# HiveD: Sharing a GPU Cluster for Deep Learning with Guarantees

# Paper #198

#### **Abstract**

Deep learning training on a shared GPU cluster is becoming a common practice. However, we observe severe sharing anomaly in production multi-tenant clusters where jobs in some tenants experience worse queuing delay than they would have in a private cluster with their allocated shares of GPUs. This is because tenants use *quota*, the number of GPUs, to reserve resources, whereas deep learning jobs often use GPUs with a desirable *GPU affinity*, which quota cannot guarantee.

HiveD is the first framework to share a GPU cluster *safely*, so that such anomaly would never happen by design. In HiveD, each tenant reserves resources through a Virtual Private Cluster (VC), defined in terms of multi-level *cell* structures corresponding to different levels of GPU affinity in a cluster. This design allows HiveD to incorporate any existing schedulers within each VC to achieve their respective design goals while sharing the cluster safely.

HiveD develops an elegant *buddy cell allocation* algorithm to ensure *sharing safety* by efficiently managing the dynamic binding of cells from VCs to those in a physical cluster. A straightforward extension of buddy cell allocation can further support low-priority jobs to scavenge the unused GPU resources to improve cluster utilization.

With a combination of real deployment and trace-driven simulation, we show that: (i) sharing anomaly exists in three state-of-the-art deep learning schedulers, incurring extra queuing delay up to 1,000 minutes; (ii) HiveD can incorporate these schedulers and eliminate the sharing anomaly in all the schedulers, achieving separation of concerns that allows the schedulers to focus on their own scheduling goals without violating sharing safety.

#### 1 Introduction

Deep learning training on a GPU cluster is becoming a major computing workload. It is a common practice for an organization to train deep learning models in a multi-tenant GPU cluster, where each tenant reserves resource using a quota that consists of the number of GPUs and other associated resources such as CPU and memory [46].

Surprisingly, from a production multi-tenant GPU cluster, we observe unexpected anomalies that a tenant's deep learning training jobs wait significantly longer for GPUs than they would have in a private cluster whose size equals to the tenant's quota. This is because the current resource reservation

mechanism is based on *quota*, i.e., the number of GPUs. This cannot capture the GPU *affinity* requirement of deep learning training jobs: e.g., an 8-GPU job on one node usually runs way faster than on eight nodes [35, 46, 76]. Quota cannot guarantee a tenant's GPU affinity like the tenant's private cluster does. As a result, multi-GPU jobs often have to wait in a queue or run at a relaxed affinity, both resulting in worse performance (longer queuing delay or slower training speed).

In this paper, we present HiveD, a resource reservation framework to share a GPU cluster for deep learning training that guarantees *sharing safety* by completely eliminating sharing anomalies. Instead of using quota, HiveD presents each tenant a virtual private cluster (abbreviated as VC) defined by a new abstraction: *cell*. Cell uses a multi-level structure to capture the different levels of affinity that a group of GPUs satisfies. Those cell structures naturally form a hierarchy in a typical GPU cluster; e.g., from a single GPU, to GPUs attached to a PCIe switch, to GPUs connected to a CPU socket, to GPUs in a node, to GPUs in a rack, and so on.

With cell, HiveD virtualizes a physical GPU cluster as a VC for each tenant, where the VC preserves the necessary affinity structure in a physical cluster. This allows any state-of-the-art deep learning schedulers to make scheduling decisions within the boundary defined by the VC, without damaging the affinity requirement from other VCs, hence ensuring sharing safety. In this way, HiveD achieves the separation of concerns [41]: It focuses on the resource reservation mechanism and leaves other resource allocation goals to VC schedulers (e.g., cluster utilization and job completion time).

HiveD develops an elegant and efficient buddy cell allocation algorithm to bind cells from a VC to a physical cluster. Buddy cell allocation advocates dynamic cell binding over static binding for flexibility. It dynamically creates and releases the binding of cells in a VC to GPUs in the physical cluster, while providing proven sharing safety despite unpredictable workloads. Moreover, the algorithm can be naturally extended to support preemptible low-priority jobs to scavenge unused cells opportunistically to improve the overall utilization. Combined, HiveD achieves the best of a private cluster (for guaranteed availability of cells independent of other tenants) and a shared cluster (for improved utilization and access to more resources when other tenants are not using them).

We evaluate HiveD using experiments on a 96-GPU real cluster and trace-driven simulations. The evaluation shows that (i) sharing anomaly exists in all the evaluated state-of-theart deep learning schedulers [35,46,76]; (ii) HiveD eliminates all sharing anomalies, decreases excessive queuing delay from 1,000 minutes to zero, while preserving these schedulers' design goals. (iii) HiveD guarantees sharing safety regardless of cluster loads, whereas a quota-based cluster can result in  $7 \times$  excessive queuing delay for a tenant under a high load.

We have implemented HiveD on top of Kubernetes [24], open-sourced the system, and integrated it in a production deep learning training platform [15]. HiveD has been deployed to multiple GPU clusters serving research and production workloads at scale, including a cluster of 800 GPUs where HiveD has been up and running reliably for more than 6 months (as of May 2020).

In summary, this paper makes the following contributions: (i) We are the first to observe and identify sharing anomaly from a production multi-tenant GPU cluster for deep learning training. (ii) We define the notion of sharing safety against the anomaly and propose a new resource abstraction, i.e., multi-level cells, to model virtual private clusters. (iii) We develop an elegant and efficient buddy cell allocation algorithm to manage cells with a proven sharing safety, and to support low-priority jobs. (iv) We perform extensive evaluations both on a real cluster and through simulation, driven by a production trace, to show that HiveD achieves the design goals in terms of sharing safety, queuing delay, and utilization.

### 2 Background and Motivation

**The current approach of managing a multi-tenant GPU cluster.** In large corporations, a large-scale GPU cluster is usually built by multiple business teams, each is a tenant contributing their resources (budget or hardware). The tenants share a GPU cluster in a way similar to sharing a CPU cluster [1,46]: Each tenant is assigned with a number of tokens as its *quota*. Each token corresponds to the right to use a GPU along with other types of resource. The quota denotes an expectation that the tenant can access "at least" the share of resources it contributes.

To improve training speed in the cluster, user usually specifies a GPU *affinity requirement* for a deep learning job [46,76]. For example, it is often desirable for a 64-GPU job to run in the  $8\times8$  affinity, i.e., to run the job on 8 nodes each with 8 GPUs, instead of  $64\times1$ , i.e., to run on 64 nodes each using 1 GPU. Given the affinity requirements, the resource manager will satisfy them in a guaranteed (hard) or best-effort (soft) manner. If there is no placement satisfying a job's affinity requirement, the job will wait in the queue if it has a hard affinity requirement or will be scheduled with relaxed affinity if the requirement is soft (e.g.,  $64\times1$  as opposed to  $8\times8$ ).

**Sharing anomaly.** In a production GPU cluster similar to the one described above, we observe an anomaly: a tenant is assigned with a quota of 64 GPUs, but cannot run a single (and the only one)  $8\times8$  deep learning job. Such anomaly appears because the tenant's reserved affinity is fragmented

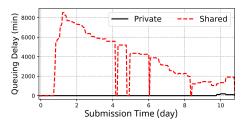


Figure 1: Sharing anomaly: a tenant suffers longer queuing delay in a shared cluster than in its own private cluster.

by jobs from other tenants. Even though the tenant has enough GPU quota, the 64-GPU job has to stay a in queue or execute with degraded performance with relaxed affinity. In this case, the promise to a tenant that it can access at least its share of resource is broken. Rather than sharing with others, the tenant would prefer to run a private cluster with eight 8-GPU nodes to reserve its  $8\times 8$  GPU affinity with zero queuing delay. This anomaly demonstrates that simply reserving resource through quota cannot guarantee the affinity requirement of a tenant.

A multi-tenant cluster is said to suffer from sharing anomaly if a tenant's sequence of GPU requests (possibly with affinity requirement) cannot be satisfied in this shared cluster; but it can be satisfied in a private cluster whose size equals to the tenant's quota. Figure 1 highlights how severe sharing anomaly could become, selected from a trace-driven simulation in a setup similar to [46] (more details in § 5). The figure shows the job queuing anomaly of one tenant in a shared GPU cluster when jobs have hard affinity requirement. In the 10-day submission window (denoted as X-axis), the tenant's average job queuing delay (denoted as Y-axis) in the shared cluster is significantly higher than that in its own private cluster <sup>1</sup>. In particular, the jobs submitted around Day 1 have to stay in the queue for more than 8,000 minutes (5 days) while they have zero queuing delay in the private cluster! Moreover, tenants reserving large resources tend to suffer the most. Consequently, we have witnessed important corporate users reverted to private clusters, after experiencing high queuing delay brought by severe sharing anomalies.

The above observation motivates us to design HiveD, a framework to reserve resource in a GPU cluster in terms of GPU affinity, in addition to quota.

## 3 HiveD Design

# 3.1 System Overview

HiveD proposes to guarantee *sharing safety* (i.e., eliminating sharing anomaly described in § 2) as a prerequisite of sharing a GPU cluster. Specifically, if a sequence of GPU requests with affinity requirements can be satisfied in a private cluster, it should be satisfied in the corresponding virtual private cluster and the shared physical cluster. To achieve this, HiveD separates the concern of sharing safety from other resource al-

 $<sup>^1{</sup>m The}$  anomaly is dominated by queuing delay in the job completion time when the affinity requirement is hard. Details discussed in § 5.1.

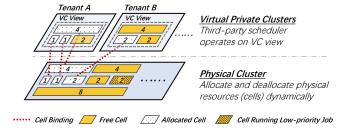


Figure 2: System architecture: a two-layer design.

location objectives [41]: Instead of developing a complicated scheduler that achieves all possible goals (a complex multi-objective optimization problem), HiveD focuses on sharing safety and is able to integrate any state-of-the-art deep learning schedulers to address concerns like cluster utilization [76], job completion time [35, 57], and fairness [25, 53].

Figure 2 illustrates the overall system architecture. HiveD presents each tenant a Virtual Private Cluster (VC). Each VC is pre-assigned with a set of *cells*, a novel resource abstraction that captures not only quota, but also the affinity structure of GPUs (the number inside each cell in the figure shows the number of affinitized GPUs of the cell). The cells assigned to a VC form a VC view with the GPU affinity structure identical to that of the corresponding private cluster. Any third-party scheduler can be incorporated to work on the VC view to achieve a certain goal of resource allocation [35,46,53,76]. Moreover, HiveD ensures that any scheduling decision is constrained within the boundary defined by the VC view, as if on its private cluster, thus it guarantees sharing safety.

Cells in a VC are logical. When a job uses a GPU in a logical cell, e.g., one GPU in the 4-GPU cell in the VC view of Tenant A in Figure 2, the logical cell will be bound to a physical cell allocated from the physical cluster, denoted at the bottom of Figure 2. When none of the GPUs is in use, the cell will be de-allocated from the physical cluster. To improve cluster utilization, such de-allocated GPUs can be used by preemptible low-priority jobs to scavenge unused cells opportunistically. Such dynamic binding is more flexible than a static binding: a dynamic binding can avoid a physical cell whose hardware is failing; it can avoid cells used by low-priority jobs to reduce preemptions; it can also pack the cells to minimize the fragmentation of GPU affinity.

To achieve this, HiveD adopts *buddy cell allocation*, an efficient and elegant algorithm, to handle the dynamic binding. A key challenge of dynamic binding is to guarantee the safety property in response to dynamic workloads: jobs arrive unpredictably and request varying levels of cells. Buddy cell allocation algorithm is proven to ensure sharing safety: any legitimate cell request within a VC is guaranteed to be satisfied. The algorithm can also support low-priority jobs. Figure 2 shows a possible cell allocation, where cells in physical cluster are bound to those defined in two VCs, and also to a low-priority job.

In § 3.2, we explain the details of cells and show how a VC

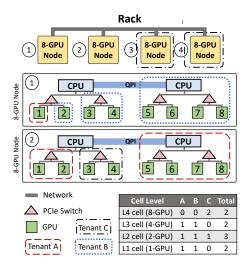


Figure 3: Multi-level cell assignment for a rack: an example.

can be defined by cells. And in § 3.3, we introduce the buddy cell allocation algorithm, prove its sharing safety guarantee, and extend it to support low-priority jobs.

#### 3.2 Virtual Private Cluster with Cells

To model a (private) GPU cluster, HiveD defines a *hierarchy* of multi-level cell structures. A cell at a certain level is the corresponding collection of affinitized GPUs with their interconnection topology. Each virtual private cluster (VC) is then defined as number of cells at each level, modeled after the corresponding private cluster.

Figure 3 shows an example, where there are 4 levels of cell structures: at the GPU, PCIe switch, CPU socket, and node levels, respectively. The cluster has one rack that consists of four 8-GPU nodes, shared by three tenants, A, B, and C. The cell assignment for each tenant's VC is summarized in the table in Figure 3. Tenants A and B's VCs both reserve one level-3 cell (4 GPUs under the same CPU socket), one level-2 cell (2 GPUs under the same PCIe switch), and one level-1 cell (single GPU). Tenant C is a larger tenant, which reserves two level-4 cells (node level) and one level-2 cell. Given the VC views defined in Figure 3, HiveD can adopt a third-party scheduler [35, 46, 53, 76] to work on the views. From the scheduler's point of view, the VC view is no different from a private cluster consisting of nodes with different sizes. For example, a scheduler can simply treat tenant C as a private cluster with 2 8-GPU nodes and 1 2-GPU node, despite the fact that the 2-GPU node is actually a level-2 cell.

In the cell hierarchy, a level-k cell c consists of a set S of level-(k-1) cells. The cells in S are called *buddy cells* for each other; buddy cells can be merged into a cell at the next higher level. We assume cell demonstrates *hierarchical uniform composability*: (i) all level-k cells are equivalent in terms of satisfying a tenant request for a level-k cell, and (ii) how a level-k cell splits into level-(k-1) cells is uniform.

**Heterogeneity.** A heterogeneous cluster can be divided into multiple homogeneous ones satisfying hierarchical uniform composability. This is natural in practice because a production cluster typically consists of sufficiently large homogeneous sub-clusters (each often a result of adding a new GPU model and/or interconnect) [46]. Users typically use homogeneous GPUs for a job for better performance and specify the desired GPU/topology type (e.g., V100 vs. K80).

**Initial cell assignment.** A cluster provider must figure out the number of cells at each level to be assigned to each tenant's VC. A VC assignment is *feasible* in a physical cluster if it can accommodate all cells assigned to all VCs; that is, there exists a one-to-one mapping from the logical cells in each VC to the physical cells in the physical cluster. The initial cell assignment for VCs depends on factors like budget, business priority, and workload, thus it is handled outside of HiveD (§ 6 for further discussion). A cluster might spare more physical resource than the assigned cells to handle hardware failures.

Note that dash-lines in Figure 3 illustrate only one possible cell binding. HiveD advocates dynamic cell binding for flexibility, which reduces job preemption and fragmentation of GPU affinity. § 5.3 confirms its benefits over static binding.

# 3.3 Buddy Cell Allocation Algorithm

HiveD manages the dynamic binding between the logical cells in VCs and the physical cells in the physical cluster, and handles requests to allocate and release cells. This is done by the *buddy cell allocation* algorithm. The algorithm maintains for each VC the information of (i) the corresponding physical cell for each allocated logical cell (i.e., the binding); (ii) a global free list at each cell level k to track all unallocated physical cells at that level. The algorithm always keeps available cells at the highest possible level: for example, if all the buddy cells at level-(k-1) are available for a cell at level-k, only the cell at level-k is recorded. And the algorithm aims to keep as many higher-level cells available as possible. Algorithm 1 shows the pseudo-code of the algorithm.

To allocate a level-k cell in a VC, the algorithm starts at level-k and goes up the levels if needed: it first checks whether or not a free level-k cell is available and allocates one if available. If not, the algorithm will move up level-by-level, until a free level-k cell is available, where k. The algorithm will then split a free level-k cell recursively into multiple lower-level cells, until a level-k cell is available. Each split produces a set of buddy cells at the next lower level, which will be added to the free list at that lower level. One of those new low-level cells is again split until free level-k cells are produced.

The cell release process also works in a bottom-up manner. When a level-k cell c is released, the algorithm adds c into the free list of level-k cells and checks the status of c's buddy cells. If all of c's buddy cells are free, the algorithm will merge c and its buddy cells into a level-(k+1) cell. The merge process continues recursively going up the levels, until no cells

# Algorithm 1 Buddy Cell Allocation Algorithm

- 1: // Initial state of free\_cells: only top level has cells
- 2: procedure ALLOCATECELL(cell\_level)
- 3: **if** free\_cells[cell\_level].size() == 0 **then**
- 4:  $c = AllocateCell(cell\_level+1)$
- 5: cells = Split(c) ▷ Split cells are buddies
- 6: free\_cells[cell\_level].extend(cells)
- 7: **Return** free\_cells[cell\_level].pop()

8:

- 9: procedure RELEASECELL(cell)
- 10: **if** cell.buddies ⊆ free\_cells[cell.level] **then**
- 11: higher\_cell = Merge(cell, cell.buddies)
- 12: free\_cells[cell.level].remove(cell.buddies)
- 13: ReleaseCell(higher cell)
- 14: **else**
- 15: free\_cells[cell.level].add(cell)

can be merged. In this way, the buddy cell allocation algorithm reduces GPU fragmentation and creates opportunities to schedule jobs that require higher-level cells.

Before processing an allocation request, the algorithm ensures the request is legal in that it is within the assigned quota for the VC at this cell level. HiveD stores the cell assignment in a table r, a tenant t's preassigned number for level-k cells is stored in  $r_{t,k}$ . The buddy cell allocation algorithm guarantees to satisfy all legal cell requests under a feasible initial VC assignment, which is formally stated in Theorem 1.

**Theorem 1.** Buddy cell allocation algorithm satisfies any legal cell allocation, under the condition of hierarchical uniform composability, if the original VC assignment is feasible.

*Proof.* Denote as  $r_{t,k}$  the number of level-k cells reserved by tenant t, i.e., cell assignment for t. Denote as  $r_k$  the number of reserved level-k cells for all tenants, i.e.  $r_k = \sum_l r_{t,k}$ . Denote as  $a_{t,k}$  the number of level-k cells that have already been allocated to t by the buddy cell allocation algorithm. Cell allocations that maintain  $a_{t,k} \le r_{t,k}$  are legal. Denote as  $a_k$  the number of allocated level-k cells for all tenants (i.e.,  $a_k = \sum_t a_{t,k}$ ), and  $f_k$  the number of free level-k cells in the physical cluster, and  $h_k$  the number of level-(k-1) buddy cells that a level-k cell can be split into (hierarchical uniform composability). Define  $F_k$  as the number of level-k cells that can be obtained by splitting the higher level cells while still satisfying the safety check for the cell assignment.  $F_k$  can be calculated by Eqn. (1).

$$F_k = \begin{cases} (f_{k+1} + F_{k+1} - (r_{k+1} - a_{k+1}))h_{k+1} & k < \hat{k}; \\ 0 & k = \hat{k}, \end{cases}$$
 (1)

where  $\hat{k}$  is the highest level.

To prove the theorem, we prove the following invariant:

$$r_k - a_k \le f_k + F_k \qquad \forall k = 1, 2, ..., \hat{k}.$$
 (2)

The L.H.S. is the number of level-*k* cells all tenants yet to allocate, and the R.H.S. is the number of available level-*k* cells the cluster can provide.

We prove it by induction on discrete time slots. Denote as w the sequence number of time slots. A change of the cluster state will increase w by 1. When w = 0,  $a_k = 0$ , the invariant (2) holds as long as the original VC assignment is feasible. Assuming the invariant (2) holds at time w = i, we shall prove the invariant (2) still holds at time w = i + 1 after a tenant allocates a legal level-k cell.

Because the allocation is legal,  $a_k < r_k$  should hold at time i+1. In order to satisfy Invariant (2), either  $f_k > 0$  or  $f_k = 0$ . When  $f_k > 0$ , according to Algorithm 1,  $a_k = a_k + 1$  and  $f_k = f_k - 1$  after an allocation of level-k cell at time i+1. The gap of both sides in the invariable (2) remains constant, thus it still holds.

When  $f_k = 0$ , i.e., no free cell at level-k, the algorithm will split a level-k' cell by finding the smallest k' where k' > k and  $f_{k'} > 0$ . In this case, the invariant (2) remains true as in the  $f_k > 0$  case, while the gap of the invariant (2) at level-k' will decrease by 1. If the invariant (2) at the level-k' breaks after cell splitting, this means  $r_{k'} - a_{k'} = f_{k'} + F_{k'}$  at time w = i. By definition,  $F_k$  should be 0 at time w = i. But since  $a_k < r_k$  (because the allocation request is legal), thus invariant (2) cannot hold true at level k. This leads to a contradiction. Therefore, the invariant (2) must hold at level k' after splitting a level-k' cell. Following the same step, we can prove the invariant (2) holds at level k'' when the algorithm recursively splitting a level-k'' cell, where  $k'' \in [k+1,k'-1]$ . Hence the invariant (2) holds on all levels when  $f_k = 0$ .

Merging the buddy cells can only either increase or keep the gap of the invariant (2) thus it still holds. Q.E.D.  $\Box$ 

The buddy cell allocation algorithm has the time complexity of  $O(\hat{k})$ , where  $\hat{k}$  is the number of levels, and can therefore scale to a large GPU cluster efficiently:  $\hat{k}$  is usually 5, from the level of racks to the level of GPUs.

Hierarchical uniform composability ensures the algorithm's correctness and efficiency: it does not have to check explicitly after each split whether or not the subsequent legal allocation requests are satisfiable. Instead, it just needs to check whether every allocation request is legal. For the case where cells are heterogeneous (e.g., due to different GPU models or different inter-GPU connectivity), HiveD partitions the cluster into several pools within which cells at the same level are homogeneous, and applies Algorithm 1 in each pool.

The algorithm resembles buddy memory allocation [49], hence the name. Our key contribution here is making the non-obvious observation: GPU affinity can be modeled as cells, thus making buddy allocation applicable. Moreover, we prove that buddy cell allocation satisfies sharing safety, while traditional buddy memory allocation does not have such safety concern and hence does not provide this guarantee. Our algorithm also reveals the different characteristics of GPU

hierarchy vs. memory regions; for example, the hierarchical uniform composability condition captures GPU hierarchy and is a generalization of the artificially-created power-of-2 rule in buddy memory allocation. Our algorithm also supports priority (elaborated next).

Allocating low-priority cells. The buddy cell allocation algorithm can be naturally extended to support low-priority jobs (a.k.a. opportunistic jobs), whose allocated cells can be preempted by high-priority jobs. Supporting such lowpriority jobs helps improve overall GPU utilization, without compromising the sharing safety guarantees provided to the VCs. HiveD maintains two cell views, one for allocating highpriority (guaranteed) cells, and the other for allocating the lowpriority cells. Both views manage the same set of cells in the physical cluster using the same cell allocation algorithm (i.e., Algorithm 1). Similar to YARN [73] and Omega [63], HiveD enforces strict priority that high-priority bindings can preempt low-priority cells. When allocating low-priority cells, HiveD chooses the cells that are farthest away from those occupied by high-priority jobs (e.g., a non-buddy cell of a high-priority cell) in order to minimize the chance of being preempted. Likewise, when allocating high-priority cells, HiveD chooses the free cells with the fewest GPUs used by low-priority jobs to reduce the chances of unnecessary preemptions.

HiveD adopts weighted max-min fairness [32,43] to decide the numbers of low-priority cells allocated to tenants. With a similar approach, we can easily extend HiveD to support multiple levels of priority.

## 4 Implementation

HiveD has been integrated in an open-source deep learning training platform [15] based on Kubernetes [24]. It has been deployed to multiple GPU clusters, managing various types of GPUs from NVIDIA Volta [16] to AMD MI50 [14]. This includes a cluster with 800 heterogeneous GPUs where HiveD has been running reliably for 6+ months (as of May 2020). HiveD has served research and production workloads at scale, ranging from long-lasting training for large NLP models (e.g., BERT large [30]) to AutoML experiments that consist of hundreds of short-lived 1-GPU jobs. Next we share some experience in implementing and operating HiveD.

HiveD is implemented in 7,700+ lines of Go codes. In addition, it has a few more thousands of lines of JavaScript, Shell scripts, and YAML specifications to integrate with the training platform. It is implemented as a *scheduler extender* [9], a standalone process that works in tandem with the Kubernetes default scheduler (kube-scheduler [7]). This way, HiveD is able to leverage kube-scheduler's basic scheduling logic (e.g., filtering bad nodes).

**Cell specification.** HiveD relies on a cell specification to understand the cell hierarchies in a cluster and the cell assignments for VCs. Figure 4 presents an example specification for a heterogeneous GPU cluster with two racks of

```
cellHierarchy:
 name: V100-RACK # cell hierarchy for V100 rack
  hierarchy:
   cellType: V100-GPU # level-1 cell
  - cellType: V100-PCIe-SWITCH
    splitFactor: 2 # split to 2 level-1 cells
  - cellType: V100-CPU-SOCKET
    splitFactor: 2
   cellType: V100-NODE
    splitFactor:
  - cellType: V100-RACK # level-5 (top-level)cell
    splitFactor: 8
 name: P100-RACK # cell hierarchy for P100 rack
  hierarchy:
  - cellType: P100-RACK # omit lower-level cells
    splitFactor: 8
physicalCluster:
                                vcAssignment:
 topLevelCellType: V100-RACK
                                - vc: vc1 #omit other VCs
  topLevelCellAddresses:
                                  cells:
                                  - subCluster: P100-RACK
  - 10.0.1.0~7
  - 10.0.2.0~8
                                    - cellType: P100-RACK
 topLevelCellType: P100-RACK
                                      cellNumber: 1
  topLevelCellAddresses:
                                  - subCluster: V100-RACK
                                    - cellType: V100-NODE
  - 10.0.3.0~7
                                      cellNumber: 4
```

Figure 4: A simplified cell specification (in .yaml format).

NVIDIA V100 GPUs and one rack of NVIDIA P100 GPUs. cellHierarchy describes the two types of multi-level cell structures. physicalCluster specifies the cell layout in a physical cluster: two V100 racks and one P100 rack, and their IP addresses. With physicalCluster and cellHierarchy, vcAssignment specifies the cell assignment for a VC: the only P100 rack and 4 V100 nodes are assigned to the VC vc1. A third-party scheduler can leverage the VC view of vc1 to make scheduling decisions, as if vc1 is a physical cluster. With the cell specification, HiveD can check if the initial VC assignment is feasible.

Handling faulty hardware. When multiple free cells are available, the buddy cell allocation allows HiveD to avoid using faulty hardware. It prefers binding to a healthy cell when possible. When a VC has no other choice, HiveD will proactively bind to a faulty physical cell so that the third-party scheduler in the VC can see the faulty hardware and avoid using GPUs in the cell.

Fault tolerance. The HiveD process itself is also faulttolerant. It is deployed as a Kubernetes StatefulSet [10] to ensure a single running instance. HiveD maintains several centralized in-memory data structures to keep all the run-time information used for cell allocation (e.g., the free cell list, and the cell allocation list). To reduce overheads, these data structures are not persistent. HiveD partitions and stores the cell binding decision for each pod in its "pod annotation", which is kept reliably by Kubernetes. If a job has multiple pods, the annotation in each pod stores the cell binding decisions for all the pods of the job. When recovering from a crash, HiveD reconstructs all the in-memory data structures like the cell allocation list and the free cell list from the pod annotation in all the running pods. Moreover, with the cell binding decisions stored in pod annotation, HiveD could detect whether or not there are unscheduled pods and resume the scheduling

Tenant	1-GPU	2-GPU	4-GPU	8-GPU	>16-GPU	Total	Ouota
res-a	429	14	260	625	40	1,368	0.37%
res-b	18,319	1.593	931	148	238	21,229	0.73%
res-c	3.285	161	716	185	0	4,347	0.73%
res-d	1.754	0	0	0	0	1.754	1.47%
res-e	2,682	110	3,005	0	0	5,797	1.83%
res-f	8,181	88	618	1,337	559	10,783	28.57%
prod-a	227	54	23	1,132	138	1,574	8.79%
prod-b	16,446	67	605	1,344	22	18,484	10.62%
prod-c	4,692	301	1,905	4,415	1,206	12,519	11.36%
prod-d	781	6	545	650	95	2,077	15.75%
prod-e	58,407	532	2,118	959	2	62,018	19.78%
Total	115,203	2,926	10,726	10,795	2,300	141,950	100%

Table 1: Number of jobs with different GPU demands and quota assignment of tenants.

Type	Model	Dataset		
	Bi-Att-Flow [64]	SQuAD [59]		
NLP	Language Model [80]	PTB [54]		
NLP	GNMT [75]	WMT16 [13]		
	Transformer [72]	WMT16		
Speech	WaveNet [71]	VCTK [12]		
Speech	DeepSpeech [39]	CommonVoice [5]		
	InceptionV3 [69]	ImageNet [29]		
	ResNet-50 [40]	ImageNet		
CV	AlexNet [50]	ImageNet		
	VGG16 [67]	ImageNet		
	VGG19	ImageNet		

Table 2: Deep learning models used in the experiments [76].

for the unscheduled ones. In case none of the pods of a job gets scheduled when HiveD crashes, the job manager, another single instance StatefulSet, will receive a timeout and resubmit the job. The fault tolerance of the third-party scheduler is handled by the scheduler itself.

**Reconfiguration.** A cluster administrator may update the cell specification to reconfigure a cluster: upgrading hardware, adjusting cell assignment for a VC. HiveD treats reconfiguration similar to crash recovery. The difference is during a reconfiguration HiveD will check if there is any inconsistency between the old cell bindings in the pod annotation and the new cell specification. For example, the total bound cells from a VC may exceed the new cell assignment. In this case, HiveD will downgrade the jobs with the inconsistent pods to low-priority jobs and preempt them when necessary.

#### 5 Evaluation

We evaluate HiveD using experiments in a 96-GPU cluster on a public cloud and trace-driven simulations on a production workload. Overall, our key findings include: (i) HiveD eliminates all the sharing anomalies found in all the tested schedulers. Excessive job queuing delay decreases from 1,000 minutes to zero. (ii) HiveD can incorporate the state-of-the-art deep learning schedulers and complement them with sharing safety, while maintaining their scheduling goals and preserving sharing benefits with low-priority jobs. (iii) HiveD guarantees sharing safety under various cluster load. In contrast, high cluster load in quota-based scheme can result in  $7\times$  excessive queuing delay. (iv) HiveD's buddy cell allocation algorithm

reduces job preemption by 55% with dynamic binding and fragmentation of GPU affinity by up to 20%.

**Experimental setup.** We collect a 2-month trace from a production cluster of 279 8-GPU nodes (2,232 GPUs). The trace contains 141,950 deep learning training jobs, each specifying its submission time, training time, number of GPUs with the affinity requirement, and the associated tenant. The cluster is shared by 11 tenants. Table 1 shows each tenant's quota assignment in the real deployment and the distribution of a job's GPU number. We run experiments in a 96-GPU cluster deployed on a public cloud. The cluster consists of 24 virtual machines, each with 4 NVIDIA K80 GPUs.

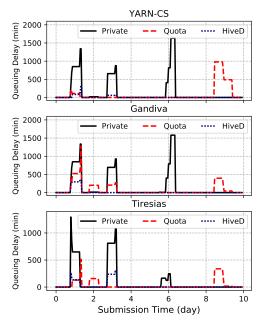
# 5.1 Sharing Safety: Cluster Experiments

In this section, we examine sharing safety in traditional quotabased scheme and HiveD on the deployed cluster.

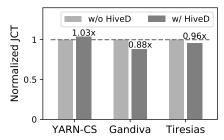
**Methodology.** We collect a 10-day trace from the original 2-month production trace. To approximate the load of the 2,232-GPU cluster on a 96-GPU one, we scale down the number of jobs by randomly sampling from the 10-day trace proportionally (96 out of 2,232). Due to security reasons, we do not have access to the code and data of the jobs. Therefore, we replace the jobs with 11 popular deep learning models in domains of Natural Language Processing (NLP), Speech, and Computer Vision (CV) from GitHub (summarized in Table 2). We mix these models following a distribution of NLP:Speech:CV = 6:3:1, as reported in [76].

We test three state-of-the-art deep learning schedulers: YARN-CS [46], Gandiva [76], and Tiresias [35]. We obtained the source code of Gandiva and Tiresias [11], and use the same implementation in our experiments. YARN-CS is a modified YARN Capacity Scheduler. It packs jobs as close as possible to spare good GPU affinity, similar to [46]. We further refine the preemption policy of YARN-CS: instead of preempting the latest jobs, it preempts low-priority jobs based on the desired GPU affinity requirement. Otherwise, the baseline of YARN-CS will be much worse. To enforce quota in Tiresias, jobs exceeding the quota will get scheduled in a low-priority queue, which is also sorted by Tiresias. For each scheduler, we compare: (i) each tenant running its jobs in a private cluster with the capacity set to its quota; (ii) tenants sharing the cluster using quota; and (iii) tenants sharing the cluster using the scheduler with HiveD enabled. In a shared cluster, all schedulers will schedule jobs as high-priority ones if the tenant has sufficient resource in its quota or VC, otherwise the job will be scheduled as a low-priority one.

In HiveD's experiments, we use a cell hierarchy with four levels: node (8-GPU), CPU socket (4-GPU), PCIe switch (2-GPU), and GPU. We assign each tenant a set of node-level cells with a total number of GPUs equal to its quota. To model the cell hierarchy after the production cluster, we treat every two 4-GPU VMs as one 8-GPU cell. Similar to [76], to speed up replaying the 10-day trace, we "fast-forward" the



(a) Average queuing delay of Tenant prod-a



(b) Average job completion time across all tenants

Figure 5: The experiments for the three schedulers in a 96-GPU cluster, with and without HiveD.

experiment by instructing running jobs to skip a number of iterations whenever there are no scheduling events, including job arrival, completion, preemption, migration, etc. The time skipped is calculated by measuring job training performance in a stable state. To enable the skipping, HiveD bypasses the kube-scheduler and talks to job pods directly.

The trace shows that the GPU affinity requirements of most jobs are hard, showing that users are not willing to sacrifice training performance. In this case, queuing delay is the major source of sharing anomaly in the overall job completion time (JCT). As JCT consists of queuing delay and actual training time, and job training time is highly deterministic as long as GPU affinity is the same, as reported in [76]. Therefore, we show the queuing delay to illustrate the sharing anomaly when job's GPU affinity requirement is hard. We also evaluate the JCT when job's affinity requirement is soft.

**Results.** Figure 5(a) shows the queuing delay for jobs from tenant prod-a using the three schedulers. The X-axis denotes the job submission time. The Y-axis denotes the queuing delay averaged in a 12-hour moving window. Figure 5(a) shows that

all the three schedulers demonstrate sharing anomaly without HiveD. For YARN-CS, from Day 8 to Day 10, jobs in prod-a suffer 1,000 minutes longer queuing delay in a quota-based cluster than in its private cluster. Although YARN-CS packs jobs as compactly as possible, a large number of 1-GPU jobs from other tenants with varying durations make the available GPUs affinity highly fragmented. As a result, multi-GPU jobs have to wait a long time for the desired affinity. Since the majority of jobs in prod-a use multiple GPUs (Table 1), the tenant suffers more from sharing anomaly.

Similarly, in Gandiva, jobs in prod-a suffer up to 400 minutes longer queuing delay in the shared cluster on Day 2 and Day 8. The excessive queuing delay is shorter than that in YARN-CS because Gandiva can mitigate the fragmentation of GPU affinity by job migration. However, unaware of cells in a VC, Gandiva's greedy algorithm may accidentally migrate jobs to improve the job performance in a tenant at the expense of other tenant's GPU affinity, thus violating safety. For example, Gandiva may greedily migrate away an interfering job in a VC while increasing the fragmentation and violating the sharing safety of other VCs. In contrast, HiveD achieves separation of concerns, allowing Gandiva to migrate jobs for its own goal without worrying about sharing safety. We will discuss job migration more in § 6.

In Tiresias, Tenant prod-a shows sharing anomaly on Day 2 and 8. With quota enforcement, Tiresias suffers over 330 minutes longer queuing delay than that in its private cluster. To reduce job completion time (JCT), Tiresias prefers running shorter and smaller jobs first. We do observe shorter queuing delay (and JCT) in Tiresias, compared to the other two schedulers. However, without HiveD, the global advantage of small jobs in a tenant might increase the fragmentation of GPU affinity in other tenants, thus results in sharing anomaly.

The experiment suggests that the evaluated schedulers are effective in their design objectives but they do not consider sharing safety, a factor that could severely impact user experience. HiveD complements the three schedulers with sharing safety by reserving the GPU affinity in each tenant's VC. With HiveD, prod-a (and all the other tenants) never experiences an excessive queuing delay in the shared cluster, using each of the three schedulers. Even during Day  $8{\sim}10$ , the multi-GPU jobs are scheduled immediately as the tenant has enough 8-GPU cells in its VC (hence the reserved cells in the physical cluster). HiveD also allows jobs to have a significantly shorter queuing delay in the shared cluster when a tenant runs out of its own capacity in the private cluster (Day 1, 3, and 6), by giving it chances to run low-priority jobs.

With sharing safety, HiveD can still preserve the scheduling efficiency. Figure 5(b) shows that HiveD exhibits similar job completion time compared to those without HiveD: at most 3% worse (for YARN-CS) and 12% better (for Gandiva).

We also evaluate the job completion time (JCT) when job's GPU affinity requirement is soft. Without HiveD, some jobs experience worse training speed due to a relaxed affinity re-

quirement and thus result in higher JCT in a shared cluster than in a private cluster (i.e., sharing anomaly). Again, HiveD eliminates all sharing anomalies in this case. Overall we observe a trend similar to the result when the affinity requirement is hard, hence the details are omitted in this paper.

# 5.2 Sharing Safety: Full Trace Simulation

We further use simulations to reveal the factors that influence sharing safety. The simulations use YARN-CS as the scheduler in the rest of this section. To validate simulation accuracy, the simulator replays the experiments in § 5.1 and we compare the obtained job queuing delay to that in § 5.1. The largest difference across all the experiments is within 7%. In the simulations we also observe similar sharing anomalies shown in the real experiments, so we believe the variations do not affect the our main conclusion.

Queuing delay in a cluster with the original size. The top two figures in Figure 6(a) show the queuing delay for jobs from two representative tenants, prod-a and prod-e, submitted in 20 days. The jobs run in a cluster of the same size as the original production cluster (279 8-GPU nodes). The result is averaged in a 12-hour sliding window over job submission time. In the bottom figure of Figure 6(a) we also show the level of fragmentation of GPU affinity to observe its correlation with queuing delay. At any time, the level of fragmentation is defined as the proportion of 8-GPU nodes that cannot provide 8-GPU affinity for a high-priority job.

Among the three solutions, HiveD achieves the shortest queuing delay in both tenants. Tenant prod-a suffers a longer queuing delay in its private cluster in several time slots (e.g., the first 5 days) when the resource demands exceed its capacity. Both the quota-based scheme and HiveD reduce the queuing delay significantly by running low-priority jobs. However, from Day 11 to Day 12, prod-a experiences a longer queuing delay (200 minutes) in the quota-based cluster than that in the private cluster. In this period, the fact that no queuing delay observed in its private cluster suggests prod-a has enough GPU quota. But the fragmentation level in the cluster reaches 100%, suggesting the quota-based scheme cannot find even one node to run an 8-GPU job for prod-a. In comparison, proda in HiveD has zero queuing delay since it has enough 8-GPU cells available. Overall, the fragmentation level in HiveD is lower than that in the quota-based scheme, because HiveD reserves cells for each tenant, preventing the fragmentation of reserved GPU affinity.

Queuing delay in a higher-load cluster. When a cluster is under-utilized, sharing anomaly is less likely to happen due to sufficient GPU affinity. To further understand the impact of cluster load on sharing safety, we keep the workload unchanged but reduce the cluster size to 200 8-GPU nodes (1,600 GPUs) and rerun the simulation. In this setup, around 90% of the GPUs are used by high-priority jobs. The results are shown in Figure 6(b). In the quota-based scheme, prod-a

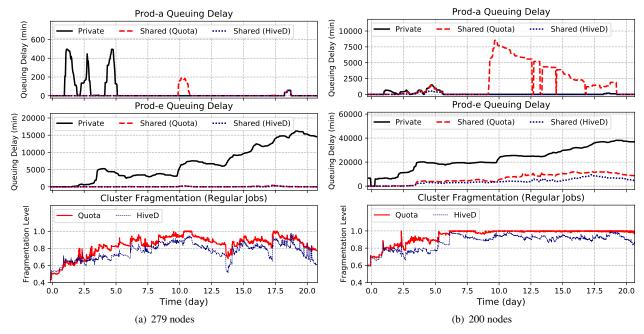


Figure 6: The average job queuing delay of Tenant prod-a and prod-e vs. the level of fragmentation of GPU affinity.

experiences more severe sharing anomaly when the cluster load is higher. The anomaly lasts from Day 9 to Day 19: the queuing delay can be 8,000 minutes longer than that in the private cluster. The higher cluster load incurs a higher level of GPU affinity fragmentation: the fragmentation level stays at 100% for most of the time, which delays the multi-GPU jobs.

For tenant prod-e, the queuing delays for both Quota and HiveD are always shorter in a shared cluster than in the private cluster. This is because its workload is dominated by a large number of 1-GPU jobs (refer to Table 1), which are immune to the fragmentation of GPU affinity. HiveD can further reduce prod-e's queuing delay by guaranteeing its multi-GPU affinities for its multi-GPU jobs.

We also compare the average queuing delay in the three schemes for each tenant and show the result in Figure 7. The bars marked as "Private" and "Quota" show that prod-a's queuing delay in Quota is nearly  $7\times$  that in its private cluster. In contrast, the bars marked as "HiveD" show that every single tenant has a shorter queuing delay in HiveD than in the private cluster. Compared to Quota, HiveD reduces the queuing delay in 9 out of the 11 tenants (accounting for over 98% quota) due to lower fragmentation level. This reduction is up to 94% (for tenant prod-a), and on average 9% for all the 11 tenants.

In all the previous experiments, the cluster utilization in HiveD is similar to or slightly better than that in quota-based scheme. At some time instances, HiveD shows to improve the utilization over quota-based scheme by up to 20% in the 200-node case and 14% in the 279-node case, as a result of reduced queuing delay. In fact, cluster utilization may depend on the "shape" of jobs (i.e., number of GPUs per job). For example, with a sufficient number of 1-GPU jobs, one can

easily saturate the whole cluster. Therefore, our evaluation does not focus on cluster utilization.

Sharing anomalies leading to diminishing benefits of **sharing.** Figure 7 shows prod-a suffers from severe sharing anomaly  $(7 \times \text{ queuing delay})$ . It is no longer beneficial for prod-a to contribute its GPUs to the shared cluster. We then run the experiment again to evaluate the effect of decommissioning prod-a (removing its GPUs and workload) from the cluster. The result is shown in the bars marked as "Quota (w/o prod-a)" in Figure 7. This time, res-f becomes the victim of sharing anomalies, suffering over  $1.7 \times$  longer queuing delay. As the largest tenant, res-f previously benefits less (9% shorter queuing delay in Quota than its private cluster) from contributing GPUs to the cluster, compared to the smaller tenants. Because prod-a contains mostly multi-GPU jobs, after decommissioning prod-a, the fragmentation of GPU affinity in the whole cluster becomes worse, leading to longer queuing delay of res-f's multi-GPU jobs and hence the sharing anomaly. This experiment shows the importance of ensuring sharing safety for large tenants. They already benefit less from the shared cluster. They will prefer not contributing their resource to the cluster if experiencing sharing anomaly.

We further decommission res-f from the cluster and rerun the experiment. The result is shown in the bars marked as "Quota (w/o prod-a and res-f)" in Figure 7. This time, we do not discover further sharing anomaly. However, the decommissioning of the two tenants greatly reduces the sharing benefits of other tenants. prod-a and res-f contribute 37% of the GPUs in the original cluster. The queuing delay of other tenants in the smaller cluster is clearly longer than that in the larger clusters (before removing prod-a and res-f).

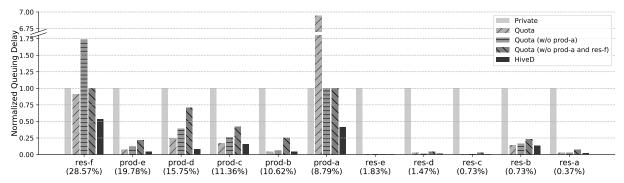


Figure 7: Average queuing delay of each tenant, normalized to that in its private cluster (200 nodes).

In contrast, with HiveD, not a single tenant suffers from sharing anomaly in all the settings. And HiveD's queuing delay is consistently shorter than those without HiveD, across all settings. This highlights the necessity of sharing safety.

GPU affinity requirement vs. Sharing safety. that the distribution of the GPU affinity requirement for jobs across tenants affects sharing safety. Large number of 1-GPU jobs from other tenants may interfere (or fragment) the GPU affinity of a tenant, leading to sharing anomaly. To show this, we "reshape" the GPU affinity requirement of jobs and observe the queuing delay. In the experiment, we divide the 11 tenants into two groups: jobs in one group are reshaped to the GPU affinity of  $1 \times 8$  (8-GPU), and those in the other group are changed to  $1 \times 1$  (1-GPU). The reshaping does not change the total number of GPUs used in each tenant: the number of jobs N is defined by the total number of GPUs divided by the GPU number of a job (8 and 1 in this case). And the job submission time is set by randomly sampling N jobs from the original trace. We further define workload fragmentation as the ratio of the total number of jobs and the total number of GPUs. Jobs with higher affinity level have a lower workload fragmentation. The metric will be 1 if all jobs use 1 GPU.

Initially, only res-f is in the 8-GPU group, while the rest tenants go to the 1-GPU group. Figure 8 shows the queuing delay of res-f (normalized by that in its private cluster) and the workload fragmentation, when tenants prod-e, prod-d, and prod-c are moved to the 8-GPU group one by one. When only res-f is in the 8-GPU group, the workload is highly fragmented (0.91).

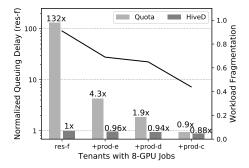


Figure 8: Queuing delay of res-f normalized by private cluster vs. workload fragmentation level (200 nodes).

This leads to severe sharing anomaly in Quota-based system:  $132\times$  of the queuing delay in the private cluster. When more tenants are moved to the 8-GPU group, the workload fragmentation level goes down. This correspondingly reduces sharing anomaly. res-f experiences shorter queuing delay after the other three tenants are added  $(4.3\times, 1.9\times, 0.9\times,$  respectively, as shown in Figure 8). In contrast, HiveD guarantees sharing safety even under the highest fragmentation and consistently provides shorter queuing delay. Similar trends are observed in other tenants, we hence omit the detailed results here.

Soft affinity requirement. We also study the impact on sharing safety when the GPU affinity requirement of some jobs is soft, i.e., relax the affinity if it cannot be satisfied. According to [76], not all training jobs will suffer from performance degradation with relaxed affinity. Hence in the study, we make the most optimistic assumption on the performance degradation: jobs with soft affinity requirement will not sacrifice the training speed. Surprisingly, sharing anomaly could still happen in this case for a quota-based scheme. Figure 9 shows the average queuing delay of tenant prod-a when some multi-GPU jobs in the trace are randomly selected to relax its GPU affinity. We use the 200-node setting in the experiments.

Figure 9 shows that prod-a still has sharing anomaly when 50% of the multi-GPU jobs are allowed to relax their affinity. The average queuing delay in the quota-based scheme is  $1.3 \times 0$  of that in its private cluster. Although no obvious anomaly found in the average queuing delay when the job ratio set to 25% and 75%, we still observe sharing anomalies in certain time instance. This is similar to the behaviors in Figure 5(a)

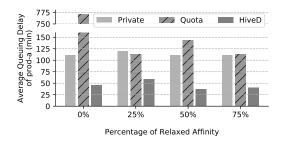


Figure 9: Sharing anomaly still happens when some jobs' GPU affinity requirement is soft.

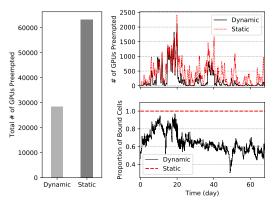


Figure 10: Preemption in dynamic and static bindings.

and 6. We omit the details due to space limit. On the other hand, HiveD eliminates all the sharing anomalies and always has the shortest queuing delay. Note that Figure 9 shows the best case scenario for relaxed affinity. In reality, jobs with relaxed affinity could perform much worse than in the same jobs with the desired affinity [76]. Thus sharing anomaly may happen more likely than described in Figure 9.

Although relaxing affinity may reduce the queuing delay for jobs with soft affinity requirement, the behavior may increase the fragmentation of GPU affinity in the cluster. This in turn will increase the queuing delay for jobs with hard affinity requirement. It becomes a complex tradeoff among queuing delay, fragmentation of GPU affinity, training performance, and cluster utilization. HiveD reserves cells to achieve sharing safety and avoids the complex tradeoff altogether.

## 5.3 Buddy Cell Allocation

In this section, we evaluate the buddy cell allocation algorithm through trace-driven simulations, to understand its effectiveness in reducing preemption and fragmentation of GPU affinity, and its algorithm efficiency.

Reducing preemption with dynamic binding. In the buddy cell allocation algorithm, cells are bound to those in the physical cluster dynamically. This reduces unnecessary preemption of low-priority jobs when there are idle cells. Figure 10 shows the numbers of job preemption when using dynamic binding and static binding, respectively. This experiment uses the same setup of the 279-node experiment in § 5.2. In total, dynamic binding reduces the number of preempted GPUs by 55%. We also measure the correlation between preemption and the proportion of bound cells in the time dimension (in a 12-hour window). When there are more cells being bound to the physical cluster (e.g., Day 10, Day 20 in dynamic binding), there are also more GPUs being preempted. This is because we have fewer choices of physical cells to bind, hence fewer opportunities to reduce preemption. This observation is also consistent with the fact that static binding, where this proportion is always 100%, incurs many more unnecessary preemption.

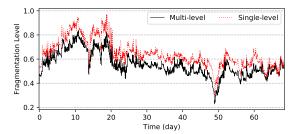


Figure 11: Fragmentation with multi- and single-level cells.

**Reducing fragmentation of GPU affinity with multi-level cells.** Multi-level cells allow the buddy cell allocation algorithm to pack the cells at the same level across tenants to reduce the fragmentation of GPU affinity. For example, if two tenants both have a level-1 (1-GPU) cell, the algorithm prefers selecting two cells from the same physical node, i.e., buddy cells, to run a 1-GPU job. Instead, if both tenants only reserve level-4 cells (8-GPU, node level), the two tenants have to use a level-4 cell to run its 1-GPU job. Hence the two 1-GPU jobs will be placed on two different nodes, which increases the

fragmentation of GPU affinity at node level.

To demonstrate this, instead of only assigning level-4 cells, we assign cells from level-1 to level-4 while keeping the total number of GPUs assigned to each tenant the same as in the above 279-node simulation. Each tenant's assignment matches the distribution of its demands on each level of the cells. Figure 11 shows the fragmentation level of GPU affinity over time when using multi-level and single-level (level-4) cells, respectively. The fragmentation level is always lower with multi-level cells. The gap is over 10% (up to 20%) for most of the time, which means we can spare roughly 30 more level-4 cells. HiveD therefore recommends that tenants model their job's affinity requirements more precisely, for a cluster to perform more efficient cross-VC packing.

Algorithm efficiency. We profile the performance of our implementation of buddy cell allocation in a setup of a 65,536-GPU cluster with 8 racks, each consisting of 1024 8-GPU nodes. We issued 10,000 cell allocation requests at random levels. The average time to complete a request is 2.18ms. The majority of cost comes from ordering cells according to low-priority jobs, which consists of 88% of the time. As the algorithm is clearly not the system bottleneck, we do not perform further optimization (e.g., lock-free operations).

#### 6 Discussion

VC assignment. The VC assignment to a tenant, in terms of both the number of GPUs and their cell structures in a VC, has impacts on the effective VC utilization, queuing delay across tenants. The VC assignment is usually a business process, a common practice in large production clusters, e.g., Borg [74]. Factors to consider in VC assignment include overall capacity, tenant demands, composition of tenant workload, workload variation over time, business priority, and budget constraints. Therefore, HiveD leaves the choice of VC assignment to users.

In most cases, a tenant can just reserve several node-level cells as a VC and adopt a deep learning scheduler for the VC. If a tenant has more details about workloads, e.g., the GPU number distribution of the jobs, the tenant can reserve different levels of cells to fit to the job requirement and enjoy less fragmentation and preemption, as discussed in § 5.3. VC assignment is a new kind of resource reservation based on cells, and HiveD is a framework to enforce such a reservation.

**HiveD** in the cloud. Major cloud providers are offering GPU VMs in the cloud. Our findings in HiveD are highly relevant even in the cloud setting and can shed light on the types of offering in the cloud. Our buddy cell allocation algorithm can also be used by the cloud providers to manage their reserved [2,6,23] and spot [4,8,68] GPU instances, as our VC cells are essentially reserved instances and our low-priority cells are essentially preemptible spot instances. HiveD's implementation already satisfies requirements of a typical cloud provider, e.g., supports different GPU models, reserves payas-you-go instances [61], and handles expansion in capacity. For practical deployment, HiveD can use a hybrid strategy to leverage the cloud as an extension of a multi-tenant GPU cluster when the demand temporarily exceeds the capacity, or can be deployed entirely on a cloud using reserved resources at a lower price, with the options to (i) use spot instances, (ii) buy pay-as-you-go instances when needed, and (iii) purchase and sell reserved capacity in the marketplace [3, 19].

**Job migration.** Migrating jobs between GPUs is a powerful mechanism that has been shown effective [76] in improving quality of GPU allocations. De-fragmentation via migration can in theory be used to resolve potential sharing safety violations, but our experience has shown that there are significant challenges in applying migration in production. Fully transparent migration remains challenging in practice, due to implementation issues in different deep learning frameworks (e.g., inconsistent or limited use of certain programming APIs; challenges of multi-language, multi-framework, and multi-version support [17, 26, 55, 56]). Moreover, the choice of which jobs to migrate and where can be complex, with different conflicting objectives to balance and among a large search space. As shown in § 5.1, a greedy migration algorithm [76] can still violate sharing safety. In contrast, HiveD's cell abstraction and buddy cell allocation algorithm enable separation of concerns. As shown, HiveD can also leverage migration, especially within each tenant—it will be a search space constrained to within a tenant under the sharing-safety guarantee.

#### 7 Related Work

Affinity-aware schedulers for deep learning training. Affinity has been well considered important when scheduling deep learning jobs [18,35,45,46,52,57,62,76], as well as other (big-data) jobs [31,33,79]. HiveD complements these sched-

ulers by applying them in virtualized cluster views, thereby leveraging their efficiency while avoiding sharing anomalies, as identified and shown in our experiments.

**Fairness in shared clusters.** Identifying the fair share of resources in large clusters has been widely studied. Max-min fairness [48] has been extended in a CPU cluster to address fair allocation of multiple resource types (DRF [32]), job scheduling with locality constraints [33, 34, 42, 79], and correlated and elastic demands (HUG [27]). There are recent proposals to achieve fairness and efficiency for machine learning workloads [25,53].

In contrast, HiveD focuses on sharing safety with respect to *given* resource shares (i.e., VC assignment). As we have discussed in § 6, determining the resource shares is usually a business process. HiveD assumes a pre-agreed resource partition among multiple tenants, and enforces it with the sharing safety guarantee. This is driven by witnessing that corporate users are annoyed by the uncertainty on the availability of GPU resources that are already assigned to them. In this sense, HiveD is a framework to guarantee a type of resource reservation [81], defined in terms of cells in VCs. HiveD can address fairness by applying the fairness schemes (e.g., Themis [53]) to determine fine-grained fair-share for jobs within a tenant (or across tenants for low-priority jobs), given the coarse-grained VC assignment enforced by HiveD.

**Performance isolation.** Performance in a shared cluster is sensitive to various sources of interference, including I/O, network, and cache. There are research works on performance isolation that include storage isolation [28, 36, 37, 70], appliance isolation [20, 66], network isolation [38, 51, 58, 65, 77], and GPU isolation [21, 22, 44, 47, 60, 78]. In HiveD, we identify a new source of interference: the fragmentation of GPU affinity in a tenant may affect the GPU affinity in other tenants in a shared GPU cluster. To eliminate such interference, HiveD adopts the notion of VC to encapsulate the requirement in multi-level cells and constrains the scheduling behavior within each VC.

## 8 Conclusion

Motivated by observations from production clusters and validated through extensive evaluations, HiveD takes a new approach to the challenge of sharing a multi-tenant GPU cluster for deep learning by (i) defining a simple and practical guarantee, sharing safety, that is easily appreciated by tenants, (ii) proposing an affinity-aware resource abstraction, cell, to model virtual private clusters, (iii) developing an elegant and efficient algorithm, buddy cell allocation, that is proven to guarantee sharing safety and is naturally extended to support low-priority jobs, and (iv) devising a flexible architecture, to incorporate state-of-the-art schedulers for both sharing safety and scheduling efficiency. Combined, HiveD strikes the right balance between multiple objectives such as sharing safety and cluster utilization.

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