

# MIRT DIF

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1. Adaptive Lasso was adopted in high DIF proportion studies. To check whether the adaptive Lasso implementation is correct, we run adaptive Lasso in low DIF proportion condition (simulation 5).

## Results of 50 Replications

*Type I error and Power of Adaptive LASSO method*

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.675	0.090	0.675
Type I	0.00286	0.00286	0

*Type I error and Power of LASSO regularization method*

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.625	0.14	0.625
Type I	0.0314	0.0171	0.0185

*Type I error and Power of mirt LRT*

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.515	0.375	0.646
Type I	0.0185	0.0238	0.0149

BIC was used for parameter selection in both Lasso and adaptive Lasso. The results of adaptive Lasso were comparable to that of Lasso. So the adaptive Lasso implementation should be fine.

2. Defining the incidence matrix  $\Lambda = (\lambda_{jky})$  where  $\lambda_{jky} = I(\gamma_{jky} \neq 0)$ . The true  $\Lambda$  is on the solution path of regularization methods. But BIC and GIC would select more sparse  $\Lambda$ . We try to use AIC to reduce penalty in adaptive Lasso (simulation 6).

## Results of 50 Replications

*Type I error and Power of adaptive Lasso method*

Adaptive LASSO (parameter selected by GIC)

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.383	0.0086	0.3836
Type I	0	0	0

Adaptive LASSO (parameter selected by AIC)

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.852	0.258	0.847
Type I	0.040	0.030	0.023

*Type I error and Power of Lasso method*

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.45	0.06	0.443
Type I	0.0067	0.0033	0.0033

*Type I error and Power of mirt LRT*

Group	Omnibus DIF	Group with DIF=0.5	Group with DIF=1
Power	0.656	0.185	0.746
Type I	0.0067	0.01	0.0233

The power of results selected by AIC was much better than those of BIC and GIC, and the type I error is also acceptable.

3. Simulate traits with lower correlation ( $\text{Cor}(\theta_1, \theta_2) = 0.85 \rightarrow \text{Cor}(\theta_1, \theta_2) = 0.25$ )