#### Monday, February 22, 2016 at 10:31 PM

Washington University, Saint Louis, MO, United States · 37°F Mostly Clear

ReadMe

# **Assignment 2: Shapes**

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Date: 02/22/2016, Monday

Late days used this lab: o

#### Structure

#### Shape (Base class)

- triangle: struct
  - contains 3 points and 1 normal vector to this triangle/face, and a vector of 3 normal vectors corresponding to the 3 vertices
- computeNormal: compute the normal vector (of face) given a triangle.
- drawShapeWireFrame(): do the wire frame
- drawShapeFlat(): do the flat shading
- drawShapeSmooth(): do the smooth shading
- ReverseTriangleVertex(): make the triangle counter-clockwise if they are not
- tessellation is a vector of triangles, I use it to store triangles.

#### Cube (derived class #1)

- computeTriangle(int n): given 1st parameter n, it generate all correct triangles, and push those triangles to tesselation.
- computeVertexNormal(triangle &tr): given a triangle with p1, p2, p3 it can calculate the face's normal.

#### Cylinder(derived class #2)

• computeTriangle(int n, int m): functionality is similar as cube

#### Cone(derived class #3)

• computeTriangle(int n, int m): functionality is similar as cube

#### Sphere(derived class #4)

I found this python code on line

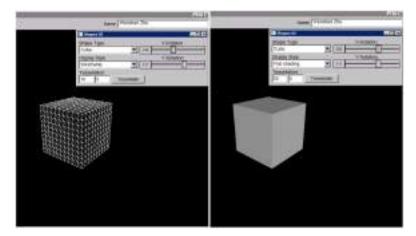
https://sites.google.com/site/dlampetest/python/triangulating-a-sphere-recursively

(https://sites.google.com/site/dlampetest/python/triangulating-a-sphere-recursively)

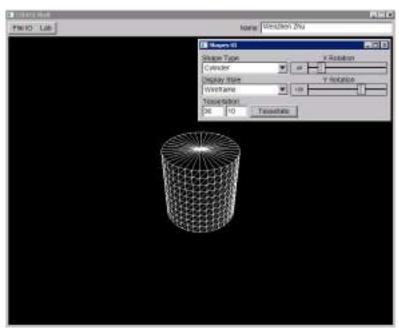
However, after I tried it in python notebook, it doesn't work. I think I understand this recursive midpoint divide process. I did a prototype in Mathematica, which you can find in the appendix.

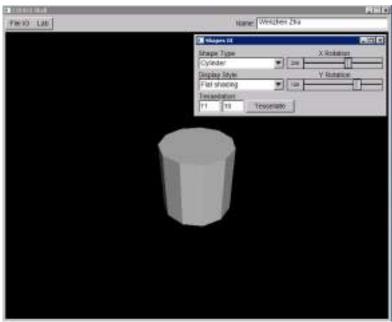
#### **Pictures**

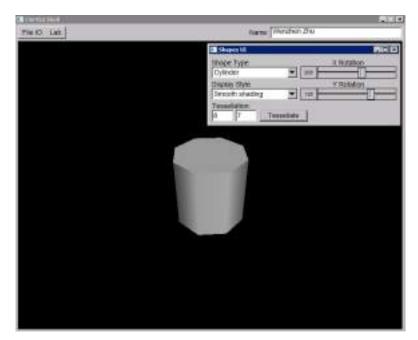
#### Cube



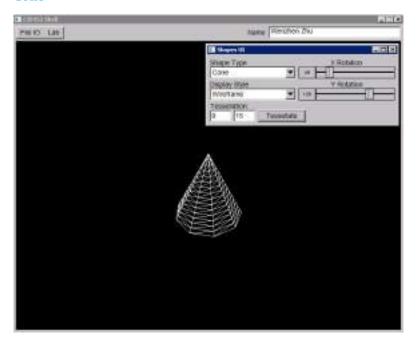
#### Cylinder

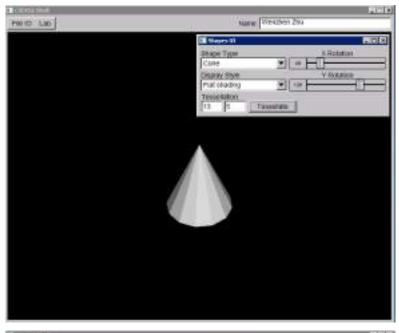


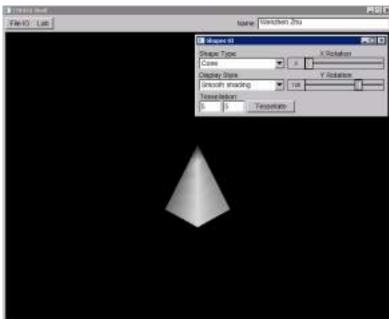




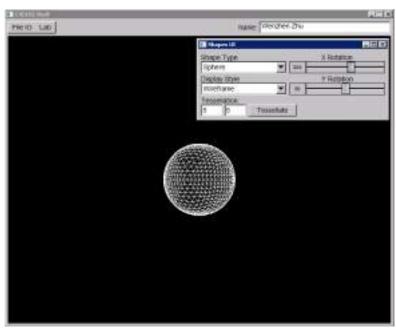
#### Cone

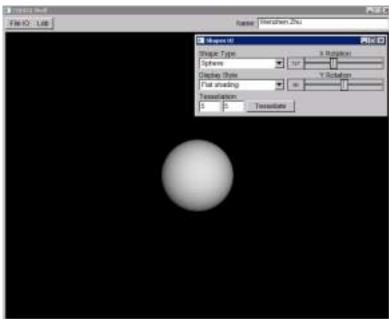


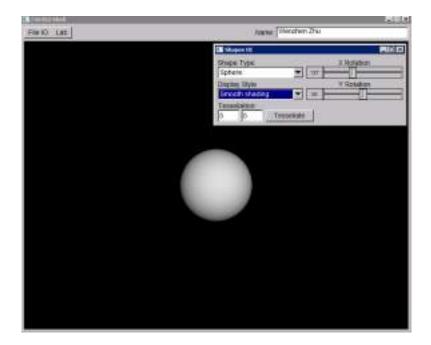




Sphere





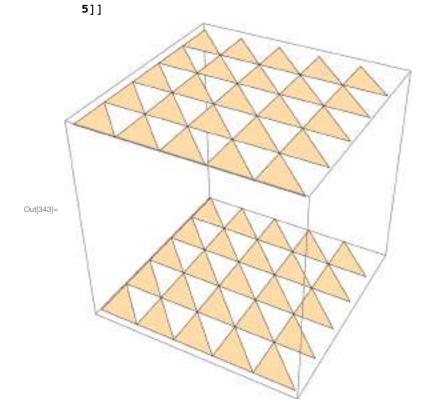


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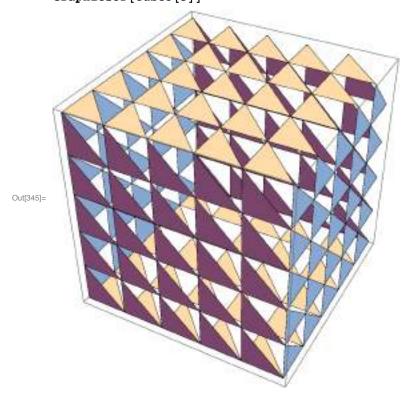
# Shapes ReadMe

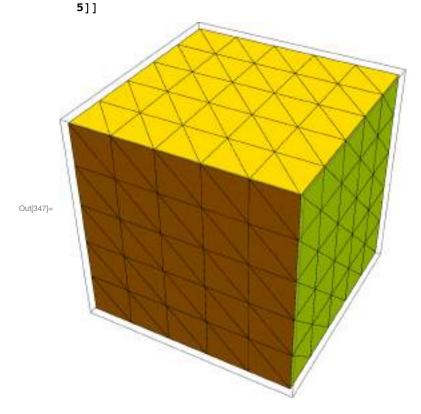
# Cube

```
 \text{Cubel}[n_{-}] := \text{Table} \Big[ \text{Polygon} \Big[ \Big\{ \Big\{ \frac{i-1}{n} - 0.5, \frac{j-1}{n} - 0.5, -0.5 \Big\}, \Big\} \Big] \\  \Big\{ \frac{i}{n} - 0.5, \frac{j-1}{n} - 0.5, -0.5 \Big\}, \Big\{ \frac{i-1}{n} - 0.5, \frac{j}{n} - 0.5, -0.5 \Big\} \Big\} \Big], \{i, 1, n\}, \{j, 1, n\} \Big]  Graphics 3D [ cubel [ 5] ]
```



```
Graphics3D[cube3[5]]
```

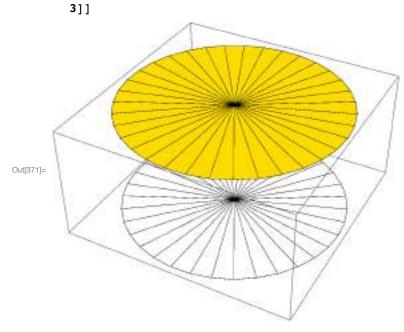




# Cylinder

 $\label{eq:loss_problem} $$ \ln[370] = \mbox{cylinder0[n_, m_] := {FaceForm[Yellow, Transparent], Table[} $$ $$ \mbox{cylinder0[n_, m_] := {FaceForm[Yellow, Transparent], Table[} $$ \mbox{cylinder0[n_, m_] := {FaceForm[Yellow,$  $Polygon \Big[ \text{If} \left[ k = -0.5, \text{Reverse, Identity} \right] @ \left\{ \left\{ 0, \, 0, \, k \right\}, \, \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n} \, 2 \, \pi \right], \, k \right\}, \\ \left\{ \text{Cos} \left[ \frac{i}{n}$  $\left\{ \text{Cos} \left[ \, \frac{\text{i} + 1}{n} \, 2 \, \pi \right], \, \text{Sin} \left[ \, \frac{\text{i} + 1}{n} \, 2 \, \pi \right], \, k \right\} \right\} \right], \, \left\{ \text{i}, \, 1, \, n \right\}, \, \left\{ \text{k}, \, \left\{ -0.5, \, 0.5 \right\} \right\} \right] \right\}$ Graphics3D[cylinder0[

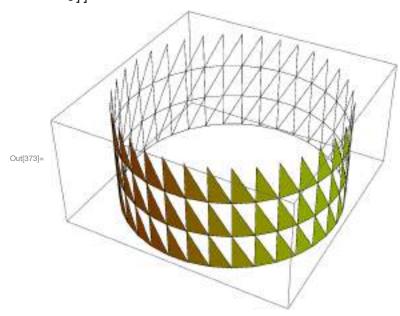
35,



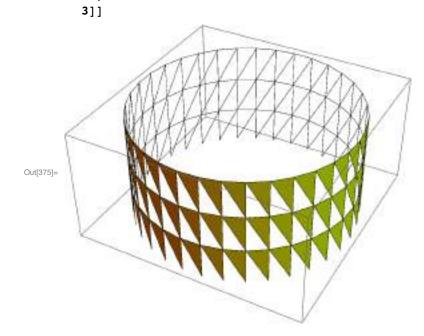
 $\begin{aligned} & \text{In} [372] = \text{ cylinder1} \big[ n_-, \, m_- \big] := \Big\{ \text{FaceForm} \big[ \text{Yellow, Transparent} \big], \, \text{Table} \Big[ \\ & \text{Polygon} \Big[ \Big\{ \Big\{ \text{Cos} \Big[ \frac{\textbf{i}}{n} \; 2 \; \pi \Big], \, \text{Sin} \Big[ \frac{\textbf{i}}{n} \; 2 \; \pi \Big], \, -0.5 + \frac{\textbf{j}}{m} \Big\}, \, \Big\{ \text{Cos} \Big[ \frac{\textbf{i}}{n} \; 2 \; \pi \Big], \, \text{Sin} \Big[ \frac{\textbf{i}}{n} \; 2 \; \pi \Big], \, -0.5 + \frac{\textbf{j}-1}{m} \Big\} \Big\} \Big], \, \Big\{ \textbf{i}, \, 1, \, \textbf{n} \big\}, \, \big\{ \textbf{j}, \, 1, \, \textbf{m} \big\} \Big] \Big\} \end{aligned}$ 

Graphics3D[cylinder1[

35, 3]]

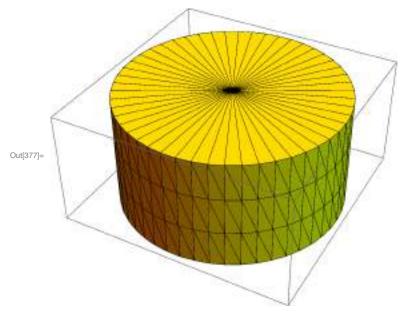


$$\begin{aligned} & \text{Table} \big[ \text{Polygon} \big[ \big\{ \big\{ \text{Cos} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big], \ \text{Sin} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big], \ -0.5 + \frac{\textbf{j}}{m} \big\}, \ \big\{ \text{Cos} \big[ \frac{\textbf{i}}{n} \ 2 \, \pi \big], \ \text{Sin} \big[ \frac{\textbf{i}}{n} \ 2 \, \pi \big], \ -0.5 + \frac{\textbf{j}}{m} \big\}, \ \big\{ \text{Cos} \big[ \frac{\textbf{i}}{n} \ 2 \, \pi \big], \ \text{Sin} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big], \ -0.5 + \frac{\textbf{j} - \textbf{1}}{m} \big\} \big\} \big], \ \{ \textbf{i}, \ 1, \ n \}, \ \{ \textbf{j}, \ 1, \ m \} \big] \big\} \\ & \text{Graphics3D} \big[ \text{cylinder2} \big[ \big] \end{aligned}$$



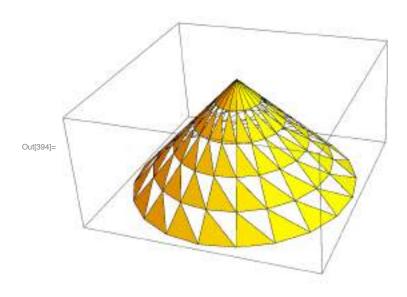
In[376]:= cylinder[n\_, m\_] := { {FaceForm[Yellow, Transparent], Table[ Polygon [If [k == -0.5, Reverse, Identity] @  $\{0, 0, k\}$ ,  $\{\cos\left[\frac{i}{n}2\pi\right], \sin\left[\frac{i}{n}2\pi\right], k\}$ ,  $\left\{ \cos \left[ \frac{i+1}{n} 2\pi \right], \sin \left[ \frac{i+1}{n} 2\pi \right], k \right\} \right\}, \{i, 1, n\}, \{k, \{-0.5, 0.5\}\} \right],$ Table [Polygon [  $\{\left\{\cos\left[\frac{\mathbf{i}}{n} \ 2 \ \pi\right], \ \sin\left[\frac{\mathbf{i}}{n} \ 2 \ \pi\right], \ -0.5 + \frac{\mathbf{j}}{m}\right\}, \ \left\{\cos\left[\frac{\mathbf{i}}{n} \ 2 \ \pi\right], \ \sin\left[\frac{\mathbf{i}}{n} \ 2 \ \pi\right], \ -0.5 + \frac{\mathbf{j}}{m}\right\}$  $\frac{\mathtt{j}-1}{\mathtt{m}}\big\},\, \big\{\mathsf{Cos}\big[\frac{\mathtt{i}+1}{\mathtt{n}}\,2\,\pi\big],\, \mathsf{Sin}\big[\frac{\mathtt{i}+1}{\mathtt{n}}\,2\,\pi\big],\, -0.5+\frac{\mathtt{j}-1}{\mathtt{m}}\big\}\big\}\big],\, \{\mathtt{i},\,1,\,\mathtt{n}\},\, \{\mathtt{j},\,1,\,\mathtt{m}\}\big],$ Table Polygon  $\left[\left\{\cos\left[\frac{i+1}{n}2\pi\right], \sin\left[\frac{i+1}{n}2\pi\right], -0.5 + \frac{j}{m}\right\}, \left\{\cos\left[\frac{i}{n}2\pi\right], \sin\left[\frac{i}{n}2\pi\right], \right\}$  $-0.5 + \frac{j}{m} \Big\}, \, \Big\{ \text{Cos} \Big[ \, \frac{\text{i}+1}{n} \, 2 \, \pi \Big], \, \text{Sin} \Big[ \, \frac{\text{i}+1}{n} \, 2 \, \pi \Big], \, -0.5 + \frac{j-1}{m} \Big\} \Big\} \Big], \, \{ \text{i}, \, 1, \, n \}, \, \{ \text{j}, \, 1, \, m \} \, \Big] \Big\}$ 

Graphics3D[cylinder[50, 3]]



### Cone

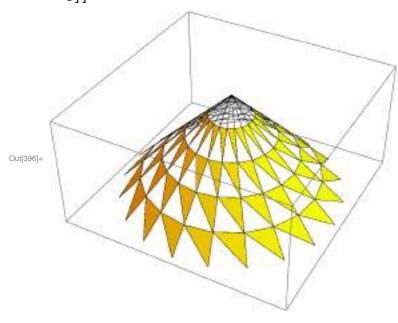
$$\begin{split} & \text{Table} \big[ \\ & \text{Polygon} \big[ \big\{ \big\{ \text{Cos} \big[ \frac{\textbf{i}}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}}{m} \big), \ \text{Sin} \big[ \frac{\textbf{i}}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}}{m} \big), \ -0.5 + \frac{\textbf{j}}{m} \big\}, \ \big\{ \text{Cos} \big[ \frac{\textbf{i}}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}-1}{m} \bigg), \\ & \text{Sin} \big[ \frac{\textbf{i}}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}-1}{m} \bigg), \ -0.5 + \frac{\textbf{j}-1}{m} \big\}, \ \big\{ \text{Cos} \big[ \frac{\textbf{i}+1}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}-1}{m} \bigg), \\ & \text{Sin} \big[ \frac{\textbf{i}+1}{n} \ 2 \ \pi \big] \ \bigg( 1 - \frac{\textbf{j}-1}{m} \bigg), \ -0.5 + \frac{\textbf{j}-1}{m} \big\} \big\} \big], \ \{\textbf{i}, 1, n\}, \ \{\textbf{j}, 1, m\} \big] \big\} \\ & \text{Graphics3D} \big[ \\ & \text{cone1} \big[ \\ & 20, \\ & 5 \big] \big] \end{aligned}$$



$$\begin{split} & \text{Table} \big[ \text{Polygon} \big[ \big\{ \big\{ \text{Cos} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j}}{m} \right), \, \text{Sin} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j}}{m} \right), \, -0.5 + \frac{\textbf{j}}{m} \big\}, \\ & \left\{ \text{Cos} \big[ \frac{\textbf{i}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j}}{m} \right), \, \text{Sin} \big[ \frac{\textbf{i}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j}}{m} \right), \, -0.5 + \frac{\textbf{j}}{m} \right\}, \, \left\{ \text{Cos} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j} - \textbf{1}}{m} \right), \, \text{Sin} \big[ \frac{\textbf{i} + \textbf{1}}{n} \ 2 \, \pi \big] \, \left( 1 - \frac{\textbf{j} - \textbf{1}}{m} \right), \, -0.5 + \frac{\textbf{j} - \textbf{1}}{m} \right) \right\} \big], \, \{ \textbf{i}, \, 1, \, n \}, \, \{ \textbf{j}, \, 1, \, m \} \, \big] \, \} \end{split}$$
Graphics3D[

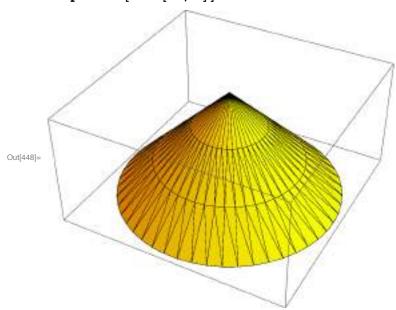
cone2[

20, 5]]



ln[447]:= cone[n\_, m\_] := {FaceForm[Yellow, Transparent], Table [Polygon [  $\{0, 0, -0.5\}$ ,  $\{\cos\left[\frac{i+1}{n}2\pi\right], \sin\left[\frac{i+1}{n}2\pi\right], -0.5\}$ ,  $\left\{ \cos \left[ \frac{i}{n} 2\pi \right], \sin \left[ \frac{i}{n} 2\pi \right], -0.5 \right\} \right\}, \{i, 1, n\} \right],$ Table Polygon  $\left[\left\{\left(\cos\left[\frac{\mathbf{j}}{n} \ 2 \ \pi\right] \left(1 - \frac{\mathbf{j}}{m}\right), \ \sin\left[\frac{\mathbf{j}}{n} \ 2 \ \pi\right] \left(1 - \frac{\mathbf{j}}{m}\right), \ -0.5 + \frac{\mathbf{j}}{m}\right\}\right]$  $\left\{ \cos \left[ \frac{i}{\pi} 2 \pi \right] \left( 1 - \frac{j-1}{\pi} \right), \sin \left[ \frac{i}{\pi} 2 \pi \right] \left( 1 - \frac{j-1}{\pi} \right), -0.5 + \frac{j-1}{\pi} \right\}, \left\{ \cos \left[ \frac{i+1}{\pi} 2 \pi \right] \right\}$  $\left(1-\frac{{\rm j}-1}{{\rm m}}\right),\; {\rm Sin}\Big[\frac{{\rm i}+1}{{\rm n}}\; 2\; \pi\Big]\; \left(1-\frac{{\rm j}-1}{{\rm m}}\right),\; -0.5+\frac{{\rm j}-1}{{\rm m}}\Big\}\Big\}\Big]\;,\; \{{\rm i}\;,\; 1\;,\; {\rm n}\}\;,\; \{{\rm j}\;,\; 1\;,\; {\rm m}\}\;\Big]\;,$ Table [Polygon [  $\left\{ \left\{ \cos \left[ \frac{\mathbf{i}+1}{n} 2\pi \right] \left( 1-\frac{\mathbf{j}}{m} \right), \sin \left[ \frac{\mathbf{i}+1}{n} 2\pi \right] \left( 1-\frac{\mathbf{j}}{m} \right), -0.5+\frac{\mathbf{j}}{m} \right\} \right\}$  $\left\{ \cos \left[ \frac{\mathbf{i}}{n} \, 2 \, \pi \right] \left( 1 - \frac{\mathbf{j}}{n} \right), \, \sin \left[ \frac{\mathbf{i}}{n} \, 2 \, \pi \right] \left( 1 - \frac{\mathbf{j}}{n} \right), \, -0.5 + \frac{\mathbf{j}}{n} \right\}, \, \left\{ \cos \left[ \frac{\mathbf{i} + 1}{n} \, 2 \, \pi \right] \left( 1 - \frac{\mathbf{j} - 1}{n} \right), \, -0.5 + \frac{\mathbf{j}}{n} \right\}$  $\sin\left[\frac{i+1}{n}2\pi\right]\left(1-\frac{j-1}{m}\right), -0.5+\frac{j-1}{m}\right\}\right], \{i, 1, n\}, \{j, 1, m\}\right]$ 

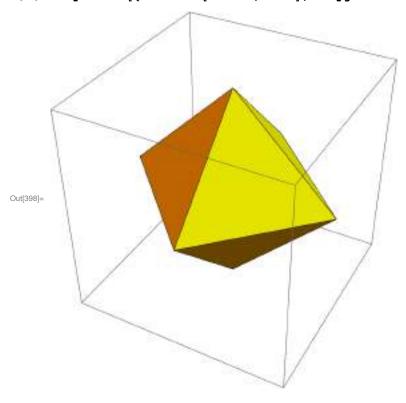
Graphics3D[cone[50, 3]]



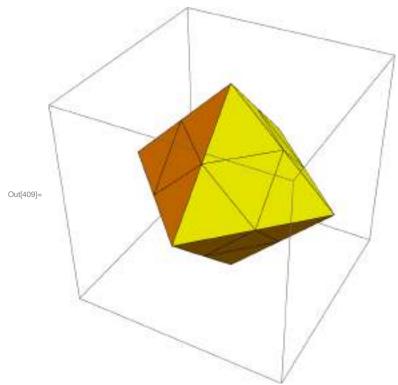
## **Sphere**

```
octahedronVertices = 1. {
             {1, 0, 0},
             \{-1, 0, 0\},\
             {0, 1, 0},
             \{0, -1, 0\},\
             {0,0,1},
             \{0, 0, -1\}
           };
       octahedronTriangles = {
             {0, 4, 2},
             {2, 4, 1},
             {1, 4, 3},
             {3, 4, 0},
             \{0, 2, 5\},\
             {2, 1, 5},
             {1, 3, 5},
            {3,0,5}
           } + 1;
       divide[points_] := Block[
           a = Mean[{points[1], points[3]}}],
           b = Mean[{points[1], points[2]}],
           c = Mean[{points[2], points[3]}]
          },
          {{points[1], b, a}, {b, points[2], c}, {a, b, c}, {a, c, points[3]}}}
        1
In[397]:= vertex = Table[octahedronVertices[tr]], {tr, octahedronTriangles}]
\texttt{Out} \texttt{[397]} = \{\{\{1., 0., 0.\}, \{0., 0., 1.\}, \{0., 1., 0.\}\}, \{\{0., 1., 0.\}, \{0., 0., 1.\}, \{-1., 0., 0.\}\}, \{0., 0., 0., 0.\}\}, \{0., 0., 0., 0.\}\}
        \{\{-1., 0., 0.\}, \{0., 0., 1.\}, \{0., -1., 0.\}\},\
        \{\{0., -1., 0.\}, \{0., 0., 1.\}, \{1., 0., 0.\}\},\
        \{\{1., 0., 0.\}, \{0., 1., 0.\}, \{0., 0., -1.\}\},\
         \{\{0., 1., 0.\}, \{-1., 0., 0.\}, \{0., 0., -1.\}\},\
         \{\{-1., 0., 0.\}, \{0., -1., 0.\}, \{0., 0., -1.\}\},\
         \{\{0., -1., 0.\}, \{1., 0., 0.\}, \{0., 0., -1.\}\}\}
```

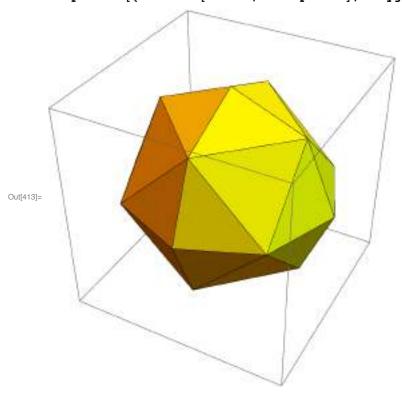
 $\label{eq:lowerse} $$ \ln[398] = $ Graphics3D[{FaceForm[Yellow, Blue}], Polygon/@Reverse/@vertex}] $$$ 



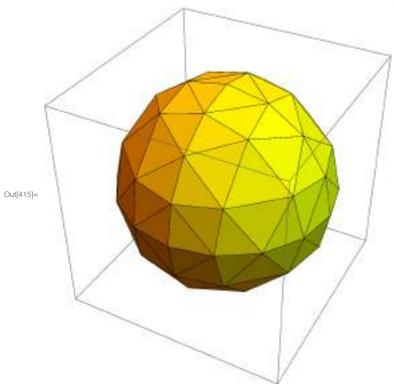
In[408]:= vertex1 = Flatten[divide /@ vertex, 1];  ${\tt Graphics3D[\{FaceForm[Yellow,\,Transparent]\,,\,Polygon\,/@\,Reverse\,/@\,vertex1\}]}$ 



ln[412]:= vertex1 = Map[normalize, Flatten[divide/@vertex, 1], {2}]; Graphics3D[{FaceForm[Yellow, Transparent], Polygon /@ Reverse /@ vertex1}]



ln[414]:= vertex2 = Map[normalize, Flatten[divide/@vertex1, 1], {2}]; Graphics3D[{FaceForm[Yellow, Transparent], Polygon /@ Reverse /@ vertex2}]



normalize[v\_] := v / Norm[v]

 $\label{eq:local_local_local_local_local} $$\inf_{a \in \mathbb{R}_{+}} := \operatorname{Polygon} / \operatorname{@Nest}[\operatorname{Map}[\operatorname{normalize}, \operatorname{Flatten}[\operatorname{divide} / \operatorname{@\#}, 1], \{2\}] \&, $$$  ${\tt Table[octahedronVertices[tr]], \{tr, octahedronTriangles\}], n]}\\$ 

In[445]:= Graphics3D[sphere[4]]; Graphics3D[{FaceForm[Blue, Yellow], sphere[4]}]

