

propagation
de-
lay

submodular
????????

influence

ef-
fi-
ciency

??
??

??
 $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ $\mathcal{GV}\mathcal{E}$
 $\mathcal{H} = (\mathcal{V}, \mathcal{Z})$ $\mathcal{HG}??\mathcal{V}\mathcal{Z}$
 n \mathcal{GH}
 m \mathcal{G}

k
 $p_{u,v}^{\mathcal{G}}$ uv
 $I(S)$ S
 $RR(v)$ $v??$
 $eff_{u,v}$ $uv??$
 $T(S)$ $SG??$
 $T'(S)$ $SH??$

$\mathcal{G} =$
 $(\mathcal{V}, \mathcal{E})\mathcal{V}\mathcal{E}e_{u,v} \in$
 $\mathcal{E}p_{u,v}^{\mathcal{G}}uvp_{u,v}^{\mathcal{G}}uv\mathcal{G}p_{u,v}uv$
 $S \subseteq$

$\mathcal{V}Stt \geq$
 $0t =$
 $0S_0 =$
 $Stt -$
 $1u \in$
 $N^{in}(v) \cap$
 $(S_{t-1} \setminus S_{t-2})v \in$
 $\mathcal{V} \setminus$
 $S_{t-1}vp_{u,v}ut -$
 $1uttS_t =$
 S_{t-1}

?? $\mathcal{G}S =$
 $\{v_1\}??p_{u,v}^{\mathcal{G}}t =$
 $0v_1v_1t =$
 $1v_1t =$
 $0\mathcal{G}v_1v_2v_1v_2v_2t =$
 $1S_1 =$
 $\{v_1, v_2\}t =$
 $2v_2v_3v_4v_5v_6??v_3v_5S_2 =$
 $\{v_1, v_2, v_3, v_5\}t =$
 $3I(S)SGI(S) =$
 4

$SE_{\mathcal{G}}[I(S)]\mathcal{GG}kE_{\mathcal{G}}[I(S)]k????$
 $??\mathcal{G}k =$

$1??k =$
 $1v_1E_{\mathcal{G}}[I(\{v_1\})] =$
 $1+$
 $1+$
 $4 \times$
 $0.8 =$
 $5.2\{v_2\}E_{\mathcal{G}}[I(\{v_2\})] =$
 $1+$
 $4 \times$
 $0.8 =$
 $4.2E_{\mathcal{G}}[I(\{v_3\})] =$
 $E_{\mathcal{G}}[I(\{v_4\})] =$
 $E_{\mathcal{G}}[I(\{v_5\})] =$
 $E_{\mathcal{G}}[I(\{v_6\})] =$

$1\mathcal{G}k =$
 $1S^* =$
 $\{v_1\}$

$\mathcal{G}k =$
 $1\mathcal{G}k >$
 $1E_{\mathcal{G}}[I(S)]uSf(S \cup \{u\}) \geq$
 $f(S)uS \subseteq$
 $Wf(S \cup \{u\}) -$
 $f(S) \geq$
 $f(W \cup \{u\}) -$
 $f(W)S =$
 $\emptyset f(S \cup \{u\}) -$
 $f(S)uSku$

$u = \arg \max_{w \in V \setminus S} (E_{\mathcal{G}}[I(S \cup w)] - E_{\mathcal{G}}[I(S)])$

(1)

$\frac{1}{1-\alpha}$