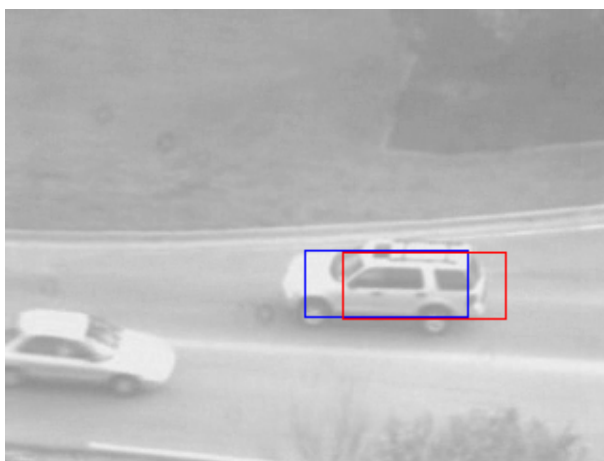
Frame 100

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Frame 200

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Frame 300

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**Frame 400**

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## Q2.1

We are given the following equation

$$I_{t+1}(x) = I_t(x) + \sum_{k=1}^k \omega_k B_k$$

$$\Rightarrow I_{t+1}(x) - I_t(x) = \sum_{k=1}^k \omega_k B_k$$

For every  $\omega_i$  where  $i = 1, 2, \dots, K$ , we multiply  $B_i$  to both sides of equation :

$$B_i * (I_{t+1}(x) - I_t(x)) = B_i * \sum_{k=1}^k \omega_k B_k(x)$$

Since the bases are orthogonal to each other,  $B_i * B_k = 0$  for all  $i \neq k$ :

$$B_i(I_{t+1}(x) - I_t(x)) = \omega_i * \|B_i(x)\|^2$$

$$\Rightarrow \omega_i = \frac{B_i(I_{t+1}(x) - I_t(x))}{\|B_i(x)\|^2}, \forall i = 1, 2, \dots, K$$

Q2.3



Frame 1

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Frame 100

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Frame 200

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Frame 300

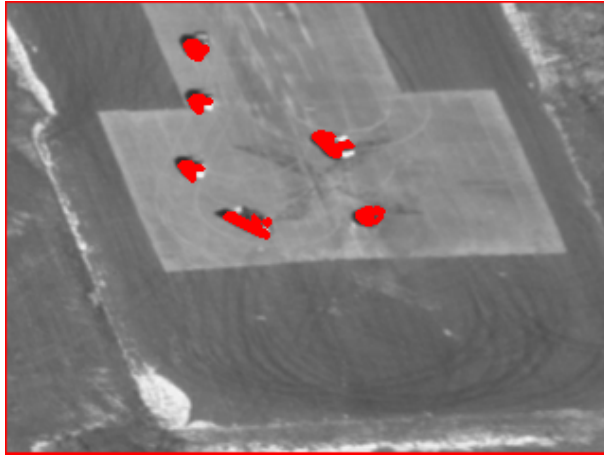
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Frame 400

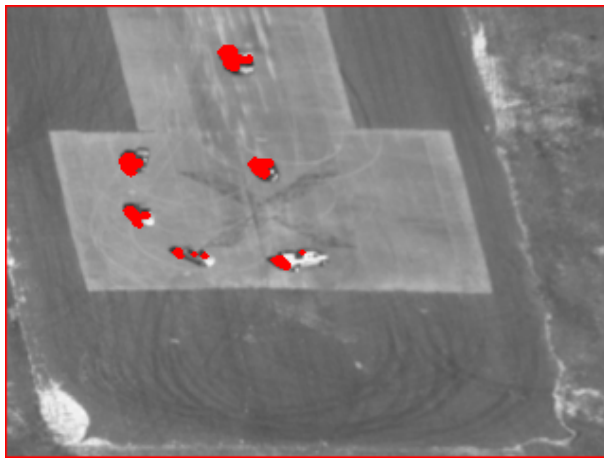
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Q3.3



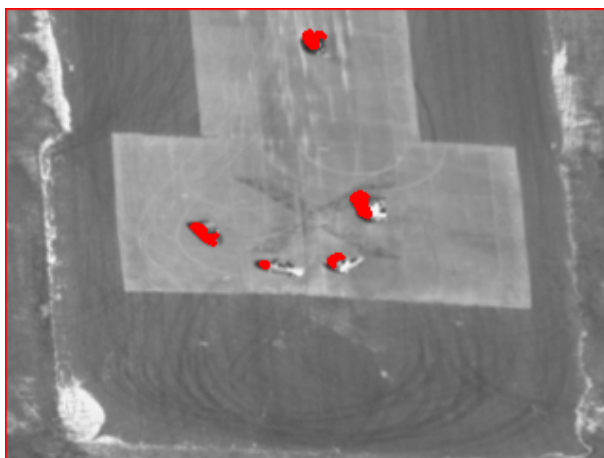
Frame 30

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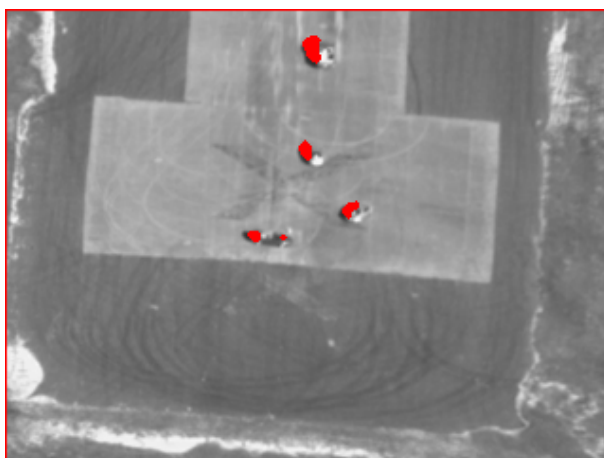
Frame 60

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Frame 90

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Frame 120

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## Q4.1

Because the most time consuming tasks such as computing the gradient of the image, evaluating the jacobian, computing the steepest descent images and computing the Hessian could be pre-computed. So doing the gradient descent optimization iterations, the aforementioned computations wouldn't be repeated.