

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/4714861>

Visual optimization of DCT quantization matrices for individual images

Article · February 1993

DOI: 10.2514/6.1993-4512 · Source: NTRS

CITATIONS

252

READS

270

1 author:



[Andrew B. Watson](#)

Apple Inc.

199 PUBLICATIONS 12,419 CITATIONS

SEE PROFILE

Some of the authors of this publication are also working on these related projects:



Human motion perception [View project](#)



vision [View project](#)

DCTune: A TECHNIQUE FOR VISUAL OPTIMIZATION OF DCT QUANTIZATION MATRICES FOR INDIVIDUAL IMAGES.

Andrew B. Watson

NASA Ames Research Center, Moffett Field, CA 94035-1000

1. ABSTRACT

Image compression standards based on the Discrete Cosine Transform do not specify the quantization matrix. This matrix should be designed to provide maximum visual quality for minimum bitrate. I show how this goal can be achieved for individual images in the context of a DCT-based model of visual quality.

2. JPEG DCT QUANTIZATION

The JPEG image compression standard provides a mechanism by which images may be compressed and shared among users^{1, 2}. The image is first divided into blocks of size {8,8}. Each block is transformed into its DCT, which we write c_{ijk} , where i, j indexes the DCT frequency (or basis function), and k indexes a block of the image. Each block is then quantized by dividing it, coefficient by coefficient, by a quantization matrix (QM) q_{ij} , and rounding to the nearest integer

$$u_{ijk} = \text{Round}[c_{ijk}/q_{ij}] \quad (1)$$

The quantization error e_{ijk} in the DCT domain is then

$$e_{ijk} = c_{ijk} - u_{ijk} q_{ij} \quad (2)$$

3. IMAGE-INDEPENDENT PERCEPTUAL QUANTIZATION

The JPEG QM is not defined by the standard, but is supplied by the user and stored or transmitted with the compressed image. The principle that should guide the design of a JPEG QM is that it provide optimum visual quality for a given bit rate. QM design thus depends upon the visibility of quantization errors at the various DCT frequencies. In recent papers, Peterson *et al.*^{3, 4} have provided measurements of threshold amplitudes for DCT basis functions. For each frequency ij they measured psychophysically the smallest coefficient that yielded a visible signal. Call this threshold t_{ij} . From Eqn.s (1) and (2) it is clear that the maximum possible quantization error e_{ijk} is $q_{ij}/2$. Thus to ensure that all errors are invisible (below threshold), we set

$$q_{ij} = 2 t_{ij} \quad (3)$$

I call this the Image-Independent Perceptual approach (IIP). It is perceptual because it depends explicitly upon detection thresholds for DCT basis functions, but is image-independent because a single matrix is computed independent of any image. Ahumada *et al.*^{5, 6} have

extended the value of this approach by measuring t_{ij} under various conditions and by providing a formula that allows extrapolation to other display luminances (L) and pixel sizes (px, py), as well as other display properties. For future reference, we write this formula in symbolic form as

$$t_{ij} = \text{ap}[i, j, L, px, py, \dots] \quad (4)$$

4. LIMITATIONS OF THE IIP APPROACH

While a great advance over the *ad hoc* matrices that preceded it, the IIP approach has several shortcomings. The fundamental drawback is that the matrix is computed independent of the image. This would not be a problem if visual thresholds for artifacts were fixed and independent of the image upon which they are superimposed, but this is not the case.

First, visual thresholds increase with background luminance, and variations in local mean luminance within the image will in fact produce substantial variations in DCT threshold. We call this *luminance masking*.

Second, threshold for a visual pattern is typically reduced in the presence of other patterns, particularly those of similar spatial frequency and orientation, a phenomenon usually called *contrast masking*. This means that threshold error in a particular DCT coefficient in a particular block of the image will be a function of the value of that coefficient in the original image.

Third, the IIP approach ensures that any single error is below threshold. But in a typical image there are many errors, of varying magnitudes. The visibility of this error ensemble is not generally equal to the visibility of the largest error, but reflects a pooling of errors, over both frequencies and blocks of the image. I call this *error pooling*.

Fourth, when all errors are kept below a perceptual threshold a certain bit rate will result. The IIP method gives no guidance on what to do when a lower bit rate is desired. The *ad hoc* "quality factors" employed in some JPEG implementations, which usually do no more than multiply the quantization matrix by a scalar, will allow an arbitrary bit rate, but do not guarantee (or even suggest) optimum quality at that bit rate. I call this the problem of *selectable quality*.

Here I present a general method of designing a custom quantization matrix tailored to a particular image. This *image-dependent perceptual* (IDP) method incorporates solutions to each of the problems described above. The strategy is to develop a very simple model of perceptual

error, based upon DCT coefficients, and to iteratively estimate the quantization matrix which yields a designated perceptual error.

5. LUMINANCE MASKING

Detection threshold for a luminance pattern typically depends upon the mean luminance of the local image region: the brighter the background, the higher the luminance threshold^{7, 8}. This is usually called "light adaptation," but here we call it "luminance masking" to emphasize the similarity to contrast masking, discussed in the next section.

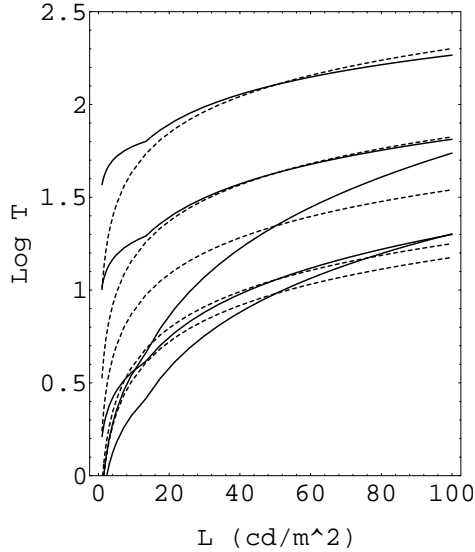


Figure 1. Log of t_{ij} as a function of luminance L of the block. From the top, the curves are for frequencies of $\{7,7\}$, $\{0,7\}$, $\{0,0\}$, $\{0,3\}$, and $\{0,1\}$. The dashed curves are the power function approximation described in the text.

To illustrate this effect, the solid lines in Fig. 1 plot values of the formula for t_{ij} provided by Ahumada and Peterson⁵ as a function of the mean luminance of the block, assuming that the maximum display luminance is 100 cd m^{-2} and that the greyscale resolution is 8 bits. The three curves are for five representative frequencies. These curves illustrate that variations by as much as 0.5 log unit in t_{ij} might be expected to occur within an image, due to variations in the mean luminance of the block.

We can compute a luminance-masked threshold matrix for each block in either of two ways. The first is to make use of a formula such as that supplied by Ahumada and Peterson⁵,

$$t_{ijk} = ap[i, j, L_0 c_{00k} / \bar{c}_{00}] \quad (5)$$

where c_{00k} is the DC coefficient of the DCT for block k , L_0 is the mean luminance of the display, and \bar{c}_{00} is the DC coefficient corresponding to L_0 (1024 for an 8 bit image).

A second, simpler solution is to approximate the dependence of t_{ij} upon c_{00k} with a power function:

$$t_{ijk} = t_{ij} (c_{00k} / \bar{c}_{00})^{a_T} \quad (6)$$

This approximation is illustrated by the dashed lines in Fig. 1. The initial calculation of t_{ij} should be made assuming a display luminance of L_0 . The parameter a_T takes its name from the corresponding parameter in the formula of Ahumada and Peterson, wherein they suggest a value of 0.649. Note that luminance masking may be suppressed by setting $a_T = 0$. More generally, a_T controls the degree to which this masking occurs. Note also that the power function makes it easy to incorporate a non-unity display Gamma, by multiplying a_T by the Gamma exponent.

6. CONTRAST MASKING

Contrast masking refers to the reduction in the visibility of one image component by the presence of another. Here we consider only masking within a block and a particular DCT coefficient. We employ a model of visual masking that has been widely used in vision models,^{9, 10}. Given a DCT coefficient c_{ijk} and a corresponding absolute threshold t_{ijk} our masking rule states that the masked threshold m_{ijk} will be

$$m_{ijk} = \text{Max} \left[t_{ijk}, |c_{ijk}|^{w_{ij}} t_{ijk}^{1-w_{ij}} \right] \quad (7)$$

where w_{ij} is an exponent that lies between 0 and 1. Because the exponent may differ for each frequency, we allow a matrix of exponents equal in size to the DCT. Note that when $w_{ij} = 0$, no masking occurs, and the threshold is constant at t_{ijk} . When $w_{ij} = 1$, we have what is usually called "Weber Law" behavior, and threshold is constant in log or percentage terms (for $c_{ijk} > t_{ijk}$). The function is pictured for a typical empirical value of $w_{ij} = 0.7$ in Fig. 2.

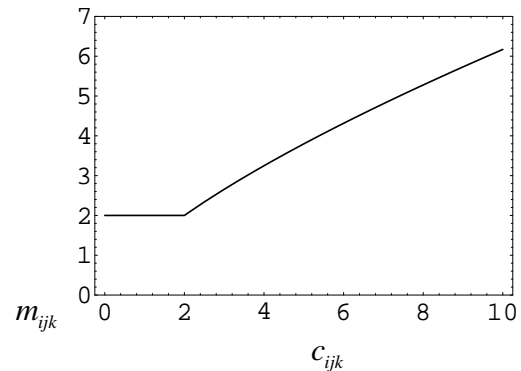


Figure 2. Contrast masking function, describing the masked threshold m_{ijk} as a function of DCT coefficient c_{ijk} , for parameters $w_{ij} = 0.7$, $t_{ijk} = 2$.

Because the effect of the DC coefficient upon thresholds has already been expressed by luminance masking, we specifically exclude the DC term from the contrast masking, by setting the value of $w_{00} = 0$.

7. PERCEPTUAL ERROR AND JUST-NOTICEABLE-DIFFERENCES

In vision science, we often express the magnitude of a signal in multiples of the threshold for that signal. These threshold units are often called "just-noticeable differences," or *jnd*'s. Having computed a masked threshold m_{ijk} , the error DCT may therefore be expressed in *jnd*'s as

$$d_{ijk} = e_{ijk} / m_{ijk} \quad (8)$$

8. SPATIAL ERROR POOLING

To pool the errors in the *jnd* DCT we employ another standard feature of current vision models: the so-called Minkowski metric. It often arises from an attempt to combine the separate probabilities that individual errors will be seen, in the scheme known as "probability summation" ¹¹. We pool the *jnds* for a particular frequency $\{i,j\}$ over all blocks k as

$$p_{ij} = \left(\sum_k |d_{ijk}|^{\beta_s} \right)^{1/\beta_s} \quad (9)$$

In psychophysical experiments that examine summation over space a β_s of about 4 has been observed ¹¹. The exponent β_s is given here as a scalar, but may be made a matrix equal in size to the QM to allow differing pooling behavior for different DCT frequencies. This matrix p_{ij} is now a simple measure of the visibility of artifacts within each of the frequency bands defined by the DCT basis functions. I call it the "perceptual error matrix."

9. FREQUENCY ERROR POOLING

This perceptual error matrix p_{ij} may itself be of value in revealing the frequencies that result in the greatest pooled error for a particular image and quantization matrix. But to optimize the matrix we would like a single-valued perceptual error metric. We obtain this by combining the elements in the perceptual error matrix, using a Minkowski metric with a possibly different exponent, β_f

$$P = \left(\sum_{ij} p_{ij}^{\beta_f} \right)^{1/\beta_f} \quad (10)$$

It is now straightforward, at least conceptually, to optimize the quantization matrix to obtain minimum bit-rate for a given P , or minimum P for a given bit rate. In practice, however, a solution may be difficult to compute. But if $\beta_f = \infty$, then P is given by the maximum of the p_{ij} . Under this condition minimum bit-rate for a given $P = \psi$ is achieved when all $p_{ij} = \psi$.

10. OPTIMIZATION METHOD

Under the assumption $\beta_f = \infty$, the joint optimization of the quantization matrix reduces to the vastly simpler separate optimization of the individual elements of the matrix. Each entry of the perceptual error matrix p_{ij} may be considered an independent monotonically increasing function of the corresponding entry q_{ij} of the quantization matrix.

In the following examples, unless otherwise stated, the parameter values used were $a_T = 0.649$, $\beta = 4$, $w_{ij} = 0.7$, display mean luminance $L_0 = 65 \text{ cd m}^{-2}$, image greylevels = 256, $\bar{c}_{00} = 1024$. The viewing distance was assumed to yield 32 pixels/degree. For a 256 by 256 pixel image, this corresponds to a viewing distance of 7.115 picture heights.

11. OPTIMIZING QM FOR A GIVEN BIT-RATE

It is of interest to relate the JPEG bit-rate to the perceptual error level ψ . This is shown for the Lena and Mandrill images in Fig. 3. This is a sort of inverse "rate-distortion" function. Note that useful bit-rates below 2 bits/pixel yield perceptual errors above about 2.

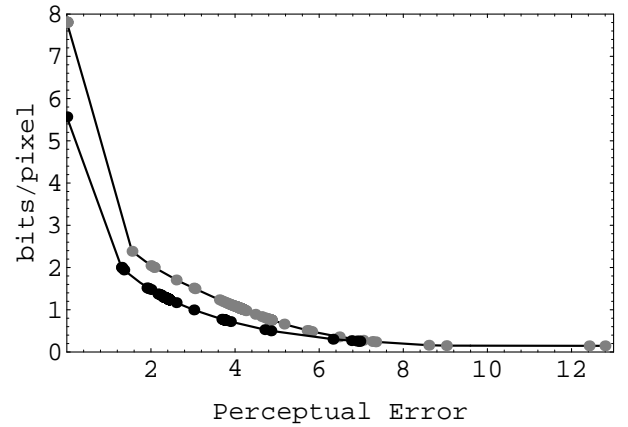


Figure 3. JPEG bit-rate versus perceptual error ψ for the Lena (lower curve) and Mandrill (upper curve) images.

To obtain a QM that yields a given bit rate h_0 with minimum perceptual error ψ we note that the bit rate is a decreasing function of ψ , as shown in Fig. 3.

The most meaningful contest between IDP and IIP approaches is to compare images compressed by the two methods to a constant low bit rate. Figure 4 shows that the IDP method is superior, even in relatively low-quality printed renditions.



Figure 4. IIP (top) and IDP (bottom) compressions at 0.25 bits/pixel .

12. SUMMARY

I have shown how to compute a visually optimal quantization matrix for a given image. These image-dependent quantization matrices produce better results than image independent matrices. The algorithm can be easily incorporated into JPEG-compliant applications.

In a practical sense, the IDP method proposed here solves two problems. The first is to provide maximum visual quality for a given bit rate. The second problem it solves is to provide the user with a sensible and meaningful quality scale for JPEG compression. Without such a scale, each image must be repeatedly compressed, reconstructed, and evaluated by eye to find the desired level of visual quality.

13. ACKNOWLEDGMENTS

I thank Albert J. Ahumada, Jr. and Heidi A. Peterson for valuable discussions. This work was supported by NASA RTOPs 505-64-53 and 506-59-65.

14. REFERENCES

1. G. Wallace. "The JPEG still picture compression standard," *Communications of the ACM*. **34**(4), 30-44 (1991).
2. W. B. Pennebaker and J. L. Mitchell. *JPEG Still image data compression standard* (Van Nostrand Reinhold, New York, 1993).
3. H. A. Peterson. "DCT basis function visibility in RGB space," in *Society for Information Display Digest of Technical Papers*, J. Morreale, ed. (Society for Information Display, Playa del Rey, CA, 1992).
4. H. A. Peterson, H. Peng, J. H. Morgan and W. B. Pennebaker. "Quantization of color image components in the DCT domain," *Human Vision, Visual Processing, and Digital Display*. *Proc. SPIE*. **1453**: 210-222, 1991.
5. A. J. Ahumada Jr. and H. A. Peterson. "Luminance-Model-Based DCT Quantization for Color Image Compression," in *Human Vision, Visual Processing, and Digital Display III*, B. E. Rogowitz, ed. (Proceedings of the SPIE, 1992).
6. H. A. Peterson, A. J. Ahumada Jr. and A. B. Watson. "An improved detection model for DCT coefficient quantization," *SPIE Proceedings*. **1913** (*In press*), (1993).
7. F. L. van Nes and M. A. Bouman. "Spatial modulation transfer in the human eye," *Journal of the Optical Society of America*. **57**, 401-406 (1967).
8. H. B. Barlow. "Dark and light adaptation: Psychophysics," in *Handbook of Sensory Physiology*, L. Hurvich and D. Jameson, ed. (Springer-Verlag, New York, 1972).
9. G. E. Legge and J. M. Foley. "Contrast masking in human vision," *Journal of the Optical Society of America*. **70**(12), 1458-1471 (1980).
10. G. E. Legge. "A power law for contrast discrimination," *Vision Research*. **21**, 457-467 (1981).
11. J. G. Robson and N. Graham. "Probability summation and regional variation in contrast sensitivity across the visual field," *Vision Research*. **21**, 409-418 (1981).
12. A. Weber. *Image data base (USCIP Report 1070)* (Image Processing Institute, University of Southern California, Los Angeles, CA, 1983).