# Two-dimensional packing problem

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#### Abstract

Abstract.

## 1 Two-dimensional packing problem

## **Notations**

#### Sets and indices

- I: Set of components,  $I = \{0, 1, \dots, n\}$ .
- i: Index of components,  $i \in I$ .

#### **Parameters**

- $W_{UB}$ : Upper bound of the width.
- $L_{UB}$ : Upper bound of the length.
- $w_i$ : Width of component i.
- $l_i$ : Length of component i.

## Decision variables

- W: width of the packing.
- L: length of the packing.
- $x_i$ : X-coordinate of component i.
- $y_i$ : Y-coordinate of component i.

 $\min WL$ 

- $u_{i,j}$ : Binary variable indicating whether component i is placed at the left of component j.
- $v_{i,j}$ : Binary variable indicating whether component i is placed at the above of component j.
- $\mu_i$ : Binary variable indicating whether component i is in rotation mode.

### Optimization model

s.t. 
$$x_i + w_i(1 - \mu_i) + l_i\mu_i \le x_j + W_{UB}(1 - u_{i,j}) \quad \forall i, j \in I, i \ne j$$
 (2)  
 $y_i + l_i(1 - \mu_i) + w_i\mu_i \le y_j + L_{UB}(1 - v_{i,j}) \quad \forall i, j \in I, i \ne j$  (3)  
 $u_{i,j} + u_{j,i} + v_{i,j} + v_{j,i} \ge 1 \quad \forall i, j \in I, i \ne j$  (4)

$$u_{i,j}, v_{i,j} \in \{0, 1\} \quad \forall i, j \in I, i \neq j$$

$$(4)$$

$$(5)$$

(1)

$$\mu_i \in \{0, 1\} \quad \forall i \in I \tag{6}$$

$$0 \le x_i \le W - w_i(1 - \mu_i) - l_i \mu_i \quad \forall i \in I \tag{7}$$

$$0 \le y_i \le L - l_i(1 - \mu_i) - w_i \mu_i \quad \forall i \in I$$
(8)