

1 Description

The first we just calculated several Extended Barycentric Cubical Tori. The distribution of calculated toruses we can see in the Figure 1a.

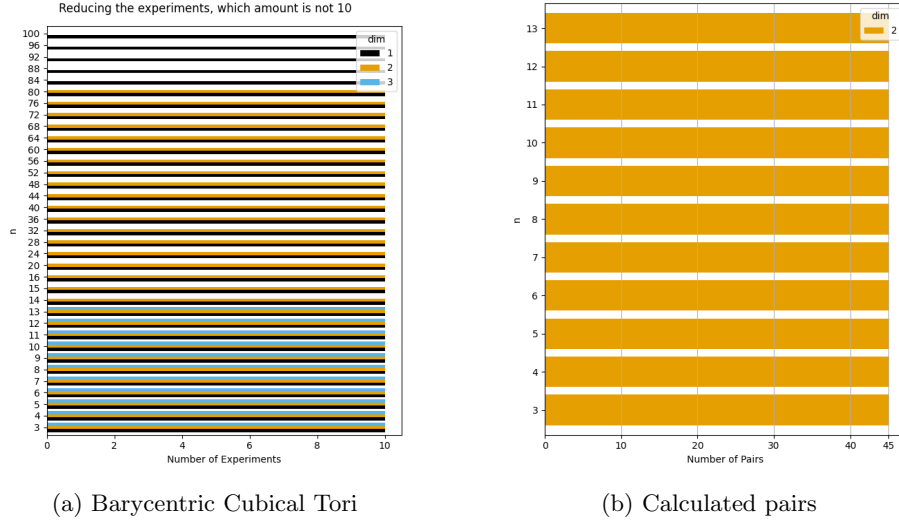


Figure 1: Size/dimension distribution

Then for each pair of filtrations with similar dimension and n $f_0, f_1 : \mathbb{T}_n^d \rightarrow \mathbb{R}$ we can define a linear homotopy $h : [0, 1] \times \mathbb{T}_n^d \rightarrow \mathbb{R}$:

$$h(t, \sigma) = (1 - t) \cdot f_0(\sigma) + t \cdot f_1(\sigma)$$

The moment of time $t \in [0, 1]$ such there exist a pair of cells $\sigma_0, \sigma_1 \in \mathbb{T}_n^d$ such that $h(t, \sigma_0) = h(t, \sigma_1)$ is a moment of transposition of these cells during the homotopy (the probability, that this will be full segment is 0 for pair of independent barycentric cubical tori).

We have found all transposing pairs like this, classified them and calculated how these transpositions changes the Depth Poset. The distribution of calculated pairs of filtration we can see in the Figure 1b.

2 Switch Types Distributions

The distribution of transpositions types for the model \mathbb{T}_n^2 we can see in the figure Fig. 2.

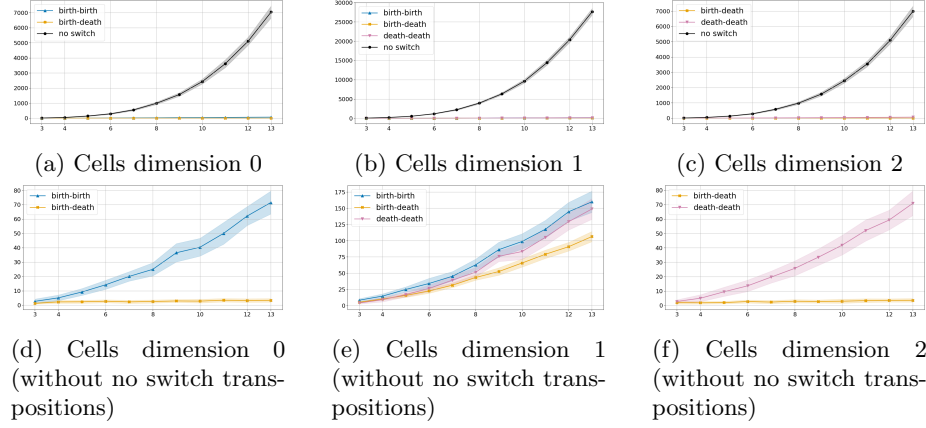


Figure 2: The switch type distribution for \mathbb{T}_n^2

3 Similarity Scores

- **birth_relation_cell_similarity** - The Jacard index of arcs (edges) in the birth relation (given by row left to right reduction algorithm). Consider 2 birth-death pairs are similar if they correspond the similar cells.
- **death_relation_cell_similarity** - The Jacard index of arcs (edges) in the death relation (given by column bottom to top reduction algorithm). Consider 2 birth-death pairs are similar if they correspond the similar cells.
- **poset_closure_arcs_cell_similarity** - The Jacard index of arcs (edges) in the transitive closure of the Depth Posets. Consider 2 birth-death pairs are similar if they correspond the similar cells.
- **poset_reduction_arcs_cell_similarity** - The Jacard index of arcs (edges) in the transitive reduction of the Depth Posets. Consider 2 birth-death pairs are similar if they correspond the similar cells.

The distribution of the similarity scores for different models \mathbb{T}_n^{dim} we can see in the following figures:

| dim | 2 |
|--------------------------------------|--------|
| birth_relation_cell_similarity | Fig. 3 |
| death_relation_cell_similarity | Fig. 4 |
| poset_closure_arcs_cell_similarity | Fig. 5 |
| poset_reduction_arcs_cell_similarity | Fig. 6 |

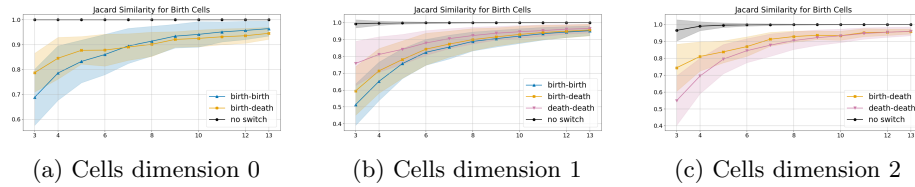


Figure 3: Similarity score birth_relation_cell_similarity for \mathbb{T}_n^2

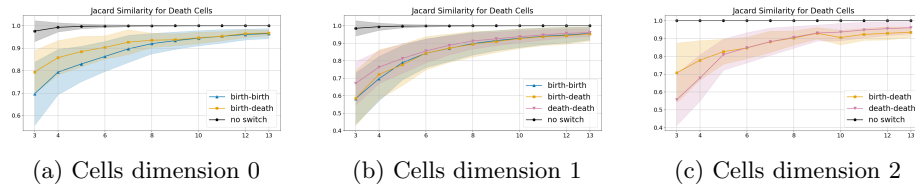


Figure 4: Similarity score death_relation_cell_similarity for \mathbb{T}_n^2

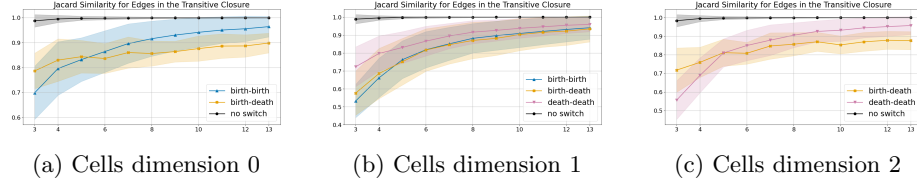


Figure 5: Similarity score poset_closure_arcs_cell_similarity for \mathbb{T}_n^2

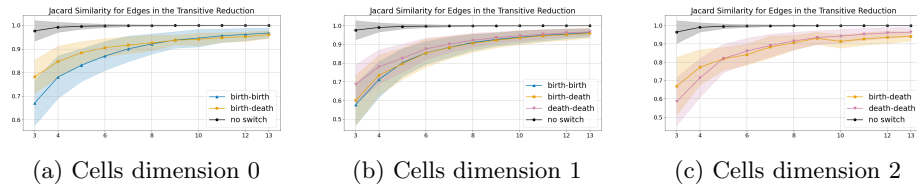


Figure 6: Similarity score poset_reduction_arcs_cell_similarity for \mathbb{T}_n^2