

# C++ Header Files

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## Header.hpp

```
cpp #pragma GCC optimize("Ofast,no-stack-protector,unroll-loops") #define ALL(v) v.begin(),v.end()
#define For(i,_) for(int i=0,i##end=_;i<i##end;++i) // [0,_) #define FOR(i,_,__) for(int
i=_,i##end=__;i<i##end;++i) // [_,__) #define Rep(i,_) for(int i=(_)-1;i>=0;--i) // [0,_)
#define REP(i,_,__) for(int i=(__)-1,i##end=_;i>=i##end;--i) // [_,__) typedef long
long ll; typedef unsigned long long ull; #define V vector #define pb push_back #define
pf push_front #define qb pop_back #define qf pop_front #define eb emplace_back typedef
pair<int,int> pii; typedef pair<ll,int> pli; #define fi first #define se second const int
dir[4][2]={{-1,0},{0,1},{1,0},{0,-1}},inf=0x3f3f3f3f,mod=1e9+7; const ll inf1=0x3f3f3f3f3f3f3f11;
template<class T>inline bool ckmin(T &x,const T &y){return x>y?x=y,1:0;} template<class
T>inline bool ckmax(T &x,const T &y){return x<y?x=y,1:0;} int init=[](){return cin.tie(nullptr)->sync_w
```

## STèj".hpp

```
cpp template<class T,T(*merge)(T,T)> struct ST{      V<V<T>>>st;      inline ST(){}      inline
ST(const V<T> &a){          int n=a.size(),B=__lg(n);          V<V<T>>>(B+1).swap(st);
```

```

st[0]=a;          FOR(i,1,B+1){          st[i].resize(n-(1<<i)+1);          For(j,n-(1<<i)+1)st[i]
}          }          inline ST(const V<T> &a,const V<int> &pos){          assert(a.size()==pos.size());
int n=a.size(),B=__lg(n);          V<V<T>>(B+1).swap(st);          For(i,B+1){          st[i].resize(n
if(i)For(j,n-(1<<i)+1)st[i][j]=merge(st[i-1][j],st[i-1][j+(1<<i-1)]);          else
For(i,n)st[0][pos[i]]=a[i];          }          }          inline T query(int l,int r){          int
n=st[0].size();          assert(0<=l),assert(1<=r),assert(r<n);          int k=__lg(r-l+1);
return merge(st[k][l],st[k][r-(1<<k)+1]);          } };

```

## custom\_hash.hpp

```

cpp struct custom_hash {          static uint64_t splitmix64(uint64_t x){          x+=0x9e3779b97f4a7c15;
x=(x^(x>>30))*0xbf58476d1ce4e5b9;          x=(x^(x>>27))*0x94d049bb133111eb;          return
x^(x>>31);          }          size_t operator()(uint64_t x)const{          static const uint64_t
FIXED_RANDOM=chrono::steady_clock::now().time_since_epoch().count();          return
splitmix64(x+FIXED_RANDOM);          } };

```

## dq.hpp

```

cpp template<class T> struct dq{          int hd;          V<T>q;          inline dq(){hd=0;}          inline
T front(int k=0){assert(hd+k<q.size());return q[hd+k];}          inline T back(int k=0){assert(hd+k<q.size())
q[q.size()-1-k];}          inline int size(){return q.size()-hd;}          inline void clear(){hd=0,V<T>().swap(q);
inline void push(const T &v){q.pb(v);}          inline void pop_back(){q.qb();}          inline
void pop_front(){assert(hd<q.size());++hd;} };

```

## fraction.hpp

```

cpp struct fraction{          ll p,q;          inline void simplify(){ll g=gcd(p<0?-p:p,q);p/=g;q/=g;}
inline explicit fraction(ll _p=0):p(_p),q(1){          inline fraction(ll _p,ll _q):p(_p),q(_q){assert(q);i
inline explicit fraction(const string&s){size_t pos=s.find('.');q=1;if(pos==string::npos)p=stoll(s);else
i=0;i<s.size()-1-pos;i++)q*=10;p=(pos?stoll(s.substr(0,pos))*q:0)+stoll(s.substr(pos+1));}else
p=stoll(s.substr(0,pos));simplify();}          inline explicit fraction(const V<char>&s):fraction(string(s.l
inline fraction& operator=(const fraction&r){p=r.p;q=r.q;return*this;}          inline fraction&
operator=(ll r){p=r;q=1;return*this;}          inline fraction operator+(const fraction&r)const{if(q==r.q)re
g=gcd(q,r.q),m=q/g;return{p*(r.q/g)+r.p*m,m*r.q};}          inline fraction operator+(ll
r)const{return{p+r*q,q};}          inline fraction add(const fraction&r)const{return{p*r.q+r.p*q,q*r.q};}
inline fraction operator-(const fraction&r)const{if(q==r.q)return{p-r.p,q};ll g=gcd(q,r.q),m=q/g;return
inline fraction operator-(ll r)const{return{p-r*q,q};}          inline fraction sub(const
fraction&r)const{return{p*r.q-r.p*q,q*r.q};}          inline fraction operator*(const fraction&r)const{fract
t;ll g1=gcd(p,r.q),g2=gcd(r.p,q);t.p=(p/g1)*(r.p/g2);t.q=(q/g2)*(r.q/g1);return t;}
inline fraction operator*(ll r)const{fraction t=*this;ll g=gcd(r,q);t.p*=r/g;t.q/=g;return
t;}          inline fraction mul(const fraction&r)const{return{p*r.p,q*r.q};}          inline
fraction operator/(const fraction&r)const{assert(r.p);fraction t;ll g1=gcd(p,r.p),g2=gcd(r.q,q);t.p=(p/
t;}          inline fraction operator/(ll r)const{assert(r);fraction t=*this;ll g=gcd(p,r);t.p/=g;t.q*=r/g;r
t;}          inline fraction div(const fraction&r)const{assert(r.p);return{p*r.q,q*r.p};}
inline bool operator==(const fraction&r)const{return p==r.p&&q==r.q;}          inline bool
operator==(ll r)const{return p==r&&q==1;}          inline bool eq(const fraction&r)const{return
p==r.p&&q==r.q;}          inline bool operator<(const fraction&r)const{return p*r.q<r.p*q;}
inline bool operator<(ll r)const{ll g=gcd(p,r);return p/g<q*(r/g);}          inline bool
lt(const fraction&r)const{return p*r.q<r.p*q;}          inline bool operator>(const fraction&r)const{return
p*r.q>r.p*q;}          inline bool operator>(ll r)const{ll g=gcd(p,r);return p/g>q*(r/g);}
inline bool gt(const fraction&r)const{return p*r.q>r.p*q;}          inline bool operator<=(const
fraction&r)const{return p*r.q<=r.p*q;}          inline bool operator<=(ll r)const{ll g=gcd(p,r);return
p/g<=q*(r/g);}          inline bool le(const fraction&r)const{return p*r.q<=r.p*q;}          inline
bool operator>=(const fraction&r)const{return p*r.q>=r.p*q;}          inline bool operator>=(ll

```

```

r)const{lll g=gcd(p,r);return p/g>=q*(r/g);}      inline bool ge(const fraction&r)const{return
p*r.q>=r.p*q;}      inline string to_string()const{return ::to_string(p)+'/'+::to_string(q);}
};

```

## modint.hpp

```

cpp template<int p> struct modint{      int val;      inline modint(int v=0):val(v){}
inline modint& operator=(int v){val=v;return *this;}      inline modint& operator+=(const
modint&k){val=val+k.val>=p?val+k.val-p:val+k.val;return *this;}      inline modint& operator-=(const
modint&k){val=val-k.val<0?val-k.val+p:val-k.val;return *this;}      inline modint& operator*=(const
modint&k){val=int(1ll*val*k.val%p);return *this;}      inline modint& operator^=(int
k){modint r(1),b=*this;for(;k;k>>=1,b*=b)if(k&1)r*=b;val=r.val;return *this;}      inline
modint& operator/=(modint k){return *this*=(k^=p-2);}      inline modint& operator+=(int
k){val=val+k>=p?val+k-p:val+k;return *this;}      inline modint& operator-=(int k){val=val<k?val-k+p:val
*this;}      inline modint& operator*=(int k){val=int(1ll*val*k%p);return *this;}      inline
modint& operator/=(int k){return *this*=((modint(k))^=p-2);}      template<class T>friend
modint operator+(modint a,T b){return a+=b;}      template<class T>friend modint operator-(modint
a,T b){return a-=b;}      template<class T>friend modint operator*(modint a,T b){return
a*=b;}      template<class T>friend modint operator/(modint a,T b){return a/=b;}      friend
modint operator^(modint a,int b){return a^=b;}      friend bool operator==(modint a,int
b){return a.val==b;}      friend bool operator!=(modint a,int b){return a.val!=b;}      inline
bool operator!()const{return !val;}      inline modint operator-()const{return val?modint(p-val):modint(0);}
inline modint operator++(int){modint t=*this;*this+=1;return t;}      inline modint&
operator++(){return *this+=1;}      inline modint operator--(int){modint t=*this;*this-=1;return
t;}      inline modint& operator--(){return *this-=1;} }; using mi=modint<mod>;

```

## pbds.hpp

“cpp #include <ext/pb\_ds/tree\_policy.hpp> #include <ext/pb\_ds/assoc\_container.hpp> using names-  
pace \_\_gnu\_pbds;

```

template struct rbt{ typedef pair<T,int> pti; int cnt; typedef tree<pti,null_type,less,rb_tree_tag,tree_order_statistics_node
rbt_t; rbt_t t; inline rbt(){cnt=0;} inline void clear(){cnt=0,rbt_t().swap(t);} inline typename
rbt_t::iterator begin(){return t.begin();} inline typename rbt_t::iterator end(){return t.end();} inline
void insert(const T &x){t.insert({x,cnt++});} inline typename rbt_t::iterator find(const T &x){return
t.lower_bound({x,0});} inline void erase(const T &x){t.erase(find(x));} inline T pre(const T &x){ auto
it=find(x); assert(it!=begin()); return prev(it)->fi; } inline T nxt(const T &x){ auto it=find(x+1);
assert(it!=end()); return it->fi; } // all 0-indexed inline int rk(const T &x){return t.order_of_key({x,0});}
inline T at(unsigned x){return t.find_by_order(x)->fi; } };

```

```

#include <ext/pb_ds/priority_queue.hpp> inline V dijkstra(int n,int s,const V<V> &to){ as-
sert(0<=n),assert(0<=s),assert(s<n),assert(to.size()<=n); for(const V &i:to) for(const pii &j:i) as-
sert(0<=min(j.fi,j.se)),assert(j.fi<n); Vdis(n,infl); dis[s]=0; __gnu_pbds::priority_queue<pli,greater,pairing_heap_tag>q;
V<decltype(q)::point_iterator>it(n); it[s]=q.push({0,s}); while(q.size()){ int p=q.top().se;q.pop();
for(const pii &i:to[p]) if(ckmin(dis[i.fi],dis[p]+i.se)){ if(it[i.fi]!=NULL)q.modify(it[i.fi],{dis[i.fi],i.fi}); else
it[i.fi]=q.push({dis[i.fi],i.fi}); } } for(ll &i:dis)if(i==infl)i=-1; return dis; }“

```

## poly.hpp

“cpp inline V poly\_conv\_add(const V &\_a,const V &\_b,int g){ // c[k]= $\sum_i A[a[i]*b[j]]$  for  $i+j=k$  verified  
with lg3803 assert(\_a.size()&&\_b.size()); if(max(\_a.size(),\_b.size())<17){ Vc(\_a.size()+\_b.size()-1);  
For(i,\_a.size())For(j,\_b.size())c[i+j]+=\_a[i]\*\_b[j]; return c; } int lg=0,n=1; while(n<\_a.size()+\_b.size()-  
1)++lg,n<=1; Va=\_a,b=\_b; a.resize(n),b.resize(n); static V<V>bt; while(bt.size()<=lg){ int  
n=1<bt.size(); bt.pb({}); V&bf=bt.back(); bf.resize(n); For(i,n)bf[i]=(bf[i]>1)>1|((i&1)?n:1:0); }  
const V&bf=bt[lg]; auto NTT=&{ For(i,n)if(i<bf[i])swap(f[i],f[bf[i]]); for(int k=1,l=2;k<n;k<=1,l<=1){ mi

```

wn=coef~((mod-1)/l); for(int i=0;i<n;i+=1){ mi w=1; For(j,k){ mi x=f[i][j],y=w*f[i][j]/k; f[i][j]=x+y,f[i][j]/k=x-
y; w=wn; } } } ; NTT(a,g),NTT(b,g); For(i,n)a[i]*=b[i]; NTT(a,mi(1)/g); a.resize(_a.size()+_b.size()-1);
mi invn=mi(1)/n; for(mi &i:a)i*=invn; return a; }

```

```

inline V poly_conv_sub(const V &_a,const V &_b,int g){ // c[k]=iE(a[i]*b[j]) for i-j=k verified with
gym105386H assert(_a.size()&&_b.size()); Vb=_b; reverse(ALL(b)); b=poly_conv_add(_a,b,g); // (-
b.size(),a.size()) -> [0,a.size()) b.erase(b.begin(),b.begin()+_b.size()-1); return b; }

```

```

inline int find_g(int m){ auto phi=&{ int ret=k; for(int i=2;i<=k;++i)if(k%i==0){ret=ret/i;do
k/=i;while(k%i==0);} if(k>1)ret=ret/k; return ret; }; int p=phi(m); Vfac; { int j=p; for(int
i=2;i<=j;++i)if(j%i==0){fac.pb(p/i);do j/=i;while(j%i==0);} if(j>1)fac.pb(p/j); } auto check_g=&{
auto qpow=&{ int z=1; for(;y;x=1ll*x%m,y*=1)if(y&1)z=1ll*z%m; return z; }; if(qpow(g,p)!=1)return
false; for(int i:fac)if(qpow(g,i)==1)return false; return true; }; FOR(i,1,m)if(check_g(i))return i; return -1; }
inline V poly_conv_mul(const V &_a,const V &_b,int g,int p,int pg=-1){ // c[k]=iE(a[i]b[j]) for ij%p=k
verified by qoj9247 assert(_a.size()&&_b.size()); if(!pg)pg=find_g(p); assert(~pg); Vexp(p-1),lg(p); lg[0]=
1; for(int i=1,j=0;j<p-1;i=1ll*i*pg%p,++j)exp[j]=i,lg[i]=j; Va(p-1),b(p-1); FOR(i,1,_a.size())a[lg[i]]=_a[i];
FOR(i,1,_b.size())b[lg[i]]=_b[i]; Vc=poly_conv_add(a,b,g); FOR(i,p-1,c.size())c[i-(p-1)]+=c[i]; Vd(p);
d[0]=_a[0]*reduce(ALL(_b))+_b[0]*reduce(ALL(_a))-_a[0]*_b[0]; For(i,p-1)d[exp[i]]=c[i]; return d; }

```

```

inline V poly_conv_div(const V &_a,const V &_b,int g,int p,int pg=-1){ // c[k]=iE(a[i]*b[j]) for i/j%p=k
not verified assert(_a.size()&&_b.size()),assert(!_b[0].val); Vinv(p); inv[1]=1; FOR(i,1,p)inv[i]=1ll(p-
p/i)inv[p%i]%mod; Vb(p); FOR(i,1,_b.size())b[inv[i]]=_b[i]; return poly_conv_mul(_a,b,g,p,pg); }

```

```

inline V poly_conv_and(const V &_a,const V &_b){ // c[k]=iE(a[i]*b[j]) for i&j=k verified with
lg4717 assert(_a.size()&&_b.size()); int n=1; while(n<max(_a.size(),_b.size()))n<<=1; Va=_a,b=_b;
a.resize(n),b.resize(n); auto FWT=&{ for(int k=1,l=2;k<n;k<<=1,l<<=1)for(int i=0;i<n;i+=1)For(j,k)f[i][j]+=f[i][j]k coef;
}; FWT(a,1),FWT(b,1); For(i,n)a[i]=b[i]; FWT(a,mod-1); return a; }

```

```

inline V poly_conv_or(const V &_a,const V &_b){ // c[k]=iE(a[i]*b[j]) for i|j=k verified with
lg4717 assert(_a.size()&&_b.size()); int n=1; while(n<max(_a.size(),_b.size()))n<<=1; Va=_a,b=_b;
a.resize(n),b.resize(n); auto FWT=&{ for(int k=1,l=2;k<n;k<<=1,l<<=1)for(int i=0;i<n;i+=1)For(j,k)f[i][j]k+=f[i][j] coef;
}; FWT(a,1),FWT(b,1); For(i,n)a[i]=b[i]; FWT(a,mod-1); return a; }

```

```

inline V poly_conv_xor(const V &_a,const V &_b){ // c[k]=iE(a[i]*b[j]) for i^j=k verified with
lg4717 assert(_a.size()&&_b.size()); int n=1; while(n<max(_a.size(),_b.size()))n<<=1; Va=_a,b=_b;
a.resize(n),b.resize(n); auto FWT=&{ for(int k=1,l=2;k<n;k<<=1,l<<=1)for(int i=0;i<n;i+=1)For(j,k){
mi x=f[i][j],y=f[i][j]k; f[i][j]=(x+y)coef,f[i][j]k=(x-y)coef; } }; FWT(a,1),FWT(b,1); For(i,n)a[i]*=b[i];
FWT(a,mod+1>1); return a; }

```

```

inline V poly_conv_gcd(const V &_a,const V &_b){ // c[k]=iE(a[i]*b[j]) for gcd(i,j)=k verified with
lc418t4 assert(_a.size()&&_b.size()); int n=max(_a.size(),_b.size()); Va=_a,b=_b; a.resize(n),b.resize(n);
Vpri; Vvis(n); FOR(i,2,n)if(!vis[i]){ pri.pb(i); for(int k=(n-1)/i,j=ki;k<j=i,-k)a[k]+=a[j],b[k]+=b[j],vis[j]=true;
} FOR(i,1,n)a[i]=b[i]; for(int i:pri)for(int j=i,k=1;j<n;j+=i,++k)a[k]-=a[j]; a[0]=_a[0]*_b[0]; FOR(i,1,n)a[i]+=_a[0]*_b[i];
return a; }

```

```

inline V poly_conv_lcm(const V &_a,const V &_b){ // c[k]=iE(a[i]*b[j]) for lcm(i,j)=k not verified
assert(_a.size()&&_b.size()); int n=max(_a.size(),_b.size()); Va=_a,b=_b; a.resize(n),b.resize(n); Vpri;
Vvis(n); FOR(i,2,n)if(!vis[i]){ pri.pb(i); for(int j=i,k=1;j<n;j+=i,++k)a[j]+=a[k],b[j]+=b[k],vis[j]=true; }
FOR(i,1,n)a[i]=b[i]; for(int i:pri)for(int k=(n-1)/i,j=ki;k<j=i,-k)a[j]-=a[k]; a[0]=_a[0]*_b[0]; FOR(i,1,n)a[i]+=_a[0]*_b[i];
return a; }

```

```

inline V poly_inv(const V &a,int g){ // b=1/a verified with lg4238 assert(a.size()),assert(a[0].val);
Vb{1/a[0]}; mi invg=mi(1)/g,invm=1; int m=1; while(b.size()<a.size()){ int n=min(a.size(),b.size())<<1;
while(m<=n-1)invm=mod+1>1,m<<=1; Vc(a.begin(),a.begin()+n); b.resize(m),c.resize(m); Vbf(m);
For(i,m)bf[i]=(bf[i]1)>1)/(iE1)?m>1:0; auto NTT=E{ For(i,m)if(i<bf[i])swap(f[i],f[bf[i]]); for(int
k=1,l=2;k<m;k<<=1,l<<=1){ mi wn=coef~((mod-1)/l); for(int i=0;i<m;i+=1){ mi w=1; For(j,k){ mi
x=f[i][j],y=w*f[i][j]k; f[i][j]=x+y,f[i][j]k=x-y; w=wn; } } } ; NTT(b,g),NTT(c,g); For(i,m)b[i]=2-b[i]c[i];
NTT(b,invg); b.resize(n); for(mi &i:b)i=invm; } return b; }

```

```

inline V poly_diff(const V &a){ // b=a' int n=a.size(); assert(n); if(n==1)return {0}; Vb(n-1); For(i,n-1)b[i]=a[i+1]*(i+1); return b; }

inline V poly_intg(const V &a){ // b=∫a int n=a.size(); assert(n); Vb(n+1),inv(n+1); b[1]=a[0],inv[1]=1; FOR(i,2,n)b[i]=a[i-1](inv[i]=(mod-mod/i)inv[mod%i]); return b; }

inline V poly_ln(const V &a,int g){ // b=ln(a) verified with lg4725 int n=a.size(); assert(n),assert(a[0].val==1); Vb=poly_conv_add(poly_diff(a),poly_inv(a,g),g); b.resize(n); return poly_intg(b); }

inline V poly_exp(const V &a,int g){ // b=exp(a) verified with lg4726 int n=a.size(); assert(n); Vb{1}; if(a[0].val){ mi e=0,ifac=mod-1; Rep(i,mod)e+=ifac,ifac*=i; b[0]=e^a[0].val; // check that a[0] isnt modulo } while(b.size()<a.size()){ int m=min(b.size()«1,a.size()); b.resize(m); Vc=poly_ln(b,g); For(i,m)c[i]=a[i]-c[i]; ++c[0]; b=poly_conv_add(b,c,g); b.resize(m); } return b; }

inline V poly_series(const V &a,mi b0,int g){ // b[i]=i!E(b[j]a[i-j]) for j>0 verified with lg4721 assert(a.size()); Vb=a; b[0]=1; FOR(i,1,b.size())b[i]=-b[i]; b=poly_inv(b,g); if(b0.val!=1)for(mi &i:b)i=b0; return b; }

inline V poly_pow(const V &a,mi b,int g){ // c=a^(b%mod) verified with lg5245 int n=_a.size(); assert(n); Va(n); if(!b){ a[0]=1; return a; } int i=0; while(i<n&&!_a[i])++i; if(i==n)return a; ll z=1llb.val; if(z>=n)return a; assert(_a[i].val==1); a=poly_ln(V(_a.begin()+i,_a.end()),g); for(mi &j:a)j*=b; a=poly_exp(a,g); Vret(z); ret.insert(ret.end(),a.begin(),a.begin()+n-z); return ret; }

inline V poly_pow(const V &a,ll b,int g){ // c=a^b verified with Library Checker int n=_a.size(); assert(n); Va(n); if(!b){ a[0]=1; return a; } int i=0; while(i<n&&!_a[i])++i; if(i==n||__int128(b)*i>=n)return a; a=V(_a.begin()+i,_a.end()); mi coef=a[0],inv=1/coef; for(mi &j:a)j*=inv; a=poly_ln(a,g); mi _b=b%mod; for(mi &j:a)j*=_b; a=poly_exp(a,g); coef^=b%(mod-1); for(mi &j:a)j=coef; ll z=bi; Vret(z); ret.insert(ret.end(),a.begin(),a.begin()+n-z); return ret; }

inline V poly_multi_pt(const V &a,const V &b,int g){ // c[i]=a(b[i]) verified with lg5050 assert(_a.size()); if(b.empty())return {}; int n=max(_a.size(),b.size()); V<V>t(n«2); auto build=&->void{ if(l==r){ t[p]={1,l<b.size()?-b[r]:0}; return; } int mid=l+r»1; self(self,p«1,l,mid); self(self,p«1|1,mid+1,r); t[p]=poly_conv_add(t[p«1],t[p«1|1],g); }; build(build,1,0,n-1); auto poly_conv_sub=&{ assert(_b.size()),assert(_a.size())>=Vb=_b; reverse(ALL(b)); b=poly_conv_add(_a,b,g); return V(b.begin()+_b.size()-1,b.end()); }; Vret(b.size()); auto push_down=&->void{ if(l>=b.size())return; if(l==r){ ret[l]=c[0]; return; } c.resize(r-l+1); int mid=l+r»1; self(self,p«1,l,mid,poly_conv_sub(c,t[p«1|1],g)); self(self,p«1|1,mid+1,r,poly_conv_sub(c,t[p«1],g)); }; Va=_a; a.resize(n+1); push_down(push_down,1,0,n-1,poly_conv_sub(a,poly_inv(t[1],g),g)); return ret; }

inline V poly_prod(const V<V> &a,int g){ // b[i]=∏(a[i]) assert(a.size()); auto cmp=&{return x.size()>y.size();}; priority_queue<V,V<V>,decltype(cmp)>q(cmp); for(const auto &i:a)q.push(i); while(q.size()>1){ Vx=q.top();q.pop(); Vy=q.top();q.pop(); q.push(poly_conv_add(x,y,g)); } return q.top(); }

inline V poly_multi_pt_sum(const V &a,int m,int g){ // b[i]=sum(a[j]^i) for i in [0,m] int n=a.size(); assert(n); V<V>b(max(n,m)); For(i,max(n,m))b[i]={1,-a[i]}; Vc=poly_ln(poly_prod(b,g),g); c.resize(m+1); c[0]=n; FOR(i,1,m+1)c[i]*=mod-i; return c; }“

```

## trie.hpp

```

cpp struct trie{ int siz; trie *son[2]; inline trie(){siz=0,son[0]=son[1]=NULL;}
}; void insert(int dep,trie *p,int k){ ++p->siz; if(dep<0)return; int nxt=k>>dep&1;
if(!p->son[nxt])p->son[nxt]=new trie(); insert(dep-1,p->son[nxt],k); } int query(int
dep,trie *p,int k,int lim){ if(!p)return 0; if(dep<0)return p->siz; int
nxt=k>>dep&1; if(lim>>dep&1)return (p->son[nxt]?p->son[nxt]->siz:0)+query(dep-1,p->son[nxt^1],k,lim);
return query(dep-1,p->son[nxt],k,lim); } void insert(int dep,trie *p1,trie *p2,int k){
if(p1)p2->siz=p1->siz; ++p2->siz; if(dep<0)return; int nxt=k>>dep&1; if(p1)p2->son[nxt^1]
p2->son[nxt]=new trie(); insert(dep-1,p1?p1->son[nxt]:NULL,p2->son[nxt],k); } int
query(int dep,trie *p1,trie *p2,int k){ if(dep<0)return 0; int nxt=k>>dep&1;

```

```

if (p2->son[nxt^1]&&(!p1||!p1->son[nxt^1]||p2->son[nxt^1]->siz>p1->son[nxt^1]->siz))return
query(dep-1,p1?p1->son[nxt^1]:NULL,p2->son[nxt^1],k)|(1<<dep);      return query(dep-1,p1?p1->son[nxt]:NULL,
}

```

## vector.hpp

```

“cpp template inline V<V> rot(const V<V>& v){ V<V>ret(v[0].size(),V(v.size())); For(i,v.size())
For(j,v[0].size()) ret[j][v.size()-i-1]=v[i][j]; return ret; }

inline ll contor(const V &v){ int d=min_element(ALL(v),n=v.size()); Vvis(n); for(int i:v)vis[i-
d]=true; if(any_of(ALL(vis),{return !b;}))return -1; Vfac(n); fac[0]=1; BIT3t(n); FOR(i,1,n+1){
if(i<n)fac[i]=fac[i-1]/i; ++t.c[i]; if(i+(i&-i)<=n)t.c[i+(i&-i)]+=t.c[i]; } ll ret=0; For(i,n){ t.add(v[i]-d,-1);
ret+=fac[n-i-1]*t.query(v[i]-d); } return ret; } inline V inv_contor(int n,ll k){ Vfac(n+1); fac[0]=1;
FOR(i,1,n+1)fac[i]=fac[i-1]/i; if(k>=fac[n])return {-1}; Vret(n); Vvis(n); For(i,n){ int dgt=k/fac[n-i-
1]+1,j=-1; k%=fac[n-i-1]; do dgt-=!vis[+ +j];while(dgt); ret[i]=j,vis[j]=true; } return ret; }“

```

## ã\_ã\_ .hpp

```

“cpp template struct mhsh{ // 0-indexed Vbs,h; inline mhsh(){ } inline mhsh(const string &s){
bs.reserve(s.size()),h.reserve(s.size()); bs.pb(1),h.pb(s[0]); FOR(i,1,s.size())bs.pb(bs.back()base),h.pb(h.back()base+s[i]);
} inline mhsh(const V &v){ bs.reserve(v.size()),h.reserve(v.size()); bs.pb(1),h.pb(v[0]); FOR(i,1,v.size())bs.pb(bs.back()base),h.pb(h.back()base+v[i]);
} inline ull get(int l,int r){ assert(0<=l),assert(l<=r),assert(r<h.size()); return h[r]-(l?h[l-1]*bs[r-l+1]:0); }
inline int lcp(int x,int y){ assert(0<=min(x,y)),assert(max(x,y)<h.size()); int l=1,r=h.size()-max(x,y),ret=0;
while(l<=r){ int mid=l+r>>1; if(get(x,x+mid-1)==get(y,y+mid-1))l=mid+1,ret=mid; else r=mid-1; } re-
turn ret; } };

```

```

template struct modhsh{ // 0-indexed Vbs,h; inline modhsh(){ } inline modhsh(const string &s){
bs.reserve(s.size()),h.reserve(s.size()); bs.pb(1),h.pb(s[0]); FOR(i,1,s.size())bs.pb(bs.back()base%mod),h.pb((h.back()base+s[i])%mod);
} inline modhsh(const V &v){ bs.reserve(v.size()),h.reserve(v.size()); bs.pb(1),h.pb(v[0]); FOR(i,1,v.size())bs.pb(bs.back()base%mod),h.pb((h.back()base+v[i])%mod);
} inline ull get(int l,int r){ assert(0<=l),assert(l<=r),assert(r<h.size()); ull ret=h[r]+mod-(l?h[l-1]*bs[r-l+1]%mod:0); return ret>=mod?ret-mod:ret; } };
template struct dmhsh{ // 0-indexed modhsh<base1,mod1>hsh1; modhsh<base2,mod2>hsh2; inline dmhsh(const string &s){ hsh1=modhsh<base1,mod1>(s),hsh2=modhsh<base2,mod2>(s);
} inline dmhsh(const V &v){ hsh1=modhsh<base1,mod1>(v),hsh2=modhsh<base2,mod2>(v); } inline
pair<ull,ull> get(int l,int r){ assert(0<=l),assert(l<=r),assert(r<hsh1.h.size()); return {hsh1.get(l,r),hsh2.get(l,r)};
} inline int lcp(int x,int y){ assert(0<=min(x,y)),assert(max(x,y)<hsh2.h.size()); int l=1,r=hsh2.h.size()-max(x,y),ret=0; while(l<=r){ int mid=l+r>>1; if(get(x,x+mid-1)==get(y,y+mid-1))l=mid+1,ret=mid; else
r=mid-1; } return ret; } };

```

```

mt19937 rnd(time(0)); inline int genPri(int l,int r){ auto isp=&{ if(k<2)return false; for(int i=2;i<=k;++i)if(k%i==0)return false; return true; }; int p=uniform_int_distribution(l,r)(rnd); while(!isp(p))++p; return p; }; struct
rndhsh{ // 0-indexed int base,mod; Vbs,h; inline rndhsh(){base=genPri(2,1e5),mod=genPri(2,1e9);} inline
rndhsh(const string &s){ bs.reserve(s.size()),h.reserve(s.size()); bs.pb(1),h.pb(s[0]); FOR(i,1,s.size())bs.pb(bs.back()base%mod),h.pb((h.back()base+s[i])%mod);
} inline rndhsh(const V &v){ bs.reserve(v.size()),h.reserve(v.size()); bs.pb(1),h.pb(v[0]); FOR(i,1,v.size())bs.pb(bs.back()base%mod),h.pb((h.back()base+v[i])%mod);
} inline ull get(int l,int r){ assert(0<=l),assert(l<=r),assert(r<h.size()); ull ret=h[r]+mod-(l?h[l-1]*bs[r-l+1]%mod:0); return ret>=mod?ret-mod:ret; } };
struct drhsh{ // 0-indexed rndhsh hsh1; rndhsh hsh2; inline drhsh(const string &s){ hsh1=rndhsh(s),hsh2=rndhsh(s); } inline drhsh(const V &v){ hsh1=rndhsh(v),hsh2=rndhsh(v);
} inline pair<ull,ull> get(int l,int r){ assert(0<=l),assert(l<=r),assert(r<hsh1.h.size()); return {hsh1.get(l,r),hsh2.get(l,r)}; } inline int lcp(int x,int y){ assert(0<=min(x,y)),assert(max(x,y)<hsh2.h.size());
int l=1,r=hsh2.h.size()-max(x,y),ret=0; while(l<=r){ int mid=l+r>>1; if(get(x,x+mid-1)==get(y,y+mid-1))l=mid+1,ret=mid; else r=mid-1; } return ret; } };“

```

## ã\_ã\_@.hpp

```

“cpp inline V bfs01(int n,int s,const V<V> &to){ assert(0<=n),assert(0<=s),assert(s<n),assert(to.size()<=n);
for(const V &i:to) for(const pii &j:i) assert(0<=min(j.fi,j.se)),assert(j.fi<n); Vdis(n,inf); dis[s]=0; dequeq;
q.pb(s); Vvis(n); // added vis to prevent an obvious error while(q.size()){ int p=q.front();q.qf();

```

```
if(vis[p])continue; vis[p]=true; for(const pii &i:to[p])if(ckmin(dis[i.fi],dis[p]+i.se))i.se?q.pb(i.fi):q.pf(i.fi); }
for(ll &i:dis)if(i==infl)i=-1; return dis; }
```

```
template inline V dijkstra(int n,int s,const V<V<pair<int,T>> &to,ll null=-1){ Vdis(n,infl); dis[s]=0;
typedef pair<int,ll> pil; auto cmp=&{return x.se>y.se;}; priority_queue<pil,V,decltype(cmp)>q(cmp);
q.emplace(s,0); Vvis(n); while(q.size()){ int p=q.top().fi;q.pop(); if(vis[p])continue; vis[p]=true; for(const
auto &[i,j]:to[p])if(ckmin(dis[i],dis[p]+j)&&!vis[i])q.emplace(i,dis[i]); } for(ll &i:dis)if(i==infl)i=null; return
dis; }
```

```
inline V<array<int,3>> kruskal(int n,const V<V> &to,function<bool(const array<int,3> &,const ar-
ray<int,3> &)>cmp={return x[2]<y[2];}){ assert(0<=n),assert(to.size()<=n); for(const V &i:to)for(const
pii &j:i)assert(j.fi<n); V<array<int,3>>e; For(i,to.size())for(const pii &j:to[i])assert(0<=j.fi),assert(j.fi<n),e.pb({i,j.fi,j.se});
sort(ALL(e),cmp); dsu d(n); V<array<int,3>>ret; for(auto &i:e)if(d.merge(i[0],i[1]))ret.pb(i); return ret; }
```

```
struct ring{ int clr; Vid; V<V>scc,to; inline void init(const V<V>&to){ int cnt=clr=0,n=to.size(); Vcur(n);
Vdfn(n),low(n); V(n,-1).swap(id),V<V>().swap(scc); stackst; function<void(int)>tarjan=&{ cur[p]=true;
dfn[p]=low[p]=++cnt; st.push(p); for(int i:to[p]){ assert(0<=i&&i<n); if(!dfn[i])tarjan(i),ckmin(low[p],low[i]);
else if(cur[i])ckmin(low[p],dfn[i]); } if(dfn[p]==low[p]){ scc.pb(V()); int k; do{ k=st.top();st.pop();
cur[k]=false,id[k]=clr,scc[clr].pb(k); }while(k!=p); ++clr; } }; For(i,n)if(!dfn[i])tarjan(i); Vlst(clr,-1);
V<V>(clr).swap(this->to); For(i,clr){ lst[i]=i; for(int j:scc[i])for(int k:to[j])if(lst[id[k]]!=i)lst[id[k]]=i,this-
->to[i].pb(id[k]); } } inline ring(const V<V>&to){init(to);} inline ring(){} };
```

```
struct vDCC{ int clr; Vcut; V<V>dcc,to; inline void init(const V<V>&to){ int cnt=0,n=clr=to.size();
Vdfn(n),low(n); V(n).swap(cut),V<V>().swap(dcc); V<V>(n).swap(this->to); For(i,n) if(!dfn[i]){
stackst; function<void(int,int)>tarjan=&{ dfn[p]=low[p]=++cnt; int flag_son=0; st.push(p); for(int
i:to[p]){ assert(0<=i&&i<n); if(!dfn[i]){ tarjan(i,p),ckmin(low[p],low[i]); if(low[i]>=dfn[p]){ if(fa!=-
1||flag_son++)cut[p]=true; this->dcc.pb(V()),this->to.pb(V()); int k; do{ k=st.top();st.pop(); this-
->dcc.back().pb(k); this->to[k].pb(clr),this->to[clr].pb(k); }while(k!=i); this->dcc.back().pb(p); this-
->to[p].pb(clr),this->to[clr++].pb(p); } } else ckmin(low[p],dfn[i]); } if(!fa&&!flag_son)this->dcc.pb({p});
}; tarjan(i,-1); } } inline vDCC(const V<V>&to){init(to);} inline vDCC(){} };
```

```
struct eDCC{ int clr; V<V>dcc,to; Vid; inline void init(const V<V>&to){ int cnt=clr=0,n=to.size();
Vdfn(n),low(n); V<V>().swap(dcc),V(n,-1).swap(id); stackst; function<void(int,int)>tarjan=&{
dfn[p]=low[p]=++cnt; bool flag=false; st.push(p); for(int i:to[p]){ if(i!=fa){ if(!dfn[i])tarjan(i,p),ckmin(low[p],low[i]);
else ckmin(low[p],dfn[i]); } if(i==fa){ if(flag)ckmin(low[p],dfn[i]); else flag=true; } } if(dfn[p]<=low[p]){
dcc.pb(V()); int k; do{ k=st.top();st.pop(); id[k]=clr,dcc[clr].pb(k); }while(k!=p); ++clr; } };
For(i,n)if(!dfn[i])tarjan(i,-1); Vlst(clr,-1); V<V>(clr).swap(this->to); For(i,clr){ lst[i]=i; for(int j:dcc[i])for(int
k:to[j])if(lst[id[k]]!=i)lst[id[k]]=i,this->to[i].pb(id[k]); } } inline eDCC(const V<V>&to){init(to);} inline
eDCC(){} };
```

```
struct range_2sat{ int n; V<V>to; inline int idx(int l,int r){return (l+r|!=r)>>1;} #define p idx(l,r) inline
void resize(int n_){ n=n_; V<V>((n<<1)+(n-1<<2)).swap(to); function<int(int,int,int)>build_dw=&{
if(l==r)return (k&1)n+l; int mid=l+r>>1; to[(n<<1)+k*(n-1)+p].pb(build_dw(l,mid,k)); to[(n<<1)+k*(n-
1)+p].pb(build_dw(mid+1,r,k)); return (n<<1)+k(n-1)+p; }; build_dw(0,n-1,0),build_dw(0,n-1,1); func-
tion<int(int,int,int)>build_up=&{ if(l==r)return (k&1)n+r; int mid=l+r>>1; to[build_up(l,mid,k)].pb((n<<1)+k(n-
1)+p); to[build_up(mid+1,r,k)].pb((n<<1)+k(n-1)+p); return (n<<1)+k(n-1)+p; }; build_up(0,n-
1,2),build_up(0,n-1,3); } inline range_2sat(){resize(n);} inline V
range_dw(int ql,int qr,int k){ Vret; function<void(int,int)>dfs=&{ if(ql<=l&&r<=qr){ if(l==r)ret.pb(kn+l);
else ret.pb((n<<1)+k(n-1)+p); return; } int mid=l+r>>1; if(ql<=mid)dfs(l,mid); if(qr>mid)dfs(mid+1,r);
}; dfs(0,n-1); return ret; } inline V range_up(int ql,int qr,int k){ Vret; function<void(int,int)>dfs=&{
if(ql<=l&&r<=qr){ if(l==r)ret.pb(kn+r); else ret.pb((n<<1)+(k+2)(n-1)+p); return; } int mid=l+r>>1;
if(ql<=mid)dfs(l,mid); if(qr>mid)dfs(mid+1,r); }; dfs(0,n-1); return ret; } #undef p inline void link_pp(int
x,int y,bool op_x,bool op_y,bool rev=true){ to[op_x*n+x].pb(op_y*n+y); if(rev)to[(op_y^1)*n+y].pb((op_x^1)n+x);
} inline void link_pr(int x,int yl,int yr,bool op_x,bool op_y,bool rev=true){ for(int y:range_dw(yl,yr,op_y))to[op_x*n+x].pb
if(rev)for(int y:range_up(yl,yr,op_y^1))to[y].pb((op_x^1)n+x); } inline void link_rp(int xl,int xr,int
y,bool op_x,bool op_y,bool rev=true){ for(int x:range_up(xl,xr,op_x))to[x].pb(op_y*n+y); if(rev)for(int
x:range_dw(xl,xr,op_x^1))to[(op_y^1)*n+y].pb(x); } inline void link_rr(int xl,int xr,int yl,int yr,bool
```

```
op_x,bool op_y,bool rev=true){ VX=range_up(xl,xr,op_x); for(int y:range_dw(yl,yr,op_y))for(int
x:X)to[x].pb(y); if(rev){ VY=range_up(yl,yr,op_y^1); for(int x:range_dw(xl,xr,op_x^1))for(int
y:Y)to[y].pb(x); } } };
```

## â .hpp

```
“cpp template<class T,class U=less> struct delpq{ priority_queue<T,V,U>q1,q2; inline delpq(){ inline
delpq(const U &func){priority_queue<T,V,U>(func).swap(q1),priority_queue<T,V,U>(func).swap(q2);}
inline void push(const T &x){q1.push(x);} inline void pop(const T &x){q2.push(x);} inline T top(){
while(q2.size()&&q1.top()==q2.top())q1.pop(),q2.pop(); assert(q1.size()); return q1.top(); } inline bool
empty(){return q1.size()==q2.size();} inline int size(){assert(q1.size()>=q2.size());return q1.size()-
q2.size();} };
```

```
template struct kpq{ int k; multisets1,s2; ll sum; inline kpq(int _k=0):k(_k),sum(0){} inline void
insert(const T &x){ if(s1.size()<k)s1.insert(x),sum+=x; else{ if(x>s1.begin())s2.insert(s1.begin()),sum-
=s1.begin(),s1.erase(s1.begin()),s1.insert(x),sum+=x; else s2.insert(x); } } inline void erase(const T &x){
if(s1.size()<k&&x<s1.begin()){ auto it=s2.find(x); assert(it!=s2.end()); s2.erase(it); } else{ auto it=s1.find(x);
assert(it!=s1.end()); s1.erase(it); sum-=x; if(s1.size()<k&&s2.size())s1.insert(s2.rbegin()),sum+=s2.rbegin(),s2.erase(prev(s2
) ) } } };
```

## â ç¬ä².hpp

```
“cpp inline int lcs(const string &a,const string &b){ if(a.empty()||b.empty())return 0; int n=a.size(),m=b.size(),k=(n+62)/63;
Vf(k); char mn=min_element(ALL(a)),mx=max_element(ALL(a)); V<V>g(mx-mn+1,V(k)); For(i,n)g[a[i]-
mn][i/63]=1ull«i%63; for(char i:b){ if(i<mn||i>mx)continue; i=mn; ull z=1; For(j,k){ ull x=f[j],y=f[j]|g[i][j];
((x«1)|=z)+=(~y)&((1ull«63)-1); f[j]=x&y,z=x»63; } } return accumulate(ALL(f),0,&{return
x+__builtin_popcountll(y);}); } template inline int lcs(const V &a,const V &b){ if(a.empty()||b.empty())return
0; int n=a.size(),m=b.size(),k=(n+62)/63; discd(a); Vf(k); V<V>g(d.size(),V(k)); For(i,n)g[d.query(a[i])][i/63]=1ull«i%63;
for(const T &i:b){ auto it=lower_bound(ALL(d.d),i); if(it==d.d.end()||*it!=i)continue; i=it-d.d.begin();
ull z=1; For(j,k){ ull x=f[j],y=f[j]|g[i][j]; ((x«1)|=z)+=(~y)&((1ull«63)-1); f[j]=x&y,z=x»63; } } return
accumulate(ALL(f),0,&{return x+__builtin_popcountll(y);}); }
```

```
struct subseq_table{ V<V>nxt; inline subseq_table(const string &v){ int n=v.size(); V<V>(128).swap(nxt);
For(i,n){ assert(v[i]>=0&&v[i]<128); nxt[v[i]].pb(i); } } inline int lcp(const string &v){ int nw=0,ret=0;
for(char i:v){ assert(i>=0&&i<128); auto it=lower_bound(ALL(nxt[i]),nw); if(it==nxt[i].end())break;
nw=*it+1,++ret; } return ret; } inline bool query(const string &v){ return lcp(v)==v.size(); } };
```

```
template<class T,class container=unordered_map<T,int> struct subseq_Table{ genID<T,container>g;
V<V>nxt; inline subseq_Table(const V &v){ int n=v.size(); For(i,n){ int k=g.get_id(v[i]); if(k>=nxt.size())nxt.pb(V());
nxt[k].pb(i); } } inline int lcp(const V &v){ int nw=0,ret=0; for(const T &i:v){ if(!g.count(i))break; int
k=g.get_id(i); auto it=lower_bound(ALL(nxt[k]),nw); if(it==nxt[k].end())break; nw=*it+1,++ret; }
return ret; } inline bool query(const V &v){ return lcp(v)==v.size(); } };
```

```
struct manacher{ int n; Vp; inline manacher(const string &s){ n=s.size(); p.assign(n«1|1,1); string t(n«1|1,
'#' ); For(i,n)t[i«1|1]=s[i]; for(int i=0,mid=-1,mx=-1;i<p.size();++i){ if(i<=mx)p[i]=min(p[(mid«1)-i],mx-
i)+1; while(i>=p[i]&&i+p[i]<p.size())&&t[i-p[i]]==t[i+p[i]])++p[i]; if(i+-p[i]>mx)mid=i,mx=i+p[i]; } } in-
line int odd(int k){ assert(0<=k&&k<n); return p[k«1|1]; } inline int even(int k){ assert(0<=k&&k+1<n);
return p[k+1«1|1]; } inline bool isp(int l,int r){ assert(0<=l),assert(1<=r),assert(r<n); return p[l+r+1]>=r-
l+1; } };
```

```
inline V get_kmp(const string &s){ int n=s.size(); Vkmp(n); for(int i=1,j=0;i<n;++i){ while(j&&s[j]!=s[i])j=kmp[j-
1]; if(s[j]==s[i])++j; kmp[i]=j; } return kmp; } inline V find_kmp(const V &kmp,const string &s,const
string &t){ int n=s.size(),m=t.size(); Vret; for(int i=0,j=0;i<n;++i){ while(j&&t[j]!=s[i])j=kmp[j-1];
if(t[j]==s[i])++j; if(j==m)ret.pb(i); } return ret; }“
```



## ã¹¶æ ¥é .hpp

```
““cpp struct dsu{ Vfa; inline void resize(int n){V(n,-1).swap(fa);} inline dsu(int n=0){resize(n);} int
find(int k){return fa[k]<0?k:fa[k]=find(fa[k]);} inline bool merge(int x,int y){ x=find(x),y=find(y);
if(x!=y)fa[x]+=fa[y],fa[y]=x; return x!=y; } inline bool same(int x,int y){return find(x)==find(y);} inline
int size(int k){return -fa[find(k)];} }; inline pair<V<V>,V> kruskal_tree(int n,V<array<int,3> &e){
int cnt=n; dsu d(n+n-1); V<V>to(n+n-1); Vval(n+n-1); sort(ALL(e),&{return x[2]<y[2];}); for(const
auto &i:e){ int fx=d.find(i[0]),fy=d.find(i[1]); if(fx!=fy){ d.fa[fx]=d.fa[fy]=cnt; to[cnt].pb(fx),to[cnt].pb(fy);
val[cnt++]=i[2]; } } assert(cnt==n+n-1); return {to,val}; }
```

```
struct range_dsu{ V<V>fa; int lg,n; inline void resize(int __n){ V<V>(lg=((n=__n)?__lg(n):-
1)+1).swap(fa); For(i,lg)fa[i].resize(n-(1«i)+1,-1); } inline range_dsu(int __n=0){resize(__n);} int
find(int d,int k){return fa[d][k]<0?k:fa[d][k]=find(d,fa[d][k]);} inline void merge(int d,int x,int y){
x=find(d,x),y=find(d,y); if(x>y)swap(x,y); if(x!=y)fa[d][x]+=fa[d][y],fa[d][y]=x; } inline void merge(int
x1,int x2,int y1,int y2){ assert(x2-x1==y2-y1); Rep(i,lg)if(x1+(1«i)-1<=x2){ merge(i,x1,y1); x1+=1«i,y1+=1«i;
} } inline void init(){ REP(i,1,lg)For(j,n-(1«i)+1){ int k=find(i,j); merge(i-1,j,k),merge(i-1,j+(1«i-1),k+(1«i-
1)); } } int find(int k){return fa[0][k]<0?k:fa[0][k]=find(fa[0][k]);} inline bool same(int x,int y){return
find(x)==find(y);} inline int size(int k){return -fa[0][find(k)];} };
```

## æ °è®.hpp

““cpp // assumed that [mod<=INT\_MAX] is true

```
template T exgcd(const T &a,const T &b,T &x,T &y){ if(!b){x=1,y=0;return a;} T g=exgcd(b,a%b,y,x);
y-=a/bx; return g; }; template inline T inv_exgcd(T n,T p=mod){ // ninv = 1 (mod p) // ninv + pk =
1 // ax + by = 1 T inv=0,tmp=0; exgcd(n,p,inv,tmp); return inv<0?inv+p:inv; } template inline ll ex
CRT(const V &a,const V &m){ int n=a.size(); assert(n==m.size()); For(i,n)assert(0<=a[i]&&0<m[i]); func
tion<ll(ll,ll,ll)>mul=&{ ll z=0; auto add=&{return x+y>=p?x+y-p:x+y;}; for(x%=p;y=x+add(x,x),y«=1)(y&1)&&(z=add
return z; }; ll md=m[0],ret=a[0],x,y; FOR(i,1,n){ ll g=exgcd(md,(ll)m[i],x,y),res=a[i]-ret%m[i]; if(res<0)res+=m[i];
if(res%g)return -1; ll mg=m[i]/g; if(x<0)x+=m[i]; ret+=(x=mul(x,res/g,mg))md; ret%=(md=mg);
if(ret<0)ret+=md; } return ret; }
```

```
inline V inverse(int n,int p=mod){ Vinv(n+1); inv[1]=1; FOR(i,2,n+1)inv[i]=1ll(p-p/i)inv[p%i]%p; return
inv; }
```

```
inline V<V> comb(int n,int m=-1,int p=mod){ if(m===-1)m=n; if(n<m||m<0)return V<V>();
V<V>C(n+1,V(m+1)); For(i,n+1){ C[i][0]=1; FOR(j,1,min(i+1,m+1)){ C[i][j]=C[i-1][j-1]+C[i-1][j];
if(C[i][j]>=p)C[i][j]-=p; } } return C; }
```

```
struct comb_table{ int n; Vfac,ifac; inline comb_table(int n_=0){n=n_,init();} inline void init(){
V(n+1).swap(fac),V(n+1).swap(ifac); fac[0]=1; FOR(i,1,n+1)fac[i]=fac[i-1]*i; ifac[n]=1/fac[n]; Rep(i,n)ifac[i]=ifac[i+1]/(i+1)
} inline mi C(int x,int y){return x<y||y<0?0:fac[x]*ifac[y]/ifac[x-y];} };
```

```
struct pri_table{ int n; // fac[i] is the minimum prime factor of i Vfac,pri; inline pri_table(int
n_=0){n=n_,init();} inline void init(){ if(n<1)return; V(n+1).swap(fac),V().swap(pri); fac[1]=1;
FOR(i,2,n+1){ if(!fac[i])fac[i]=i,pri.pb(i); for(int j:pri){ if(i*j>n)break; fac[i*j]=j; if(i%j==0)break; }
} } inline bool isp(int k){return k<2?false:(fac[k]==k);} inline V div(int k){ assert(k<=n); if(k<2)return
V(); Vret; while(k>1){ int f=fac[k]; do k/=f;while(k%f==0); ret.pb(f); } return ret; } };
```

```
struct mu_table{ int n; Vmu,pri; Vvis; inline mu_table(int n_=0){n=n_,init();} inline void init(){
if(n<1)return; V(n+1).swap(mu),V().swap(pri),V(n+1).swap(vis); mu[1]=1; FOR(i,2,n+1){ if(!vis[i])mu[i]=
1,pri.pb(i); for(int j:pri){ if(i*j>n)break; vis[i*j]=true; if(i%j==0)break; mu[i*j]=-mu[i]; } } } inline int
get(int k){return k<1?0:mu[k];} };
```

```
struct phi_table{ int n; Vphi,pri; inline phi_table(int n_=0){n=n_,init();} inline void init(){ if(n<1)return;
V(n+1).swap(phi),V().swap(pri); phi[1]=1; FOR(i,2,n+1){ if(!phi[i])phi[i]=i-1,pri.pb(i); for(int j:pri){
if(i*j>n)break; if(i%j==0){ phi[i*j]=phi[i]/j; break; } phi[i*j]=phi[i]*(j-1); } } } inline int get(int k){return
k<1?0:phi[k];} };
```

```

struct d_table{ int n; Vcnt,d,pri; Vvis; inline d_table(int n_=0){n=n_,init();} inline void init(){
if(n<1)return; V(n+1).swap(cnt),V(n+1).swap(d),V().swap(pri),V(n+1).swap(vis); cnt[1]=d[1]=1;
FOR(i,2,n+1){ if(!vis[i])cnt[i]=1,d[i]=2,pri.pb(i); for(int j:pri){ if(ij>n)break; vis[i*j]=true; if(i%j==0){
int x=cnt[i*j]; x=cnt[i]+1; d[i*j]=d[i]/x(x+1); break; } cnt[i*j]=1,d[i*j]=d[i]«1; } } } inline int get(int
k){return k<1?0:d[k]; } };

inline mi lagrange(int l,const V &y,int x){ assert(y.size()); int n=y.size(); if(n==1)return y[0];
if(l<=x&&x<l+n)return y[x-l]; int r=l+n-1; r%=mod;if(r<0)r+=mod; x%=mod;if(x<0)x+=mod;
if(r>=x&&x>r-n)return y[n-(r-x)-1]; Vifac(n); ifac[0]=ifac[1]=1; FOR(i,2,n)ifac[i]=(mod-mod/i)ifac[mod%i];
FOR(i,2,n)ifac[i]=ifac[i-1]; Vsuf(n); suf[n-1]=1; REP(i,1,n)suf[i-1]=suf[i](x+mod-r+n-1-i); mi pre=1,ret=0;
For(i,n){ if((n-i)&1)ret+=y[i]presuf[i]ifac[i]ifac[n-1-i]; else ret-=y[i]presuf[i]ifac[i]ifac[n-1-i]; pre=x+mod-
r+n-1-i; } return ret; } inline mi sumexp(int n,int k){ assert(min(n,k)>=0); Vpri; Vpw(k+2);
pw[0]=!k,pw[1]=1; FOR(i,2,k+2){ if(!pw[i])pri.pb(i),pw[i]=mi(i)^k; for(int j:pri){ if(ij>k+1)break;
pw[i*j]=pw[i]pw[j]; if(i%j==0)break; } } FOR(i,2-!k,k+2)pw[i]+=pw[i-1]; return lagrange(0,pw,n);
}

/ pre_f=sum(mu) pre_g=n pre_fg=1 pre_f=sum(phi) pre_g=n pre_fg=n(n+1)/2 pre_f=sum(phiid)
pre_g=n(n+1)/2 pre_fg=n(n+1)(2n+1)/6 / template<class T,class container> T du_sieve(T
n,const V &pre_f,const function<T(T)> &pre_g,const function<T(T)> &pre_fg,container &h){
if(n<pre_f.size())return pre_f[n]; auto it=h.emplace(n,0); T x=it.fi->se; if(it.se){ T pre=pre_g(1);
x=pre_fg(n); for(T i=2;i<=n;++i){ T div=n/i,j=n/div,cur=pre_g(j); x=(cur-pre)du_sieve(div,pre_f,pre_g,pre_fg,h);
i=j,pre=cur; } } return x; }

struct vote_1{ pii v; inline vote_1(){v={-1,0};} inline vote_1(int id,int cnt=1){v={id,cnt};} in-
line vote_1 operator+(const vote_1 &rhs){ vote_1 ret=*this; if(!~ret.v.fi)ret=rhs; else if(~rhs.v.fi){
if(ret.v.fi==rhs.v.fi)ret.v.se+=rhs.v.se; else{ if(ret.v.se<rhs.v.se)ret={rhs.v.fi,rhs.v.se-ret.v.se}; else ret.v.se-
=rhs.v.se; } } return ret; } };

template<int(n)()> struct vote{ Vv; inline vote(){V(n(),{-1,0}).swap(v);} inline vote(int id,int
cnt=1){V(n(),{-1,0}).swap(v),v[0]={id,cnt};} inline vote operator+(const vote &rhs){ voteret=this;
for(pii i:rhs.v){ if(!~i.fi)break; for(pii &j:ret.v)if(!~j.fi|i.fi==j.fi){ j.fi=i.fi,j.se+=i.se; goto skip; } for(pii
&j:ret.v)if(i.se>j.se)swap(i,j); for(pii &j:ret.v)j.se=i.se; skip;; } return ret; } };

template struct fp2{ mi a,b; inline fp2(mi _a=0,mi _b=0):a(_a),b(_b){} inline fp2 operator+(mi
rhs)const{return fp2(a+rhs,b);} inline fp2 operator-(mi rhs)const{return fp2(a-rhs,b);} inline fp2 op-
erator(mi rhs)const{return fp2(arhs,brhs);} inline fp2 operator/(mi rhs)const{mi inv=1/rhs;return
fp2(a*inv,b*inv);} inline fp2 operator^(int k)const{fp2 pw=this,ret(1);for(;k>=1,pw=pw*pw)if(k&1)ret=ret*pw;return
ret;} inline fp2& operator+=(mi rhs){a+=rhs;return this;} inline fp2& operator-=(mi rhs){a-=rhs;return
this;} inline fp2& operator=(mi rhs){a=rhs,b=rhs;return this;} inline fp2& operator/=(mi rhs){mi
inv=1/rhs;a=inv,b=inv;return this;} inline fp2& operator^=(int k){fp2 tmp(1),base=this;for(;k>=1,base=base)if(k&1)tmp=
tmp*base;} inline fp2 operator+(const fp2&rhs)const{return fp2(a+rhs.a,b+rhs.b);} inline fp2 operator-
(const fp2&rhs)const{return fp2(a-rhs.a,b-rhs.b);} inline fp2 operator(const fp2&rhs)const{return
fp2(arhs.a+brhs.bw2,arhs.b+rhs.ab);} inline fp2 operator/(const fp2&rhs)const{assert(rhs.a.val||rhs.b.val);mi
inv=1/(rhs.arhs.a-rhs.brhs.bw2);return fp2((arhs.a-brhs.bw2)inv,(rhs.ab-arhs.b)inv);} inline fp2& opera-
tor+=(const fp2&rhs){a+=rhs.a,b+=rhs.b;return this;} inline fp2& operator-=(const fp2&rhs){a-=rhs.a,b-
=rhs.b;return this;} inline fp2& operator=(const fp2&rhs){mi x=arhs.a+brhs.bw2,y=arhs.b+rhs.ab;a=x,b=y;return
this;} inline fp2& operator/=(const fp2&rhs){assert(rhs.a.val||rhs.b.val);mi inv=1/(rhs.arhs.a-rhs.brhs.bw2);mi
x=(arhs.a-brhs.bw2)inv,y=(rhs.ab-arhs.b)inv;a=x,b=y;return this;} inline fp2 operator-()const{return
fp2(-a,-b);} friend fp2 operator+(mi lhs,const fp2&rhs){return fp2(lhs+rhs.a,rhs.b);} friend fp2 operator-
(mi lhs,const fp2&rhs){return fp2(lhs-rhs.a,-rhs.b);} friend fp2 operator(mi lhs,const fp2&rhs){return
fp2(lhsrhs.a,lhsrhs.b);} friend fp2 operator/(mi lhs,const fp2&rhs){assert(rhs.a.val||rhs.b.val);mi inv=1/(rhs.arhs.a-
rhs.brhs.bw2);return fp2(lhsrhs.a*inv,-lhsrhs.b*inv);} };“

```

## æ '.hpp

```

“cpp template inline V cart_seq(const V &v,function<bool(T,T)>cmp={return x>y;}){ int n=v.size();
Vret(n,pii(-1,n)); stackst; For(i,n){ while(st.size()&&cmp(v[i],v[st.top()]))ret[st.top()].se=i-1,st.pop();

```

```

if(st.size())ret[i].fi=st.top()+1; st.push(i); } return ret; } template inline V cart_son(const V
&v,function<bool(T,T)>cmp={return x>y;}){ int n=v.size(); Vret(n,pii(-1,n)); stackst; For(i,n){
while(st.size()&&cmp(v[i],v[st.top()])))ret[i].fi=st.top(),st.pop(); if(st.size())ret[st.top()].se=i; st.push(i); }
return ret; }

```

```

struct lca_table{ int n,rt; V<V>to; inline void resize(int n_){V<V>(n=n_).swap(to);} inline lca_table(int
n_=0){resize(n_);} inline void add_edge(int x,int y){ assert(0<=x),assert(x<n),assert(0<=y),assert(y<n),assert(x!=y);
to[x].pb(y),to[y].pb(x); } inline lca_table(const V<V>&to_){n=(to=to_).size();init();} Vdep,fa,siz,son,top;
inline void init(int _rt=0){ rt=_rt; V(n).swap(dep),V(n).swap(fa),V(n).swap(siz),V(n,-1).swap(son);
function<void(int,int)>dfs1=&{ if(~f)dep[p]=dep[f]+1; fa[p]=f,siz[p]=1; for(int i:to[p]) if(i!=f){ dfs1(i,p);
siz[p]+=siz[i]; if(!~son[p]||siz[i]>siz[son[p]])son[p]=i; } }; V(n,-1).swap(top); dfs1(rt,-1); function<void(int,int)>dfs2=&{
top[p]=k; if(~son[p]){ dfs2(son[p],k); for(int i:to[p]) if(!~top[i]) dfs2(i,i); } }; dfs2(rt,rt); } in-
line int lca(int x,int y){ assert(0<=x),assert(x<n),assert(0<=y),assert(y<n); while(top[x]!=top[y]){
if(dep[top[x]]<dep[top[y]])swap(x,y); x=fa[top[x]]; } return dep[x]<dep[y]?x:y; } };

```

```

struct tree_chain{ int n,rt; V<V>to; inline void resize(int n_){V<V>(n=n_).swap(to);} inline
tree_chain(int n_=0){resize(n_);} inline void add_edge(int x,int y){ assert(0<=x),assert(x<n),assert(0<=y),assert(y<n),as
to[x].pb(y),to[y].pb(x); } inline tree_chain(const V<V>&to_){n=(to=to_).size();init();} Vdep,fa,rev,seg,siz,son,top;
inline void init(int _rt=0){ rt=_rt; V(n).swap(dep),V(n).swap(fa),V(n).swap(siz),V(n,-1).swap(son); func-
tion<void(int,int)>dfs1=&{ if(~f)dep[p]=dep[f]+1; fa[p]=f,siz[p]=1; for(int i:to[p]) if(i!=f){ dfs1(i,p);
siz[p]+=siz[i]; if(!~son[p]||siz[i]>siz[son[p]])son[p]=i; } }; int cnt=0; V(n).swap(rev),V(n).swap(seg),V(n,-
1).swap(top); dfs1(rt,-1); function<void(int,int)>dfs2=&{ seg[p]=cnt,rev[cnt++]=p,top[p]=k; if(~son[p]){
dfs2(son[p],k); for(int i:to[p]) if(!~top[i]) dfs2(i,i); } }; dfs2(rt,rt); } inline int lca(int x,int y)const{ as-
sert(0<=x),assert(x<n),assert(0<=y),assert(y<n); while(top[x]!=top[y]){ if(dep[top[x]]<dep[top[y]])swap(x,y);
x=fa[top[x]]; } return dep[x]<dep[y]?x:y; } inline int kthac(int p,int k){ assert(0<=p),assert(p<n),assert(k>=0),assert(k<=d
while(k>dep[p]-dep[top[p]]){ k=dep[p]-dep[top[p]]+1; p=fa[top[p]]; } return rev[seg[p]-k]; } inline V
path(int x,int y,bool dir=0){ assert(0<=x),assert(x<n),assert(0<=y),assert(y<n); Vret,ter; bool rv=0;
while(top[x]!=top[y]){ if(dep[top[x]]<dep[top[y]])rv^=1,swap(x,y); if(dir){ if(rv)ter.eb(seg[top[x]],seg[x]);
else ret.eb(seg[x],seg[top[x]]); } else (rv?ter:ret).eb(seg[top[x]],seg[x]); x=fa[top[x]]; } if(dep[x]>dep[y])rv^=1,swap(x,y);
if(dir){ if(rv)ter.eb(seg[y],seg[x]); else ret.eb(seg[x],seg[y]); } else (rv?ret:ter).eb(seg[x],seg[y]); re-
verse(ALL(ter)); ret.insert(ret.end(),ALL(ter)); return ret; } }; inline void virt_tree(V &p,const
tree_chain &tc,V<V> &to){ sort(ALL(p),&{return tc.seg[x]<tc.seg[y];}); p.erase(unique(ALL(p)),p.end());
auto add_edge=&{to[x].pb(y),to[y].pb(x);}; Vst; for(int i:p){ if(st.size()){ int anc=tc.lca(i,st.back());
if(anc!=st.back()){ while(st.size()>1&&tc.seg[anc]<tc.seg[st[st.size()-2]])add_edge(st[st.size()-2],st.back()),st.qb();
if(st.size()==1||tc.seg[anc]>tc.seg[st[st.size()-2]])V().swap(to[anc]),add_edge(anc,st.back()),st.back()=anc;
else add_edge(anc,st.back()),st.qb(); } } V().swap(to[i]),st.pb(i); } while(st.size()>1)add_edge(st[st.size()-
2],st.back()),st.qb(); }

```

```

// root: n-1 inline V pru2fa(const V &p){ int n=_p.size()+2; Vdeg(n),p=_p.pb(n-1); for(int
i:_p)++deg[i]; Vfa(n-1); int j=0; For(i,n-1){ while(deg[j])+>j; fa[j]=p[i]; while(i<n-1&&!~deg[p[i]]&&p[i]<j){
if(i+1<n-1)fa[p[i]]=p[i+1]; ++i; } ++j; } return fa; } inline V<V> pru2tr(const V &p){ int n=p.size()+2;
Vfa=pru2fa(p); V<V>to(n); For(i,n-1)to[i].pb(fa[i]),to[fa[i]].pb(i); return to; } inline V fa2pru(const V
&fa){ int n=fa.size()+1; Vdeg(n); for(int i:fa)++deg[i]; int j=0; Vp(n-2); For(i,n-2){ while(deg[j])+>j;
p[i]=fa[j]; while(i<n-2&&!~deg[p[i]]&&p[i]<j){ if(i+1<n-2)p[i+1]=fa[p[i]]; ++i; } ++j; } return p; }
inline V tr2pru(const V<V> &to){ int n=to.size(); Vfa(n-1,-1); queueq; q.push(n-1); while(q.size()){ int
p=q.front();q.pop(); for(int i:to[p])if(i<n-1&&!~fa[i])fa[i]=p,q.push(i); } return fa2pru(fa); }“

```

## æ ' ç ¶æ °ç» .hpp

```

“cpp template struct BIT{ // d-indexed [-d+1,n]->[1,n+d] Vc1,c2; int d,n; inline void resize(int n_,int
d_=1){ d=d_,n=n_; V(n+d+1).swap(c1); V(n+d+1).swap(c2); } inline BIT(int n=0,int d=1){resize(n,d);}
inline void add(int l,int r,const T &v){ if(l>r)return; l+=d,assert(0<l),assert(l<=n+d); for(int
i=l;i<=n+d;i+=i&-i)c1[i]+=v,c2[i]+=(l-1)v; r+=d,assert(0<r),assert(r<=n+d); for(int i=r+1;i<=n+d;i+=i&-
i)c1[i]-=v,c2[i]-=rv; } inline void add(int k,const T &v){add(k,k,v);} inline T query(int l,int r){
if(l>r)return T(); T ret=0; r+=d,assert(0<r),assert(r<=n+d); for(int i=r;i^=i&-i)ret+=rc1[i]-c2[i];

```

```
l+=d,assert(0<l),assert(l<=n+d); for(int i=l-1;i^=i&~i)ret=(l-1)c1[i]-c2[i]; return ret; } inline T
query(int k){return query(k,k);} };
```

```
template struct BIT3{ // d-indexed [-d+1,n]->[1,n+d] Vc; int d,n; inline void resize(int n_,int d_=1){
d=d_,n=n_; V(n+d+1).swap(c); } inline BIT3(int n=0,int d=1){resize(n,d);} inline void add(int k,const
T &v){ k+=d; assert(1<=k),assert(k<=n+d); for(int i=k;i<=n+d;i+=i&~i)c[i]+=v; } inline T query(int
k){ k+=d; assert(1<=k),assert(k<=n+d); T ret=0; for(int i=k;i>0;i^=i&~i)ret+=c[i]; return ret; } };
```

```
template struct BIT4{ // d-indexed [-d+1,n]->[1,n+d] Vc; int d,n; inline void resize(int n_,int d_=1){
d=d_,n=n_; V(n+d+1).swap(c); } inline BIT4(int n=0,int d=1){resize(n,d);} inline void add(int k,const
T &v){ k+=d; assert(1<=k),assert(k<=n+d); for(int i=k;i>0;i^=i&~i)c[i]+=v; } inline T query(int k){
k+=d; assert(1<=k),assert(k<=n+d); T ret=0; for(int i=k;i<=n+d;i+=i&~i)ret+=c[i]; return ret; }
}; template inline ll invpair(const T &a){ ll ret=0; BIT4t(*max_element(ALL(a))+1); for(const auto
&i:a)ret+=t.query(i+1),t.add(i,1); return ret; }“
```

## ç ©é µ.hpp

```
“cpp template struct matrix{ int n,m; V<V>a; inline matrix(int _n=0,int _m=0,T v=T()):n(_n),m(_m){
V<V>(n,V(m,v)).swap(a); } inline V &operator{return a[idx];} inline const V &operatorconst{return
a[idx];} inline matrix operator(const matrix &rhs){ assert(m==rhs.n); matrix ret(n,rhs.m); For(i,n)For(j,rhs.m)For(k,m)ret[i]
return ret; } inline matrix trans(){ matrix ret(m,n); For(i,n)For(j,m)ret[j][i]=a[i][j]; return ret; } inline bool
gauss(){ assert(n<=m); int nw=0; For(i,n){ if(!a[nw][i])FOR(j,nw+1,n)if(a[j][i]){swap(a[nw],a[j]);break;}
if(a[nw][i]){ For(j,n)if(nw!=j){ T coef=a[j][i]/a[nw][i]; FOR(k,i,m)a[j][k]-=coefa[nw][k]; } ++nw; } } return
nw==n; } inline matrix unit(){ assert(n==m); matrix ret(n,n); For(i,n)ret[i][i]=1; return ret; } inline ma-
trix pow(ull k){ matrix base=this,ret=unit(); for(;k>=1,base=basebase)if(k&1)ret=retbase; return ret; } in-
line matrix mul_pow(const matrix &rhs,ull k){ matrix base=rhs,ret=this; for(;k>=1,base=basebase)if(k&1)ret=ret*base;
return ret; } };
```

```
template struct dis_matrix{ int n,m; V<V>a; inline dis_matrix(int _n=0,int _m=0,T v=T()):n(_n),m(_m){
assert((is_same<T,int>::value)|| (is_same<T,ll>::value)|| (is_same<T,ull>::value)); V<V>(n,V(m)).swap(a);
}; inline V &operator{return a[idx];} inline const V &operatorconst{return a[idx];} inline dis_matrix oper-
ator(const dis_matrix &rhs){ assert(m==rhs.n); dis_matrix ret(n,rhs.m,is_same<T,int>::value?inf:infl);
For(i,n)For(j,rhs.m)For(k,m)ckmin(ret[i][j],a[i][k]+rhs[k][j]); return ret; } inline dis_matrix pow(ull k){
dis_matrix base=this,ret(n,n,is_same<T,int>::value?inf:infl); for(;k>=1,base=basebase)if(k&1)ret=retbase;
return ret; } };
```

## ç! »æ £å .hpp

```
“cpp template struct disc{ // 0-indexed vectord; inline disc(){ } inline void insert(const T &x){d.pb(x);} in-
line void insert(const V &v){d.insert(d.end(),ALL(v));} inline void init(){sort(ALL(d));d.erase(unique(ALL(d)),d.end());}
inline disc(const vector &v){d=move(v);init();} inline int query(const T &x){return lower_bound(ALL(d),x)-
d.begin();} inline int size(){return d.size();} };
```

```
template<class T,class container> struct genID{ int cnt; container id; inline genID():cnt(0){ } inline bool
count(const T &ele){return id.count(ele);} inline int get_id(const T &ele){ auto it=id.emplace(ele,-1);
if(it.se)it.fi->se=cnt++; return it.fi->se; } };
```

## çºŒ §å °.hpp

```
“cpp template<class T,int n> struct LB{ Vd; int cnt,failed; inline void clear(){cnt=failed=0,V(n).swap(d);}
inline LB(){ assert(n>0); assert(n<=(is_same<T,int>::value?31:is_same<T,unsigned>::value?32:is_same<T,ll>::value?63:
1)); clear(); } inline bool insert(T k){ Rep(i,n)if(k>i&1){ if(!d[i]){ ++cnt,d[i]=k; return true; } else
if(!(k^=d[i]))break; } ++failed; return false; } inline bool can(T k){ Rep(i,n)if(k>i&1){ if(!d[i])return false;
else if(!(k^=d[i]))break; } return true; } inline T mx(T k=0){ Rep(i,n)ckmax(k,k^d[i]); return k; } inline
LB operator+(const LB &rhs){ LB ret=rhs; ret.failed+=failed; For(i,n)if(d[i])ret.insert(d[i]); return ret; }
inline LB &operator+=(const LB &rhs){ failed+=rhs.failed; For(i,n)if(rhs.d[i])insert(rhs.d[i]); return *this;
```

```

} // assumed that empty set isn't allowed inline T count(){return (T(1)«cnt)-!failed;} // 0-indexed inline
T rk(T k){ T pw2=1,ret=0; For(i,n)if(d[i]){ if(k»i&1)ret|=pw2; pw2«=1; } return ret; } inline T at(T k){
if(!failed)+k; FOR(i,1,n)Rep(j,i)if(d[i]»j&1)d[i]^=d[j]; T ret=0; For(i,n)if(d[i]){ if(k&1)ret^=d[i]; k«=1; }
return k?-1:ret; } };

```

```

template<class T,int n> struct LB_ts{ // timestamp Vd; Vt; inline void clear(){V(n).swap(d),V(n).swap(t);}
inline LB_ts(){ assert(n>0); assert(n<=(is_same<T,int>::value?31:is_same<T,unsigned>::value?32:is_same<T,ll>::value
1)); clear(); } inline bool insert(T k,int tm){ Rep(i,n)if(k»i&1){ if(!d[i]){ d[i]=k,t[i]=tm; return true; } else
if(tm>t[i])swap(d[i],k),swap(t[i],tm); if(!(k^=d[i]))break; } return false; } inline bool can(T k,int tm=0){
Rep(i,n)if(k»i&1){ if(!d[i]||t[i]<tm)return false; else if(!(k^=d[i]))break; } return true; } inline T mx(T
k=0,int tm=0){ Rep(i,n)if(t[i]>=tm)ckmax(k,k^d[i]); return k; } inline LB_ts operator+(const LB_ts
&rhs){ LB_ts ret=rhs; For(i,n)if(d[i])ret.insert(d[i],t[i]); return ret; } inline LB_ts &operator+=(const
LB_ts &rhs){ For(i,n)if(rhs.d[i])insert(rhs.d[i],rhs.t[i]); return *this; } };

```

## ç°¿æ®µæ ' .hpp

```

““cpp template<class T,T e,T(*merge)(T,T)> struct SGT{ int n; Vt; inline void resize(int n_){V((n=n_)&2,e).swap(t);}
inline SGT(int n_=0){resize(n_);} inline void push_up(int p){t[p]=merge(t[p«1],t[p«1|1]);} void build(int
p,int l,int r,const V&v){ if(l==r){t[p]=v[l];return;} int mid=l+r»1; build(p«1,l,mid,v),build(p«1|1,mid+1,r,v);
push_up(p); } inline void build(const V&v){ assert(v.size()==n); build(1,0,n-1,v); } void build(int p,int l,int
r){ if(l==r){t[p]=e;return;} int mid=l+r»1; build(p«1,l,mid,v),build(p«1|1,mid+1,r,v); push_up(p); } inline
void build(){ build(1,0,n-1); } void query(int p,int l,int r,int ql,int qr,T &ret){ if(ql<=l&&r<=qr){ret=merge(ret,t[p]);return;}
int mid=l+r»1; if(ql<=mid)query(p«1,l,mid,ql,qr,ret); if(qr>mid)query(p«1|1,mid+1,r,ql,qr,ret); }
inline T query(int l,int r){ assert(0<=l),assert(l<=r),assert(r<n); T ret=e; query(1,0,n-1,l,r,ret); re-
turn ret; } void modify(int p,int l,int r,int k,const T &v){ if(l==r){t[p]=v;return;} int mid=l+r»1;
k<=mid?modify(p«1,l,mid,k,v):modify(p«1|1,mid+1,r,k,v); push_up(p); } inline void modify(int k,const
T& v){ assert(0<=k),assert(k<n); modify(1,0,n-1,k,v); } };

```

```

template<class T,T e> struct SGTlazy{ int n; Vt,tag; inline void resize(int n_){n=n_,V(n«2,e).swap(t),V(n«2,e).swap(tag);}
inline SGTlazy(int n_=0){resize(n_);} inline void push_up(int p){} inline void add_tag(int p,const T &v){}
inline void push_down(int p){add_tag(p«1,tag[p]),add_tag(p«1|1,tag[p]),tag[p]=e;} void build(int p,int
l,int r,const V&v){ if(l==r){t[p]=v[l];return;} int mid=l+r»1; build(p«1,l,mid,v),build(p«1|1,mid+1,r,v);
push_up(p); } inline void build(const V&v){ assert(v.size()==n); build(1,0,n-1,v); } void query(int
p,int l,int r,int ql,int qr,T &ret){ if(ql<=l&&r<=qr){return;} push_down(p); int mid=l+r»1;
if(ql<=mid)query(p«1,l,mid,ql,qr,ret); if(qr>mid)query(p«1|1,mid+1,r,ql,qr,ret); } inline T query(int
l,int r){ assert(0<=l),assert(l<=r),assert(r<n); T ret=e; query(1,0,n-1,l,r,ret); return ret; } void
modify(int p,int l,int r,int k,const T &v){ if(l==r){t[p]=v;return;} push_down(p); int mid=l+r»1;
k<=mid?modify(p«1,l,mid,k,v):modify(p«1|1,mid+1,r,k,v); push_up(p); } inline void modify(int k,const
T& v){ assert(0<=k),assert(k<n); modify(1,0,n-1,k,v); } void add(int p,int l,int r,int ql,int qr,const T &v){
if(ql<=l&&r<=qr){add_tag(p,v);return;} push_down(p); int mid=l+r»1; if(ql<=mid)add(p«1,l,mid,ql,qr,v);
if(qr>mid)add(p«1|1,mid+1,r,ql,qr,v); push_up(p); } inline void add(int l,int r,const T &v){ as-
sert(0<=l),assert(l<=r),assert(r<n); add(1,0,n-1,l,r,v); } // int find_l(int p,int l,int r,int ql,int
qr,const T &v){ // if(l==r)return l; // push_down(p); // int mid=l+r»1; // if(ql>mid||)return
find_l(p«1|1,mid+1,r,ql,qr,v); // return find_l(p«1,l,mid,ql,qr,v); // } // inline int find_l(int l,int r,const
T &v){ // assert(0<=l),assert(l<=r),assert(r<n),assert(t[1]>=v); // return find_l(1,0,n-1,l,r,v); // } // int
find_r(int p,int l,int r,int ql,int qr,const T &v){ // if(l==r)return r; // push_down(p); // int mid=l+r»1;
// if(qr<=mid||)return find_r(p«1,l,mid,ql,qr,v); // return find_r(p«1|1,mid+1,r,ql,qr,v); // } // inline
int find_r(int l,int r,const T &v){ // assert(0<=l),assert(l<=r),assert(r<n),assert(t[1]>=v); // return
find_r(1,0,n-1,l,r,v); // } };

```

```

template struct SGT_2n{ int n; Vt,tag; inline int idx(int l,int r){return l+r||=r;} #define p idx(l,r) #define
ls idx(l,mid) #define rs idx(mid+1,r) inline void resize(int n_){n=n_,V(n«1).swap(t),V(n«1).swap(tag);}
inline SGT_2n(int n_=0){resize(n_);} void build(int l,int r,const V&v){ if(l==r){t[p]=v[l];return;} int
mid=l+r»1; build(l,mid,v),build(mid+1,r,v); t[p]=max(t[ls],t[rs]); } inline void build(const V&v){build(0,n-
1,v);} void modify(int l,int r,int k,const T &v){ if(l==r){t[p]=v;return;} int mid=l+r»1; if(tag[p])t[ls]+=tag[p],t[rs]+=tag[p],t

```

```
k<=mid?modify(l,mid,k,v):modify(mid+1,r,k,v); t[p]=max(t[ls],t[rs]); } inline void modify(int k,const T&
v){modify(0,n-1,k,v);} #undef p #undef ls #undef rs };
```

## ç½ ç» æµ .hpp

```
“cpp struct maxflow{ Ve; V<V>hd; int n,S,T; inline void add_edge(int x,int y,int z){ assert(0<=x),assert(x<n),assert(0<=y),
hd[x].pb(e.size()),e.eb(y,z),hd[y].pb(e.size()),e.eb(x,0); } inline maxflow(int _n=0,int _S=-1,int _T=-1){
V<V>(n=_n).swap(hd); S=_S,T=_T; } inline maxflow(const V<V> &to,int _S=-1,int _T=-1){
V<V>(n=to.size()).swap(hd); For(i,n)for(const pii &j:to[i])add_edge(i,j.fi,j.se); S=_S,T=_T; } inline ll
dinic(){ assert(S!=-1),assert(T!=-1); Vdep; auto bfs=&{ V(n).swap(dep); dep[S]=1; queueq; q.push(S);
while(q.size()){ int p=q.front();q.pop(); for(int i:hd[p])if(e[i].se&&!dep[e[i].fi])dep[e[i].fi]=dep[p]+1,q.push(e[i].fi);
} return dep[T]; }; function<ll(int,ll)>dfs=&{ if(p==T)return lim; ll sum=0; for(int i:hd[p])if(e[i].se&&dep[p]+1==dep[e[i].fi])
ll f=dfs(e[i].fi,min((ll)e[i].se,lim-sum)); e[i].se=f,e[i-1].se+=f; if((sum+=f)==lim)break; } if(!sum)dep[p]=0;
return sum; }; ll ret=0; while(bfs())ret+=dfs(S,infl); return ret; } };
```

```
struct mincost{ V<array<int,3>>e; V<V>hd; int n,S,T; inline void add_edge(int x,int y,int z,int w){ as-
sert(0<=x),assert(x<n),assert(0<=y),assert(y<n),assert(z>=0); hd[x].pb(e.size()),e.pb({y,z,w}),hd[y].pb(e.size()),e.pb({x,0,
w}); } inline mincost(int _n=0,int _S=-1,int _T=-1){ V<V>(n=_n).swap(hd); S=_S,T=_T; }
inline mincost(const V<V<array<int,3>> &to,int _S=-1,int _T=-1){ V<V>(n=to.size()).swap(hd);
For(i,n)for(const array<int,3> &j:to[i])add_edge(i,j[0],j[1],j[2]); S=_S,T=_T; } typedef pair<ll,ll> pll;
inline pll primal_dual(){ assert(S!=-1),assert(T!=-1); Vh; Vvis(n); auto spfa=[&]{ h.assign(n,infl); h[S]=0;
queueq; q.push(S); while(q.size()){ int p=q.front();q.pop(); vis[p]=false; for(int i:hd[p])if(e[i][1]&&ckmin(h[e[i][0]],h[p]+e[i][2])
} } spfa(); Vdis; Vpre(n); auto dijkstra=[&{ V(n,infl).swap(dis); dis[S]=0; priority_queueq; q.emplace(0,S);
Vvis(n); while(q.size()){ int p=q.top().se;q.pop(); if(vis[p])continue; vis[p]=true; for(int i:hd[p])if(e[i][1]&&ckmin(dis[e[i][0]],dis[
h[e[i][0]]])){ pre[e[i][0]]={p,i}; if(!vis[e[i][0]])q.emplace(-dis[e[i][0]],e[i][0]); } } return dis[T]!=infl; }; ll
ret1=0,ret2=0; while(dijkstra()){ For(i,n)h[i]+=dis[i]; ll f=infl; for(int i=T;i!=S;i=pre[i].fi)ckmin(f,(ll)e[pre[i].se][1]);
for(int i=T;i!=S;i=pre[i].fi)e[pre[i].se][1]-=f,e[pre[i].se-1][1]+=f; ret1+=f,ret2+=fh[T]; } return {ret1,ret2};
} inline pll dinic(){ assert(S!=-1),assert(T!=-1); Vcur(n); Vdis; V<V>tmp=hd; Vvis(n); auto spfa=[&{
dis.assign(n,infl); dis[S]=0; hd=tmp; queueq; q.push(S); while(q.size()){ int p=q.front();q.pop(); vis[p]=false;
for(int i:hd[p])if(e[i][1]&&ckmin(dis[e[i][0]],dis[p]+e[i][2])&&vis[e[i][0]])q.push(e[i][0]),vis[e[i][0]]=true;
} return dis[T]<infl; }; ll ret1=0,ret2=0; auto dfs=[&ll{ if(p==T)return f; vis[p]=true; ll
ret=0; while(hd[p].size()){ int i=hd[p].back(); if(!vis[e[i][0]]&&e[i][1]&&dis[e[i][0]]==dis[p]+e[i][2]){ ll
d=self(self,e[i][0],min((ll)e[i][1],f-ret)); if(d){ ret+=d,ret2+=de[i][2]; e[i][1]-=d,e[i-1][1]+=d; if(ret==f)break;
} } hd[p].qb(); } vis[p]=false; return ret; }; while(spfa()){ ll d; while(d=dfs(dfs,S,infl))ret1+=d; } return
{ret1,ret2}; } };
```

## è®ç® å ä½ .hpp

```
“cpp const double eps=1e-8; struct vec2D{ double x,y; inline vec2D(double x_=0,double y_=0):x(x_),y(y_){}
inline vec2D operator+(const vec2D &rhs)const{return {x+rhs.x,y+rhs.y};} inline vec2D operator-(const
vec2D &rhs)const{return {x-rhs.x,y-rhs.y};} inline double cross(const vec2D &rhs){return xrhs.y-yrhs.x;}
inline double operator(const vec2D &rhs)const{return xrhs.x+yrhs.y;} // unsafe since overflow, use
!cross() instead // inline bool coln(const vec2D &rhs){return (thisrhs)(thisrhs)==(thisthis)(rhsrhs);}
inline bool coln(const vec2D &rhs){return fabs(cross(rhs))<eps;} inline int dir(const vec2D
&rhs){return !coln(rhs)?cross(rhs)>=eps?1:-1:0;} inline double norm(){return sqrt(xx+yy);}
inline double proj(const vec2D &rhs){return 1.(thisrhs)/(thisthis);} inline vec2D rot(double theta){
double c=cos(theta),s=sin(theta); return {xc+ys,yc-x*s}; } inline int quad(){ if(x>0&&y>=0)return 1;
if(x<=0&&y>0)return 2; if(x<0&&y<=0)return 3; if(x>=0&&y<0)return 4; return 0; } };
```

```
struct vec2d{ ll x,y; inline vec2d(ll x_=0,ll y_=0):x(x_),y(y_){} inline vec2d operator+(const
vec2d &rhs)const{return {x+rhs.x,y+rhs.y};} inline vec2d operator-(const vec2d &rhs)const{return
{x-rhs.x,y-rhs.y};} inline ll cross(const vec2d &rhs){return xrhs.y-yrhs.x;} inline ll operator(const
vec2d &rhs)const{return xrhs.x+yrhs.y;} // unsafe since overflow, use !cross() instead // inline bool
coln(const vec2d &rhs){return (thisrhs)(thisrhs)==(thisthis)(rhsrhs);} inline bool coln(const vec2d
&rhs){return !cross(rhs);} inline int dir(const vec2d &rhs){return cross(rhs)?cross(rhs)>0?1:-
```

```

1:0;} inline double norm(){return sqrt(xx+yy);} inline double proj(const vec2d &rhs){return
1.(thisrhs)/(thisthis);} inline vec2D rot(double theta){ double c=cos(theta),s=sin(theta); return {xc+ys,yc-
x*s}; } inline int quad(){ if(x>0&&y>=0)return 1; if(x<=0&&y>0)return 2; if(x<0&&y<=0)return 3;
if(x>=0&&y<0)return 4; return 0; } };
```