Problem 5

October 23, 2019

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[1]: # For the column player
    from gurobipy import *
    # Create new model
    m = Model("problem5-1")
    # Create variables (lowerbound of 0 by default)
    y1 = m.addVar(vtype=GRB.CONTINUOUS, name="y1", lb=0)
    y2 = m.addVar(vtype=GRB.CONTINUOUS, name="y2", 1b=0)
    y3 = m.addVar(vtype=GRB.CONTINUOUS, name="y3", 1b=0)
    y4 = m.addVar(vtype=GRB.CONTINUOUS, name="y4", 1b=0)
    v = m.addVar(vtype=GRB.CONTINUOUS, name="v", 1b=0)
    # Update the model
    m.update()
    # Set Objective
    m.setObjective(v, GRB.MAXIMIZE)
    #Add constraints
    m.addConstr(2*y1-y2+3*y3-2*y4 >= v)
    m.addConstr(y1+4*y2-3*y3 >= v)
    m.addConstr(-2*y2-y3+3*y4 >= v)
    m.addConstr(y1+y2+y3+y4 == 1)
    # Optimize (model is updated when we optimize)
    m.optimize()
    #print model status (2 is optimal)
    #https://www.qurobi.com/documentation/6.5/refman/optimization_status_codes.html
    print ('Model status:', m.status)
    #print decision variables
    for v in m.getVars():
        print (v.varName, v.x)
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#print objective function value
    print ('Obj:', m.objVal)
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   Optimize a model with 4 rows, 5 columns and 17 nonzeros
   Coefficient statistics:
                      [1e+00, 4e+00]
     Matrix range
     Objective range [1e+00, 1e+00]
                       [0e+00, 0e+00]
     Bounds range
     RHS range
                       [1e+00, 1e+00]
   Presolve removed 1 rows and 1 columns
   Presolve time: 0.03s
   Presolved: 3 rows, 4 columns, 12 nonzeros
   Iteration
                Objective
                                Primal Inf.
                                                Dual Inf.
                                                               Time
          0
               3.0000000e+00
                                1.375000e+00
                                               0.000000e+00
                                                                 0s
          2
               7.9487179e-01
                               0.000000e+00
                                               0.000000e+00
                                                                 0s
   Solved in 2 iterations and 0.04 seconds
   Optimal objective 7.948717949e-01
   Model status: 2
   y1 0.6923076923076922
   y2 0.02564102564102566
   y3 0.0
   y4 0.28205128205128205
   v 0.7948717948717948
   Obj: 0.7948717948717948
[2]: # For the column player
    from gurobipy import *
    # Create new model
    m = Model("problem5-2")
    # Create variables (lowerbound of 0 by default)
    x1 = m.addVar(vtype=GRB.CONTINUOUS, name="x1", lb=0)
    x2 = m.addVar(vtype=GRB.CONTINUOUS, name="x2", 1b=0)
    x3 = m.addVar(vtype=GRB.CONTINUOUS, name="x3", 1b=0)
    u = m.addVar(vtype=GRB.CONTINUOUS, name="u")
    # Update the model
    m.update()
    # Set Objective
    m.setObjective(u, GRB.MINIMIZE)
    #Add constraints
```

```
m.addConstr(2*x1+x2 \le u)
m.addConstr(-x1+4*x2-2*x3 \le u)
m.addConstr(3*x1-3*x2-x3 \le u)
m.addConstr(-2*x1+3*x3 \le u)
m.addConstr(x1+x2+x3 == 1)
# Optimize (model is updated when we optimize)
m.optimize()
#print model status (2 is optimal)
\verb|#https://www.gurobi.com/documentation/6.5/refman/optimization_status\_codes.html|
print ('Model status:', m.status)
#print decision variables
for v in m.getVars():
    print (v.varName, v.x)
#print objective function value
print ('Obj:', m.objVal)
Optimize a model with 5 rows, 4 columns and 17 nonzeros
Coefficient statistics:
                   [1e+00, 4e+00]
 Matrix range
  Objective range [1e+00, 1e+00]
 Bounds range
                   [0e+00, 0e+00]
                   [1e+00, 1e+00]
 RHS range
Presolve time: 0.01s
Presolved: 5 rows, 4 columns, 17 nonzeros
Iteration
             Objective
                             Primal Inf.
                                             Dual Inf.
                                                            Time
            0.0000000e+00
                            1.500000e+00
                                            0.000000e+00
                                                              0s
            7.9487179e-01
                            0.000000e+00
                                            0.000000e+00
                                                              0s
Solved in 3 iterations and 0.02 seconds
Optimal objective 7.948717949e-01
Model status: 2
x1 0.17948717948717952
x2 0.4358974358974359
x3 0.3846153846153846
u 0.7948717948717949
Obj: 0.7948717948717949
```