

```
In [13]: #####
### Name : Md Ziauddin Ridoy #####
### Matriculation : 220100676 #####
```

```
In [14]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
```

```
In [15]: def Rosenbrock(x,y):
        return (1 + x)**2 + 100*(y - x**2)**2

def Grad_Rosenbrock(x,y):
    g1 = -400*x*y + 400*x**3 + 2*x -2
    g2 = 200*y -200*x**2
    return np.array([g1,g2])

def Hessian_Rosenbrock(x,y):
    h11 = -400*y + 1200*x**2 + 2
    h12 = -400 * x
    h21 = -400 * x
    h22 = 200
    return np.array([[h11,h12],[h21,h22]])
```

```
In [17]: def Gradient_Descent(Grad,x,y, gamma = 0.00125, epsilon=0.00001, nMax = 100000 ):
    #Initialization
    i = 0
    iter_x, iter_y, iter_count = np.empty(0),np.empty(0), np.empty(0)
    error = 10
    X = np.array([x,y])

    #Looping as long as error is greater than epsilon
    while np.linalg.norm(error) > epsilon and i < nMax:
        i +=1
        iter_x = np.append(iter_x,x)
        iter_y = np.append(iter_y,y)
        iter_count = np.append(iter_count ,i)
        #print(X)

        X_prev = X
        X = X - gamma * Grad(x,y)
        error = X - X_prev
        x,y = X[0], X[1]

    print(X)
    return X, iter_x,iter_y, iter_count

root,iter_x,iter_y, iter_count = Gradient_Descent(Grad_Rosenbrock,-2,2)

[0.99112457 0.98229221]
```

```
In [20]: x = np.linspace(-2,2,250)
y = np.linspace(-1,3,250)
X, Y = np.meshgrid(x, y)
Z = Rosenbrock(X, Y)

#Angles needed for quiver plot
anglesx = iter_x[1:] - iter_x[:-1]
anglesy = iter_y[1:] - iter_y[:-1]

%matplotlib inline
fig = plt.figure(figsize = (16,8))

#Surface plot
ax = fig.add_subplot(1, 2, 1, projection='3d')
ax.plot_surface(X,Y,Z,rstride = 5, cstride = 5, cmap = 'jet', alpha = .4, edgecolor = 'none' )
ax.plot(iter_x,iter_y, Rosenbrock(iter_x,iter_y),color = 'r', marker = '*', alpha = .4)

ax.view_init(45, 280)
ax.set_xlabel('x')
ax.set_ylabel('y')

#Contour plot
ax = fig.add_subplot(1, 2, 2)
ax.contour(X,Y,Z, 50, cmap = 'jet')
#Plotting the iterations and intermediate values
ax.scatter(iter_x,iter_y,color = 'r', marker = '*')
ax.quiver(iter_x[:-1], iter_y[:-1], anglesx, anglesy, scale_units = 'xy', angles = 'xy', scale = 1, color = 'r')
ax.set_title('Gradient Descent with {} iterations'.format(len(iter_count)))

plt.show()
```

