All Matrix Operations

Simplify. Write "undefined" for expressions that are undefined.

$$1) \begin{bmatrix} 2 & -1 \\ -6 & 1 \end{bmatrix} \cdot \begin{bmatrix} 4 & 4 \\ -3 & -5 \end{bmatrix}$$

$$2) \begin{bmatrix} 2 & 6 \\ -6 & 4 \end{bmatrix} \cdot \begin{bmatrix} 5 & 3 \\ -6 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 2 & 0 \end{bmatrix}$$

$$3) \begin{bmatrix} -1 & 5 \\ 5 & -5 \end{bmatrix} \cdot \begin{bmatrix} -3 & 6 \\ -3 & 0 \end{bmatrix}$$

$$4) \begin{bmatrix} 1 & -6 \\ 3 & 5 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 5 \end{bmatrix} + \begin{bmatrix} -3 \\ 0 \\ 3 \\ -2 \end{bmatrix}$$

$$5) \begin{bmatrix} -2 \\ -3 \\ -6 \\ 2 \end{bmatrix} + \begin{bmatrix} -4 \\ 6 \\ 0 \\ -3 \end{bmatrix}$$

$$6) -4 \cdot \left[\begin{array}{rr} -3 & -6 \\ 1 & 4 \end{array} \right] \cdot \left[\begin{array}{rr} -2 & 6 \\ -1 & -4 \end{array} \right]$$

7)
$$\begin{bmatrix} 3 & 1 & 3 \\ 0 & 5 & -3 \end{bmatrix} + \begin{bmatrix} -1 & 3 \\ 6 & 1 \end{bmatrix} \cdot \begin{bmatrix} 0 & -6 & -1 \\ 1 & 1 & 4 \end{bmatrix}$$

8)
$$-5$$
 $\begin{bmatrix} 2 \\ -1 \\ -6 \end{bmatrix}$ $+$ $\begin{bmatrix} 2 \\ -4 \\ 4 \end{bmatrix}$

$$9)\begin{bmatrix} -1 & -1 \\ -6 & 3 \end{bmatrix} + \begin{bmatrix} -5 & -1 \\ -4 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 6 \\ 1 & 6 \end{bmatrix}$$

$$10) \begin{bmatrix} -2 \\ -6 \end{bmatrix} - 3 \begin{bmatrix} -6 \\ 0 \end{bmatrix}$$

11)
$$-2\begin{bmatrix} -3 & -5 & -5 \\ 0 & 5 & -6 \end{bmatrix} + \begin{bmatrix} 4 & -1 & -3 \\ 6 & 3 & 2 \end{bmatrix}$$

$$12) \begin{bmatrix} -5 & 1 \\ -4 & -5 \end{bmatrix} \cdot \begin{bmatrix} 5 & -4 & 2 \\ -6 & 3 & -6 \end{bmatrix} + \begin{bmatrix} 3 & -5 & 2 \\ 5 & 5 & 3 \end{bmatrix}$$

13)
$$\begin{bmatrix} -4y & 2y \\ 2 & 3 \end{bmatrix} + \begin{bmatrix} 2y & 6 \\ 2 & 2x \end{bmatrix} \cdot \begin{bmatrix} 5 \\ -5 \end{bmatrix}$$

14)
$$\begin{bmatrix} 6y & y^2 \\ -2y & -2y \end{bmatrix} \cdot \begin{bmatrix} -y & xy \\ -6 & x^2 \end{bmatrix} - \begin{bmatrix} 6y & -6 \\ -3y & y \end{bmatrix}$$

Critical thinking questions:

- 15) Give an example of a matrix expression in which you would first perform a matrix subtraction and then a matrix multiplication. Use any numbers and dimensions you would like but be sure that your expression isn't undefined.
- 16) A, B, and C are matrices: A(B+C) = AB + CA
 - A) Always true
- B) Sometimes true
- C) False