

Enhancing Efficiency in Microchip Distribution: Strategic Supply Chain Route Optimization

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1 Introduction

A global microchip producer supplied a dataset from their outbound logistics network. This dataset includes demand information for 1000 orders which must be directed through their distribution system, consisting of 19 warehouses, 11 ports of departure, and a single port of arrival.

The project is to design an optimal distribution network that incorporates warehouses, shipping routes, and courier services to create the most economical supply chain possible. The goal is to minimize the total costs, comprising warehouse operations and transportation expenses while adhering to the constraints of demand, supply, and shipping logistics.

2 Data Source

The data for this project is from Brunel University London's public supply chain datasets.

- Link to Data Set
- Detailed descriptions of this dataset can be found in the paper: *Accelerating supply chains with Ant Colony Optimization across a range of hardware solutions*

Table 1: Tables in the dataset

Table	Explanation
<i>OrderList</i>	All orders that need to be assigned a route.
<i>FreightRates</i>	All available couriers, weight gaps for each individual lane, and rates associated.
<i>WhCosts</i>	Specifies the cost associated with storing products in a given warehouse, measured in dollars per unit.
<i>WhCapacities</i>	Lists warehouse capacities measured in the number of orders per day.
<i>ProductsPerPlant</i>	All supported warehouse-product combinations.
<i>VmiCustomers</i>	All special cases where a warehouse is only allowed to support specific customers, while any other non-listed warehouse can supply any customers.
<i>PlantPorts</i>	Allowed links between warehouses and shipping ports in the real world.

3 Problem Description

3.1 Index Notation

- $k \in [n_{\text{order}}]$ - order number
- $i \in [n_{\text{warehouse}}]$ - warehouse number
- $e \in [n_{\text{wport}}]$ - warehouse port number
- $j \in [n_{\text{freight}}]$ - freight number
- $u \in [n_{\text{product}}]$ - product number
- $v \in [n_{\text{customer}}]$ - customer number

3.2 Input Data

3.2.1 Order Data

The following are data of order k :

- q_k - unit quantity of order k
 - s_k - service delivery:
 - ot_k - maximum delivery time for order k
 - ow_k - weight for order k
 - pro_k - product type of order k
 - cus_k - customer of order k
- $$s_k = \begin{cases} 1, & \text{if Door-to-Door (DTD) or Door-to-Port (DTP)} \\ 0, & \text{if Customer Referred Freight (CRF)} \end{cases}$$

3.2.2 Freight Data

The following are data of freight j :

- o_j - original port

- d_j - destination port - in this problem, the only destination port is PORT09

- c_j - carrier number

- t_j - delivery time

- m_j - transportation mode:

$$m_j = \begin{cases} 1, & \text{if Ground} \\ 0, & \text{if Air} \end{cases}$$

- r_j - transportation rate cost per unit

- $minc_j$ - minimum transportation cost

- $maxw_j$ - maximum transportation weight

3.2.3 Warehouse Data

The following are data of warehouse i :

- p_i - storage cost per unit in warehouse i

- cap_i - order capacity per day in warehouse i

- PW_{ui}

$$PW_{ui} = \begin{cases} 1, & \text{if product } u \text{ can be stored in warehouse } i \\ 0, & \text{otherwise} \end{cases}$$

- WP_{ie}

$$WP_{ie} = \begin{cases} 1, & \text{if warehouse } i \text{ connects to warehouse port } e \\ 0, & \text{otherwise} \end{cases}$$

- WC_{iv}

$$WC_{iv} = \begin{cases} 1, & \text{if warehouse } i \text{ can serve customer } v \\ 0, & \text{if otherwise} \end{cases}$$

4 Baseline Model: Yan-Tian Greedy Algorithm

We developed a baseline model for addressing this problem, known as the Yan-Tian Greedy Algorithm. The primary concept behind this approach involves a systematic iteration through all incoming orders. For each order, we initiate a search through available warehouses and their corresponding freight options, starting from the beginning of the list. The algorithm then assigns the order to the first suitable warehouse-freight pair it encounters, following a thorough evaluation to ensure that all necessary conditions are met before making the assignment. The pseudo code is shown in the appendix as Algorithm 1. The cost of solution produced by the baseline model is **\$8,878,241.89**.

5 Formulating Optimization Model

The problem can be formulated as the following MIO.

5.1 Decision Variables

- X_{ki} where $k \in [n_{\text{order}}]$, $i \in [n_{\text{warehouse}}]$ - order k should be assigned to warehouse i
- Y_{kj} where $k \in [n_{\text{order}}]$, $j \in [n_{\text{freight}}]$ - order k should be assigned to freight assignment j

5.2 Objective Function

Some key things to note for the transportation cost:

- if $s_k = 0$ then the transportation cost is 0
- if $m_j = 1$ then the transportation cost is proportional to the weight consumed by the freight assignment order kj in respect of the total weight for the freight assignment order kj
- a minimum charge $minc_j$ is applied in cases where the air transportation is less than the minimum charge

Following from above:

$$\text{Objective} = \min(\text{Warehouse Cost} + \text{Transportation Cost})$$

$$\min \sum_{k=1}^{n_{\text{order}}} \sum_{i=1}^{n_{\text{warehouse}}} X_{ki} \cdot p_i \cdot q_k + \sum_{k=1}^{n_{\text{order}}} \sum_{j=1}^{n_{\text{freight}}} Y_{kj} \cdot TC_{kj}$$

5.3 Constraints

Converting the above constraints into mathematical notation:

- each order needs to be assigned to a warehouse

$$\sum_{i=1}^{n_{\text{warehouse}}} X_{ki} = 1, \forall k$$

- each order needs to be assigned to a freight assignment

$$\sum_{j=1}^{n_{\text{freight}}} Y_{kj} = 1, \forall k$$

- each warehouse has a daily order capacity

$$\sum_{k=1}^{n_{\text{order}}} X_{ki} \leq \text{cap}_i, \forall i$$

- each product can be stored in some warehouses only

If $PW_{pro_k i} = 0$, then $X_{ki} = 0$

$$X_{ki} \leq M(PW_{pro_k i}), \forall k, i$$

where M is the Big-M.

- some warehouses can only service certain customers

If $WC_{icus_k} = 0$, then $X_{ki} = 0$

$$X_{ki} \leq M(WC_{icus_k}), \forall k, i$$

where M is the Big-M.

- each warehouse can only begin transporting things via some specific warehouse ports

If $X_{ki} = 1$ and $WP_{io_j} = 0$ then $Y_{kj} = 0$

$$Y_{kj} \leq M(1 - X_{ki} + WP_{io_j}), \forall k, i, j$$

where M is the Big-M.

- orders need to be shipped within a certain time to the customer

$$\sum_{j=1}^{n_{\text{freight}}} Y_{kj} \cdot t_j \leq \text{ot}_k, \forall k$$

- for each route via a carrier, different parts of the carrier should not exceed a maximum weight

$$\sum_{k=1}^{n_{\text{order}}} Y_{kj} \cdot \text{ow}_k \leq \text{maxw}_j, \forall j$$

- total transportation cost

$$TC_{kj} \leq s_k[(1 - m_j) \cdot TCA_{kj} + m_j \cdot TCG_j], \forall k, j$$

- air transportation cost

$$\text{minc}_j \leq TCA_{kj}, \forall k, j$$

$$\text{ow}_k \cdot r_j \leq TCA_{kj}, \forall k, j$$

- ground transportation cost

$$z_j r_j \leq TCG_j, \forall j$$

$$z_j \leq \sum_{k=1}^{n_{\text{order}}} Y_{kj}, \forall j$$

$$Y_{kj} \leq z_j, \forall k, j$$

where z_j is a binary variable.

6 Data Pre-Processing

Due to many variables in the dataset not being of factor type eg. PORT09, mapping tables were created to map each of these values to a number. For eg. 1 \rightarrow PORT09. Mapping tables were created for the following variables:

- Order ID, Warehouse ID, Product ID, Origin Port, Carrier, Customer, Service Level, Destination Port, Transportation Mode

A variable to capture the maximum delivery time for order k , ot_k was also created

- Maximum delivery time = TPT + Ship ahead day count + Ship late day count + 2

Also, due to the large number of orders and freight paths, 1000 orders were randomly sampled and freight paths were reduced through aggregation.

7 Exploratory Data Analysis

Figure 1 shows that most warehouses are connected to only a single warehouse port and many warehouses are connected to warehouse port 4. This suggests that many warehouses may only be sent via one freight and many orders may be sent through freights going through warehouse port 4. Figure 2 shows that most products are only ordered a small number of times.

Figure 3 shows that most warehouses have negative correlation between the cost per unit cost and the daily order capacity. We should expect the warehouses with lower cost per unit to have the most number of orders allocated to it.

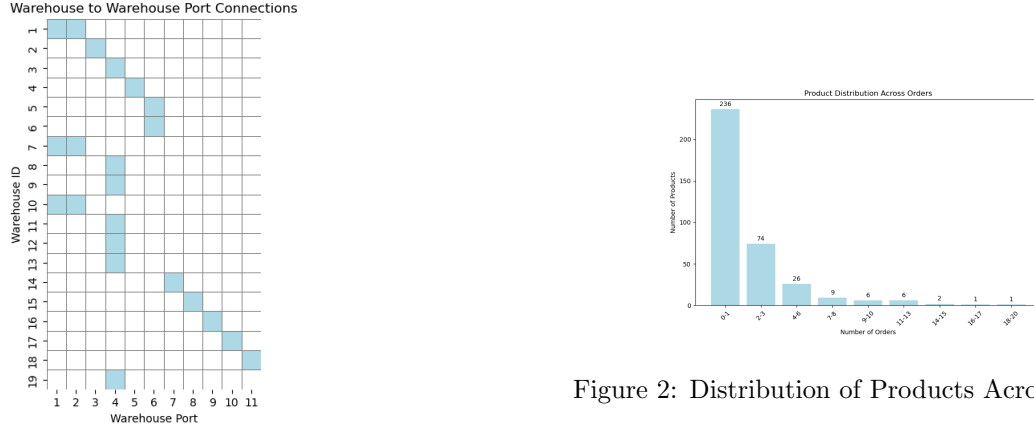


Figure 2: Distribution of Products Across Orders

Figure 1: Warehouse to Warehouse Port Connections

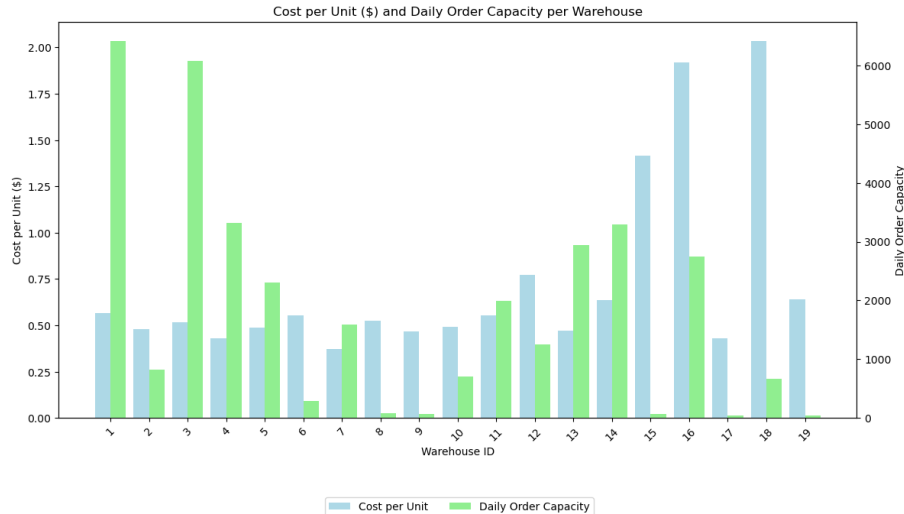


Figure 3: Cost per Unit (\$) and Daily Order Capacity Per Warehouse

8 Results

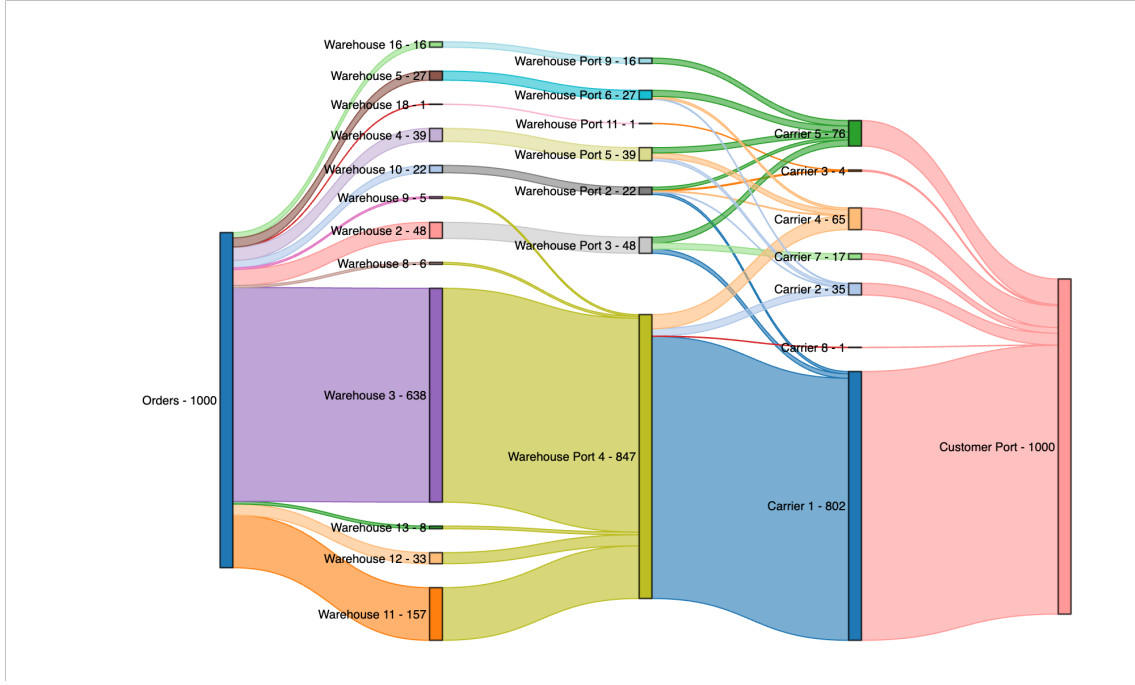


Figure 4: Optimization Result - Sankey Diagram of Order Assignment

Figure 4 shows the optimal warehouse and freight allocation for each of 1000 orders. Note that freight allocation is composed of a warehouse port and carrier.

Total cost reduction:

- The optimal cost of our solution is **\$5,365,566.57**.
- The cost of solution produced by the baseline model is **\$8,878,241.89**.
- Our solution reduced the total cost by **\$3,512,675.32**, which is **39.5%** reduction in cost.

9 Conclusion

The solution produced by our model surpasses the previously provided solution by the freight company.

- We successfully reduced the total cost, including storage cost and transportation cost by 39.5%.

The outcomes obtained in our study align with the expectations derived from our preliminary exploratory analysis.

- many orders to pass through warehouse port 4.
- many orders allocated to warehouse 3 and warehouse 11 due to their lower daily cost per unit.
- not many orders allocated to warehouse 15, 16 or 18 due to their high daily cost.

10 Next Steps

Here are some ideas for future model improvement:

1. Split orders into multiple orders which may be fulfilled through different warehouses.
2. If a warehouse has reached full capacity, allow some orders to still be fulfilled there the next day is delivery time can still be met.

References

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Appendix

Algorithm 1 Yan-Tian Greedy Algorithm For Order Assignment

```
// Assign orders to warehouse and freight
for orderk from 1 to  $n_{order}$  do
  for warehousei from 1 to  $n_{warehouse}$  do
    for freightj from 1 to  $n_{freight}$  do
      if warehousei can produce orderk's product then
        if warehousei can serve orderk's customer then
          if warehousei has capacity then
            if freightj has capacity then
              if warehousei can transport products to freightj's warehouse port then
                if freightj's transportation time satisfy orderk's demanding time then
                  Assign orderk to warehousei and freightj
                  BREAK
                end if
              end if
            end if
          end if
        end if
      end if
    end for
  end for
end for
// Calculate transportation cost  $TC$  and Warehouse Cost  $WC$ , Penalty Cost  $PC$ , and total cost  $C$ 
Initialize  $TC = 0$ ,  $WC = 0$ ,  $PC = 0$ , and  $C = 0$ 
for warehousei from 1 to  $n_{warehouse}$  do
   $WC = WC + \text{warehouse}_i\text{'s cost}$ 
end for
for freightj from 1 to  $n_{freight}$  do
   $TC = TC + \text{freight}_j\text{'s cost}$ 
end for
for orderk from 1 to  $n_{order}$  do
  if orderk is not assigned then
     $PC = PC + \text{unit penalty cost}$ 
  end if
end for
 $C = PC + TC + WC$ 
// Output results
```
