



# Enhancing Efficiency in Microchip Distribution: Strategic Supply Chain Route Optimization

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## 1 Introduction

A global microchip producer supplied a dataset from their outbound logistics network. This dataset includes demand information for 1000 orders which must be directed through their distribution system, consisting of 19 warehouses, 11 ports of departure, and a single port of arrival.

The project is to design an optimal distribution network that incorporates warehouses, shipping routes, and courier services to create the most economical supply chain possible. The goal is to minimize the total costs, comprising warehouse operations and transportation expenses while adhering to the constraints of demand, supply, and shipping logistics.

### 2 Data Source

The data for this project is from Brunel University London's public supply chain datasets.

- Link to Data Set
- Detailed descriptions of this dataset can be found in the paper: Accelerating supply chains with Ant Colony Optimization across a range of hardware solutions

Table	1:	Tables	$^{\mathrm{1n}}$	the	dataset	

Table	Explanation
OrderList	All orders that need to be assigned a route.
FreightRates	All available couriers, weight gaps for each individual lane, and rates associated.
WhCosts	Specifies the cost associated with storing products in a given warehouse, measured in dollars per unit.
Wh Capacities	Lists warehouse capacities measured in the number of orders per day.
ProductsPerPlant	All supported warehouse-product combinations.
VmiCustomers	All special cases where a warehouse is only allowed to support specific customers, while any other non-listed warehouse can supply any customers.
PlantPorts	Allowed links between warehouses and shipping ports in the real world.

# 3 Problem Description

### 3.1 Index Notation

- $k \in [n_{\text{order}}]$  order number
- $i \in [n_{\text{warehouse}}]$  warehouse number
- $e \in [n_{\text{wport}}]$  warehouse port number

- $j \in [n_{\text{freight}}]$  freight number
- $u \in [n_{\text{product}}]$  product number
- $v \in [n_{\text{customer}}]$  customer number

### 3.2 Input Data

#### 3.2.1 Order Data

The following are data of order k:

- $q_k$  unit quantity of order k
- $s_k$  service delivery:

- $ot_k$  maximum delivery time for order k
- $ow_k$  weight for order k
- $s_k = \begin{cases} 1, & \text{if Door-to-Door (DTD) or Door-to-Port (DTP)} \\ 0, & \text{if Customer Referred Freight (CRF)} \end{cases}$
- $cus_k$  customer of order k

 $\bullet \ pro_k$  - product type of order k

#### 3.2.2 Freight Data

The following are data of freight j:

•  $o_j$  - original port

•  $d_j$  - destination port - in this problem, the only destination port is PORT09

•  $c_i$  - carrier number

•  $t_i$  - delivery time

•  $m_j$  - transportation mode:

$$m_j = \begin{cases} 1, & \text{if Ground} \\ 0, & \text{if Air} \end{cases}$$

•  $r_j$  - transportation rate cost per unit

•  $minc_j$  - minimum transportation cost

•  $maxw_j$  - maximum transportation weight

#### 3.2.3 Warehouse Data

The following are data of warehouse i:

 $\bullet \ p_i$  - storage cost per unit in warehouse i

 $\bullet$   $PW_{ui}$ 

 $PW_{ui} = \begin{cases} 1, & \text{if product } u \text{ can be stored in warehouse } i \\ 0, & \text{otherwise} \end{cases}$ 

 $\bullet$   $WP_{ie}$ 

 $WP_{ie} = \begin{cases} 1, & \text{if warehouse } i \text{ connects to warehouse port } e \\ 0, & \text{otherwise} \end{cases}$ 

•  $WC_{iv}$ 

 $WC_{iv} = \begin{cases} 1, & \text{if warehouse } i \text{ can serve customer } v \\ 0, & \text{if otherwise} \end{cases}$ 

# 4 Baseline Model: Yan-Tian Greedy Algorithm

We developed a baseline model for addressing this problem, known as the Yan-Tian Greedy Algorithm. The primary concept behind this approach involves a systematic iteration through all incoming orders. For each order, we initiate a search through available warehouses and their corresponding freight options, starting from the beginning of the list. The algorithm then assigns the order to the first suitable warehouse-freight pair it encounters, following a thorough evaluation to ensure that all necessary conditions are met before making the assignment. The pseudo code is shown in the appendix as Algorithm 1. The cost of solution produced by the baseline model is \$8,878,241.89.

# 5 Formulating Optimization Model

The problem can be formulated as the following MIO.

#### 5.1 Decision Variables

- $X_{ki}$  where  $k \in [n_{\text{order}}], i \in [n_{\text{warehouse}}]$  order k should be assigned to warehouse i
- $Y_{kj}$  where  $k \in [n_{\text{order}}], j \in [n_{\text{freight}}]$  order k should be assigned to freight assignment j

### 5.2 Objective Function

Some key things to note for the transportation cost:

- if  $s_k = 0$  then the transportation cost is 0
- if  $m_j = 1$  then the transportation cost is proportional to the weight consumed by the freight assignment order kj in respect of the total weight for the freight assignment order kj
- a minimum charge  $minc_i$  is applied in cases where the air transportation is less than the minimum charge

Following from above:

Objective = min(Warehouse Cost + Transportation Cost)

$$\min \sum_{k=1}^{n_{\text{order}}} \sum_{i=1}^{n_{\text{warehouse}}} X_{ki} \cdot p_i \cdot q_k + \sum_{k=1}^{n_{\text{order}}} \sum_{j=1}^{n_{\text{freight}}} Y_{kj} \cdot TC_{kj}$$

#### 5.3 Constraints

Converting the above constraints into mathematical notation:

• each order needs to be assigned to a warehouse

$$\sum_{i=1}^{n_{\text{warehouse}}} X_{ki} = 1, \forall k$$

• each order needs to be assigned to a freight assignment

$$\sum_{j=1}^{n_{\text{freight}}} Y_{kj} = 1, \forall k$$

each warehouse has a daily order capacity

$$\sum_{k=1}^{n_{\text{order}}} X_{ki} \le cap_i, \forall i$$

• each product can be stored in some warehouses only

If 
$$PW_{pro_ki} = 0$$
, then  $X_{ki} = 0$   $X_{ki} \le M(PW_{pro_ki}), \forall k, i$  No need M actually

where M is the Big-M.

• some warehouses can only service certain customers

If 
$$WC_{icus_k} = 0$$
, then  $X_{ki} = 0$  No need M actually  $X_{ki} \leq M(WC_{icus_k}), \forall k, i$ 

where M is the Big-M.

• each warehouse can only begin transporting things via some specific warehouse ports

If 
$$X_{ki}=1$$
 and  $WP_{io_j}=0$  then  $Y_{kj}=0$  don't need to worry about  $X=0$  and  $X=0$  and  $X=0$  and  $X=0$  and  $X=0$  are minimizing the objective

where M is the Big-M.

• orders need to be shipped within a certain time to the customer

$$\sum_{j=1}^{n_{\text{freight}}} Y_{kj} \cdot t_j \le ot_k, \forall k$$

• for each route via a carrier, different parts of the carrier should not exceed a maximum weight

$$\sum_{k=1}^{n_{\text{order}}} Y_{kj} \cdot ow_k \le maxw_j, \forall j$$

• total transportation cost

$$TC_{kj} \leq s_k[(1-m_j) \cdot TCA_{kj} + m_j \cdot TCG_j], \forall k, j$$

• air transportation cost

$$minc_j \leq TCA_{kj}, \forall k, j$$
  
 $ow_k \cdot r_j \leq TCA_{kj}, \forall k, j$ 

• ground transportation cost

$$z_{j}r_{j} \leq TCG_{j}, \forall j$$

$$z_{j} \leq \sum_{k=1}^{n_{\text{order}}} Y_{kj}, \forall j$$

$$Y_{kj} \leq z_{j}, \forall k, j$$

where  $z_j$  is a binary variable.

# 6 Data Pre-Processing

Due to many variables in the dataset not being of factor type eg. PORT09, mapping tables were created to map each of these values to a number. For eg.  $1 \rightarrow PORT09$ . Mapping tables were created for the following variables:

• Order ID, Warehouse ID, Product ID, Origin Port, Carrier, Customer, Service Level, Destination Port, Transportation Mode

A variable to capture the maximum delivery time for order  $k, ot_k$  was also created

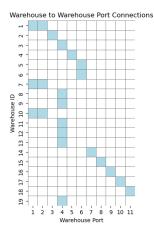
• Maximum delivery time = TPT + Ship ahead day count + Ship late day count + 2

Also, due to the large number of orders and freight paths, 1000 orders were randomly sampled and freight paths were reduced through aggregation.

# 7 Exploratory Data Analysis

Figure 1 shows that most warehouses are connected to only a single warehouse port and many warehouses are connected to warehouse port 4. This suggests that many warehouses may only be sent via one freight and many orders may be sent through freights going through warehouse port 4. Figure 2 shows that most products are only ordered a small number of times.

Figure 3 shows that most warehouses have negative correlation between the cost per unit cost and the daily order capacity. We should expect the warehouses with lower cost per unit to have the most number of orders allocated to it.



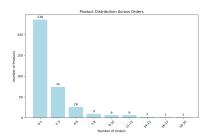


Figure 2: Distribution of Products Across Orders

Figure 1: Warehouse to Warehouse Port Connections

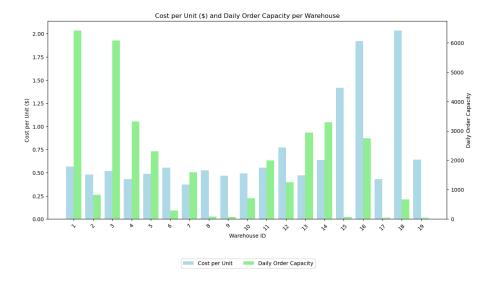


Figure 3: Cost per Unit (\$) and Daily Order Capacity Per Warehouse

### 8 Results

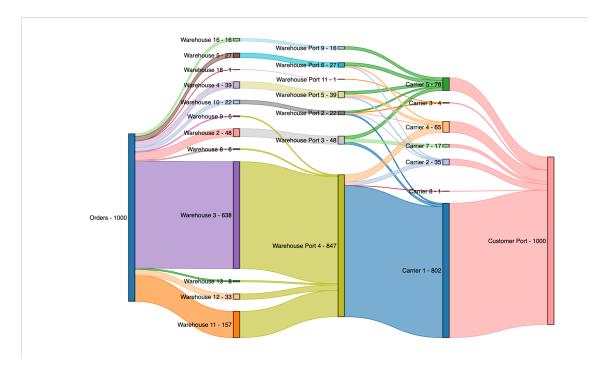


Figure 4: Optimization Result - Sankey Diagram of Order Assignment

Figure 4 shows the optimal warehouse and freight allocation for each of 1000 orders. Note that freight allocation is composed of a warehouse port and carrier.

Total cost reduction:

- The optimal cost of our solution is \$5,365,566.57.
- The cost of solution produced by the baseline model is \$8,878,241.89.
- Our solution reduced the total cost by \$3,512,675.32, which is 39.5% reduction in cost.

## 9 Conclusion

The solution produced by our model surpasses the previously provided solution by the freight company.

• We successfully reduced the total cost, including storage cost and transportation cost by 39.5%.

The outcomes obtained in our study align with the expectations derived from our preliminary exploratory analysis.

- many orders to pass through warehouse port 4.
- many orders allocated to warehouse 3 and warehouse 11 due to their lower daily cost per unit.
- not many orders allocated to warehouse 15, 16 or 18 due to their high daily cost.

# 10 Next Steps

Here are some ideas for future model improvement:

- 1. Split orders into multiple orders which may be fulfilled through different warehouses.
- 2. If a warehouse has reached full capacity, allow some orders to still be fulfilled there the next day is delivery time can still be met.

# References

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# Appendix

### Algorithm 1 Yan-Tian Greedy Algorithm For Order Assignment

```
// Assign orders to warehouse and freight
for order<sub>k</sub> from 1 to n_{order} do
  for warehouse<sub>i</sub> from 1 to n_{warehouse} do
     for freight<sub>j</sub> from 1 to n_{freight} do
        if warehouse<sub>i</sub> can produce order<sub>k</sub>'s product then
          if warehouse<sub>i</sub> can serve order<sub>k</sub>'s customer then
             if warehouse_i has capacity then
                if freight_i has capacity then
                  if warehouse i can transport products to freight j's warehouse port then
                     if freight<sub>j</sub>'s transportation time satisfy order<sub>k</sub>'s demanding time then
                        Assign order<sub>k</sub> to warehouse<sub>i</sub> and freight<sub>j</sub>
                        BREAK
                     end if
                  end if
                end if
             end if
          end if
        end if
     end for
  end for
end for
// Calculate transportation cost TC and Warehouse Cost WC, Penalty Cost PC, and total cost C
Initialize TC = 0, WC = 0, PC = 0, and C = 0
for warehouse<sub>i</sub> from 1 to n_{warehouse} do
   WC = WC + warehouse_i's cost
end for
for freight<sub>j</sub> from 1 to n_{freight} do
  TC = TC + \mathrm{freight}_j\text{'s cost}
end for
for order<sub>k</sub> from 1 to n_{order} do
  if order_k is not assigned then
     PC = PC + unit penalty cost
  end if
end for
C = PC + TC + WC
// Output results
```