



Promoting Financial Products to Bank Customers From a Prescriptive Analytics Perspective




Machine Learning Under a Optimization Lens Final Project

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PROBLEM STATEMENT



Customer Interests

-  Savings account
-  Mortgage account
-  Pension account

Marketing Channel

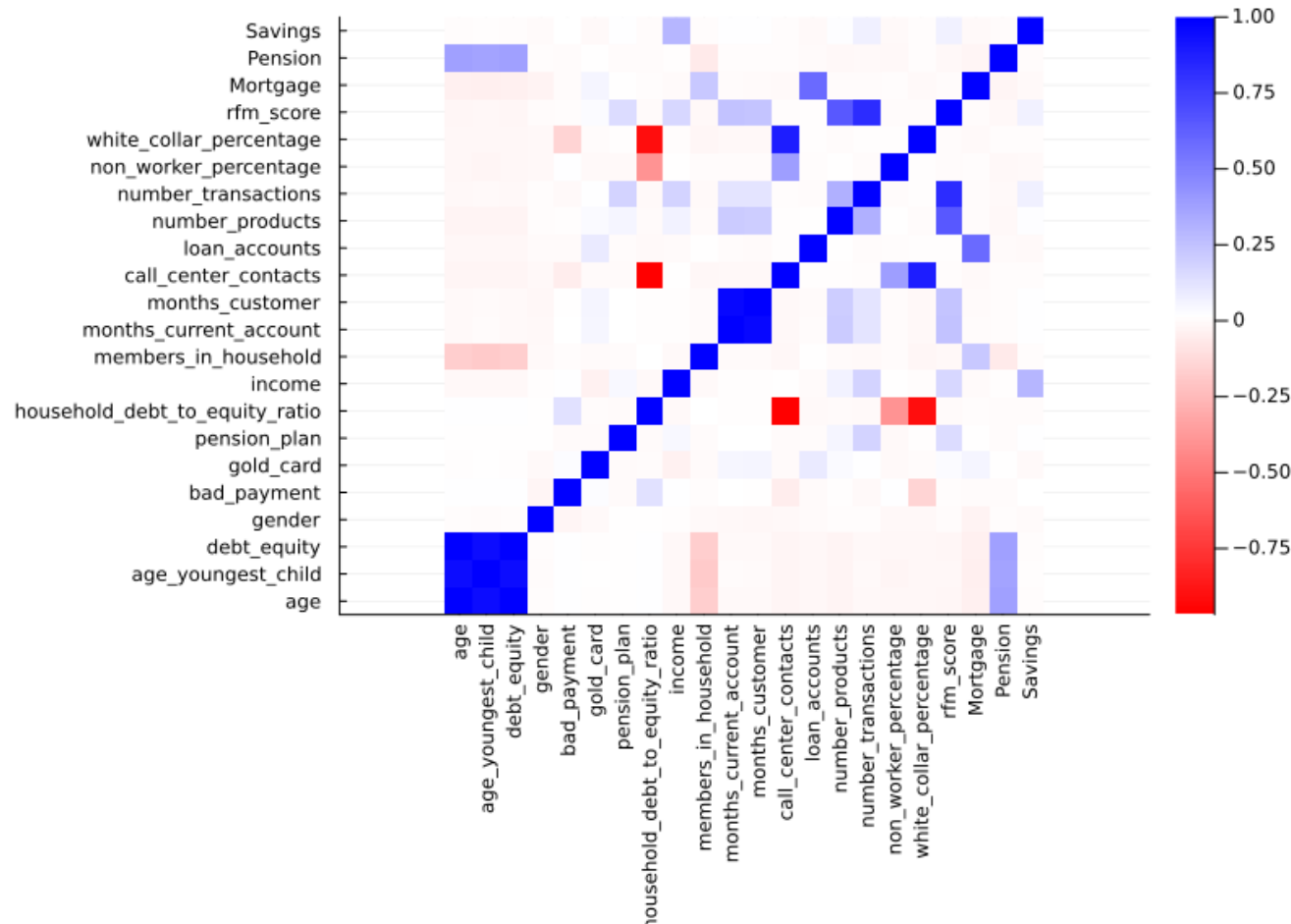
-  Gift
-  Newsletter
-  Seminar

TO BE DECIDED



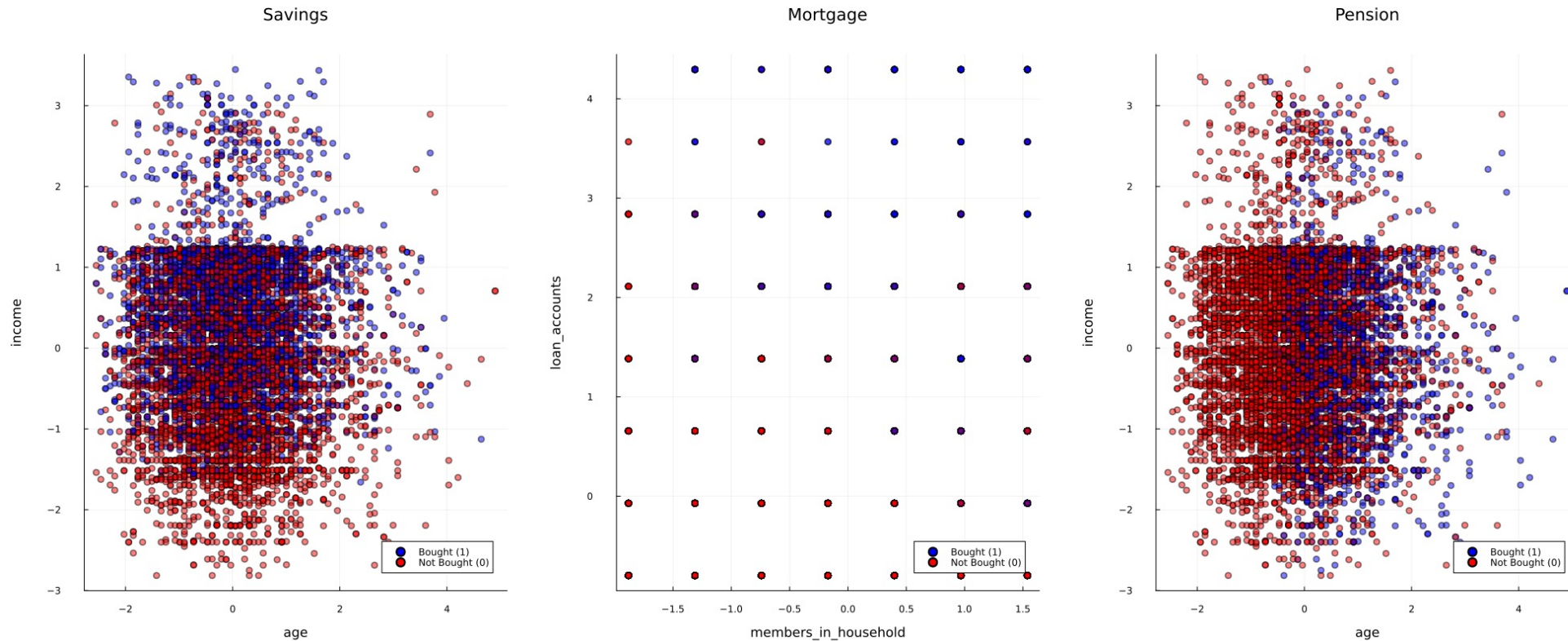
- ❓ Contact which customers?
- ❓ Promote which **product**?
- ❓ Through which **channel**?

EDA & FEATURE ENGINEERING



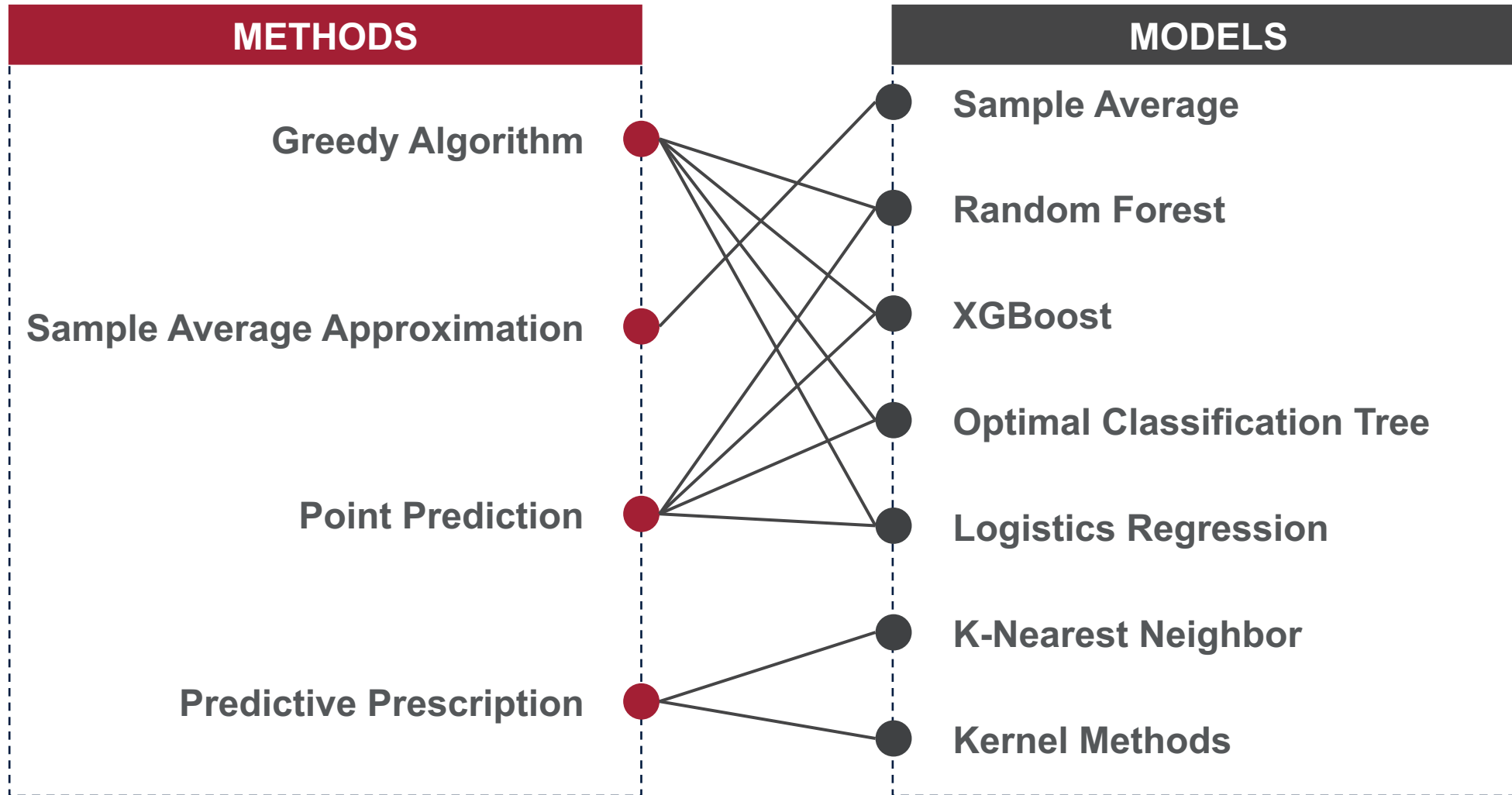
- Moderate correlation with target variables overall
- **Savings account:**
 - Income (0.2987)
- **Pension account:**
 - Age (0.3814)
 - Age of Youngest Child (0.3814)
 - Debt-to-Equity Ratio (0.3814)
 - All correlated with each other
- **Mortgage account:**
 - # Loan accounts (0.5916)
 - # Household members (0.2278)

EDA & FEATURE ENGINEERING



Selected Features: **Age**, **Income**, **Number of members in household**, **Number of loan accounts**

METHODOLOGY & PREDICTION MODELS



GREEDY METHOD | SERVE AS BASELINE



Greedy Algorithm (simplified pseudo code)

for customers from 1 to I:

for products from 1 to J:

for channels from 1 to K:

if (predicted) demand is not satisfied:

make an assignment!

OPTIMIZATION METHOD | E.G. PRESCRIPTIVE



Minimize minus expected profit



$$\min \sum_{i'=1}^{I_0} \sum_{i=1}^{I_1} \sum_{j=1}^J \sum_{k=1}^K w_{I_0}^{i'}(x_i) \cdot (c_k - p_j \cdot s_k) \cdot y_{i'j} \cdot z_{ijk}$$

Budget Constraint



$$\text{s.t.} \quad \sum_{i=1}^I \sum_{j=1}^J \sum_{k=1}^K c_k \cdot z_{ijk} \leq B$$

Minimum promotion per channel constraint



$$\sum_{i=1}^I \sum_{j=1}^J z_{ijk} \geq 0.1 \cdot I, \quad \forall k$$

At most one channel per customer



$$\sum_{k=1}^K z_{ijk} \leq 1, \quad \forall i, j$$

At most one product per customer



$$\sum_{j=1}^J z_{ijk} \leq 1, \quad \forall i, k$$

WEIGHTING MODEL | E.G. KERNEL METHODS



- To Estimate: $m(x) = \mathbb{E}[Y|X = x]$

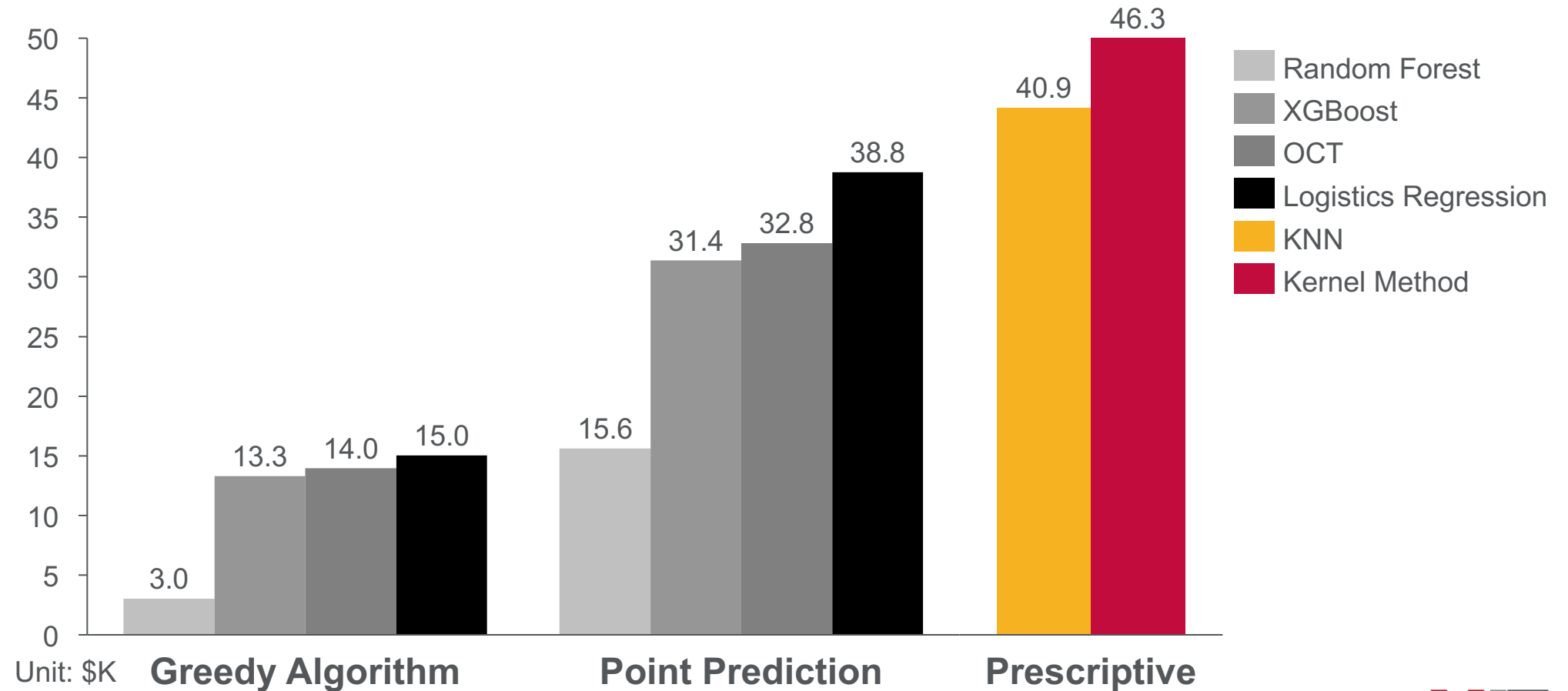
➔
$$\hat{m}_{I_0}(x) = \frac{\sum_{i'=1}^{I_0} y^{i'} K((x^{i'} - x_i)/h_{I_0})}{\sum_{i'=1}^{I_0} K((x^{i'} - x_i)/h_{I_0})}$$

- Kernel $K : \mathbb{R}^d \rightarrow \mathbb{R}$
- Bandwidth $h_{I_0} > 0$
- Naive Kernel $K(x) = \mathbb{I}[\|x\| \leq 1]$

RESULT | BEST MODEL: PREDICTIVE PRESCRIPTION POWERED BY KERNEL METHODS



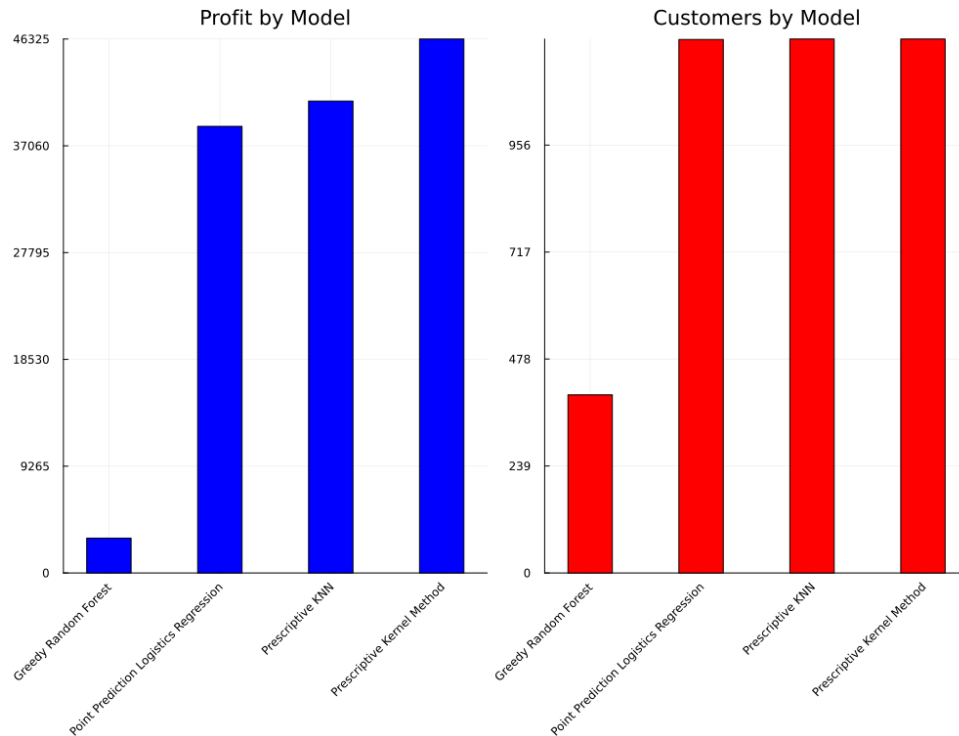
Profit generated by each method & model



RESULT | METRIC ANALYSIS

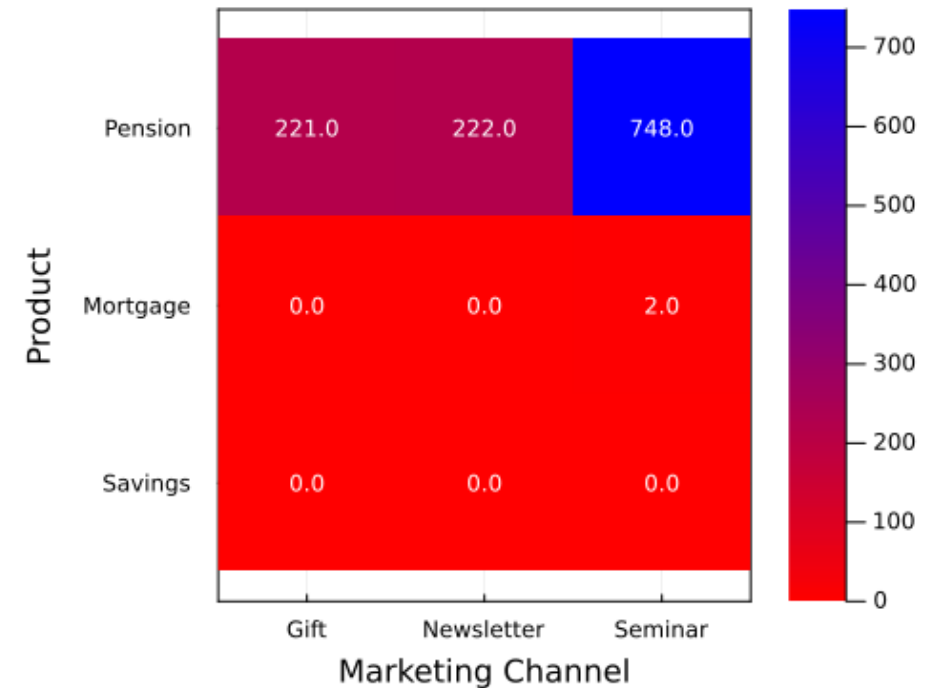


Comparison of Profitability and Offering Ability



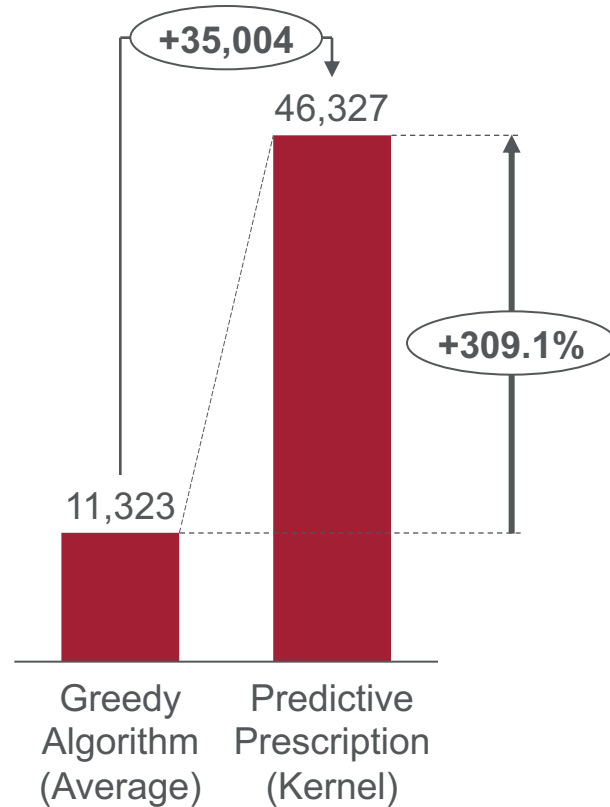
➤ Better models serve more customers

Product Offering Channels (Prescriptive Kernel Method)

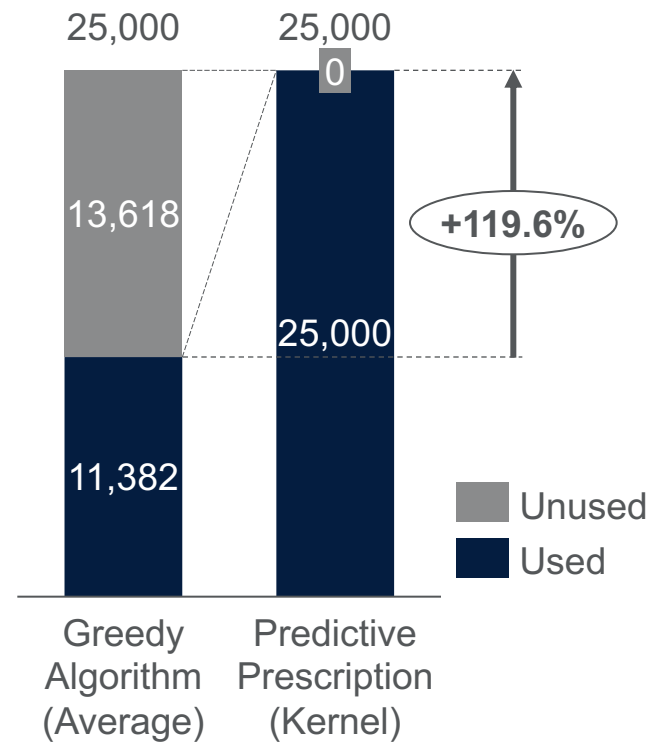


➤ Best model prioritizes profitable products/channels

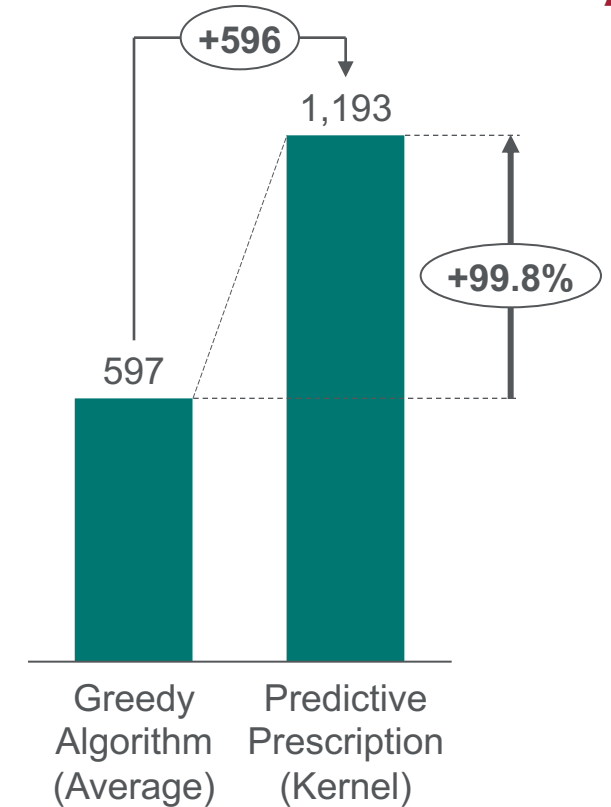
BUSINESS IMPACT | SIGNIFICANT IMPROVEMENT



\$ Profit Generated
X 3



\$ Budget Utilized
X 2



Customers Served
X 2

THANK YOU!



REFERENCES



- ❑ [1] Bertsimas, Dimitris, and Jack Dunn. "Optimal classification trees." *Machine Learning* 106 (2017): 1039-1082.
- ❑ [2] Bertsimas, Dimitris, and Nathan Kallus. "From predictive to prescriptive analytics." *Management Science* 66.3 (2020): 1025-1044.
- ❑ [3] Bertsimas, Dimitris, and Nihal Koduri. "Data-driven optimization: A reproducing kernel Hilbert space approach." *Operations Research* 70.1 (2022): 454-471.
- ❑ [4] Bertsimas, Dimitris, and Kimberly Villalobos Carballo. "Multistage Stochastic Optimization via Kernels." *arXiv preprint arXiv:2303.06515* (2023).

APPENDIX 1 | OBJECTIVE FUNCTIONS



- Sample Average Approximation

$$\hat{z}^{SAA} \in \arg \min_{z \in Z} \frac{1}{I_0} \sum_{i=1}^{I_0} \sum_{j=1}^J \sum_{k=1}^K (c_k - p_j \cdot s_k) \cdot y_{ij} \cdot z_{jk}$$

- Point-Prediction

$$\hat{z}^{point-pred} \in \arg \min_{z \in Z} \sum_{i=1}^{I_1} \sum_{j=1}^J \sum_{k=1}^K (c_k - p_j \cdot s_k) \cdot \hat{y}_{ij} \cdot z_{ijk}$$

- Predictive Prescription

$$\hat{z}_{I_0}(x) \in \arg \min_{z \in Z} \sum_{i'=1}^{I_0} \sum_{i=1}^{I_1} \sum_{j=1}^J \sum_{k=1}^K w_{I_0}^{i'}(x_i) \cdot (c_k - p_j \cdot s_k) \cdot y_{i'j} \cdot z_{ijk}$$

APPENDIX 2 | DATA STRUCTURE



Table 1: Dataset Structure and Explanation of Features

| Column Name | Explanation |
|---------------------------------------|---|
| <i>customer_id</i> | id of the customer |
| <i>age</i> | age of customer |
| <i>age_youngest_child</i> | age of the customer's youngest child |
| <i>debt_equity</i> | debt to equity ratio of customer ($\times 100$) |
| <i>gender</i> | binary variable, male-0 ,female-1 |
| <i>bad_payment</i> | binary variable, whether customer has bad payment history |
| <i>gold_card</i> | binary variable, whether customer is a gold card user |
| <i>pension_plan</i> | binary variable, whether customer has a pension plan |
| <i>household_debt_to_equity_ratio</i> | household debt to equity ratio ($\times 100$) |
| <i>income</i> | annual income of the customer (\$) |
| <i>members_in_household</i> | number of members in the customer's household |
| <i>months_current_account</i> | number of months passed since the customer opened their account |
| <i>months_customer</i> | number of months passed since customer registered with the bank |
| <i>call_center_contacts</i> | amount of time spent in contact with call center |
| <i>loan_accounts</i> | number of loan accounts the customer has |
| <i>number_products</i> | number of products (except for those to be promoted) bought |
| <i>number_transactions</i> | number of transactions the customer has made |
| <i>non_worker_percentage</i> | percentage of non-workers in the customer's household |
| <i>white_collar_percentage</i> | percentage of white-collar workers in the customer's household |
| <i>rfm_score</i> | Recency, Frequency, and Monetary (RFM) score of the customer |
| *Mortgage | whether the customer has opened Mortgage account (only in old customer dataset) |
| *Pension | whether the customer has opened Pension account (only in old customer dataset) |
| *Savings | whether the customer has opened Savings account (only in old customer dataset) |

APPENDIX 3 | MODEL BASIC EVALUATION



Table 2: Basic evaluation of each model

| Method | Model | Revenue | Budget | Profit | Customers |
|------------------|----------------------|----------|----------|----------|-----------|
| Greedy | Random Forest | \$7,525 | \$7,075 | \$3,025 | 398 |
| Greedy | Logistics Regression | \$22,660 | \$12,818 | \$15,026 | 663 |
| Greedy | OCT | \$21,595 | \$12,818 | \$13,952 | 663 |
| Greedy | XGBoost | \$20,820 | \$12,818 | \$13,291 | 663 |
| SAA | Sample Average | \$0 | \$0 | \$0 | 0 |
| Point Prediction | Random Forest | \$23,670 | \$16,889 | \$15,608 | 840 |
| Point Prediction | Logistics Regression | \$52,130 | \$24,985 | \$38,752 | 1,192 |
| Point Prediction | OCT | \$45,200 | \$24,985 | \$32,836 | 1,192 |
| Point Prediction | XGBoost | \$43,095 | \$24,295 | \$31,374 | 1,162 |
| Prescriptive | KNN | \$52,840 | \$25,000 | \$40,946 | 1,193 |
| Prescriptive | Kernel Method | \$59,090 | \$25,000 | \$46,327 | 1,193 |

APPENDIX 4 | PRODUCTS OFFER RESULTS



Table 3: Products offered under each model

| Method | Model | Savings | Mortgage | Pension |
|------------------|----------------------|---------|----------|---------|
| Greedy | Random Forest | 335 | 10 | 53 |
| Greedy | Logistics Regression | 206 | 112 | 345 |
| Greedy | OCT | 289 | 100 | 274 |
| Greedy | XGBoost | 320 | 6 | 337 |
| SAA | Sample Average | 0 | 0 | 0 |
| Point Prediction | Random Forest | 436 | 121 | 283 |
| Point Prediction | Logistics Regression | 308 | 219 | 665 |
| Point Prediction | OCT | 451 | 210 | 531 |
| Point Prediction | XGBoost | 501 | 78 | 583 |
| Prescriptive | KNN | 0 | 65 | 1,128 |
| Prescriptive | Kernel Method | 0 | 2 | 1,191 |

APPENDIX 5 | CHANNELS USED RESULTS



Table 4: Channels used under each model

| Method | Model | Gift | Newsletter | Seminar |
|------------------|----------------------|------|------------|---------|
| Greedy | Random Forest | 221 | 177 | 0 |
| Greedy | Logistics Regression | 221 | 221 | 221 |
| Greedy | OCT | 221 | 221 | 221 |
| Greedy | XGBoost | 221 | 221 | 221 |
| SAA | Sample Average | 0 | 0 | 0 |
| Point Prediction | Random Forest | 221 | 221 | 398 |
| Point Prediction | Logistics Regression | 221 | 221 | 750 |
| Point Prediction | OCT | 221 | 221 | 750 |
| Point Prediction | XGBoost | 221 | 221 | 720 |
| Prescriptive | KNN | 221 | 222 | 750 |
| Prescriptive | Kernel Method | 221 | 222 | 750 |