Real-Time 4D Deformable Image Registration Using Feature-Based Adaptive Tetrahedral Mesh

Abstract. In this paper, we propose a novel finite element method (FEM)-based deformable image registration (DIR) approach for 4D (i.e., 3D data in different phases) tracking, with fast computational speed and high accuracy. Firstly, the adaptive tetrahedral mesh is generated based on the image features of the reference phase. Subsequently, the deformation vector fields (DVFs) and deformed 4D images can be obtained through an optimization of matching each phase of the target 4D images with the corresponding deformed reference phase image in an intensitybased scheme with mesh-based modeling. The proposed 4D DIR method is designed parallelly and implemented on GPU, resulting in a real-time computation. Finally, both DVFs and deformed images are used in highquality 4D image and motion visualization, tumor tracking, and organ segmentation. The performance of the proposed algorithm is evaluated on a digital phantom and a clinical 4D CT image. Our results are compared qualitatively and quantitatively with the state-of-the-art in DIR by using the standard measurement criteria.

Keywords: Deformable image registration (DIR), adaptive tetrahedral mesh, 4D motions, GPU

1 Introduction

Online adaptive radiation therapy (ART) requires real-time and accurate target tracking and segmentation. Towards this end, deformable image registration (DIR) has been employed as an automated and effective tracking method to transfer tumor segmentations or organ contours/surfaces from treatment planning images to daily in-room images during the therapy. However, the computational time and accuracy of current DIR methods are still insufficient for online ART, especially in a large data set of 4D (space-time) images. In addition, high-fidelity modeling of the 3D shapes of the tumor and surrounding organs and tissues in real-time for tracking their deformations and motions accurately at different phases become important in radiation therapy.

To realize the clinical applications of DIR, a number of approaches have been investigated and developed, such as demons, i.e., one commonly used DIR algorithm, introduced by Thirion [1], and its variants [2,3]. Recently, Gu et al. [4] implemented the original version and the variants of the demons algorithm on the GPU to improve the efficiency for online ART applications. However, in all

previous demons-based DIR methods, the voxel-based deformation vector fields (DVFs) were employed, i.e., 256^3 for each phase in a single breathing cycle of 4D image case, where a large number of unknowns need to be estimated, so that the computational time is extremely long and cannot realize in real time for clinical applications. Consequently, the previous demons methods were only employed in two-phase registration, instead of computing the deformations between all respiration phases, such as ten or more. Even with a multi-scale strategy (i.e., uniform down-sampling) used in some applications, it improves the speed but loses the accuracy. Besides that, in reality, different organs may have different motions in 4D case, such as during respiration, the lung, diaphragm and liver slide against the thoracic cage while moving independently. So it is necessary to consider the anisotropic motion fields between different organs, instead of using a global motion model.

The objective of this work is to propose a new DIR framework, with fast computational speed and high accuracy, by using feature-based adaptive tetrahedral meshing and GPU-based parallelization. The finite element method (FEM) restricts the solution space of the image registration problem with much fewer degrees of freedom and ensures the smoothness of the transformation by interpolation. Meanwhile, the feature-based adaptive tetrahedral mesh can effectively and precisely describe the deformations according to the organ shapes and fine structures in the region of interest. In order to further improve the computational speed and make the DIR system suitable for routine clinical use, with the help of a fast optimal search and a single GPU-based implementation, the proposed DIR algorithm can be accomplished around 50 s for a 10-phase 4D CT with a phase dimension of $256 \times 256 \times 150$.

2 Method

2.1 Feature-Based Adaptive Tetrahedral Mesh Generation

In this section, we present the detailed procedure of the proposed FEM, i.e., generating the high-quality and high-fidelity feature-based adaptive tetrahedral mesh using a 4D NCAT phantom [5].

Original images are pre-analyzed using a Laplacian operator to extract features including contour edges and boundaries between organs and tissues, which are regions of highly non-linear intensity variation. When the feature edges of the volume image are obtained, a smooth density field could be calculated based on the distance between the feature edges and the voxels in the volume domain, instead of relying on manual segmentation (Fig. 1 (b)). Then, the mesh vertices are automatically computed by particle-based volume meshing method, which is based on the adaptive surface meshing framework [6]. This method is more efficient compared with other meshing methods [7,8] as it only optimizes the vertex positions and finally computes the mesh connectivities once. Regarding each mesh vertex as a particle, the potential energy between particles determines the inter-particle forces. To generate the adaptive meshing, the concept of high-dimensional embedding space is applied. In our image-based adaptive meshing

scenario, such embedding space is transformed from the original Euclidean space with a density field. When the forces applied on each particle reach an equilibrium state in this embedding space, the particle distribution on the original domain will exhibit the desired adaptive property, i.e., conforming to the user-defined density field. This property is used to formulate our particle-based adaptive tetrahedral meshing framework.

The inter-particle energy \overline{E}^{ij} between particles i and j in the embedding space is defined as:

$$\overline{E}^{ij} = e^{-\frac{(\mathbf{v}_i - \mathbf{v}_j)^T \mathbf{M}_{ij} (\mathbf{v}_i - \mathbf{v}_j)}{4\sigma^2}},\tag{1}$$

where \mathbf{v}_i and \mathbf{v}_j indicate the positions of particles i and j. \mathbf{M}_{ij} is the density field between particles i and j and it is a 3×3 diagonal matrix. σ is Gaussian kernel width. The gradient of \overline{E}^{ij} can be considered as the inter-particle force $\overline{\mathbf{F}}^{ij}$ in the embedding space:

$$\overline{\mathbf{F}}^{ij} = \frac{\partial \overline{E}^{ij}}{\partial \overline{\mathbf{v}}_j} = \frac{\mathbf{Q}_{ij}(\mathbf{v}_i - \mathbf{v}_j)}{2\sigma^2} e^{-\frac{(\mathbf{v}_i - \mathbf{v}_j)^T \mathbf{M}_{ij}(\mathbf{v}_i - \mathbf{v}_j)}{4\sigma^2}},$$
(2)

where $\mathbf{Q}_{ij} = \sqrt{\mathbf{M}_{ij}}$ and $\overline{\mathbf{v}}_j$ is the particle j's position in the embedding space. The inter-particle energy defined in Eq. (1) and force defined in Eq. (2) are used to minimize the total inter-particle energy. During the optimization, the particles need to be constrained inside the torso volume. The final adaptive

particles need to be constrained inside the torso volume. The final adaptive tetrahedral mesh can be generated by using the Delaunay triangulation method according to the optimized particle positions. In the 4D NCAT phantom and clinical data set, it takes 40 seconds for the mesh generation (i.e., 10,000 vertices of feature-based adaptive tetrahedral mesh). Note that the mesh generation step only needs to be computed once before DIR optimization.

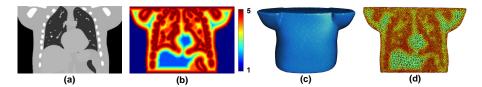


Fig. 1: Demonstration of the feature-based mesh generation on a digital 4D NCAT phantom. (a) The original image at the reference phase; (b) density field based on extracted feature edges; (c) boundary meshes well preserved the body surface; (d) a 2D view of the interior meshes with color-mapping.

As a result, the color-coded tetrahedrons of the generated feature-based mesh in Fig. 1 (c), (d) illustrate that the tetrahedral volumes are well conforming to the desired density in Fig. 1 (b) defined by the features of the given image as well as the body surface. Since most deformations occur around boundaries as well as organs and tissues, edges of contours, it is desirable to place more vertices (or sampling points) at features, while fewer vertices in non-feature regions. In this way, if DVF is specified to each mesh vertex, the organ boundaries and other

important features can be directly represented by the displacements of sampling points or represented by smaller-sized tetrahedrons, rather than interpolating through four vertices of one larger-sized tetrahedron. Thus, the deformation can be transferred from the mesh vertices to each voxel of the volume more accurately and smoothly via interpolation as follows:

$$\mathbf{D} = bary(\mathbf{W}),\tag{3}$$

where \mathbf{W} denotes the DVF specified on mesh vertices, and \mathbf{D} denotes the DVF specified on voxels. bary denotes the barycentric interpolation, which is similar to the trilinear interpolation. Therefore, the proposed FEM restricts the solution space of the image registration problem with much fewer degrees of freedom, while giving sufficient consideration of organ shapes and image features, and ensures the smoothness of the transformation \mathbf{D} by interpolation.

2.2 Mesh-Based DIR

Basic Framework

Suppose there are totally T phases in a 4D image (i.e., CT, MRI, or ultrasound), $\mu = \{\mu^t | t=0,...,T-1\}$ denotes the image intensity of all phases. Once the reference phase 0 is known and a motion model is available, the other phases [1,...,T-1] of the 4D image can be described as:

$$\boldsymbol{\mu}^t = \boldsymbol{\mu}^0(\mathbf{x} + \mathbf{d}^{0 \to t}) = \boldsymbol{\mu}^0(\mathbf{x} + bary(\mathbf{w}^{0 \to t})), \tag{4}$$

where \mathbf{x} denotes the voxels' positions at reference phase. $\mathbf{d}^{0\to t}$ can be considered as a voxel-based motion model from phase 0 to phase t, computed according to the interpolation of the DVF $\mathbf{w}^{0\to t}$ specified by the mesh model in Eq. (3), and there exists a deformation matrix to transform 4D image from phase 0 to any phase $t, t \in [1, ..., T-1]$.

The DVF $\mathbf{w}^{0\to t}$ can be computed by minimizing the energy function E, which includes two terms: the data fidelity between the images of two phases and the regularization used to achieve smoothness constraint of the mesh-based DVF. The total energy function considering all T phases is:

$$E(\mathbf{W}) = \sum_{i=0}^{T-1} \left[||\boldsymbol{\mu}^t - \boldsymbol{\mu}^0(\mathbf{x} + bary(\mathbf{w}^{0 \to t}))||_{l_2}^2 + \beta L(\mathbf{w}^{0 \to t}) \right], \tag{5}$$

where β is a parameter that controls the tradeoff between the data fidelity and the smoothness constraint of the DVF and it is set at 0.003 for all of the experimental studies in the paper. $\mathbf{W} = \{\mathbf{w}^{0 \to t} | t = 0, ..., T-1\}$. $L(\mathbf{w}^{0 \to t})$ is the smoothness constraint term defined as:

$$L(\mathbf{w}^{0\to t}) = \sum_{i=1}^{N_v} \sum_{d=1}^{3} \left[\left(\frac{\sum_{k \in N_i} (\mathbf{w}_k^{0\to t}(d) - \mathbf{w}_i^{0\to t}(d))}{|N_i|} \right)^2 \right], \tag{6}$$

where it is a summation of the square of Graph Laplacian operations on the DVF (including three components: d = 1, 2, 3) over every vertex. N_v is the total number of the mesh vertices. N_i is the set of one-ring neighboring vertices (k) of vertex i. $|N_i|$ is the size of set N_i .

Optimization

(1) Gradient of DIR Energy The gradient of $E(\mathbf{W})$ w.r.t. $\mathbf{w}_i^{0\to t}$ at mesh vertex i in phase t can be considered as:

$$\begin{split} &\frac{\partial E(\mathbf{W})}{\partial \mathbf{w}_{i}^{0 \to t}} = -2 \left[\boldsymbol{\mu}^{t} - \boldsymbol{\mu}^{0} (\mathbf{x} + bary(\mathbf{w}^{0 \to t})) \right] \frac{\partial \boldsymbol{\mu}^{0} (\mathbf{x} + bary(\mathbf{w}_{i}^{0 \to t}))}{\partial \mathbf{w}_{i}^{0 \to t}} \\ &- 2 \sum_{d=1}^{3} \left[\left(\frac{\sum_{k \in N_{i}} (\mathbf{w}_{k}^{0 \to t}(d) - \mathbf{w}_{i}^{0 \to t}(d))}{|N_{i}|^{2}} \right) \right] + 2 \sum_{d=1}^{3} \left[\left(\frac{\sum_{k \in N_{i}} (\mathbf{w}_{i}^{0 \to t}(d) - \mathbf{w}_{k}^{0 \to t}(d))}{|N_{k}|^{2}} \right) \right]. \end{split}$$

It is noted that the regularization terms are symmetrically defined on every mesh vertex and its neighbors, therefore, there are two terms in the gradient of DVF at mesh vertex i. Since the energy function Eq. (5) is a quadratic form of **W** and its gradients as shown in Eq. (7), it is obvious that the total energy $E(\mathbf{W})$ is C^2 . This is a great property for the optimization: the C^2 continuity can ensure to obtain an optimal result, instead of trapping into some local minima.

(2) L-BFGS Method Due to the smoothness (C^2 continuity) of the energy function with the explicit gradient formula, it is therefore possible to minimize the mesh-based DIR energy function using Newton-like optimization methods and expect fast convergence. Specifically, we use the L-BFGS algorithm [9], a quasi-Newton method, to optimize the DVF, which can quickly find the minimum of the energy for our DVF estimation. It converges in fewer optimization steps than the demons DIR methods [1,2,3] with iterative gradient for DVF computation. For each iteration of L-BFGS optimization, we update the energy $E(\mathbf{W})$ by summing the fidelity and regularization terms over all phases, and update its gradients $\frac{\partial E(\mathbf{W})}{\partial \mathbf{w}_i^{0 \to t}}$ on each mesh vertex. The L-BFGS method computes the approximated inverse Hessian matrix by accumulating the gradients over a small fixed number of preceding iterations. Both the memory complexity and the computational cost of each iteration of L-BFGS are O(n), where n is the number of variables, i.e., the number of mesh vertices. The energy optimization by L-BFGS method can converge very quickly in 100 iterations for all our experimental images.

GPU-Based Parallel Acceleration

The entire process of this 4D image DIR method is implemented on GPU using the CUDA programming environment. The GPU card used in our experiments is an NVIDIA GeForce GTX Titan Z with 12GB GDDR5 video memory. It has 5760 CUDA cores. Utilizing such a GPU card with tremendous parallel computing ability can significantly increase the computational efficiency. There are four GPU-based computational sections during the DIR, i.e., regularization computation, deformed volume image computation, data fidelity computation, and gradient of total energy. It is straightforward to accomplish all the computations in parallelism, since these four sections can be either parallelized based on each mesh vertex or each voxel at different GPU threads without conflicts.

3 Results

3.1 4D NCAT Digital Phantom

In this study, ten breathing phases of the 4D NCAT phantom were generated. The maximum diaphragm motion was 20 mm during the respiration and a spherical 3D tumor with diameter of 10 mm was also simulated. The dimensions of the phantom were $256 \times 256 \times 150$ with voxel size of $2 \times 2 \times 2$ mm^3 . The adaptive tetrahedral mesh on the torso was created with about 10,000 vertices from the reference phase 0 of 4D CT as shown in Fig. 1.

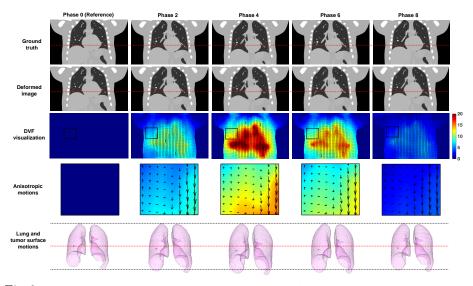


Fig. 2: The deformed images and motions of the 4D NCAT phantom at different phases.

Fig. 2 shows deformed images and motions of the 4D NCAT phantom at phase 0 (end-expiration), phase 2, phase 4 (end-inspiration), phase 6, and phase 8 from coronal views by using the proposed mesh-based DIR method. The image details are well preserved for bony, lung, tumor, and other fine structures, and meanwhile, the motions of the lung and tumor are well captured. The red dot lines go through the diaphragm of coronal view images and tumor center of surface motion at phase 0, respectively, to further illustrate the performance of the proposed DIR method. From DVF visualization (both the directions and magnitudes are computed and compared based on phase 0), the feature-based adaptive mesh can well capture the complicated anisotropic motions as shown in the zoom-in part of Fig. 2 where the tissues and tumor inside the lung are moving downward, while the thoracic cage is moving upward from end-expiration to end-inspiration.

Tab. 1 reports the quantitative evaluations on all deformed images by using conventional normalized cross correlation (NCC) and normalized root mean square error (NRMSE) measurements. As for the motions of tumor center, it is

 Phase
 2
 4
 6
 8

 NCC
 0.9965
 0.9859
 0.9945
 0.9992

 NRMSE
 0.0708
 0.1426
 0.0893
 0.0345

 Tumor center (mm)
 0.6850
 1.1450
 0.7750
 0.5600

Lung surface (mm)

1.5028 | 2.6061 | 2.0476

1.3513

Table 1: Evaluations of deformed image and motion accuracy.

measured by using the 3D distance error between the center of the tumor computed based on the DVFs and tumor center generated by manual segmentation. As for the motions of the lung surfaces, we use Hausdorff distance to measure the approximation accuracy of the deformed surfaces based on DVFs to the isosurface generated by manual segmentation. All of the quantitative results show that the proposed DIR method has very small errors (at most around one voxel size at largest deformed phase), so that it can be used as an automated and effective tracking method to transfer tumor segmentations or organ contours/surfaces at different phases, without tedious manual segmentation. The overall computational time of a 4D $256 \times 256 \times 150$ image with 10 phases is 51.60~s~(<1~m). However, the computational time of the voxel-based DIR method on CPU is much slower, i.e., about 9652~s~(>160~m), such as demons [1,2,3]. Therefore, the proposed method has dramatically improved the running speed and makes it possible to reach our ultimate target to develop a less-than-1-minute 4D DIR-based visualization and tracking system for its clinical applications.

3.2 Clinical Data Set

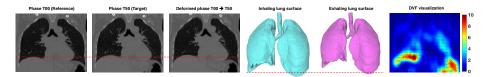


Fig. 3: The deformed images and motions of a 4D clinical CT.

Finally, a clinical evaluation study was performed on thoracic 4D CT images obtained from a clinical esophageal cancer case [10], i.e., 4DCT1 with dimensions of $256 \times 256 \times 94$ and voxel size of $0.97 \times 0.97 \times 2.5~mm^3$, which is publicly available on www.dir-lab.com. Fig. 3 shows deformed images and motions of the 4D clinical CT at phase T00 (end-inspiration) and phase T50 (end-expiration) from coronal views by using the proposed mesh-based DIR method. The inhaling lung surface is generated by computing the isosurface from the segmented lung masks manually. The exhaling lung surface is automatically computed by deforming the inhaling lung surface according to the DVF obtained in the proposed DIR method. As for the quantitative evaluations, NCC and NRMSE between the deformed image and the ground truth (target) image at phase T50 are 0.9950 and 0.0815.

The accuracy evaluation of our proposed method was also based on landmark features identified in the reference and target images by thoracic imaging experts. The number of landmark point pairs is 1280. Registration error is determined

by applying the DVFs to the landmark coordinates on the reference image, then comparing the result to the corresponding landmark coordinates on the target image. The mean and standard deviations of 3D distance error (mm) for the proposed DIR on phase T50 are 1.0641 and 1.0578, which are smaller than the demons methods as reported in [4].

4 Conclusion

In this work, we have developed a feature-based adaptive mesh technique for 4D DIR with considering complicated motions of different organs and image features, and a GPU-based parallel algorithm to further improve the efficiency to reach an aim of being real-time. It is feasible and effective to be used in tumor identification and tracking, registration and tracking of deformable organs, in real time. We use the 4D CT (a phantom and a clinical data set) as examples to demonstrate our algorithm. However, this framework can be extended to medical imaging data of different modalities, such as 4D-MRI, 4D-Ultrasound, 4D-PET, 4D-SPECT, etc.

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