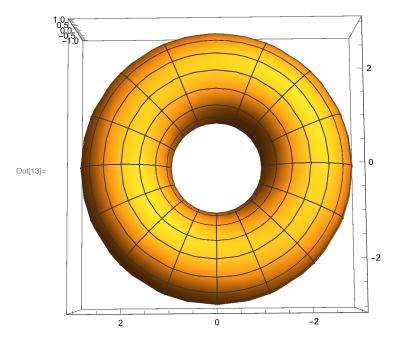
Tessellating torus

 $\label{eq:loss_problem} $ \ln[12] := \{ (2 + Cos[v]) \; Cos[u], \; (2 + Cos[v]) \; Sin[u], \; Sin[v] \} $$

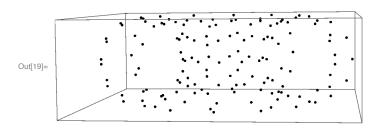
ln[13]:= ParametricPlot3D[torusxy[t, θ], {t, 0, 2 π }, { θ , 0, 2 π }]



 $\label{eq:pts} $$ \inf_{x \in \mathbb{R}} \ \ \, = \ \ \, Table[torusxy[u, v], \{u, 0, 2\pi, \pi/6\}, \{v, 0, 2\pi, \pi/6\}] $$ $$$

In[19]:= Graphics3D[Point[Flatten[pts, 1]]]

In[32]:=



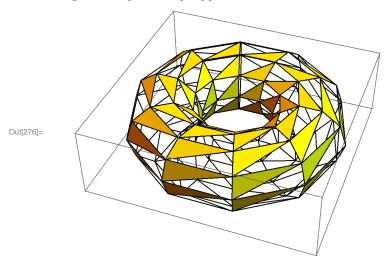
$$torusPt[n_{_}] := Table\left[\left\{\left(2 + Cos\left[\frac{i}{n}2\pi\right]\right)Cos\left[\frac{j}{n}2\pi\right], \left(2 + Cos\left[\frac{i}{n}2\pi\right]\right)Sin\left[\frac{j}{n}2\pi\right], Sin\left[\frac{i}{n}2\pi\right]\right\}, \{i, 1, n\}, \{j, 1, n\}, \{i, 1, n\},$$

torus1[n_]:={FaceForm[Yellow,Transparent],

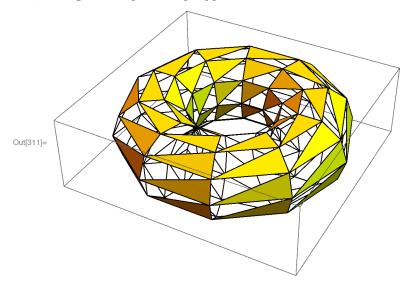
Table[Polygon[{
$$\left\{ \left(2 + \cos\left[\frac{i}{n}2\pi\right]\right) \cos\left[\frac{j}{n}2\pi\right], \left(2 + \cos\left[\frac{i}{n}2\pi\right]\right) \sin\left[\frac{j}{n}2\pi\right], \sin\left[\frac{i}{n}2\pi\right] \right\},$$

```
\left\{ \left( 2 + \cos\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right) \cos\left[\frac{\mathbf{j}}{n} 2\pi\right], \left( 2 + \cos\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right) \sin\left[\frac{\mathbf{j}}{n} 2\pi\right], \sin\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right\},
               \left\{ \left( 2 + \cos \left[ \frac{\mathbf{i}}{2} 2\pi \right] \right) \cos \left[ \frac{\mathbf{j} + 1}{2} 2\pi \right], \left( 2 + \cos \left[ \frac{\mathbf{i}}{2} 2\pi \right] \right) \sin \left[ \frac{\mathbf{j} + 1}{2} 2\pi \right], \sin \left[ \frac{\mathbf{i}}{2} 2\pi \right] \right\} \right\} \right\},
               \{i,1,n\},\{j,1,n\}\}
tesseTorus1[n_]:=Table \left[\left\{\left(2+\cos\left[\frac{i}{2}2\pi\right]\right)\cos\left[\frac{j}{2}2\pi\right],\left(2+\cos\left[\frac{i}{2}2\pi\right]\right)\sin\left[\frac{j}{2}2\pi\right],\sin\left[\frac{i}{2}2\pi\right]\right\}\right\}
                                             \left\{ \left( 2 + \cos\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right) \cos\left[\frac{\mathbf{j}}{n} 2\pi\right], \left( 2 + \cos\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right) \sin\left[\frac{\mathbf{j}}{n} 2\pi\right], \sin\left[\frac{\mathbf{i} - 1}{n} 2\pi\right] \right\},
                                             \left\{ \left( 2 + \cos \left[ \frac{\mathbf{i}}{n} 2\pi \right] \right) \cos \left[ \frac{\mathbf{j}+1}{n} 2\pi \right], \left( 2 + \cos \left[ \frac{\mathbf{i}}{n} 2\pi \right] \right) \sin \left[ \frac{\mathbf{j}+1}{n} 2\pi \right], \sin \left[ \frac{\mathbf{i}}{n} 2\pi \right] \right\} \right\},
                \{i,1,n\},\{j,1,n\}
tesseTorus2[n_{-}] := Table\left[\left\{\left[2 + \cos\left[\frac{i}{n}2\pi\right]\right] \cos\left[\frac{j}{n}2\pi\right], \left(2 + \cos\left[\frac{i}{n}2\pi\right]\right] \sin\left[\frac{j}{n}2\pi\right], \sin\left[\frac{i}{n}2\pi\right]\right\},
\left\{ \left(2 + \cos\left[\frac{i}{n}2\pi\right]\right) \cos\left[\frac{j+1}{n}2\pi\right], \left(2 + \cos\left[\frac{i}{n}2\pi\right]\right) \sin\left[\frac{j+1}{n}2\pi\right], \sin\left[\frac{i}{n}2\pi\right] \right\},
\left\{ \left( 2 + \cos\left[\frac{\mathtt{i} + 1}{n} 2\pi\right] \right) \cos\left[\frac{\mathtt{j} + 1}{n} 2\pi\right], \left( 2 + \cos\left[\frac{\mathtt{i} + 1}{n} 2\pi\right] \right) \sin\left[\frac{\mathtt{j} + 1}{n} 2\pi\right], \sin\left[\frac{\mathtt{i} + 1}{n} 2\pi\right] \right\} \right\},
                {i,1,n},{j,1,n}]
torus2[n_]:={FaceForm[Yellow,Transparent];
               \mathbf{Table}\left[\mathbf{Polygon}\left[\left\{\left(2+\mathbf{Cos}\left[\frac{\mathbf{i}}{2}2\pi\right]\right)\mathbf{Cos}\left[\frac{\mathbf{j}}{2}2\pi\right],\left(2+\mathbf{Cos}\left[\frac{\mathbf{i}}{2}2\pi\right]\right)\mathbf{Sin}\left[\frac{\mathbf{j}}{2}2\pi\right],\ \mathbf{Sin}\left[\frac{\mathbf{i}}{2}2\pi\right]\right\},\right]
 \left\{ \left(2 + \cos\left[\frac{\mathbf{i}}{2}2\pi\right]\right) \cos\left[\frac{\mathbf{j}+1}{2}2\pi\right], \left(2 + \cos\left[\frac{\mathbf{i}}{2}2\pi\right]\right) \sin\left[\frac{\mathbf{j}+1}{2}2\pi\right], \sin\left[\frac{\mathbf{i}}{2}2\pi\right] \right\},
\left\{ \left( 2 + \cos\left\lceil \frac{i+1}{n} 2\pi \right\rceil \right) \cos\left\lceil \frac{j+1}{n} 2\pi \right\rceil, \left( 2 + \cos\left\lceil \frac{i+1}{n} 2\pi \right\rceil \right) \sin\left\lceil \frac{j+1}{n} 2\pi \right\rceil, \sin\left\lceil \frac{i+1}{n} 2\pi \right\rceil \right\} \right\} \right\},
                \{i,1,n\},\{j,1,n\}\}
torus[n]:=
 {FaceForm[Yellow, Transparent],
 Table Polygon \left\{ 
ight\}
                 \left\{ \left(2 + \cos\left[\frac{\mathbf{i}}{2}2\pi\right]\right) \cos\left[\frac{\mathbf{j}}{2}2\pi\right], \left(2 + \cos\left[\frac{\mathbf{i}}{2}2\pi\right]\right) \sin\left[\frac{\mathbf{j}}{2}2\pi\right], \sin\left[\frac{\mathbf{i}}{2}2\pi\right] \right\},
               \left\{ \left(2 + \cos\left[\frac{i-1}{n} 2\pi\right]\right) \cos\left[\frac{j}{n} 2\pi\right], \left(2 + \cos\left[\frac{i-1}{n} 2\pi\right]\right) \sin\left[\frac{j}{n} 2\pi\right], \sin\left[\frac{i-1}{n} 2\pi\right] \right\},
               \left\{ \left( 2 + \cos\left[\frac{i}{n} 2\pi\right] \right) \cos\left[\frac{j+1}{n} 2\pi\right], \left( 2 + \cos\left[\frac{i}{n} 2\pi\right] \right) \sin\left[\frac{j+1}{n} 2\pi\right], \sin\left[\frac{i}{n} 2\pi\right] \right\} \right\} \right\},
               \{i,1,n\},\{j,1,n\},
Table \Big[ Polygon \Big[ \Big\{ \Big\{ \Big( 2 + Cos \Big[ \frac{i}{n} 2\pi \Big] \Big) Cos \Big[ \frac{j}{n} 2\pi \Big] , \Big( 2 + Cos \Big[ \frac{i}{n} 2\pi \Big] \Big) Sin \Big[ \frac{j}{n} 2\pi \Big] , \\ Sin \Big[ \frac{i}{n} 2\pi \Big] \Big\} ,
 \left\{ \left( 2 + \cos\left[\frac{\mathbf{i}}{n} 2\pi\right] \right) \cos\left[\frac{\mathbf{j}+1}{n} 2\pi\right], \left( 2 + \cos\left[\frac{\mathbf{i}}{n} 2\pi\right] \right) \sin\left[\frac{\mathbf{j}+1}{n} 2\pi\right], \sin\left[\frac{\mathbf{i}}{n} 2\pi\right] \right\},
\left\{ \left( 2 + \cos\left[\frac{i+1}{n} 2\pi\right] \right) \cos\left[\frac{j+1}{n} 2\pi\right], \left( 2 + \cos\left[\frac{i+1}{n} 2\pi\right] \right) \sin\left[\frac{j+1}{n} 2\pi\right], \sin\left[\frac{i+1}{n} 2\pi\right] \right\} \right\} \right\},
               \{i,1,n\},\{j,1,n\}\}
```

In[276]:= **Graphics3D[torus1[10]]**



In[311]:= Graphics3D[torus2[10]]



In[319]:= Graphics3D[torus[20]]

