

# CS6533/CS4533 Lecture 13

## Slides/Notes

### Texture Mapping Variations (Environment, Bump, and Shadow Mapping); Ray Tracing & Radiosity (Notes, Ch 15, Notes, Ch 20)

By Prof. Yi-Jen Chiang  
CSE Dept., Tandon School of Engineering  
New York University

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#### Mapping Techniques

1. Texture Mapping: Use an image as a texture to be "glued" (mapped) onto the surface of simple geometry to create sophisticated images.

2 main ways to produce texture images:

- ① computer programs (eg. checkerboard)
- ② digital cameras (image files)

2. Environment Mapping: For a shiny object, the environment is reflected on its surface.  
⇒ Render the environment into an image, treat it as a texture, then map the texture onto the obj. surface.

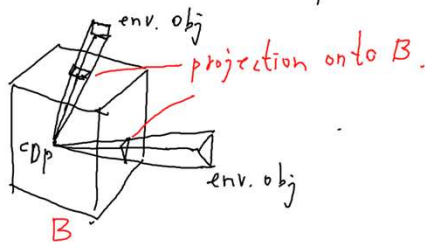
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eg. a shiny ball in the middle of a room.

2-step Method: Let  $A$  be the shiny obj whose surface we want to perform environment mapping onto.

Step 1: place the cop at the center of obj  $A$ , remove  $A$ .

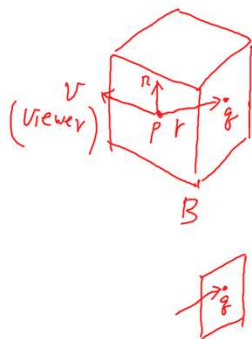
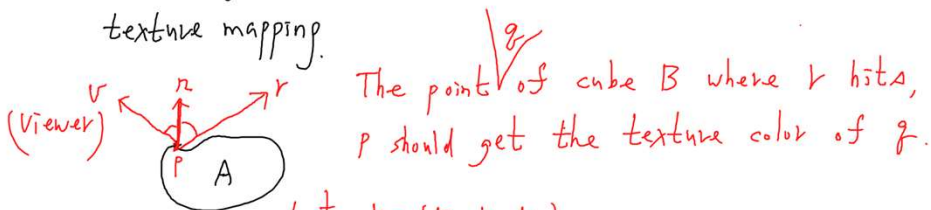
Project the environmental objs onto an intermediate surface  $B$ .  
eg. Typically we use "cube map"



\* Put the viewer (cop) at the center of  $A$ . remove  $A$ .  
Render the environment onto the 6 faces of cube  $B$  using each face as the view plane. for each face.

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Step 2: place obj  $A$  back. transfer the image on  $B$  onto  $A$  using texture mapping.



Let  $r = (r_x, r_y, r_z)$

① Decide which face of cube  $B$  the ray  $r$  hits.  
[we will then use the texture on that face.]

To decide, look at the largest among  $|r_x|, |r_y|, |r_z|$ .  
say  $|r_x|$ . If  $r_x > 0 \Rightarrow +x$  face  
 $r_x < 0 \Rightarrow -x$  face. } suppose it's  $+x$  face.

② Decide the texture coord. of  $q$  on the  $+x$  face  
by  $\frac{r}{|r_x|} = (+1, \frac{r_y}{|r_x|}, \frac{r_z}{|r_x|}) : (\frac{r_y}{|r_x|}, \frac{r_z}{|r_x|}) \rightarrow (s, t)$

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$\left( \frac{r_y}{|r_x|}, \frac{r_z}{|r_x|} \right) \in [-1, 1] \times [-1, 1]$   
 $(s, t) \in [0, 1] \times [0, 1]$

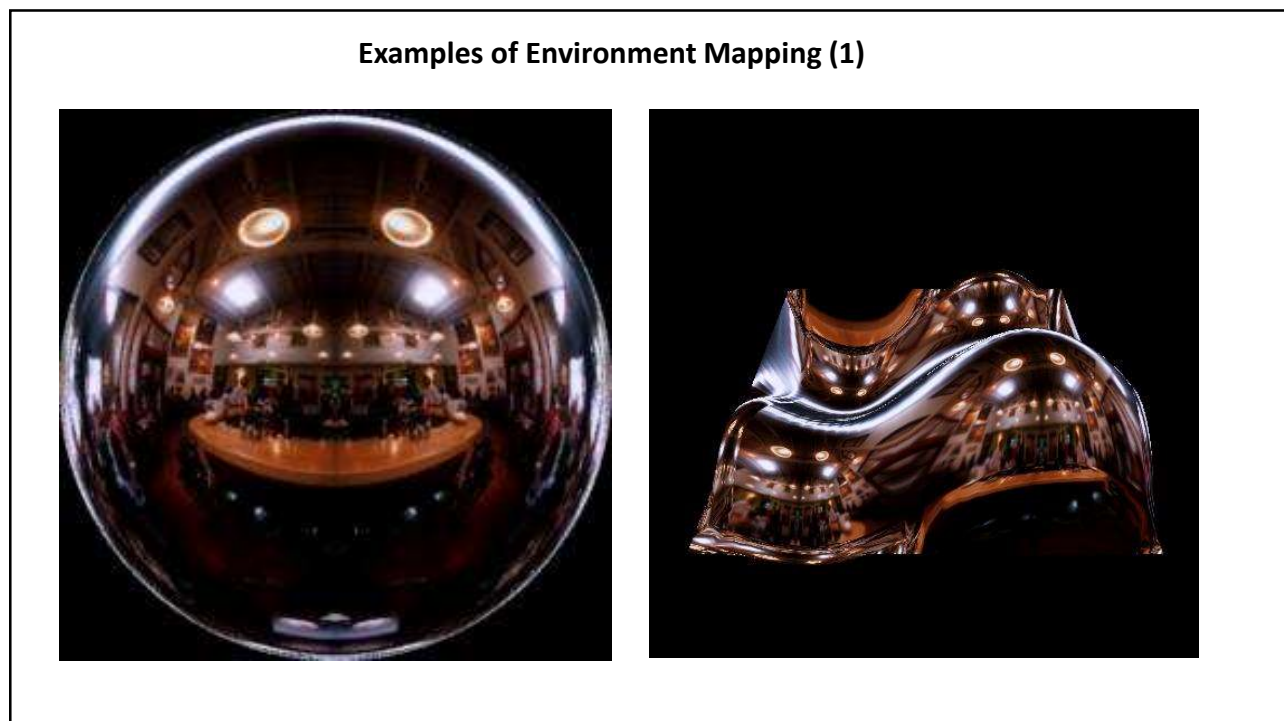
$r = (1, 0, 0)$  → center of +x face.  
 texture coord. is  $\left( \frac{1}{2}, \frac{1}{2} \right)$

$\left( \frac{r_y}{|r_x|}, \frac{r_z}{|r_x|} \right) \rightarrow (s, t) : \text{origin } (0, 0) \rightarrow \left( \frac{1}{2}, \frac{1}{2} \right)$   
 $\frac{[-1, 1]}{2} \rightarrow \frac{[0, 1]}{1}$  in both dimensions scale by factor of  $\frac{1}{2}$ .  
 $(y \rightarrow s, z \rightarrow t)$

$(s, t) = \frac{1}{2} \left( \frac{r_y}{|r_x|}, \frac{r_z}{|r_x|} \right) + \left( \frac{1}{2}, \frac{1}{2} \right)$

verify:  $\left( \frac{r_y}{|r_x|}, \frac{r_z}{|r_x|} \right) \rightarrow \left( \frac{1}{2}, \frac{1}{2} \right)$  is  $(0, 0) \rightarrow \left( \frac{1}{2}, \frac{1}{2} \right)$   
 $(0, 0)$   
 $\frac{1}{2}(-1, -1) + \left( \frac{1}{2}, \frac{1}{2} \right) = (0, 0)$  is  $(-1, -1) \rightarrow (0, 0)$   
 $\frac{1}{2}(1, 1) + \left( \frac{1}{2}, \frac{1}{2} \right) = (1, 1)$  is  $(1, 1) \rightarrow (1, 1)$   
 ok.

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### Examples of Environment Mapping (2)



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3. Bump Mapping: Goal: create a bumpy surface (eg. orange)

Naive attempt: Take a picture of the real bumpy obj (eg. orange) then use texture mapping to map the picture onto the obj surface.

Issue: When we move the light or rotate the obj. we will notice that it is NOT realistic looking. (eg. 'shadows' corresponding to the bumps are incorrect)

(eg. sphere)  
(smooth)

Bump Mapping: We can vary the look of the shape of the surface by perturbing the normal vectors then using the perturbed normal vectors in shading computation.

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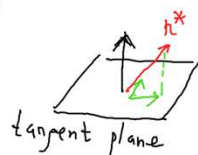
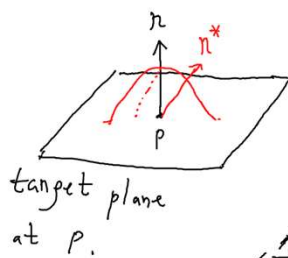
Note: \* The actual geometry is unchanged (still a flat polygon)  
 \* Bump mapping does NOT change the {boundary} of the obj  
 silhouette

$$p^* = p + d(p) n \quad p: \text{original surface pt.}$$

$p^*$ : new surface pt displaced from  $p$ .

$d(p)$ : displacement amount at  $p$ .

$n^*$ : normal vector at  $p^*$



[ There is a formal math derivation for  $n^*$ .  
 We omit it here, and only put the conclusion below:  
 $\Rightarrow n^*$  is  $n$  perturbed along a direction on the tangent plane,  
 which can be decomposed as  $x$  &  $y$  components on the tangent plane.

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$\Rightarrow$  Take  $t$ : tangent vector at  $p$  (Normalized:  $|n| = |t| = 1$ )  
 $b = n \times t$ : binormal vector at  $p$  (Normalized:  $|b| = 1$ )  
 $n \equiv z$ ,  $t \equiv x$ ,  $b \equiv y$

(\* Tangent frame:  
 • origin is at  $p$   
 •  $t, b, n$  are 3 basis vectors)

This is called the tangent frame

(also called surface local frame.) where  $t, b, n$  are in the eye frame.

Create a  $3 \times 3$  matrix  $M = \begin{bmatrix} t \\ b \\ n \end{bmatrix}$  We can use  $M$  to transform vectors from eye frame to tangent frame.

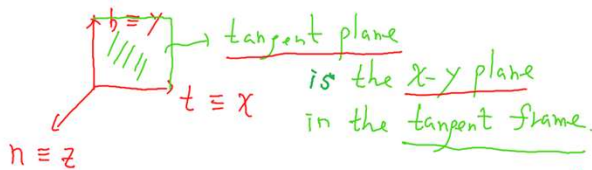
[ Verification:  $M \cdot t = \begin{bmatrix} t \\ b \\ n \end{bmatrix} \begin{bmatrix} t \\ b \\ n \end{bmatrix} = \begin{bmatrix} t \cdot t \\ b \cdot t \\ n \cdot t \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \equiv x$   $M \cdot b = \begin{bmatrix} t \\ b \\ n \end{bmatrix} \begin{bmatrix} b \\ b \\ n \end{bmatrix} = \begin{bmatrix} t \cdot b \\ b \cdot b \\ n \cdot b \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \equiv y$   
 Similarly,  $M \cdot n = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \equiv z$ . ]

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Main Idea: Use matrix  $M$  to transform everything from eye frame to tangent frame then perform shading computation in tangent frame.

\* In the tangent frame: original normal  $n = z = (0, 0, 1)$   
 perturbed normal  $n^*$  is  $n$  perturbed along  $x$  direction &  $y$  : in the tangent frame



\* original normal  $n = (0, 0, 1)$   
 perturbed normal  $n^* = (x, y, 1)$   
 with  $\begin{cases} x = f(s) \\ y = f(t) \end{cases}$   
 i.e.  $x, y$  are results of a function  $f$  on the texture coord.  $(s, t)$  of the current fragment

$n^* \leftarrow \text{normalize}(n^*)$   
 Use  $n^*$  for shading computation in tangent frame.

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**Gouraud (Per-Vertex) Shading**



**Phong (Per-Fragment) Shading**



**Bump Mapping (1)**



**Bump Mapping (2)**

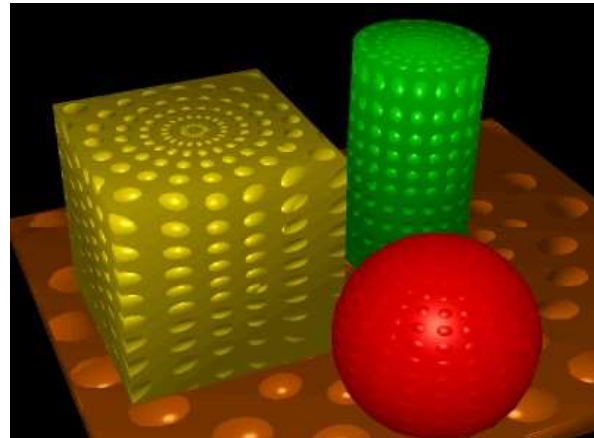


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Bump Mapping (3)

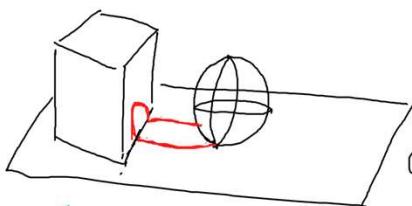


Bump Mapping (4)



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#### 4. Shadow Mapping :



(shadow map created in ① is stored & read as a texture)

Main Issue: self shadowing

sol: Add some tolerance  $\epsilon$  (small and  $> 0$ ):  
treat  $|z_f - M_p| \leq \epsilon$  as (b)  
(test case (b) first, and "else" is case (a))

① Put the viewer at the light position  $L$ , Render the scene to the z-buffer to create a "shadow map": The shadow map contains the z-values of all points that can be seen from  $L$ .

② Render the scene from the viewer. For each fragment  $f$ , compute its "z-value" when viewed from  $L$ . (when rendered from  $L$ ,  $f$  is at pixel  $p$ , with z-value  $z_f$ )  
Look at the shadow map. (in shadow map, pixel  $p$  has value  $M_p$ )

(a) if  $z_f > M_p$  then  $f$  can NOT be seen from  $L$ .  
 $\Rightarrow$  No contribution of light  $L$  to fragment  $f$

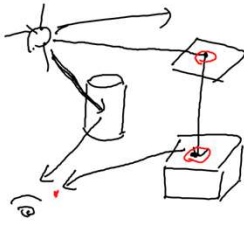
(b) else ( $z_f \leq M_p$ ) then  $f$  can be seen from  $L$ .  
 $\Rightarrow$  Add contribution of  $L$  to  $f$

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# Global Shading 1. Ray Tracing

## 2. Radiosity

1. Ray Tracing: Simulate the interactions of rays with objects where the rays are bouncing among objects.



Issues: ① Infinite # rays to trace: too slow!!

Sol: We only care about the rays coming into the eye  $\Rightarrow$  trace rays backwards!!



Cast rays from cop thru each pixel center into the scene. then trace the rays there

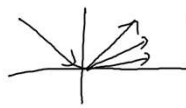
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② How do we trace the bounced rays?

(I) (i) For diffuse surface, reflected rays are along all directions.

$\Rightarrow$  can't trace so many rays!

(ii) For highly specular surface, reflected rays are along a narrow range of angles.



: OK to trace them.

OK.

Typically we assume to have a single reflected ray to trace

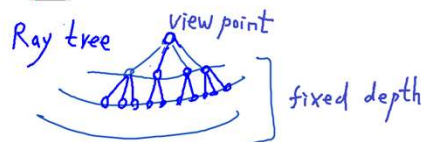
$\Rightarrow$  Ray tracing works mainly for highly specular surfaces

(II) We only trace rays

with a pre-fixed # of bounces

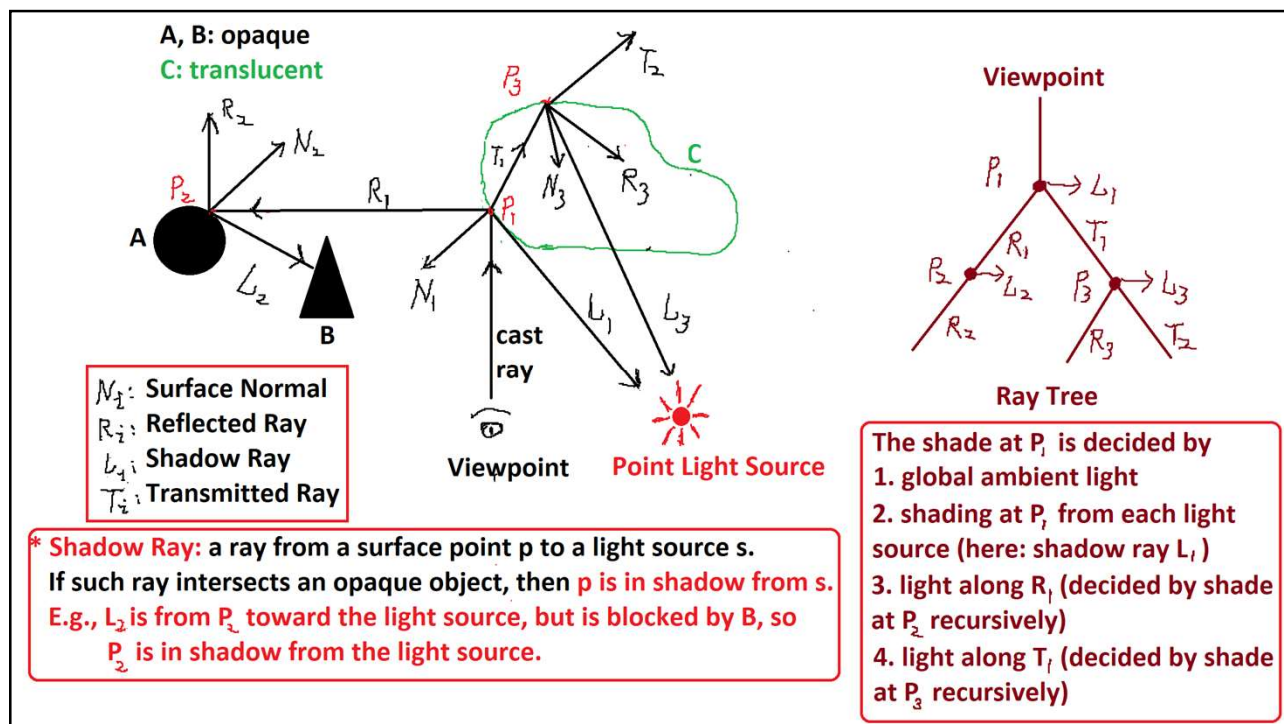
Fixed depth of the ray tree.

NOT for diffuse surfaces.



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\* Every time the viewer moves or changes the viewing direction, we need to re-do the ray-tracing computation (expensive, NOT suitable for interactive applications).

2. Radiosity: Works for diffuse surfaces

In closed environment, compute how the light energy is interacting between each pair of surface patches (small flat polygons)

Assume: All surfaces are perfectly diffuse: reflected rays are along all directions

⇒ Computation is independent of the viewer position & viewing direction.

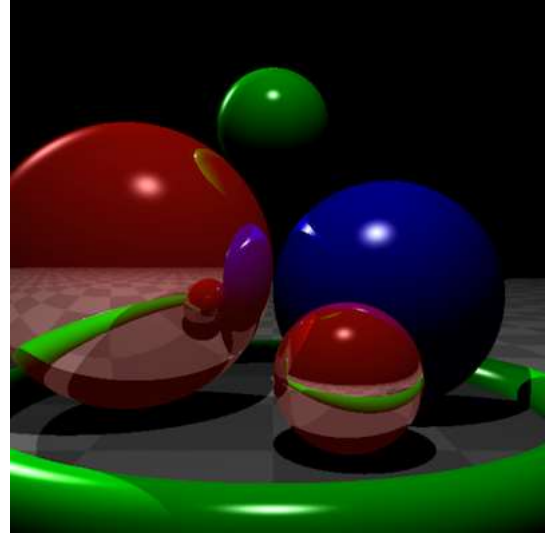
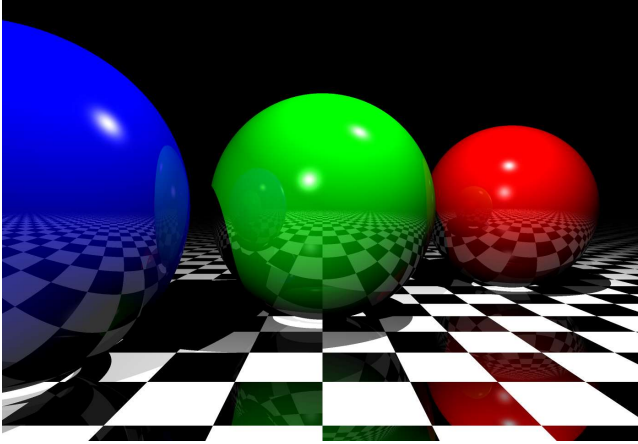
\* Can be done in preprocessing (pre-computation)

\* Suitable for interactive applications at run-time.

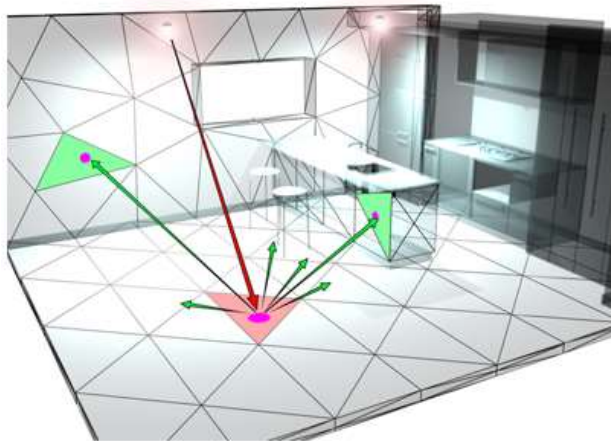
\* Radiosity and ray tracing are complementary to each other.

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## Example Results of Ray Tracing

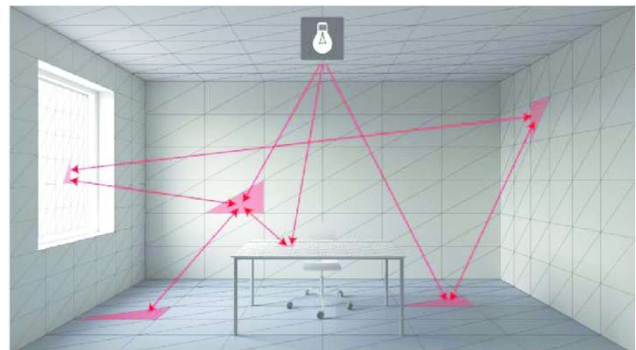


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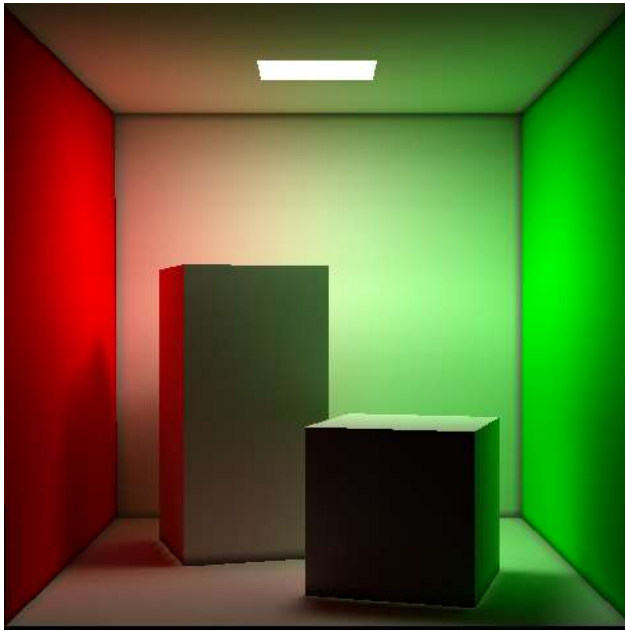


**Radiosity: Concepts of the Method**

**Radiosity Computation:** For each pair of patches, compute the light energy interactions between them



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**Radiosity Result:  
The ``Color Bleeding'' Effect**