$$\frac{\partial \pi_i}{\partial \beta_1} = \beta_1 \cdot \pi_i \cdot (1 - \pi_i)$$