

$$Q1) \quad P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$P(\text{Passing}) = 0.9, \quad P(\text{Quickly} | \text{Passing}) = 0.6,$$

$$P(\text{Quickly} | \text{Not passing}) = 0.3$$

$$\therefore P(\text{Not passing}) = 1 - 0.9 \\ = 0.1$$

$$P(\text{Passing} | \text{Quickly}) = \frac{P(\text{Quickly} | \text{Passing}) P(\text{Passing})}{P(\text{Quickly})}$$

$$= \frac{0.6 \cdot 0.9}{P(\text{Quickly})}$$

$$P(\text{Quickly}) = P(\text{Quickly} | \text{Passing}) P(\text{Passing}) + P(\text{Quickly} | \text{Not Passing}) P(\text{Not passing}) \\ = 0.6 \cdot 0.9 + 0.3 \cdot 0.1 \\ = 0.57$$

$$P(\text{Passing} | \text{Quickly}) = \frac{0.6 \cdot 0.9}{0.57} = 0.9473$$