section 12: statistical distributions

stuff to learn today:

- 1. E(X) & Var(X)
- 2. PMF, PDF, CDF
- 3. Bernoulli & Binomial Distributions
- 4. Normal Distributions
- 5. One Sample Z-Test

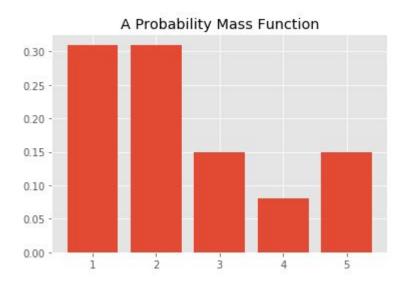
expected value & variance

- for a random variable:

 - expected value = $E(X) = \sum p(x_i) \cdot x_i$ variance = $Var(X) = \sum p(x_i) \cdot (x_i E(X))^2$
- for specific named distributions, there are often formulas for the expected value and variance

probability mass function

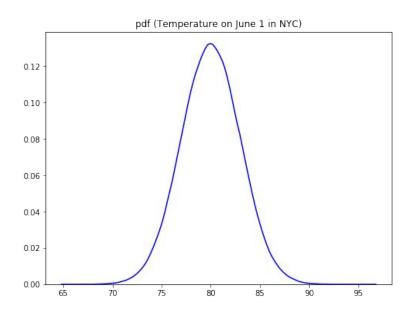
- associates probabilities with discrete random variables
- discrete = a known number of possible outcomes

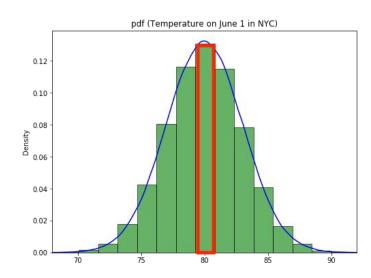


probability density function

- associates probabilities with continuous random

variables

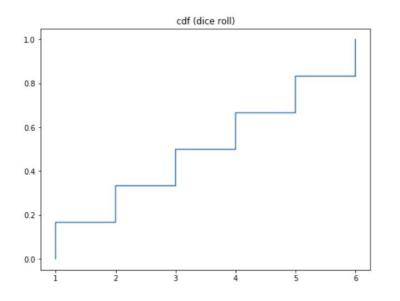


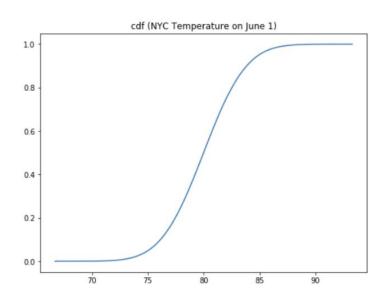


13% of the time you'll observe a temperature between 79.3 and 80.8 degrees

cumulative distribution function

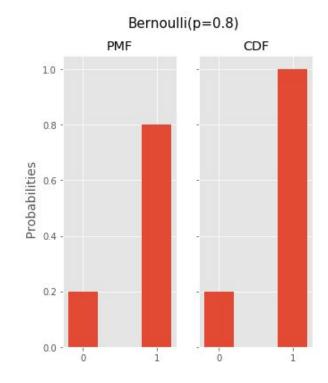
- shows $P(X \le x)$ for any x within the sample space





the bernoulli distribution

- a one-trial, binary outcome experiment
- $X \sim Ber(p=0.8)$
- E(X) = 0.8
- Var(X) = 0.16



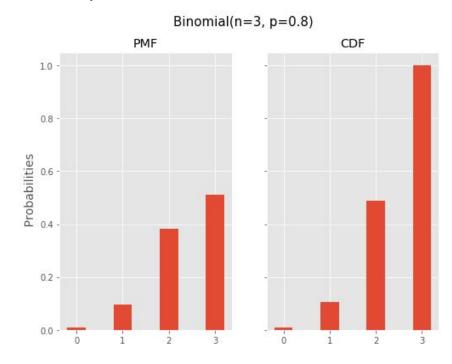
the binomial distribution

- a multi-trial, binary outcome experiment

-
$$X \sim Bi(n = 3, p=0.8)$$

-
$$P(X=k) = {}^{n}C_{k} (p)^{k} (1-p)^{n-k}$$

- E(X) = 2.4
- Var(X) = 0.48

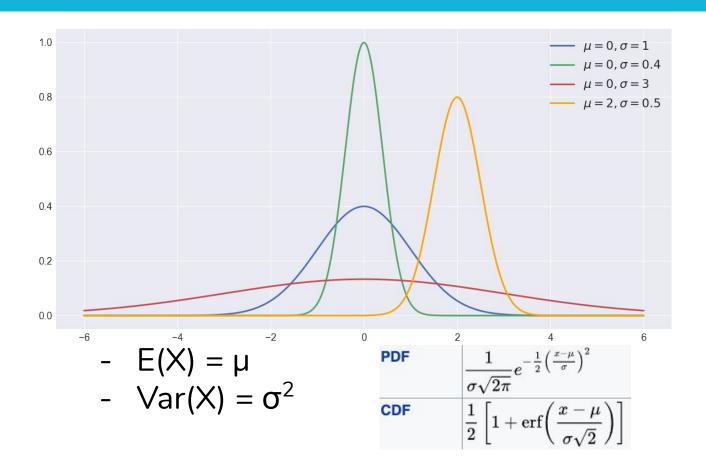


the Normal distribution

- also known as a Gaussian / bell curve
- Normal distributions are symmetric around their mean
- The mean, median, and mode of a normal distribution are equal
- The area under the bell curve is equal to 1.0
- Normal distributions are denser in the center and less dense in the tails
- Normal distributions are defined by two parameters, the meanand the standard deviation
- Around 68% of the area of a normal distribution is within one standard deviation of the mean
- Approximately 95% of the area of a normal distribution is within two standard deviations of the mean

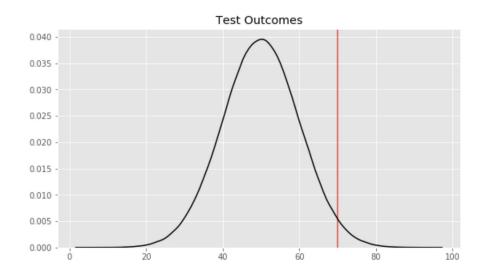


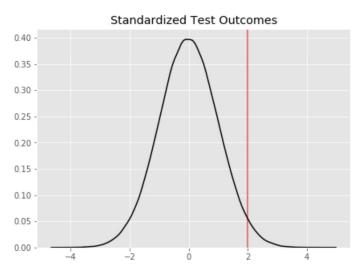
expected value & variance



the Standard Normal distribution

- E(X) = 0, Var(X) = 1
- Allows us to compare different normal distributions
- z-scores!





z-score

 a z-score tells us how many standard deviations away from the mean a point would be in a Standard Normal distribution

 z-scores are associated with cumulative probabilities, retrieved from the z-table

- $z = (x-\mu)/\sigma$ for a single point

- $z = (x-\mu)/(\sigma/\sqrt{n})$ for a sample

