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HW2

P1-P4

Xihao Zhu Comp502 HW2

P1.

a) $f(z) = \frac{1}{1+e^{-az}} = (1+e^{-az})^{-1}$

$$\frac{df(z)}{d(z)} = -1(1+e^{-az})^{-2} \times (-a) \cdot e^{-az} = \frac{a \cdot e^{-az}}{(1+e^{-az})^2}$$

which is equivalent of $a \cdot f(z) \cdot (1-f(z))$

b) $f(z) = \frac{e^{bz} - e^{-bz}}{e^{bz} + e^{-bz}}$

let $u = e^{bz} - e^{-bz}, v = e^{bz} + e^{-bz}$

$$\frac{du}{dz} = b(e^{bz} + e^{-bz}), \quad \frac{dv}{dz} = b(e^{bz} - e^{-bz})$$
$$\frac{df(z)}{dz} = \frac{u'v - uv'}{v^2} = \frac{4b}{(e^{bz} + e^{-bz})^2}$$

c). There are multiple ways to achieve this.
I would like to set the weight vector to be
 $w' = w^* a$ (where w is the old one).
 a is slope parameter.

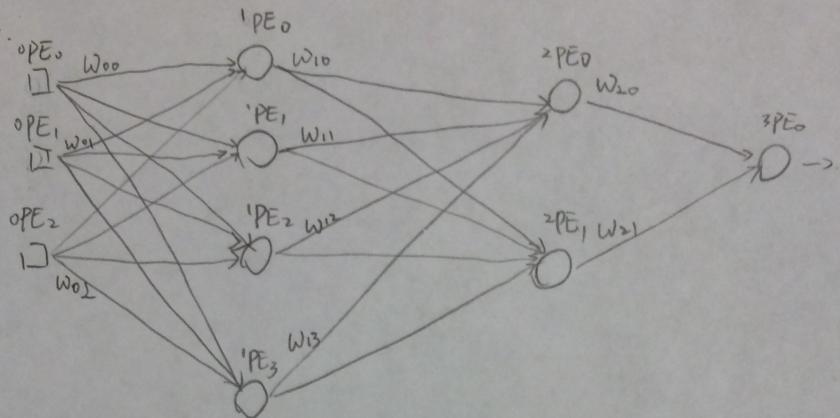
so net' = $\sum_{j=1}^n w'_j x_j = a \cdot \sum_{j=1}^n w_j x_j$.

P2. i) output = [8, -4, -4, 1.8]

ii) output = [1, 0, 0, 1].

iii) output = [0.99966, 0.07986, -0.07986, 0.858]

Problem 3.



Input layer ————— 1st hidden layer ————— 2nd hidden layer ————— Output layer.

Problem 4.

since linear transfer function, $F: x \rightarrow y$.

and because the feed forward ANN is fully connected,

inputs x will go through every "neuron" element in ANN

therefore, inputs will be multiplied by every weight

$$y = Wx \text{ where } W = w_1 + w_2 + \dots + w_{all} \text{ (for brief illustration..)}$$

So W is composed from all weights in network.

P5.

(a)

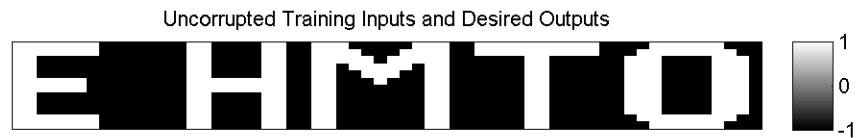
I used $MM = \text{errcorr}(X, Y, 0.005, 50, 0.5)$ to get the memory

My X is 144×5 matrix, while Y is 5×5 matrix.

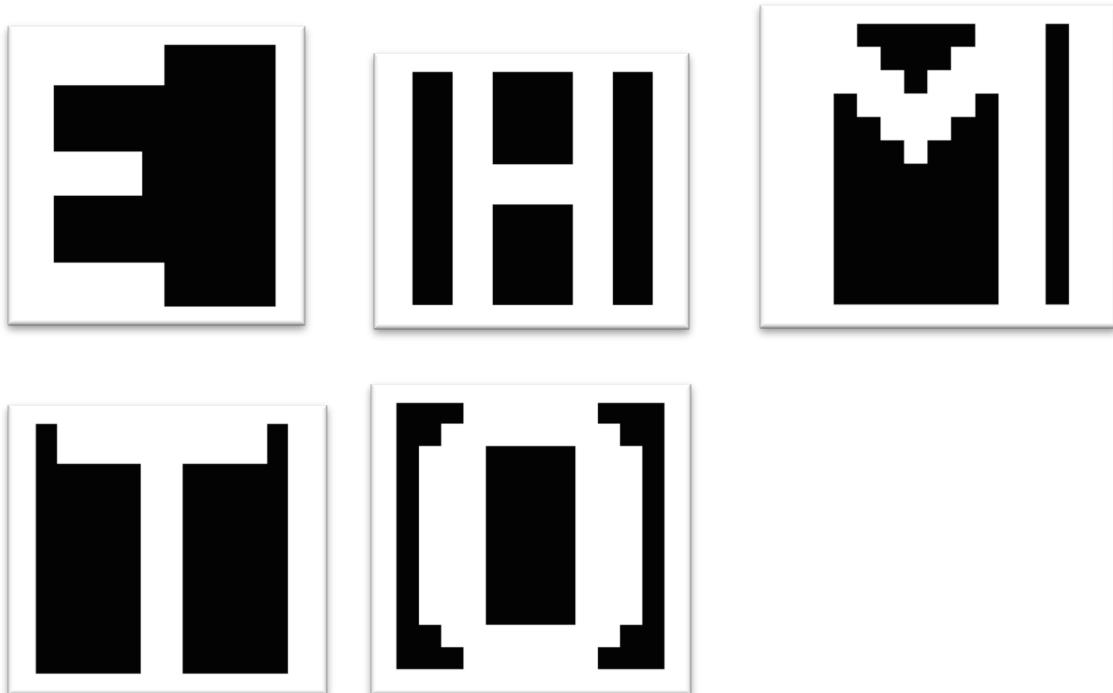
For example, $Y[1;0;0;0;0]$ is 'E', $Y[0;1;0;0;0]$ is 'H'

Percent of mismatched pixels between Thresholded Recalled and Desired Output images:

E: 0%, H: 0%, M: 0%, T: 0%, O: 0% (all: 0%)



Below is thresholded image output.



the method to get the results are shown as follows:

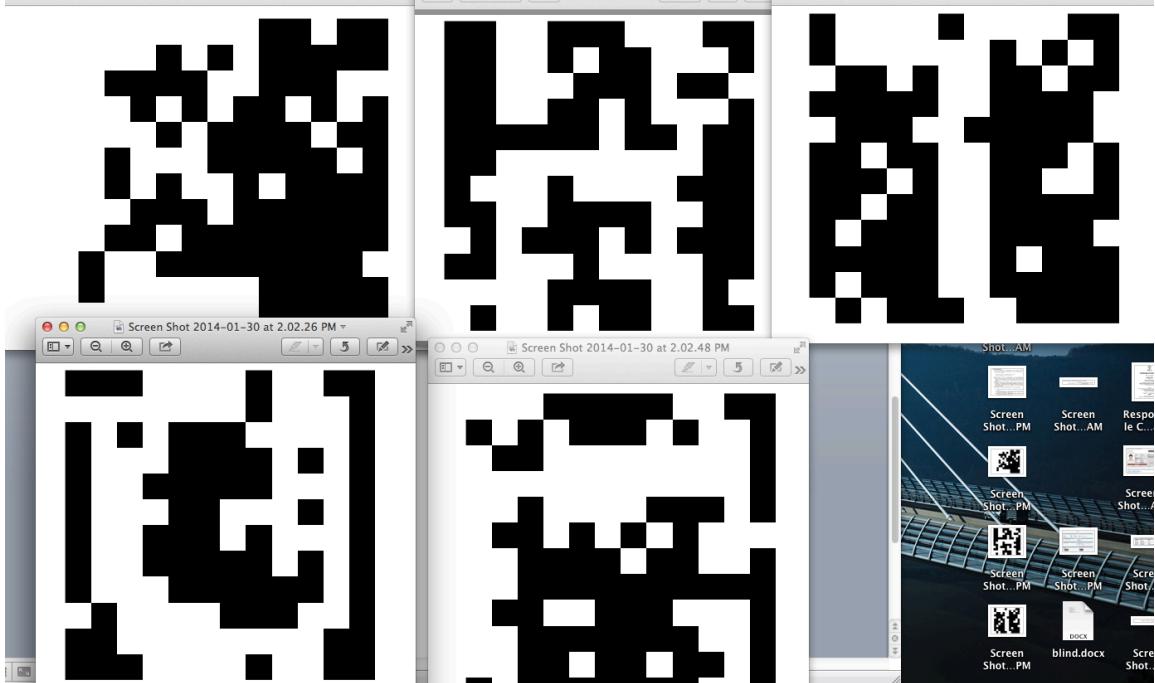
```

octave-3.4.0:172> ww(ww>0)=1;
octave-3.4.0:173> ww(ww<=0)=-1;
octave-3.4.0:174> recall=getRecall(E(:,'), ww(1,:))
mis = 0
recall = 0
octave-3.4.0:175> recall=getRecall(H(:,'), ww(2,:))
mis = 0
recall = 0
octave-3.4.0:176> recall=getRecall(T(:,'), ww(3,:))
mis = 0
recall = 0
octave-3.4.0:177> recall=getRecall(zero(:,'), ww(4,:))
mis = 0
recall = 0
octave-3.4.0:178> recall=getRecall(M(:,'), ww(5,:))
mis = 0
recall = 0

```

(b)

these are corrupted images. With corrupted rate 20%(29 pixels)

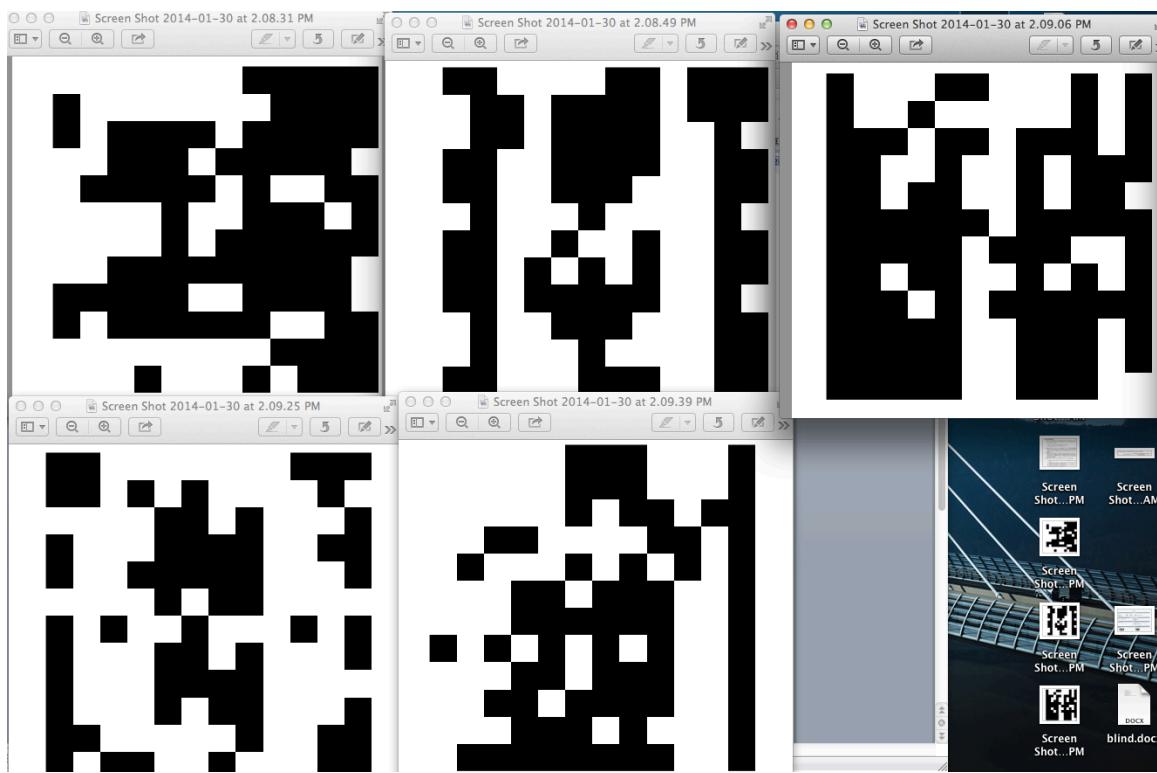


Percent of mismatched pixels between corrupted images and Desired Output images:

E: 25%, H: 25%, M: 25%, T: 25%, O: 25%
 (all: 25%)

Since we compare 25% corrupted images with good images. So there are 25% incorrect rate.

these are corrupted images. With corrupted rate 25%(36 pixels)



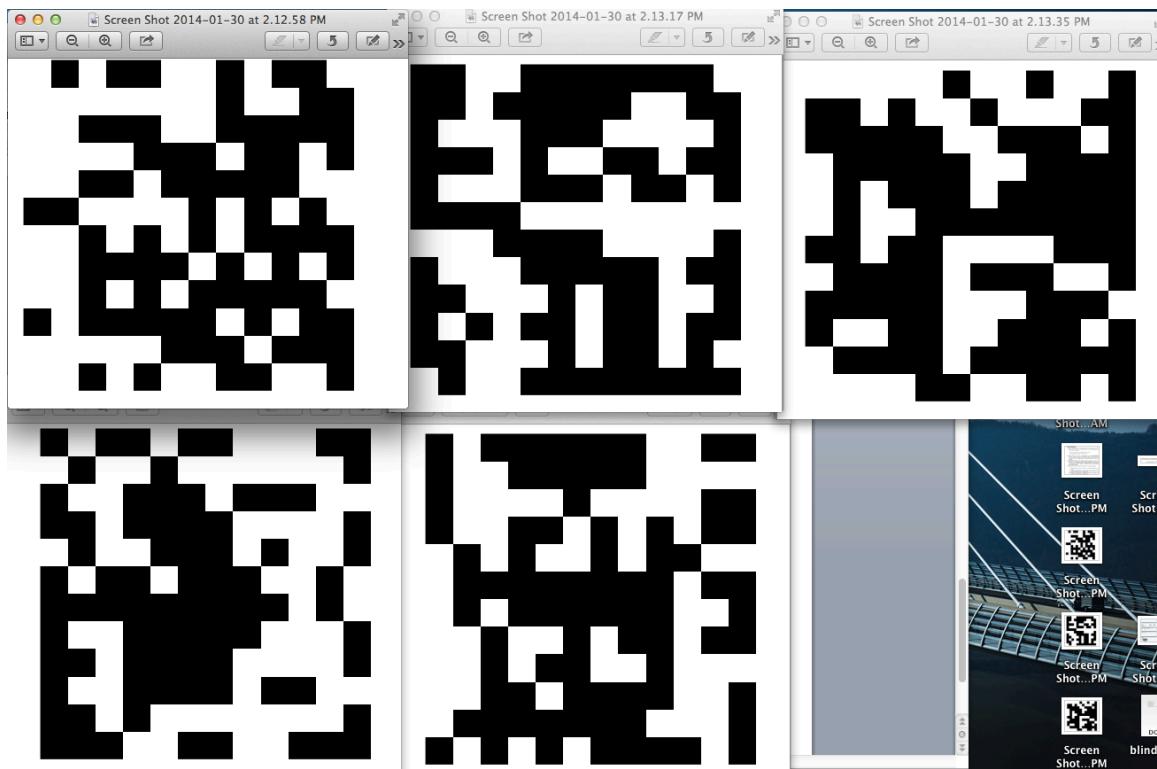
Percent of mismatched pixels between corrupted images and Desired Output images:

E: 36%, H: 36%, M: 36%, T: 36%, O: 36%

(all: 36%)

Since we compare 36% corrupted images with good images. So there are 36% incorrect rate.

these are corrupted images. With corrupted rate 50%(72 pixels)

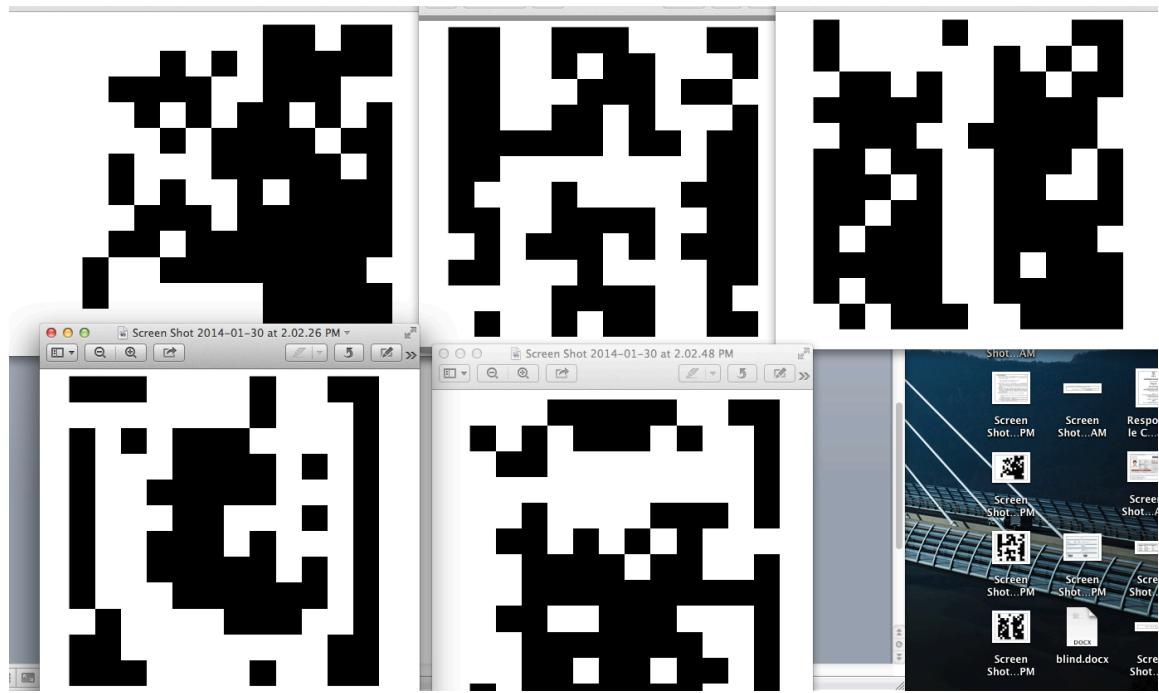


Percent of mismatched pixels between corrupted images and Desired Output images:

E: 50%, H: 50%, M: 50%, T: 50%, O: 50%
(all: 50%)

Since we compare 50% corrupted images with good images. So there are 50% incorrect rate.

(c).
20% corrupted data



using $MM = \text{errcorr}(X, Y, 0.01, 100, 1)$

Percent of mismatched pixels between corrupted images and Desired Output images:

E: 12.3%, H: 19.8%, M: 16.3%, T: 22%, O: 14.2%