

```

import numpy as np

"""
This file implements various first-order update rules that are commonly used for
training neural networks. Each update rule accepts current weights and the
gradient of the loss with respect to those weights and produces the next set of
weights. Each update rule has the same interface:

def update(w, dw, config=None):

Inputs:
- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the
    loss with respect to w.
- config: A dictionary containing hyperparameter values such as learning rate,
    momentum, etc. If the update rule requires caching values over many
    iterations, then config will also hold these cached values.

Returns:
- next_w: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the
    update rule.

NOTE: For most update rules, the default learning rate will probably not perform
well; however the default values of the other hyperparameters should work well
for a variety of different problems.

For efficiency, update rules may perform in-place updates, mutating w and
setting next_w equal to w.
"""

def sgd(w, dw, config=None):
    """
    Performs vanilla stochastic gradient descent.

    config format:
    - learning_rate: Scalar learning rate.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-2)

    w -= config['learning_rate'] * dw
    return w, config

def sgd_momentum(w, dw, config=None):
    """
    Performs stochastic gradient descent with momentum.

    config format:
    - learning_rate: Scalar learning rate.
    - momentum: Scalar between 0 and 1 giving the momentum value.
        Setting momentum = 0 reduces to sgd.
    - velocity: A numpy array of the same shape as w and dw used to store a moving
        average of the gradients.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-2)
    config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
    v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.

    # ===== #
    # YOUR CODE HERE:
    # Implement the momentum update formula. Return the updated weights
    # as next_w, and the updated velocity as v.
    # ===== #
    v = config["momentum"]*v - config["learning_rate"]*dw
    next_w = w+v
    # ===== #
    # END YOUR CODE HERE
    # ===== #

    config['velocity'] = v

    return next_w, config

def sgd_nesterov_momentum(w, dw, config=None):
    """
    Performs stochastic gradient descent with Nesterov momentum.

    config format:
    - learning_rate: Scalar learning rate.
    - momentum: Scalar between 0 and 1 giving the momentum value.
        Setting momentum = 0 reduces to sgd.
    - velocity: A numpy array of the same shape as w and dw used to store a moving
        average of the gradients.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-2)

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config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.

# ===== #
# YOUR CODE HERE:
# Implement the momentum update formula. Return the updated weights
# as next_w, and the updated velocity as v.
# ===== #
vOld = v
v = config['momentum']*vOld - config['learning_rate']*dw
next_w = w + v + config['momentum']*(v - vOld)
# ===== #
# END YOUR CODE HERE
# ===== #

config['velocity'] = v

return next_w, config

def rmsprop(w, dw, config=None):
    """
    Uses the RMSProp update rule, which uses a moving average of squared gradient
    values to set adaptive per-parameter learning rates.

    config format:
    - learning_rate: Scalar learning rate.
    - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
      gradient cache.
    - epsilon: Small scalar used for smoothing to avoid dividing by zero.
    - beta: Moving average of second moments of gradients.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-2)
    config.setdefault('decay_rate', 0.99)
    config.setdefault('epsilon', 1e-8)
    config.setdefault('a', np.zeros_like(w))

    next_w = None

    # ===== #
    # YOUR CODE HERE:
    # Implement RMSProp. Store the next value of w as next_w. You need
    # to also store in config['a'] the moving average of the second
    # moment gradients, so they can be used for future gradients. Concretely,
    # config['a'] corresponds to "a" in the lecture notes.
    # ===== #
    config['a'] = config['decay_rate']*config['a'] + (1-config['decay_rate'])*(dw*dw)
    newLearnRate = config["learning_rate"]/(np.sqrt(config['a'])+config['epsilon'])
    next_w = w - newLearnRate*dw

    # ===== #
    # END YOUR CODE HERE
    # ===== #

    return next_w, config

def adam(w, dw, config=None):
    """
    Uses the Adam update rule, which incorporates moving averages of both the
    gradient and its square and a bias correction term.

    config format:
    - learning_rate: Scalar learning rate.
    - beta1: Decay rate for moving average of first moment of gradient.
    - beta2: Decay rate for moving average of second moment of gradient.
    - epsilon: Small scalar used for smoothing to avoid dividing by zero.
    - m: Moving average of gradient.
    - v: Moving average of squared gradient.
    - t: Iteration number.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-3)
    config.setdefault('beta1', 0.9)
    config.setdefault('beta2', 0.999)
    config.setdefault('epsilon', 1e-8)
    config.setdefault('v', np.zeros_like(w))
    config.setdefault('a', np.zeros_like(w))
    config.setdefault('t', 0)

    next_w = None

    # ===== #
    # YOUR CODE HERE:
    # Implement Adam. Store the next value of w as next_w. You need
    # to also store in config['a'] the moving average of the second
    # moment gradients, and in config['v'] the moving average of the
    # first moments. Finally, store in config['t'] the increasing time.
    # ===== #
    config['t'] = config['t'] + 1
    config['v'] = config['beta1']*config['v'] + (1-config['beta1'])*dw

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config['a'] = config['beta2']*config['a'] + (1-config['beta2'])*(dw*dw)

updateV = (1/(1-config['beta1']**config['t']))*config['v']
updateA = (1/(1-config['beta2']**config['t']))*config['a']

newLearnRate = config["learning_rate"]/(np.sqrt(updateA)+config['epsilon'])

next_w = w - newLearnRate*updateV

# ===== #
# END YOUR CODE HERE
# ===== #

return next_w, config

```

```

import numpy as np

def affine_forward(x, w, b):
    """
    Computes the forward pass for an affine (fully-connected) layer.

    The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
    examples, where each example x[i] has shape (d_1, ..., d_k). We will
    reshape each input into a vector of dimension D = d_1 * ... * d_k, and
    then transform it to an output vector of dimension M.

    Inputs:
    - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
    - w: A numpy array of weights, of shape (D, M)
    - b: A numpy array of biases, of shape (M,)

    Returns a tuple of:
    - out: output, of shape (N, M)
    - cache: (x, w, b)
    """

    # ===== #
    # YOUR CODE HERE:
    # Calculate the output of the forward pass. Notice the dimensions
    # of w are D x M, which is the transpose of what we did in earlier
    # assignments.
    # ===== #
    correctDimX = x.reshape(x.shape[0], -1)
    out = correctDimX.dot(w)+b

    # ===== #
    # END YOUR CODE HERE
    # ===== #

    cache = (x, w, b)
    return out, cache

def affine_backward(dout, cache):
    """
    Computes the backward pass for an affine layer.

    Inputs:
    - dout: Upstream derivative, of shape (N, M)
    - cache: Tuple of:
      - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
      - w: A numpy array of weights, of shape (D, M)
      - b: A numpy array of biases, of shape (M,)

    Returns a tuple of:
    - dx: Gradient with respect to x, of shape (N, d_1, ..., d_k)
    - dw: Gradient with respect to w, of shape (D, M)
    - db: Gradient with respect to b, of shape (M,)
    """
    x, w, b = cache
    dx, dw, db = None, None, None

    # ===== #
    # YOUR CODE HERE:
    # Calculate the gradients for the backward pass.
    # Notice:
    # dout is N x M
    # dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is D x M
    # dw should be D x M; it relates to dout through multiplication with x, which is N x D after reshaping
    # db should be M; it is just the sum over dout examples
    # ===== #
    correctDimX = x.reshape(x.shape[0], -1)
    dx = dout.dot(w.T)
    dx = dx.reshape(x.shape)
    dw = correctDimX.T.dot(dout)
    db = np.sum(dout,axis=0)

    # ===== #
    # END YOUR CODE HERE
    # ===== #

    return dx, dw, db

def relu_forward(x):
    """
    Computes the forward pass for a layer of rectified linear units (ReLUs).

    Input:
    - x: Inputs, of any shape

    Returns a tuple of:
    - out: Output, of the same shape as x
    - cache: x
    """

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"""
# ===== #
# YOUR CODE HERE:
# Implement the ReLU forward pass.
# ===== #
out = np.maximum(x,0)

# ===== #
# END YOUR CODE HERE
# ===== #

cache = x
return out, cache

def relu_backward(dout, cache):
    """
    Computes the backward pass for a layer of rectified linear units (ReLUs).

    Input:
    - dout: Upstream derivatives, of any shape
    - cache: Input x, of same shape as dout

    Returns:
    - dx: Gradient with respect to x
    """
    x = cache

    # ===== #
    # YOUR CODE HERE:
    # Implement the ReLU backward pass
    # ===== #
    correctDimX = x.reshape(x.shape[0], -1)
    correctDimX[correctDimX<0]=0
    correctDimX[correctDimX>0]=1
    dx = dout*correctDimX

    # ===== #
    # END YOUR CODE HERE
    # ===== #

    return dx

def batchnorm_forward(x, gamma, beta, bn_param):
    """
    Forward pass for batch normalization.

    During training the sample mean and (uncorrected) sample variance are
    computed from minibatch statistics and used to normalize the incoming data.
    During training we also keep an exponentially decaying running mean of the mean
    and variance of each feature, and these averages are used to normalize data
    at test-time.

    At each timestep we update the running averages for mean and variance using
    an exponential decay based on the momentum parameter:

    running_mean = momentum * running_mean + (1 - momentum) * sample_mean
    running_var = momentum * running_var + (1 - momentum) * sample_var

    Note that the batch normalization paper suggests a different test-time
    behavior: they compute sample mean and variance for each feature using a
    large number of training images rather than using a running average. For
    this implementation we have chosen to use running averages instead since
    they do not require an additional estimation step; the torch7 implementation
    of batch normalization also uses running averages.

    Input:
    - x: Data of shape (N, D)
    - gamma: Scale parameter of shape (D,)
    - beta: Shift parameter of shape (D,)
    - bn_param: Dictionary with the following keys:
      - mode: 'train' or 'test'; required
      - eps: Constant for numeric stability
      - momentum: Constant for running mean / variance.
      - running_mean: Array of shape (D,) giving running mean of features
      - running_var Array of shape (D,) giving running variance of features

    Returns a tuple of:
    - out: of shape (N, D)
    - cache: A tuple of values needed in the backward pass
    """
    mode = bn_param['mode']
    eps = bn_param.get('eps', 1e-5)
    momentum = bn_param.get('momentum', 0.9)

    N, D = x.shape
    running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
    running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))

    out, cache = None, None
    if mode == 'train':

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# ===== #
# YOUR CODE HERE:
#   A few steps here:
#   (1) Calculate the running mean and variance of the minibatch.
#   (2) Normalize the activations with the running mean and variance.
#   (3) Scale and shift the normalized activations. Store this
#       as the variable 'out'
#   (4) Store any variables you may need for the backward pass in
#       the 'cache' variable.
# ===== #

minimean = np.mean(x,axis=0)
minivar = np.var(x,axis=0)

running_mean = momentum * running_mean + (1 - momentum) * minimean
running_var = momentum * running_var + (1 - momentum) * minivar

xNormalized = (x-minimean) / np.sqrt(minivar+eps)

out = gamma * xNormalized + beta

cache = (xNormalized, x, gamma, eps, minimean, minivar)

# ===== #
# END YOUR CODE HERE
# ===== #

elif mode == 'test':

    # ===== #
    # YOUR CODE HERE:
    #   Calculate the testing time normalized activation. Normalize using
    #   the running mean and variance, and then scale and shift appropriately.
    #   Store the output as 'out'.
    # ===== #

    testNormalized = (x-running_mean) / np.sqrt(running_var+eps)
    out = gamma * testNormalized + beta

    # ===== #
    # END YOUR CODE HERE
    # ===== #

else:
    raise ValueError('Invalid forward batchnorm mode "%s"' % mode)

# Store the updated running means back into bn_param
bn_param['running_mean'] = running_mean
bn_param['running_var'] = running_var

return out, cache

def batchnorm_backward(dout, cache):
    """
    Backward pass for batch normalization.

    For this implementation, you should write out a computation graph for
    batch normalization on paper and propagate gradients backward through
    intermediate nodes.

    Inputs:
    - dout: Upstream derivatives, of shape (N, D)
    - cache: Variable of intermediates from batchnorm_forward.

    Returns a tuple of:
    - dx: Gradient with respect to inputs x, of shape (N, D)
    - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
    - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
    """
    dx, dgamma, dbeta = None, None, None

    # ===== #
    # YOUR CODE HERE:
    #   Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
    # ===== #
    M = dout.shape[0]

    xNormalized, x, gamma, eps, minimean, minivar = cache

    dgamma = np.sum(xNormalized * dout ,axis = 0)
    dbeta = np.sum(dout,axis=0)

    dL_dxNorm = dout * gamma
    dxNorm_da = 1/(np.sqrt(minivar+eps))
    dL_da = dxNorm_da * dL_dxNorm
    da_dx=1

    dxNorm_de = -0.5*(dxNorm_da**3)*(x-minimean)
    dL_de = dxNorm_de*dL_dxNorm
    dL_dvar = np.sum(dL_de, axis=0)

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dvar_dx = (2*(x-minimean)/M)

dL_dmu=np.sum(-dL_da, axis=0)
dmu_dx =1/M

dx = da_dx*dL_da + dvar_dx*dL_dvar + dmu_dx*dL_dmu
# ===== #
# END YOUR CODE HERE
# ===== #

return dx, dgamma, dbeta

def dropout_forward(x, dropout_param):
    """
    Performs the forward pass for (inverted) dropout.

    Inputs:
    - x: Input data, of any shape
    - dropout_param: A dictionary with the following keys:
      - p: Dropout parameter. We drop each neuron output with probability p.
      - mode: 'test' or 'train'. If the mode is train, then perform dropout;
        if the mode is test, then just return the input.
      - seed: Seed for the random number generator. Passing seed makes this
        function deterministic, which is needed for gradient checking but not in
        real networks.

    Outputs:
    - out: Array of the same shape as x.
    - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
      mask that was used to multiply the input; in test mode, mask is None.
    """
    p, mode = dropout_param['p'], dropout_param['mode']
    if 'seed' in dropout_param:
        np.random.seed(dropout_param['seed'])

    mask = None
    out = None

    if mode == 'train':
        # ===== #
        # YOUR CODE HERE:
        # Implement the inverted dropout forward pass during training time.
        # Store the masked and scaled activations in out, and store the
        # dropout mask as the variable mask.
        # ===== #

        mask = (np.random.rand(x.shape[0], x.shape[1]) < p) / p
        out = x*mask

        # ===== #
        # END YOUR CODE HERE
        # ===== #

    elif mode == 'test':
        # ===== #
        # YOUR CODE HERE:
        # Implement the inverted dropout forward pass during test time.
        # ===== #

        out = x

        # ===== #
        # END YOUR CODE HERE
        # ===== #

    cache = (dropout_param, mask)
    out = out.astype(x.dtype, copy=False)

    return out, cache

def dropout_backward(dout, cache):
    """
    Perform the backward pass for (inverted) dropout.

    Inputs:
    - dout: Upstream derivatives, of any shape
    - cache: (dropout_param, mask) from dropout_forward.
    """
    dropout_param, mask = cache
    mode = dropout_param['mode']

    dx = None
    if mode == 'train':
        # ===== #
        # YOUR CODE HERE:
        # Implement the inverted dropout backward pass during training time.
        # ===== #

        dx = dout*mask

```

```

# ===== #
# END YOUR CODE HERE
# ===== #
elif mode == 'test':
# ===== #
# YOUR CODE HERE:
# Implement the inverted dropout backward pass during test time.
# ===== #

dx = dout

# ===== #
# END YOUR CODE HERE
# ===== #
return dx

def svm_loss(x, y):
    """
    Computes the loss and gradient using for multiclass SVM classification.

    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
      for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
      0 <= y[i] < C

    Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    """
    N = x.shape[0]
    correct_class_scores = x[np.arange(N), y]
    margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
    margins[np.arange(N), y] = 0
    loss = np.sum(margins) / N
    num_pos = np.sum(margins > 0, axis=1)
    dx = np.zeros_like(x)
    dx[margins > 0] = 1
    dx[np.arange(N), y] -= num_pos
    dx /= N
    return loss, dx

def softmax_loss(x, y):
    """
    Computes the loss and gradient for softmax classification.

    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
      for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
      0 <= y[i] < C

    Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    """

    probs = np.exp(x - np.max(x, axis=1, keepdims=True))
    probs /= np.sum(probs, axis=1, keepdims=True)
    N = x.shape[0]
    loss = -np.sum(np.log(probs[np.arange(N), y])) / N
    dx = probs.copy()
    dx[np.arange(N), y] -= 1
    dx /= N
    return loss, dx

```



```

import numpy as np
from .layers import *
from .layer_utils import *

class TwoLayerNet(object):
    """
    A two-layer fully-connected neural network with ReLU nonlinearity and
    softmax loss that uses a modular layer design. We assume an input dimension
    of D, a hidden dimension of H, and perform classification over C classes.

    The architecture should be affine - relu - affine - softmax.

    Note that this class does not implement gradient descent; instead, it
    will interact with a separate Solver object that is responsible for running
    optimization.

    The learnable parameters of the model are stored in the dictionary
    self.params that maps parameter names to numpy arrays.
    """

    def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
                 dropout=0, weight_scale=1e-3, reg=0.0):
        """
        Initialize a new network.

        Inputs:
        - input_dim: An integer giving the size of the input
        - hidden_dims: An integer giving the size of the hidden layer
        - num_classes: An integer giving the number of classes to classify
        - dropout: Scalar between 0 and 1 giving dropout strength.
        - weight_scale: Scalar giving the standard deviation for random
          initialization of the weights.
        - reg: Scalar giving L2 regularization strength.
        """
        self.params = {}
        self.reg = reg

        # ===== #
        # YOUR CODE HERE:
        # Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
        # self.params['W2'], self.params['b1'] and self.params['b2']. The
        # biases are initialized to zero and the weights are initialized
        # so that each parameter has mean 0 and standard deviation weight_scale.
        # The dimensions of W1 should be (input_dim, hidden_dim) and the
        # dimensions of W2 should be (hidden_dims, num_classes)
        # ===== #

        # ===== #
        # END YOUR CODE HERE
        # ===== #

    def loss(self, X, y=None):
        """
        Compute loss and gradient for a minibatch of data.

        Inputs:
        - X: Array of input data of shape (N, d_1, ..., d_k)
        - y: Array of labels, of shape (N,). y[i] gives the label for X[i].

        Returns:
        If y is None, then run a test-time forward pass of the model and return:
        - scores: Array of shape (N, C) giving classification scores, where
          scores[i, c] is the classification score for X[i] and class c.

        If y is not None, then run a training-time forward and backward pass and
        return a tuple of:
        - loss: Scalar value giving the loss
        - grads: Dictionary with the same keys as self.params, mapping parameter
          names to gradients of the loss with respect to those parameters.
        """
        scores = None

        # ===== #
        # YOUR CODE HERE:
        # Implement the forward pass of the two-layer neural network. Store
        # the class scores as the variable 'scores'. Be sure to use the layers
        # you prior implemented.
        # ===== #

        # ===== #
        # END YOUR CODE HERE
        # ===== #

        # If y is None then we are in test mode so just return scores
        if y is None:
            return scores

        loss, grads = 0, {}
        # ===== #

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# YOUR CODE HERE:
# Implement the backward pass of the two-layer neural net. Store
# the loss as the variable 'loss' and store the gradients in the
# 'grads' dictionary. For the grads dictionary, grads['W1'] holds
# the gradient for W1, grads['b1'] holds the gradient for b1, etc.
# i.e., grads[k] holds the gradient for self.params[k].
#
# Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
# for each W. Be sure to include the 0.5 multiplying factor to
# match our implementation.
#
# And be sure to use the layers you prior implemented.
# ===== #

# ===== #
# END YOUR CODE HERE
# ===== #

return loss, grads

```

```
class FullyConnectedNet(object):
```

```

"""
A fully-connected neural network with an arbitrary number of hidden layers,
ReLU nonlinearities, and a softmax loss function. This will also implement
dropout and batch normalization as options. For a network with L layers,
the architecture will be

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```
{affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax
```

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where batch normalization and dropout are optional, and the {...} block is
repeated L - 1 times.

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```

Similar to the TwoLayerNet above, learnable parameters are stored in the
self.params dictionary and will be learned using the Solver class.
"""

```

```

def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
              dropout=0, use_batchnorm=False, reg=0.0,
              weight_scale=1e-2, dtype=np.float32, seed=None):

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    """
    Initialize a new FullyConnectedNet.

```

```
Inputs:
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- hidden_dims: A list of integers giving the size of each hidden layer.
- input_dim: An integer giving the size of the input.
- num_classes: An integer giving the number of classes to classify.
- dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then the network should not use dropout at all.
- use_batchnorm: Whether or not the network should use batch normalization.
- reg: Scalar giving L2 regularization strength.
- weight_scale: Scalar giving the standard deviation for random initialization of the weights.
- dtype: A numpy datatype object; all computations will be performed using this datatype. float32 is faster but less accurate, so you should use float64 for numeric gradient checking.
- seed: If not None, then pass this random seed to the dropout layers. This will make the dropout layers deterministic so we can gradient check the model.

```

    """
    self.use_batchnorm = use_batchnorm
    self.use_dropout = dropout > 0
    self.reg = reg
    self.num_layers = 1 + len(hidden_dims)
    self.dtype = dtype
    self.params = {}

```

```

# ===== #
# YOUR CODE HERE:
# Initialize all parameters of the network in the self.params dictionary.
# The weights and biases of layer 1 are W1 and b1; and in general the
# weights and biases of layer i are Wi and bi. The
# biases are initialized to zero and the weights are initialized
# so that each parameter has mean 0 and standard deviation weight_scale.
#
# BATCHNORM: Initialize the gammas of each layer to 1 and the beta
# parameters to zero. The gamma and beta parameters for layer 1 should
# be self.params['gamma1'] and self.params['beta1']. For layer 2, they
# should be gamma2 and beta2, etc. Only use batchnorm if self.use_batchnorm
# is true and DO NOT do batch normalize the output scores.
# ===== #

```

```

for i in range(0, self.num_layers):

    name_W = 'W'+str(i+1)
    name_b = 'b'+str(i+1)
    name_gamma = 'gamma' + str(i+1)
    name_beta = 'beta' + str(i+1)

    if i == 0: #First
        self.params[name_W] = np.random.normal(loc=0.0, scale=weight_scale, size = (input_dim, hidden_dims[i]))
        self.params[name_b] = np.zeros(hidden_dims[i])

```

```

        if self.use_batchnorm:
            self.params[name_gamma] = np.ones(hidden_dims[i])
            self.params[name_beta] = np.zeros(hidden_dims[i])

    elif i == self.num_layers-1:          #Last
        self.params[name_W] = np.random.normal(loc=0.0, scale=weight_scale, size = (hidden_dims[i-1], num_classes))
        self.params[name_b] = np.zeros(num_classes)

    else:                                  #Between
        self.params[name_W] = np.random.normal(loc=0.0, scale=weight_scale, size = (hidden_dims[i-1], hidden_dims[i]))
        self.params[name_b] = np.zeros(hidden_dims[i])
        if self.use_batchnorm:
            self.params[name_gamma] = np.ones(hidden_dims[i])
            self.params[name_beta] = np.zeros(hidden_dims[i])

# ===== #
# END YOUR CODE HERE
# ===== #

# When using dropout we need to pass a dropout_param dictionary to each
# dropout layer so that the layer knows the dropout probability and the mode
# (train / test). You can pass the same dropout_param to each dropout layer.
self.dropout_param = {}
if self.use_dropout:
    self.dropout_param = {'mode': 'train', 'p': dropout}
    if seed is not None:
        self.dropout_param['seed'] = seed

# With batch normalization we need to keep track of running means and
# variances, so we need to pass a special bn_param object to each batch
# normalization layer. You should pass self.bn_params[0] to the forward pass
# of the first batch normalization layer, self.bn_params[1] to the forward
# pass of the second batch normalization layer, etc.
self.bn_params = []
if self.use_batchnorm:
    self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]

# Cast all parameters to the correct datatype
for k, v in self.params.items():
    self.params[k] = v.astype(dtype)

def loss(self, X, y=None):
    """
    Compute loss and gradient for the fully-connected net.

    Input / output: Same as TwoLayerNet above.
    """
    X = X.astype(self.dtype)
    mode = 'test' if y is None else 'train'

    # Set train/test mode for batchnorm params and dropout param since they
    # behave differently during training and testing.
    if self.dropout_param is not None:
        self.dropout_param['mode'] = mode
    if self.use_batchnorm:
        for bn_param in self.bn_params:
            bn_param['mode'] = mode

    scores = None

    # ===== #
    # YOUR CODE HERE:
    # Implement the forward pass of the FC net and store the output
    # scores as the variable "scores".
    #
    # BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
    # between the affine_forward and relu_forward layers. You may
    # also write an affine_batchnorm_relu() function in layer_utils.py.
    #
    # DROPOUT: If dropout is non-zero, insert a dropout layer after
    # every ReLU layer.
    # ===== #

    affineCaches = {}
    reluCaches = {}
    batchnormCaches = {}
    dropoutCaches = {}

    x = X

    for i in range(self.num_layers - 1):
        digit = str(i+1)

        x, affineCaches[digit] = affine_forward(x, self.params['W' + digit], self.params['b' + digit])

        if self.use_batchnorm:
            x, batchnormCaches[digit] = batchnorm_forward(x, self.params['gamma' + digit],
                                                         self.params['beta' + digit],
                                                         self.bn_params[i])

        x, reluCaches[digit] = relu_forward(x=x)

```

```

        if self.use_dropout:
            x, dropoutCaches[digit] = dropout_forward(x, self.dropout_param)

# Last layer
digit = str(self.num_layers)
scores, affineCaches[digit] = affine_forward(x, self.params['W' + digit],
                                              self.params['b' + digit])

# ===== #
# END YOUR CODE HERE
# ===== #

# If test mode return early
if mode == 'test':
    return scores

loss, grads = 0.0, {}
# ===== #
# YOUR CODE HERE:
# Implement the backwards pass of the FC net and store the gradients
# in the grads dict, so that grads[k] is the gradient of self.params[k]
# Be sure your L2 regularization includes a 0.5 factor.
#
# BATCHNORM: Incorporate the backward pass of the batchnorm.
#
# DROPOUT: Incorporate the backward pass of dropout.
# ===== #
loss, dz = softmax_loss(scores, y)

for i in range(self.num_layers, 0, -1):
    name_W = 'W'+str(i)
    name_b = 'b'+str(i)
    name_gamma = "gamma" + str(i)
    name_beta = "beta" + str(i)
    loss = loss + (0.5 * self.reg * np.sum(self.params[name_W]*self.params[name_W]))

    if i == self.num_layers:
        dh1, grads[name_W], grads[name_b] = affine_backward(dz, affineCaches[str(i)])
    else:
        if self.use_dropout:
            dh1 = dropout_backward(dh1, dropoutCaches[str(i)])
        dh1 = relu_backward(dh1, reluCaches[str(i)])
        if self.use_batchnorm:
            dh1, grads[name_gamma], grads[name_beta] = batchnorm_backward(dh1, batchnormCaches[str(i)])

        dh1, grads[name_W], grads[name_b] = affine_backward(dh1, affineCaches[str(i)])

    grads[name_W] = grads[name_W] + self.reg * self.params[name_W]

# ===== #
# END YOUR CODE HERE
# ===== #

return loss, grads

```

ECE C147/247 HW4 Q1: Optimization for Fully Connected Networks

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

`utils` has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes `nndl.fc_net`, `nndl.layers`, and `nndl.layer_utils`.

```
In [1]: 1  ## Import and setups
2
3  import time
4  import numpy as np
5  import matplotlib.pyplot as plt
6  from nndl.fc_net import *
7  from utils.data_utils import get_CIFAR10_data
8  from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
9  from utils.solver import Solver
10
11  %matplotlib inline
12  plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
13  plt.rcParams['image.interpolation'] = 'nearest'
14  plt.rcParams['image.cmap'] = 'gray'
15
16  # for auto-reloading external modules
17  # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
18  %load_ext autoreload
19  %autoreload 2
20
21  def rel_error(x, y):
22      """ returns relative error """
23      return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In [2]: 1  # Load the (preprocessed) CIFAR10 data.
2
3  data = get_CIFAR10_data()
4  for k in data.keys():
5      print('{}: {}'.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Building upon your HW #3 implementation

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- `affine_forward` in `nndl/layers.py`
- `affine_backward` in `nndl/layers.py`
- `relu_forward` in `nndl/layers.py`
- `relu_backward` in `nndl/layers.py`
- `affine_relu_forward` in `nndl/layer_utils.py`
- `affine_relu_backward` in `nndl/layer_utils.py`
- The `FullyConnectedNet` class in `nndl/fc_net.py`

Test all functions you copy and pasted

```
In [3]: 1 from nndl.layer_tests import *
2
3 affine_forward_test(); print('\n')
4 affine_backward_test(); print('\n')
5 relu_forward_test(); print('\n')
6 relu_backward_test(); print('\n')
7 affine_relu_test(); print('\n')
8 fc_net_test()
```

If affine_forward function is working, difference should be less than 1e-9:
difference: 9.769849468192957e-10

If affine_backward is working, error should be less than 1e-9::
dx error: 5.246642069540149e-10
dw error: 8.048372280462124e-10
db error: 3.7351292805588654e-11

If relu_forward function is working, difference should be around 1e-8:
difference: 4.999999798022158e-08

If relu_backward function is working, error should be less than 1e-9:
dx error: 3.2756121353965686e-12

If affine_relu_forward and affine_relu_backward are working, error should be less than 1e-9::
dx error: 1.0001998447868336e-10
dw error: 3.885786623680586e-10
db error: 2.0961442676011905e-11

Running check with reg = 0
Initial loss: 2.302333457737979
W1 relative error: 2.1485973171293862e-07
W2 relative error: 2.793853357912559e-06
W3 relative error: 5.362626357167316e-07
b1 relative error: 1.3824475354603967e-08
b2 relative error: 7.459445301676694e-09
b3 relative error: 1.1620857419132297e-10
Running check with reg = 3.14
Initial loss: 6.904975427694904
W1 relative error: 1.3481465571937882e-08
W2 relative error: 2.1015983586447737e-08
W3 relative error: 8.384358255747746e-08
b1 relative error: 1.6606336514229584e-07
b2 relative error: 1.989370654837976e-09
b3 relative error: 1.7026842164264273e-10

Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

SGD + momentum

In the following section, implement SGD with momentum. Read the `nndl/optim.py` API, and be sure you understand it. After, implement `sgd_momentum` in `nndl/optim.py`. Test your implementation of `sgd_momentum` by running the cell below.

```
In [4]: 1 from nndl.optim import sgd_momentum
2
3 N, D = 4, 5
4 w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
5 dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
6 v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
7
8 config = {'learning_rate': 1e-3, 'velocity': v}
9 next_w, _ = sgd_momentum(w, dw, config=config)
10
11 expected_next_w = np.asarray([
12     [ 0.1406,      0.20738947,  0.27417895,  0.34096842,  0.40775789],
13     [ 0.47454737,  0.54133684,  0.60812632,  0.67491579,  0.74170526],
14     [ 0.80849474,  0.87528421,  0.94207368,  1.00886316,  1.07565263],
15     [ 1.14244211,  1.20923158,  1.27602105,  1.34281053,  1.4096      ]])
16 expected_velocity = np.asarray([
17     [ 0.5406,      0.55475789,  0.56891579,  0.58307368,  0.59723158],
18     [ 0.61138947,  0.62554737,  0.63970526,  0.65386316,  0.66802105],
19     [ 0.68217895,  0.69633684,  0.71049474,  0.72465263,  0.73881053],
20     [ 0.75296842,  0.76712632,  0.78128421,  0.79544211,  0.8096      ]])
21
22 print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
23 print('velocity error: {}'.format(rel_error(expected_velocity, config['velocity'])))
```

next_w error: 8.882347033505819e-09
velocity error: 4.269287743278663e-09

SGD + Nesterov momentum

Implement sgd_nesterov_momentum in nndl/optim.py .

```
In [5]: 1 from nndl.optim import sgd_nesterov_momentum
2
3 N, D = 4, 5
4 w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
5 dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
6 v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
7
8 config = {'learning_rate': 1e-3, 'velocity': v}
9 next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
10
11 expected_next_w = np.asarray([
12     [0.08714,      0.15246105,  0.21778211,  0.28310316,  0.34842421],
13     [0.41374526,  0.47906632,  0.54438737,  0.60970842,  0.67502947],
14     [0.74035053,  0.80567158,  0.87099263,  0.93631368,  1.00163474],
15     [1.06695579,  1.13227684,  1.19759789,  1.26291895,  1.32824      ]])
16 expected_velocity = np.asarray([
17     [ 0.5406,      0.55475789,  0.56891579,  0.58307368,  0.59723158],
18     [ 0.61138947,  0.62554737,  0.63970526,  0.65386316,  0.66802105],
19     [ 0.68217895,  0.69633684,  0.71049474,  0.72465263,  0.73881053],
20     [ 0.75296842,  0.76712632,  0.78128421,  0.79544211,  0.8096      ]])
21
22 print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
23 print('velocity error: {}'.format(rel_error(expected_velocity, config['velocity'])))
```

next_w error: 1.0875186845081027e-08
velocity error: 4.269287743278663e-09

Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.


```

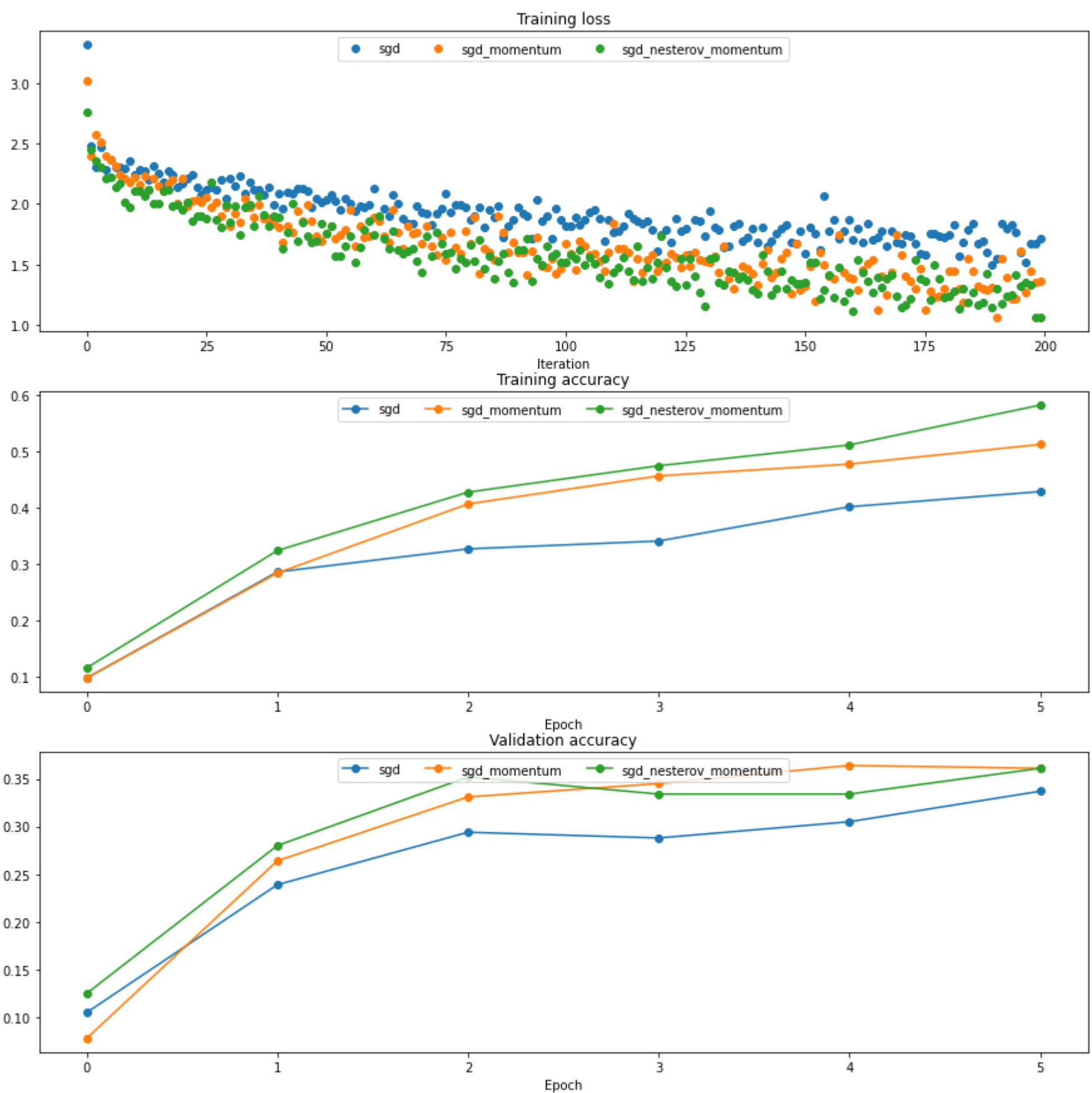
In [7]: 1 num_train = 4000
2 small_data = {
3     'X_train': data['X_train'][:num_train],
4     'y_train': data['y_train'][:num_train],
5     'X_val': data['X_val'],
6     'y_val': data['y_val'],
7 }
8
9 solvers = {}
10
11 for update_rule in ['sgd', 'sgd_momentum', 'sgd_nesterov_momentum']:
12     print('Optimizing with {}'.format(update_rule))
13     model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
14
15     solver = Solver(model, small_data,
16                     num_epochs=5, batch_size=100,
17                     update_rule=update_rule,
18                     optim_config={
19                         'learning_rate': 1e-2,
20                     },
21                     verbose=False)
22     solvers[update_rule] = solver
23     solver.train()
24     print
25
26     plt.subplot(3, 1, 1)
27     plt.title('Training loss')
28     plt.xlabel('Iteration')
29
30     plt.subplot(3, 1, 2)
31     plt.title('Training accuracy')
32     plt.xlabel('Epoch')
33
34     plt.subplot(3, 1, 3)
35     plt.title('Validation accuracy')
36     plt.xlabel('Epoch')
37
38     for update_rule, solver in solvers.items():
39         plt.subplot(3, 1, 1)
40         plt.plot(solver.loss_history, 'o', label=update_rule)
41
42         plt.subplot(3, 1, 2)
43         plt.plot(solver.train_acc_history, '-o', label=update_rule)
44
45         plt.subplot(3, 1, 3)
46         plt.plot(solver.val_acc_history, '-o', label=update_rule)
47
48     for i in [1, 2, 3]:
49         plt.subplot(3, 1, i)
50         plt.legend(loc='upper center', ncol=4)
51     plt.gcf().set_size_inches(15, 15)
52     plt.show()

```

Optimizing with sgd

Optimizing with sgd_momentum

Optimizing with sgd_nesterov_momentum



RMSProp

Now we go to techniques that adapt the gradient. Implement `rmsprop` in `nndl/optim.py`. Test your implementation by running the cell below.

```
In [6]: 1 from nndl.optim import rmsprop
2
3 N, D = 4, 5
4 w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
5 dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
6 a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
7
8 config = {'learning_rate': 1e-2, 'a': a}
9 next_w, _ = rmsprop(w, dw, config=config)
10
11 expected_next_w = np.asarray([
12     [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
13     [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
14     [0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
15     [0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
16 expected_cache = np.asarray([
17     [0.5976, 0.6126277, 0.6277108, 0.64284931, 0.65804321],
18     [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
19     [0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
20     [0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926]])
21
22 print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
23 print('cache error: {}'.format(rel_error(expected_cache, config['a'])))
```

next_w error: 9.524687511038133e-08

cache error: 2.6477955807156126e-09

Adaptive moments

Now, implement adam in nndl/optim.py . Test your implementation by running the cell below.

```
In [7]: 1 # Test Adam implementation; you should see errors around 1e-7 or Less
2 from nndl.optim import adam
3
4 N, D = 4, 5
5 w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
6 dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
7 v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
8 a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
9
10 config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
11 next_w, _ = adam(w, dw, config=config)
12
13 expected_next_w = np.asarray([
14     [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
15     [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
16     [ 0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
17     [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
18 expected_a = np.asarray([
19     [ 0.69966, 0.68908382, 0.67851319, 0.66794809, 0.65738853],
20     [ 0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385],
21     [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767],
22     [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
23 expected_v = np.asarray([
24     [ 0.48, 0.49947368, 0.51894737, 0.53842105, 0.55789474],
25     [ 0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],
26     [ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
27     [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85, ]])
28
29 print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
30 print('a error: {}'.format(rel_error(expected_a, config['a'])))
31 print('v error: {}'.format(rel_error(expected_v, config['v'])))
```

next_w error: 1.1395691798535431e-07

a error: 4.208314038113071e-09

v error: 4.214963193114416e-09

Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

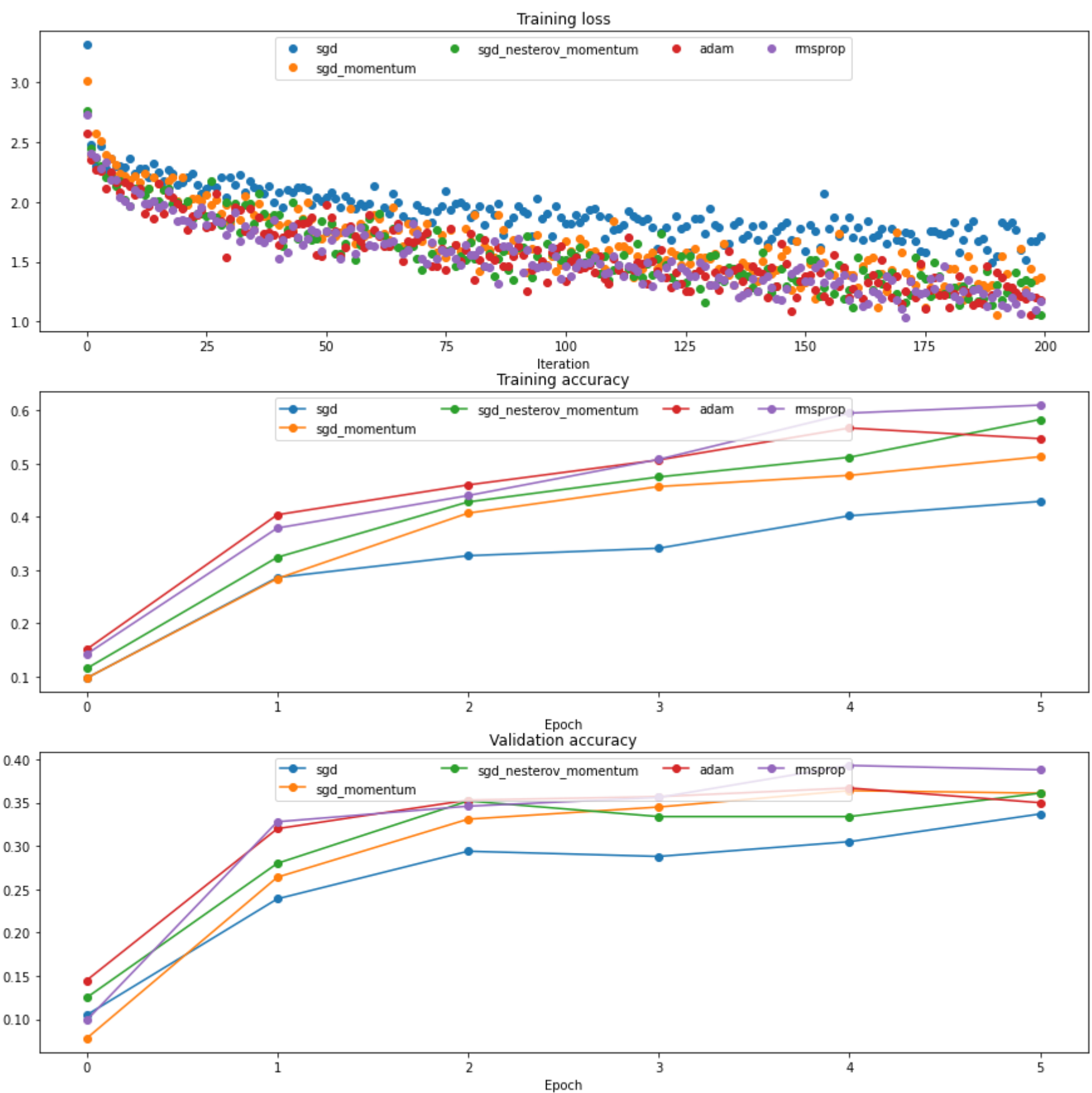
The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```

In [10]: 1 learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
2
3 for update_rule in ['adam', 'rmsprop']:
4     print('Optimizing with {}'.format(update_rule))
5     model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
6
7     solver = Solver(model, small_data,
8                     num_epochs=5, batch_size=100,
9                     update_rule=update_rule,
10                    optim_config={
11                        'learning_rate': learning_rates[update_rule]
12                    },
13                    verbose=False)
14     solvers[update_rule] = solver
15     solver.train()
16     print
17
18 plt.subplot(3, 1, 1)
19 plt.title('Training loss')
20 plt.xlabel('Iteration')
21
22 plt.subplot(3, 1, 2)
23 plt.title('Training accuracy')
24 plt.xlabel('Epoch')
25
26 plt.subplot(3, 1, 3)
27 plt.title('Validation accuracy')
28 plt.xlabel('Epoch')
29
30 for update_rule, solver in solvers.items():
31     plt.subplot(3, 1, 1)
32     plt.plot(solver.loss_history, 'o', label=update_rule)
33
34     plt.subplot(3, 1, 2)
35     plt.plot(solver.train_acc_history, '-o', label=update_rule)
36
37     plt.subplot(3, 1, 3)
38     plt.plot(solver.val_acc_history, '-o', label=update_rule)
39
40 for i in [1, 2, 3]:
41     plt.subplot(3, 1, i)
42     plt.legend(loc='upper center', ncol=4)
43 plt.gcf().set_size_inches(15, 15)
44 plt.show()

```

Optimizing with adam
 Optimizing with rmsprop



Easier optimization

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
In [11]: 1 optimizer = 'adam'
2 best_model = None
3
4 layer_dims = [500, 500, 500]
5 weight_scale = 0.01
6 learning_rate = 1e-3
7 lr_decay = 0.9
8
9 model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
10                             use_batchnorm=True)
11
12 solver = Solver(model, data,
13                 num_epochs=10, batch_size=100,
14                 update_rule=optimizer,
15                 optim_config={
16                     'learning_rate': learning_rate,
17                 },
18                 lr_decay=lr_decay,
19                 verbose=True, print_every=50)
20 solver.train()
```

```
(Iteration 1 / 4900) loss: 2.277610
(Epoch 0 / 10) train acc: 0.150000; val_acc: 0.145000
(Iteration 51 / 4900) loss: 1.880583
(Iteration 101 / 4900) loss: 1.648732
(Iteration 151 / 4900) loss: 1.618706
(Iteration 201 / 4900) loss: 1.840826
(Iteration 251 / 4900) loss: 1.514619
(Iteration 301 / 4900) loss: 1.592236
(Iteration 351 / 4900) loss: 1.660340
(Iteration 401 / 4900) loss: 1.556548
(Iteration 451 / 4900) loss: 1.584778
(Epoch 1 / 10) train acc: 0.419000; val_acc: 0.417000
(Iteration 501 / 4900) loss: 1.646061
(Iteration 551 / 4900) loss: 1.440946
(Iteration 601 / 4900) loss: 1.661109
(Iteration 651 / 4900) loss: 1.455983
(Iteration 701 / 4900) loss: 1.549595
(Iteration 751 / 4900) loss: 1.342097
(Iteration 801 / 4900) loss: 1.632072
(Iteration 851 / 4900) loss: 1.456956
(Iteration 901 / 4900) loss: 1.601276
(Iteration 951 / 4900) loss: 1.531880
(Epoch 2 / 10) train acc: 0.464000; val_acc: 0.457000
(Iteration 1001 / 4900) loss: 1.486822
(Iteration 1051 / 4900) loss: 1.345635
(Iteration 1101 / 4900) loss: 1.356986
(Iteration 1151 / 4900) loss: 1.558945
(Iteration 1201 / 4900) loss: 1.500665
(Iteration 1251 / 4900) loss: 1.413389
(Iteration 1301 / 4900) loss: 1.430202
(Iteration 1351 / 4900) loss: 1.413348
(Iteration 1401 / 4900) loss: 1.302355
(Iteration 1451 / 4900) loss: 1.397438
(Epoch 3 / 10) train acc: 0.505000; val_acc: 0.470000
(Iteration 1501 / 4900) loss: 1.397882
(Iteration 1551 / 4900) loss: 1.455172
(Iteration 1601 / 4900) loss: 1.336781
(Iteration 1651 / 4900) loss: 1.204578
(Iteration 1701 / 4900) loss: 1.426592
(Iteration 1751 / 4900) loss: 1.209779
(Iteration 1801 / 4900) loss: 1.342384
(Iteration 1851 / 4900) loss: 1.548075
(Iteration 1901 / 4900) loss: 1.458266
(Iteration 1951 / 4900) loss: 1.209324
(Epoch 4 / 10) train acc: 0.551000; val_acc: 0.512000
(Iteration 2001 / 4900) loss: 1.295164
(Iteration 2051 / 4900) loss: 1.074915
(Iteration 2101 / 4900) loss: 1.142226
(Iteration 2151 / 4900) loss: 1.276220
(Iteration 2201 / 4900) loss: 1.411585
(Iteration 2251 / 4900) loss: 1.759579
(Iteration 2301 / 4900) loss: 1.173279
(Iteration 2351 / 4900) loss: 1.104192
(Iteration 2401 / 4900) loss: 1.170074
(Epoch 5 / 10) train acc: 0.561000; val_acc: 0.511000
(Iteration 2451 / 4900) loss: 1.241937
(Iteration 2501 / 4900) loss: 1.263549
(Iteration 2551 / 4900) loss: 1.344454
(Iteration 2601 / 4900) loss: 1.324187
(Iteration 2651 / 4900) loss: 1.147330
(Iteration 2701 / 4900) loss: 1.082209
(Iteration 2751 / 4900) loss: 1.426252
(Iteration 2801 / 4900) loss: 1.045532
(Iteration 2851 / 4900) loss: 1.127736
(Iteration 2901 / 4900) loss: 1.107900
(Epoch 6 / 10) train acc: 0.581000; val_acc: 0.506000
(Iteration 2951 / 4900) loss: 1.011864
```

```

(Iteration 3001 / 4900) loss: 1.321638
(Iteration 3051 / 4900) loss: 0.991001
(Iteration 3101 / 4900) loss: 1.136626
(Iteration 3151 / 4900) loss: 0.927842
(Iteration 3201 / 4900) loss: 1.225016
(Iteration 3251 / 4900) loss: 1.182099
(Iteration 3301 / 4900) loss: 1.237375
(Iteration 3351 / 4900) loss: 1.163179
(Iteration 3401 / 4900) loss: 0.859012
(Epoch 7 / 10) train acc: 0.606000; val_acc: 0.554000
(Iteration 3451 / 4900) loss: 1.215511
(Iteration 3501 / 4900) loss: 1.230244
(Iteration 3551 / 4900) loss: 1.107438
(Iteration 3601 / 4900) loss: 1.184540
(Iteration 3651 / 4900) loss: 1.175141
(Iteration 3701 / 4900) loss: 1.010787
(Iteration 3751 / 4900) loss: 0.961439
(Iteration 3801 / 4900) loss: 0.902487
(Iteration 3851 / 4900) loss: 1.147918
(Iteration 3901 / 4900) loss: 1.140273
(Epoch 8 / 10) train acc: 0.627000; val_acc: 0.511000
(Iteration 3951 / 4900) loss: 1.272217
(Iteration 4001 / 4900) loss: 1.011301
(Iteration 4051 / 4900) loss: 0.892983
(Iteration 4101 / 4900) loss: 1.116623
(Iteration 4151 / 4900) loss: 1.102907
(Iteration 4201 / 4900) loss: 0.846823
(Iteration 4251 / 4900) loss: 1.039687
(Iteration 4301 / 4900) loss: 0.947278
(Iteration 4351 / 4900) loss: 0.927330
(Iteration 4401 / 4900) loss: 1.003371
(Epoch 9 / 10) train acc: 0.649000; val_acc: 0.544000
(Iteration 4451 / 4900) loss: 0.783613
(Iteration 4501 / 4900) loss: 0.888858
(Iteration 4551 / 4900) loss: 1.036669
(Iteration 4601 / 4900) loss: 0.898330
(Iteration 4651 / 4900) loss: 0.964396
(Iteration 4701 / 4900) loss: 0.979825
(Iteration 4751 / 4900) loss: 0.984760
(Iteration 4801 / 4900) loss: 0.790557
(Iteration 4851 / 4900) loss: 0.807668
(Epoch 10 / 10) train acc: 0.693000; val_acc: 0.560000

```

```

In [12]: 1 y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
          2 y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
          3 print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val'])))
          4 print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test'])))

```

```

Validation set accuracy: 0.56
Test set accuracy: 0.558

```

```

In [ ]: 1

```


ECE C147/247 HW4 Q2: Batch Normalization

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

`utils` has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes `nndl.fc_net` , `nndl.layers` , and `nndl.layer_utils` .

```
In [1]: 1  ## Import and setups
2
3  import time
4  import numpy as np
5  import matplotlib.pyplot as plt
6  from nndl.fc_net import *
7  from nndl.layers import *
8  from utils.data_utils import get_CIFAR10_data
9  from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
10 from utils.solver import Solver
11
12 %matplotlib inline
13 plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
14 plt.rcParams['image.interpolation'] = 'nearest'
15 plt.rcParams['image.cmap'] = 'gray'
16
17 # for auto-reloading external modules
18 # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
19 %load_ext autoreload
20 %autoreload 2
21
22 def rel_error(x, y):
23     """ returns relative error """
24     return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In [2]: 1  # Load the (preprocessed) CIFAR10 data.
2
3  data = get_CIFAR10_data()
4  for k in data.keys():
5      print('{}: {}'.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Batchnorm forward pass

Implement the training time batchnorm forward pass, `batchnorm_forward` , in `nndl/layers.py` . After that, test your implementation by running the following cell.

```
In [3]: 1 # Check the training-time forward pass by checking means and variances
2 # of features both before and after batch normalization
3
4 # Simulate the forward pass for a two-layer network
5 N, D1, D2, D3 = 200, 50, 60, 3
6 X = np.random.randn(N, D1)
7 W1 = np.random.randn(D1, D2)
8 W2 = np.random.randn(D2, D3)
9 a = np.maximum(0, X.dot(W1)).dot(W2)
10
11 print('Before batch normalization:')
12 print(' means: ', a.mean(axis=0))
13 print(' stds: ', a.std(axis=0))
14
15 # Means should be close to zero and stds close to one
16 print('After batch normalization (gamma=1, beta=0)')
17 a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'})
18 print(' mean: ', a_norm.mean(axis=0))
19 print(' std: ', a_norm.std(axis=0))
20
21 # Now means should be close to beta and stds close to gamma
22 gamma = np.asarray([1.0, 2.0, 3.0])
23 beta = np.asarray([11.0, 12.0, 13.0])
24 a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
25 print('After batch normalization (nontrivial gamma, beta)')
26 print(' means: ', a_norm.mean(axis=0))
27 print(' stds: ', a_norm.std(axis=0))
```

Before batch normalization:

```
means: [ 0.97229703 -4.37220457 64.75723456]
stds: [35.07244248 30.59655442 31.87113806]
```

After batch normalization (gamma=1, beta=0)

```
mean: [-1.11022302e-18 -5.77315973e-17 1.46216372e-15]
std: [1. 0.99999999 1.]
```

After batch normalization (nontrivial gamma, beta)

```
means: [11. 12. 13.]
stds: [1. 1.99999999 2.99999999]
```

Implement the testing time batchnorm forward pass, `batchnorm_forward`, in `nnd1/layers.py`. After that, test your implementation by running the following cell.

```
In [4]: 1 # Check the test-time forward pass by running the training-time
2 # forward pass many times to warm up the running averages, and then
3 # checking the means and variances of activations after a test-time
4 # forward pass.
5
6 N, D1, D2, D3 = 200, 50, 60, 3
7 W1 = np.random.randn(D1, D2)
8 W2 = np.random.randn(D2, D3)
9
10 bn_param = {'mode': 'train'}
11 gamma = np.ones(D3)
12 beta = np.zeros(D3)
13 for t in np.arange(50):
14     X = np.random.randn(N, D1)
15     a = np.maximum(0, X.dot(W1)).dot(W2)
16     batchnorm_forward(a, gamma, beta, bn_param)
17 bn_param['mode'] = 'test'
18 X = np.random.randn(N, D1)
19 a = np.maximum(0, X.dot(W1)).dot(W2)
20 a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)
21
22 # Means should be close to zero and stds close to one, but will be
23 # noisier than training-time forward passes.
24 print('After batch normalization (test-time):')
25 print(' means: ', a_norm.mean(axis=0))
26 print(' stds: ', a_norm.std(axis=0))
```

After batch normalization (test-time):

```
means: [-0.06327981 0.12483773 -0.04309278]
stds: [0.99684813 1.00491231 0.95546175]
```

Batchnorm backward pass

Implement the backward pass for the batchnorm layer, `batchnorm_backward` in `nnd1/layers.py`. Check your implementation by running the following cell.


```
In [5]: 1 # Gradient check batchnorm backward pass
2
3 N, D = 4, 5
4 x = 5 * np.random.randn(N, D) + 12
5 gamma = np.random.randn(D)
6 beta = np.random.randn(D)
7 dout = np.random.randn(N, D)
8
9 bn_param = {'mode': 'train'}
10 fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
11 fg = lambda a: batchnorm_forward(x, gamma, beta, bn_param)[0]
12 fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0]
13
14 dx_num = eval_numerical_gradient_array(fx, x, dout)
15 da_num = eval_numerical_gradient_array(fg, gamma, dout)
16 db_num = eval_numerical_gradient_array(fb, beta, dout)
17
18 _, cache = batchnorm_forward(x, gamma, beta, bn_param)
19 dx, dgamma, dbeta = batchnorm_backward(dout, cache)
20 print('dx error: ', rel_error(dx_num, dx))
21 print('dgamma error: ', rel_error(da_num, dgamma))
22 print('dbeta error: ', rel_error(db_num, dbeta))
```

```
dx error: 4.1852571583840105e-10
dgamma error: 9.248925423825707e-12
dbeta error: 4.4945335347653755e-12
```

Implement a fully connected neural network with batchnorm layers

Modify the `FullyConnectedNet()` class in `nnd1/fc_net.py` to incorporate batchnorm layers. You will need to modify the class in the following areas:

(1) The gammas and betas need to be initialized to 1's and 0's respectively in `__init__`.

(2) The `batchnorm_forward` layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in `loss`. You may find it helpful to write an `affine_batchnorm_relu()` layer in `nnd1/layer_utils.py` although this is not necessary.

(3) The `batchnorm_backward` layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of $1e-4$.

In [10]:

```

1 N, D, H1, H2, C = 2, 15, 20, 30, 10
2 X = np.random.randn(N, D)
3 y = np.random.randint(C, size=(N,))
4
5 for reg in [0, 3.14]:
6     print('Running check with reg = ', reg)
7     model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
8                               reg=reg, weight_scale=5e-2, dtype=np.float64,
9                               use_batchnorm=True)
10
11     loss, grads = model.loss(X, y)
12     print('Initial loss: ', loss)
13
14     for name in sorted(grads):
15         f = lambda _: model.loss(X, y)[0]
16         grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
17         print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
18     if reg == 0: print('\n')

```

```

Running check with reg = 0
Initial loss: 2.2399169009694386
W1 relative error: 9.880545613497872e-05
W2 relative error: 4.812972643791644e-06
W3 relative error: 5.8941794810581e-10
b1 relative error: 4.440892098500626e-08
b2 relative error: 2.4424906541753444e-07
b3 relative error: 8.036774155463346e-11
beta1 relative error: 2.8628873871209945e-09
beta2 relative error: 2.706002921523907e-09
gamma1 relative error: 2.7926177902806765e-09
gamma2 relative error: 6.9193573744554835e-09

```

```

Running check with reg = 3.14
Initial loss: 7.516299496155865
W1 relative error: 1.0721254128132533e-07
W2 relative error: 7.660934490494965e-06
W3 relative error: 1.490428880730247e-08
b1 relative error: 8.673617379884035e-10
b2 relative error: 2.7755575615628914e-08
b3 relative error: 2.7472477246842416e-10
beta1 relative error: 2.645056378917004e-07
beta2 relative error: 7.525803721192497e-08
gamma1 relative error: 9.348466443027856e-07
gamma2 relative error: 1.368030853566093e-07

```

Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```

In [12]: 1 # Try training a very deep net with batchnorm
2 hidden_dims = [100, 100, 100, 100, 100]
3
4 num_train = 1000
5 small_data = {
6     'X_train': data['X_train'][:num_train],
7     'y_train': data['y_train'][:num_train],
8     'X_val': data['X_val'],
9     'y_val': data['y_val'],
10 }
11
12 weight_scale = 2e-2
13 bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True)
14 model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False)
15
16 bn_solver = Solver(bn_model, small_data,
17                     num_epochs=10, batch_size=50,
18                     update_rule='adam',
19                     optim_config={
20                         'learning_rate': 1e-3,
21                     },
22                     verbose=True, print_every=200)
23 bn_solver.train()
24
25 solver = Solver(model, small_data,
26                 num_epochs=10, batch_size=50,
27                 update_rule='adam',
28                 optim_config={
29                     'learning_rate': 1e-3,
30                 },
31                 verbose=True, print_every=200)
32 solver.train()

```

```

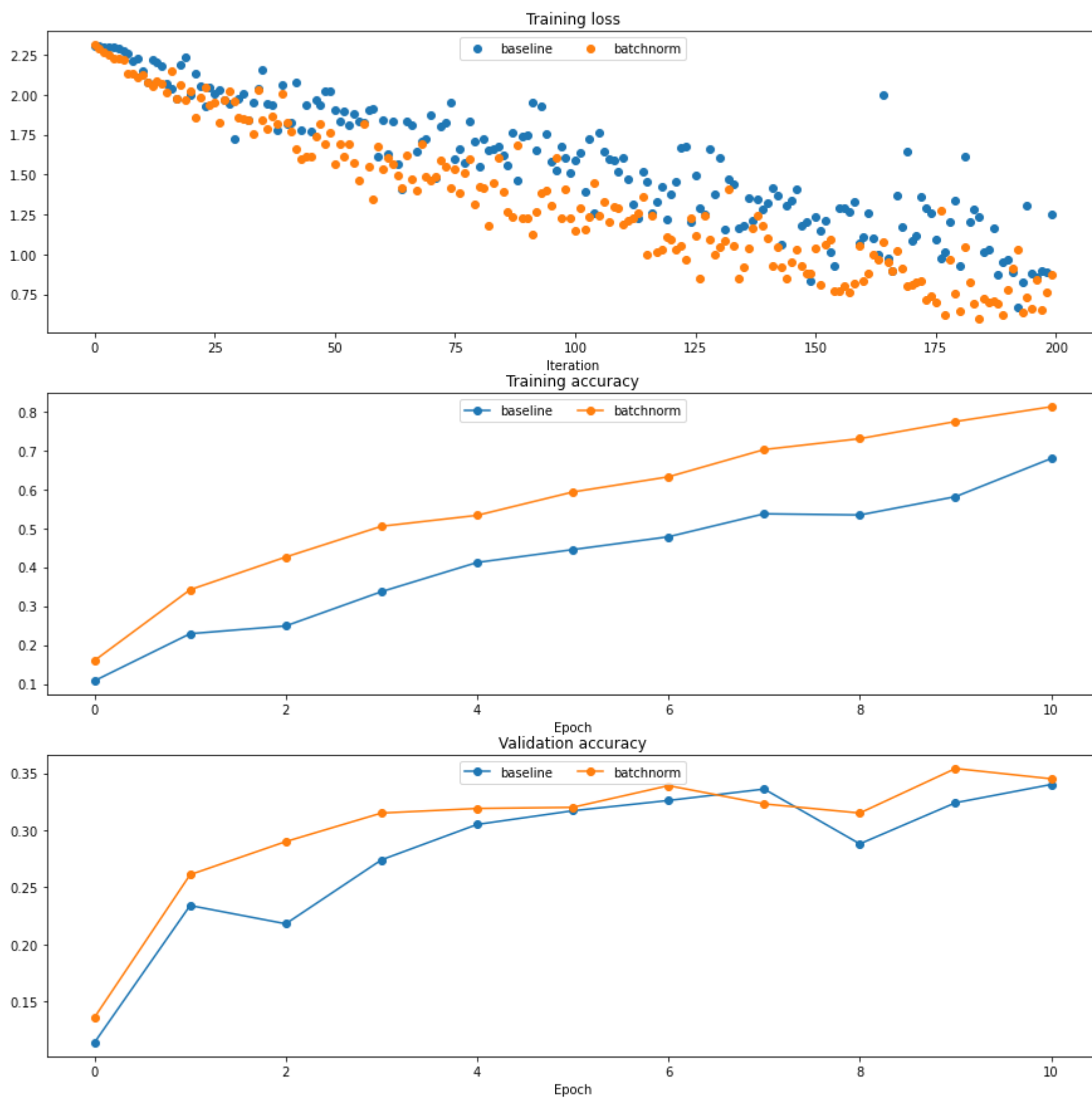
(Iteration 1 / 200) loss: 2.311343
(Epoch 0 / 10) train acc: 0.160000; val_acc: 0.136000
(Epoch 1 / 10) train acc: 0.342000; val_acc: 0.261000
(Epoch 2 / 10) train acc: 0.426000; val_acc: 0.290000
(Epoch 3 / 10) train acc: 0.505000; val_acc: 0.315000
(Epoch 4 / 10) train acc: 0.533000; val_acc: 0.319000
(Epoch 5 / 10) train acc: 0.593000; val_acc: 0.320000
(Epoch 6 / 10) train acc: 0.632000; val_acc: 0.339000
(Epoch 7 / 10) train acc: 0.702000; val_acc: 0.323000
(Epoch 8 / 10) train acc: 0.730000; val_acc: 0.315000
(Epoch 9 / 10) train acc: 0.774000; val_acc: 0.354000
(Epoch 10 / 10) train acc: 0.812000; val_acc: 0.345000
(Iteration 1 / 200) loss: 2.302660
(Epoch 0 / 10) train acc: 0.108000; val_acc: 0.114000
(Epoch 1 / 10) train acc: 0.229000; val_acc: 0.234000
(Epoch 2 / 10) train acc: 0.249000; val_acc: 0.218000
(Epoch 3 / 10) train acc: 0.337000; val_acc: 0.274000
(Epoch 4 / 10) train acc: 0.412000; val_acc: 0.305000
(Epoch 5 / 10) train acc: 0.445000; val_acc: 0.317000
(Epoch 6 / 10) train acc: 0.478000; val_acc: 0.326000
(Epoch 7 / 10) train acc: 0.537000; val_acc: 0.336000
(Epoch 8 / 10) train acc: 0.534000; val_acc: 0.288000
(Epoch 9 / 10) train acc: 0.581000; val_acc: 0.324000
(Epoch 10 / 10) train acc: 0.679000; val_acc: 0.340000

```

```

In [13]: 1 plt.subplot(3, 1, 1)
2 plt.title('Training loss')
3 plt.xlabel('Iteration')
4
5 plt.subplot(3, 1, 2)
6 plt.title('Training accuracy')
7 plt.xlabel('Epoch')
8
9 plt.subplot(3, 1, 3)
10 plt.title('Validation accuracy')
11 plt.xlabel('Epoch')
12
13 plt.subplot(3, 1, 1)
14 plt.plot(solver.loss_history, 'o', label='baseline')
15 plt.plot(bn_solver.loss_history, 'o', label='batchnorm')
16
17 plt.subplot(3, 1, 2)
18 plt.plot(solver.train_acc_history, '-o', label='baseline')
19 plt.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
20
21 plt.subplot(3, 1, 3)
22 plt.plot(solver.val_acc_history, '-o', label='baseline')
23 plt.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
24
25 for i in [1, 2, 3]:
26     plt.subplot(3, 1, i)
27     plt.legend(loc='upper center', ncol=4)
28 plt.gcf().set_size_inches(15, 15)
29 plt.show()

```



Batchnorm and initialization

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
In [14]: 1 # Try training a very deep net with batchnorm
2 hidden_dims = [50, 50, 50, 50, 50, 50, 50]
3
4 num_train = 1000
5 small_data = {
6     'X_train': data['X_train'][:num_train],
7     'y_train': data['y_train'][:num_train],
8     'X_val': data['X_val'],
9     'y_val': data['y_val'],
10 }
11
12 bn_solvers = {}
13 solvers = {}
14 weight_scales = np.logspace(-4, 0, num=20)
15 for i, weight_scale in enumerate(weight_scales):
16     print('Running weight scale {} / {}'.format(i + 1, len(weight_scales)))
17     bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True)
18     model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False)
19
20     bn_solver = Solver(bn_model, small_data,
21                        num_epochs=10, batch_size=50,
22                        update_rule='adam',
23                        optim_config={
24                            'learning_rate': 1e-3,
25                        },
26                        verbose=False, print_every=200)
27     bn_solver.train()
28     bn_solvers[weight_scale] = bn_solver
29
30     solver = Solver(model, small_data,
31                     num_epochs=10, batch_size=50,
32                     update_rule='adam',
33                     optim_config={
34                         'learning_rate': 1e-3,
35                     },
36                     verbose=False, print_every=200)
37     solver.train()
38     solvers[weight_scale] = solver
```

```
Running weight scale 1 / 20
Running weight scale 2 / 20
Running weight scale 3 / 20
Running weight scale 4 / 20
Running weight scale 5 / 20
Running weight scale 6 / 20
Running weight scale 7 / 20
Running weight scale 8 / 20
Running weight scale 9 / 20
Running weight scale 10 / 20
Running weight scale 11 / 20
Running weight scale 12 / 20
Running weight scale 13 / 20
Running weight scale 14 / 20
Running weight scale 15 / 20
Running weight scale 16 / 20
```

C:\Users\orkun\Desktop\UCLA Courses\Deep Learning\HW4\hw4-code\nndl\layers.py:425: RuntimeWarning: divide by zero encountered in log

```
loss = -np.sum(np.log(probs[np.arange(N), y])) / N
```

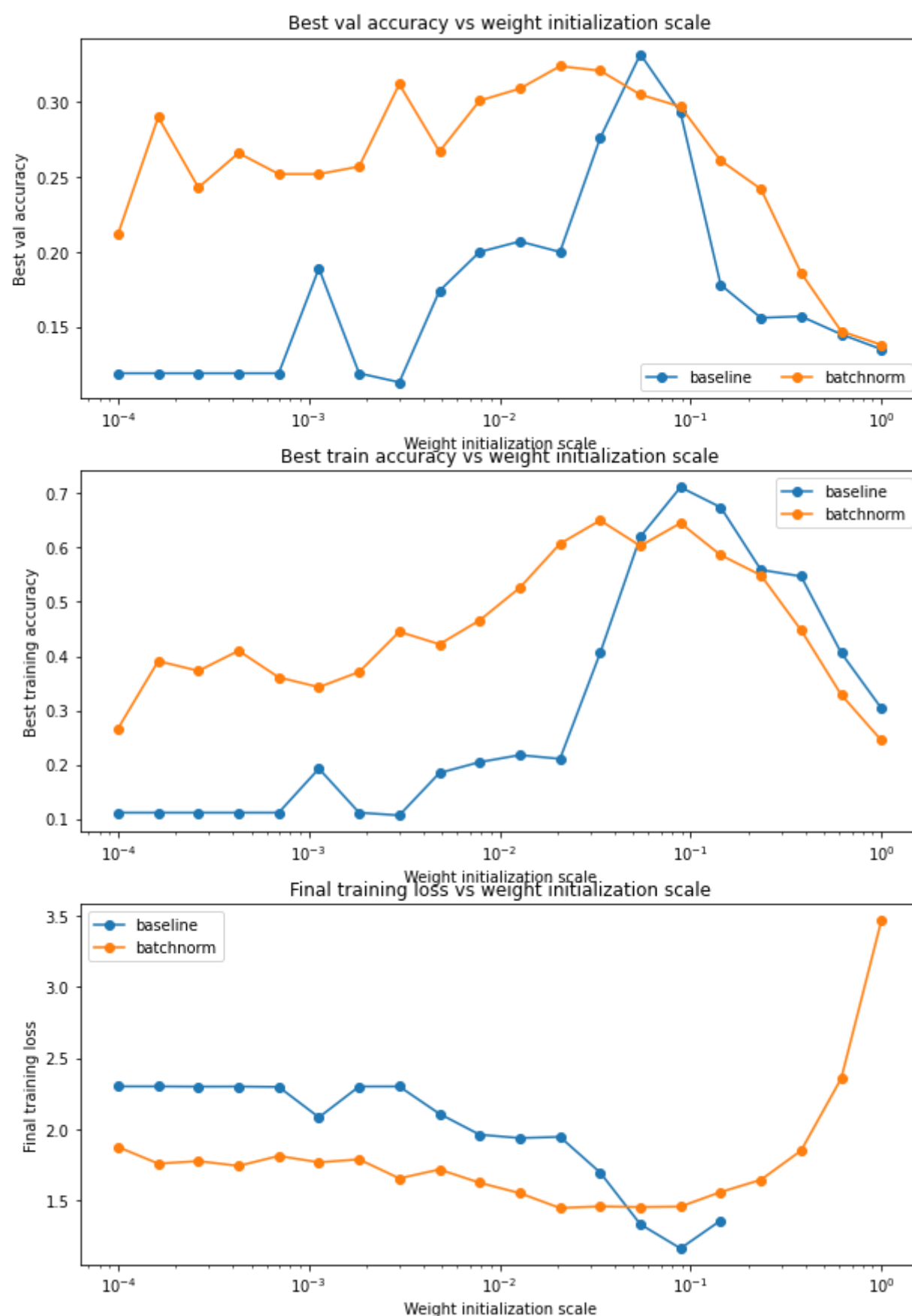
```
Running weight scale 17 / 20
Running weight scale 18 / 20
Running weight scale 19 / 20
Running weight scale 20 / 20
```

In [15]:

```

1  # Plot results of weight scale experiment
2  best_train_accs, bn_best_train_accs = [], []
3  best_val_accs, bn_best_val_accs = [], []
4  final_train_loss, bn_final_train_loss = [], []
5
6  for ws in weight_scales:
7      best_train_accs.append(max(solvers[ws].train_acc_history))
8      bn_best_train_accs.append(max(bn_solvers[ws].train_acc_history))
9
10     best_val_accs.append(max(solvers[ws].val_acc_history))
11     bn_best_val_accs.append(max(bn_solvers[ws].val_acc_history))
12
13     final_train_loss.append(np.mean(solvers[ws].loss_history[-100:]))
14     bn_final_train_loss.append(np.mean(bn_solvers[ws].loss_history[-100:]))
15
16  plt.subplot(3, 1, 1)
17  plt.title('Best val accuracy vs weight initialization scale')
18  plt.xlabel('Weight initialization scale')
19  plt.ylabel('Best val accuracy')
20  plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
21  plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
22  plt.legend(ncol=2, loc='lower right')
23
24  plt.subplot(3, 1, 2)
25  plt.title('Best train accuracy vs weight initialization scale')
26  plt.xlabel('Weight initialization scale')
27  plt.ylabel('Best training accuracy')
28  plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
29  plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
30  plt.legend()
31
32  plt.subplot(3, 1, 3)
33  plt.title('Final training loss vs weight initialization scale')
34  plt.xlabel('Weight initialization scale')
35  plt.ylabel('Final training loss')
36  plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
37  plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm')
38  plt.legend()
39
40  plt.gcf().set_size_inches(10, 15)
41  plt.show()

```



Question:

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

Answer:

From the figures, we see that the performance of the model when batch normalization is utilized is less dependant on weight initializations when compared to the baseline model. For most of the different weight initializations, the performance for the model that uses batch normalization is observed to be better than the other model, with less change in performance for different initializations. On the other hand, the baseline model performs poorly for most of the initializations and there is a high fluctuation in performance with different initializations. This is expected, since as we learned in class, batch normalization decreases the model's sensitivity to weight initializations. This is because when batch normalization is used, the input to the next layer has the same distributions during training, which means that the effect the scale of the weights has on the output is minimized.

In []:

1

ECE C147/247 HW4 Q3: Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and achieve over 55% accuracy on CIFAR-10.

`utils` has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes `nndl.fc_net`, `nndl.layers`, and `nndl.layer_utils`.

```
In [1]: 1  ## Import and setups
2
3  import time
4  import numpy as np
5  import matplotlib.pyplot as plt
6  from nndl.fc_net import *
7  from nndl.layers import *
8  from utils.data_utils import get_CIFAR10_data
9  from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
10 from utils.solver import Solver
11
12 %matplotlib inline
13 plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
14 plt.rcParams['image.interpolation'] = 'nearest'
15 plt.rcParams['image.cmap'] = 'gray'
16
17 # for auto-reloading external modules
18 # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
19 %load_ext autoreload
20 %autoreload 2
21
22 def rel_error(x, y):
23     """ returns relative error """
24     return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In [2]: 1  # Load the (preprocessed) CIFAR10 data.
2
3  data = get_CIFAR10_data()
4  for k in data.keys():
5      print('{}: {}'.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, `dropout_forward`, in `nndl/layers.py`. After that, test your implementation by running the following cell.


```
In [3]: 1 x = np.random.randn(500, 500) + 10
2
3 for p in [0.3, 0.6, 0.75]:
4     out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
5     out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})
6
7     print('Running tests with p = ', p)
8     print('Mean of input: ', x.mean())
9     print('Mean of train-time output: ', out.mean())
10    print('Mean of test-time output: ', out_test.mean())
11    print('Fraction of train-time output set to zero: ', (out == 0).mean())
12    print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
```

```
Running tests with p = 0.3
Mean of input: 10.000869762098812
Mean of train-time output: 10.008144829587012
Mean of test-time output: 10.000869762098812
Fraction of train-time output set to zero: 0.699764
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.6
Mean of input: 10.000869762098812
Mean of train-time output: 10.02942410584371
Mean of test-time output: 10.000869762098812
Fraction of train-time output set to zero: 0.398184
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.75
Mean of input: 10.000869762098812
Mean of train-time output: 10.010225631186525
Mean of test-time output: 10.000869762098812
Fraction of train-time output set to zero: 0.249352
Fraction of test-time output set to zero: 0.0
```

Dropout backward pass

Implement the backward pass, `dropout_backward`, in `nndl/layers.py`. After that, test your gradients by running the following cell:

```
In [3]: 1 x = np.random.randn(10, 10) + 10
2 dout = np.random.randn(*x.shape)
3
4 dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
5 out, cache = dropout_forward(x, dropout_param)
6 dx = dropout_backward(dout, cache)
7 dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param)[0], x, dout)
8
9 print('dx relative error: ', rel_error(dx, dx_num))
```

```
dx relative error: 5.4456097039628486e-11
```

Implement a fully connected neural network with dropout layers

Modify the `FullyConnectedNet()` class in `nndl/fc_net.py` to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

(1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.

(2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of $1e-6$ (the largest of all the relative errors).

```
In [4]: 1 N, D, H1, H2, C = 2, 15, 20, 30, 10
2 X = np.random.randn(N, D)
3 y = np.random.randint(C, size=(N,))
4
5 for dropout in [0, 0.25, 0.5]:
6     print('Running check with dropout = ', dropout)
7     model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
8                               weight_scale=5e-2, dtype=np.float64,
9                               dropout=dropout, seed=123)
10
11     loss, grads = model.loss(X, y)
12     print('Initial loss: ', loss)
13
14     for name in sorted(grads):
15         f = lambda _: model.loss(X, y)[0]
16         grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
17         print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
18     print('\n')
```

```
Running check with dropout = 0
Initial loss: 2.3051948273987857
W1 relative error: 2.5272575344376073e-07
W2 relative error: 1.5034484929313676e-05
W3 relative error: 2.753446833630168e-07
b1 relative error: 2.936957476400148e-06
b2 relative error: 5.051339805546953e-08
b3 relative error: 1.1740467838205477e-10
```

```
Running check with dropout = 0.25
Initial loss: 2.3126468345657742
W1 relative error: 1.483854795975875e-08
W2 relative error: 2.3427832149940254e-10
W3 relative error: 3.564454999162522e-08
b1 relative error: 1.5292167232408546e-09
b2 relative error: 1.842268868410678e-10
b3 relative error: 1.4026015558098908e-10
```

```
Running check with dropout = 0.5
Initial loss: 2.302437587710995
W1 relative error: 4.553387957138422e-08
W2 relative error: 2.974218050584597e-08
W3 relative error: 4.3413247403122424e-07
b1 relative error: 1.872462967441693e-08
b2 relative error: 5.045591219274328e-09
b3 relative error: 8.009887154529434e-11
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```

In [7]: 1 # Train two identical nets, one with dropout and one without
2
3 num_train = 500
4 small_data = {
5     'X_train': data['X_train'][:num_train],
6     'y_train': data['y_train'][:num_train],
7     'X_val': data['X_val'],
8     'y_val': data['y_val'],
9 }
10
11 solvers = {}
12 dropout_choices = [0, 0.6]
13 for dropout in dropout_choices:
14     model = FullyConnectedNet([100, 100, 100], dropout=dropout)
15
16     solver = Solver(model, small_data,
17                     num_epochs=25, batch_size=100,
18                     update_rule='adam',
19                     optim_config={
20                         'learning_rate': 5e-4,
21                     },
22                     verbose=True, print_every=100)
23     solver.train()
24     solvers[dropout] = solver

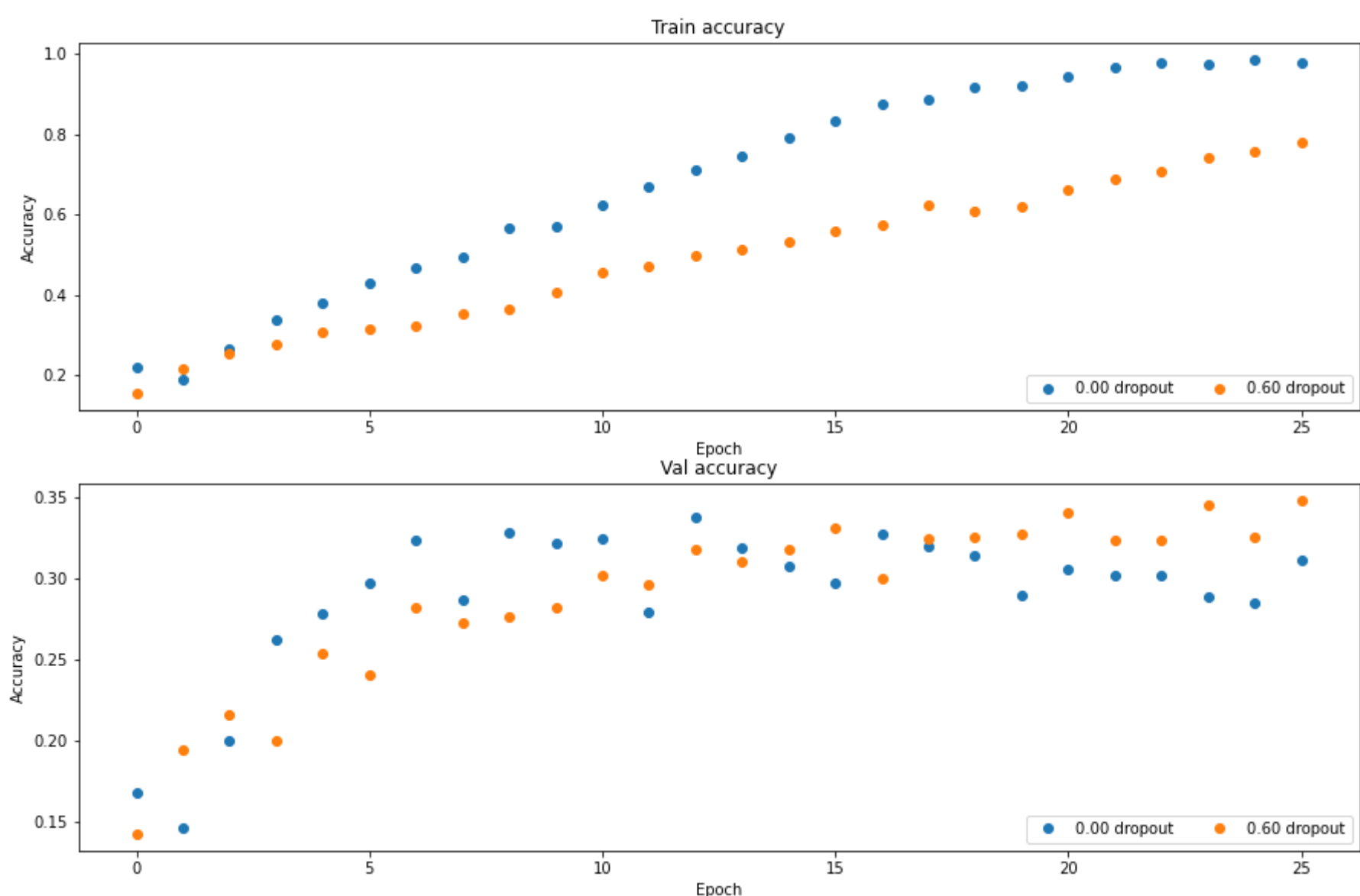
```

```

(Iteration 1 / 125) loss: 2.300804
(Epoch 0 / 25) train acc: 0.220000; val_acc: 0.168000
(Epoch 1 / 25) train acc: 0.188000; val_acc: 0.147000
(Epoch 2 / 25) train acc: 0.266000; val_acc: 0.200000
(Epoch 3 / 25) train acc: 0.338000; val_acc: 0.262000
(Epoch 4 / 25) train acc: 0.378000; val_acc: 0.278000
(Epoch 5 / 25) train acc: 0.428000; val_acc: 0.297000
(Epoch 6 / 25) train acc: 0.468000; val_acc: 0.323000
(Epoch 7 / 25) train acc: 0.494000; val_acc: 0.287000
(Epoch 8 / 25) train acc: 0.566000; val_acc: 0.328000
(Epoch 9 / 25) train acc: 0.572000; val_acc: 0.322000
(Epoch 10 / 25) train acc: 0.622000; val_acc: 0.324000
(Epoch 11 / 25) train acc: 0.670000; val_acc: 0.279000
(Epoch 12 / 25) train acc: 0.710000; val_acc: 0.338000
(Epoch 13 / 25) train acc: 0.746000; val_acc: 0.319000
(Epoch 14 / 25) train acc: 0.792000; val_acc: 0.307000
(Epoch 15 / 25) train acc: 0.834000; val_acc: 0.297000
(Epoch 16 / 25) train acc: 0.876000; val_acc: 0.327000
(Epoch 17 / 25) train acc: 0.886000; val_acc: 0.320000
(Epoch 18 / 25) train acc: 0.918000; val_acc: 0.314000
(Epoch 19 / 25) train acc: 0.922000; val_acc: 0.290000
(Epoch 20 / 25) train acc: 0.944000; val_acc: 0.306000
(Iteration 101 / 125) loss: 0.156105
(Epoch 21 / 25) train acc: 0.968000; val_acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val_acc: 0.302000
(Epoch 23 / 25) train acc: 0.976000; val_acc: 0.289000
(Epoch 24 / 25) train acc: 0.986000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.978000; val_acc: 0.311000
(Iteration 1 / 125) loss: 2.301328
(Epoch 0 / 25) train acc: 0.154000; val_acc: 0.143000
(Epoch 1 / 25) train acc: 0.214000; val_acc: 0.195000
(Epoch 2 / 25) train acc: 0.252000; val_acc: 0.216000
(Epoch 3 / 25) train acc: 0.276000; val_acc: 0.200000
(Epoch 4 / 25) train acc: 0.308000; val_acc: 0.254000
(Epoch 5 / 25) train acc: 0.316000; val_acc: 0.241000
(Epoch 6 / 25) train acc: 0.322000; val_acc: 0.282000
(Epoch 7 / 25) train acc: 0.354000; val_acc: 0.273000
(Epoch 8 / 25) train acc: 0.364000; val_acc: 0.276000
(Epoch 9 / 25) train acc: 0.408000; val_acc: 0.282000
(Epoch 10 / 25) train acc: 0.454000; val_acc: 0.302000
(Epoch 11 / 25) train acc: 0.472000; val_acc: 0.296000
(Epoch 12 / 25) train acc: 0.496000; val_acc: 0.318000
(Epoch 13 / 25) train acc: 0.512000; val_acc: 0.310000
(Epoch 14 / 25) train acc: 0.532000; val_acc: 0.318000
(Epoch 15 / 25) train acc: 0.558000; val_acc: 0.331000
(Epoch 16 / 25) train acc: 0.574000; val_acc: 0.300000
(Epoch 17 / 25) train acc: 0.624000; val_acc: 0.324000
(Epoch 18 / 25) train acc: 0.610000; val_acc: 0.325000
(Epoch 19 / 25) train acc: 0.620000; val_acc: 0.327000
(Epoch 20 / 25) train acc: 0.662000; val_acc: 0.340000
(Iteration 101 / 125) loss: 1.296187
(Epoch 21 / 25) train acc: 0.688000; val_acc: 0.323000
(Epoch 22 / 25) train acc: 0.708000; val_acc: 0.323000
(Epoch 23 / 25) train acc: 0.742000; val_acc: 0.345000
(Epoch 24 / 25) train acc: 0.756000; val_acc: 0.325000
(Epoch 25 / 25) train acc: 0.782000; val_acc: 0.348000

```

```
In [8]: 1 # Plot train and validation accuracies of the two models
2
3 train_accs = []
4 val_accs = []
5 for dropout in dropout_choices:
6     solver = solvers[dropout]
7     train_accs.append(solver.train_acc_history[-1])
8     val_accs.append(solver.val_acc_history[-1])
9
10 plt.subplot(3, 1, 1)
11 for dropout in dropout_choices:
12     plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropout)
13 plt.title('Train accuracy')
14 plt.xlabel('Epoch')
15 plt.ylabel('Accuracy')
16 plt.legend(ncol=2, loc='lower right')
17
18 plt.subplot(3, 1, 2)
19 for dropout in dropout_choices:
20     plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout)
21 plt.title('Val accuracy')
22 plt.xlabel('Epoch')
23 plt.ylabel('Accuracy')
24 plt.legend(ncol=2, loc='lower right')
25
26 plt.gcf().set_size_inches(15, 15)
27 plt.show()
```



Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

Answer:

By examining the plots of the accuracy for both validation and training data, we can conclude that dropout is performing regularization. If we look at the graph when dropout is not used, we can see that the final training accuracy is around 1 while the validation accuracy is around 0.3. This clearly indicates that the model has overfit to the training data. On the other hand, we can see that when dropout is used, the final training accuracy is around 0.8 while the final validation accuracy is around 0.35. From here, we can infer that when dropout is utilized, the discrepancy between the performance on training and validation data is lessened, indicating that the model is less likely to overfit. So, we can conclude that dropout serves as a method of regularization.

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

$$\min(\text{floor}((X - 32\%)) / 28\%, 1)$$

where if you get 60% or higher validation accuracy, you get full points.

In [19]:

```

1  # ===== #
2  # YOUR CODE HERE:
3  #   Implement a FC-net that achieves at least 55% validation accuracy
4  #   on CIFAR-10.
5  # ===== #
6  hiddenDims = [500,500,500]
7  weight_scale = 4e-2
8  dropout = 0.8
9  epochs = 17
10 batchSize = 490
11 optimizer = "adam"
12 lr = 5e-3
13 regularization = 0
14 lr_dec = 0.9
15
16 net = FullyConnectedNet(hiddenDims, weight_scale=weight_scale, dropout=dropout, use_batchnorm=True,
17                           reg = regularization)
18 solver = Solver(net, data,
19                 num_epochs=epochs, batch_size=batchSize,
20                 update_rule=optimizer,
21                 optim_config={
22                     'learning_rate': lr,
23                 },
24                 lr_decay = lr_dec, verbose=True, print_every=200)
25
26 solver.train()
27
28 # ===== #
29 # END YOUR CODE HERE
30 # ===== #

```

```

(Iteration 1 / 1700) loss: 2.448994
(Epoch 0 / 17) train acc: 0.145000; val_acc: 0.165000
(Epoch 1 / 17) train acc: 0.432000; val_acc: 0.440000
(Epoch 2 / 17) train acc: 0.509000; val_acc: 0.501000
(Iteration 201 / 1700) loss: 1.397535
(Epoch 3 / 17) train acc: 0.555000; val_acc: 0.511000
(Epoch 4 / 17) train acc: 0.595000; val_acc: 0.538000
(Iteration 401 / 1700) loss: 1.247360
(Epoch 5 / 17) train acc: 0.635000; val_acc: 0.540000
(Epoch 6 / 17) train acc: 0.650000; val_acc: 0.563000
(Iteration 601 / 1700) loss: 1.080137
(Epoch 7 / 17) train acc: 0.655000; val_acc: 0.560000
(Epoch 8 / 17) train acc: 0.690000; val_acc: 0.572000
(Iteration 801 / 1700) loss: 1.024190
(Epoch 9 / 17) train acc: 0.701000; val_acc: 0.561000
(Epoch 10 / 17) train acc: 0.719000; val_acc: 0.587000
(Iteration 1001 / 1700) loss: 0.967275
(Epoch 11 / 17) train acc: 0.769000; val_acc: 0.603000
(Epoch 12 / 17) train acc: 0.762000; val_acc: 0.603000
(Iteration 1201 / 1700) loss: 0.823831
(Epoch 13 / 17) train acc: 0.777000; val_acc: 0.588000
(Epoch 14 / 17) train acc: 0.809000; val_acc: 0.609000
(Iteration 1401 / 1700) loss: 0.694452
(Epoch 15 / 17) train acc: 0.843000; val_acc: 0.611000
(Epoch 16 / 17) train acc: 0.852000; val_acc: 0.601000
(Iteration 1601 / 1700) loss: 0.638089
(Epoch 17 / 17) train acc: 0.855000; val_acc: 0.603000

```

```

In [ ]: 1 import random
2
3 hiddenDimChoices = [100,200,300,400]
4 hiddenLayerAmounts = [1,2,3]
5 weight_scale = 2e-2
6 dropouts = [0.6,0.7,0.8,0.9]
7 epochs = [25]
8 batchSize = 490
9 optimizer = "adam"
10 lrs = [1e-3,5e-3,1e-2]
11 regularizations = [0,1e-8,1e-7]
12
13 valAcc = 0
14 while valAcc<0.6:
15     amountOfLayers = random.choice(hiddenLayerAmounts)
16     hiddenDims = []
17     for k in range(0,amountOfLayers):
18         hiddenDims.append(random.choice(hiddenDimChoices))
19     dropout = random.choice(dropouts)
20     epoch = random.choice(epochs)
21     lr = random.choice(lrs)
22     regularization = random.choice(regularizations)
23
24     net = FullyConnectedNet(hiddenDims, weight_scale=weight_scale, dropout=dropout, use_batchnorm=True,
25                             reg = regularization)
26     solver = Solver(net, data,
27                     num_epochs=epoch, batch_size=batchSize,
28                     update_rule=optimizer,
29                     optim_config={
30                         'learning_rate': lr,
31                     },
32                     verbose=True, print_every=200)
33
34     solver.train()
35     valAcc = solver.val_acc_history[-1]
36

```

```

(Iteration 1 / 2500) loss: 2.344163
(Epoch 0 / 25) train acc: 0.125000; val_acc: 0.135000
(Epoch 1 / 25) train acc: 0.435000; val_acc: 0.434000
(Epoch 2 / 25) train acc: 0.496000; val_acc: 0.492000
(Iteration 201 / 2500) loss: 1.486581
(Epoch 3 / 25) train acc: 0.510000; val_acc: 0.503000
(Epoch 4 / 25) train acc: 0.531000; val_acc: 0.514000
(Iteration 401 / 2500) loss: 1.374321
(Epoch 5 / 25) train acc: 0.555000; val_acc: 0.512000
(Epoch 6 / 25) train acc: 0.589000; val_acc: 0.516000
(Iteration 601 / 2500) loss: 1.272300
(Epoch 7 / 25) train acc: 0.581000; val_acc: 0.531000
(Epoch 8 / 25) train acc: 0.593000; val_acc: 0.536000
(Iteration 801 / 2500) loss: 1.186901
(Epoch 9 / 25) train acc: 0.642000; val_acc: 0.553000
(Epoch 10 / 25) train acc: 0.645000; val_acc: 0.550000
(Iteration 1001 / 2500) loss: 1.182109
(Epoch 11 / 25) train acc: 0.629000; val_acc: 0.545000
(Epoch 12 / 25) train acc: 0.650000; val_acc: 0.537000
(Iteration 1201 / 2500) loss: 1.044154

```

```

In [40]: 1 print(hiddenDims)
2 print(dropout)
3 print(epoch)
4 print(lr)
5 print(regularization)

```

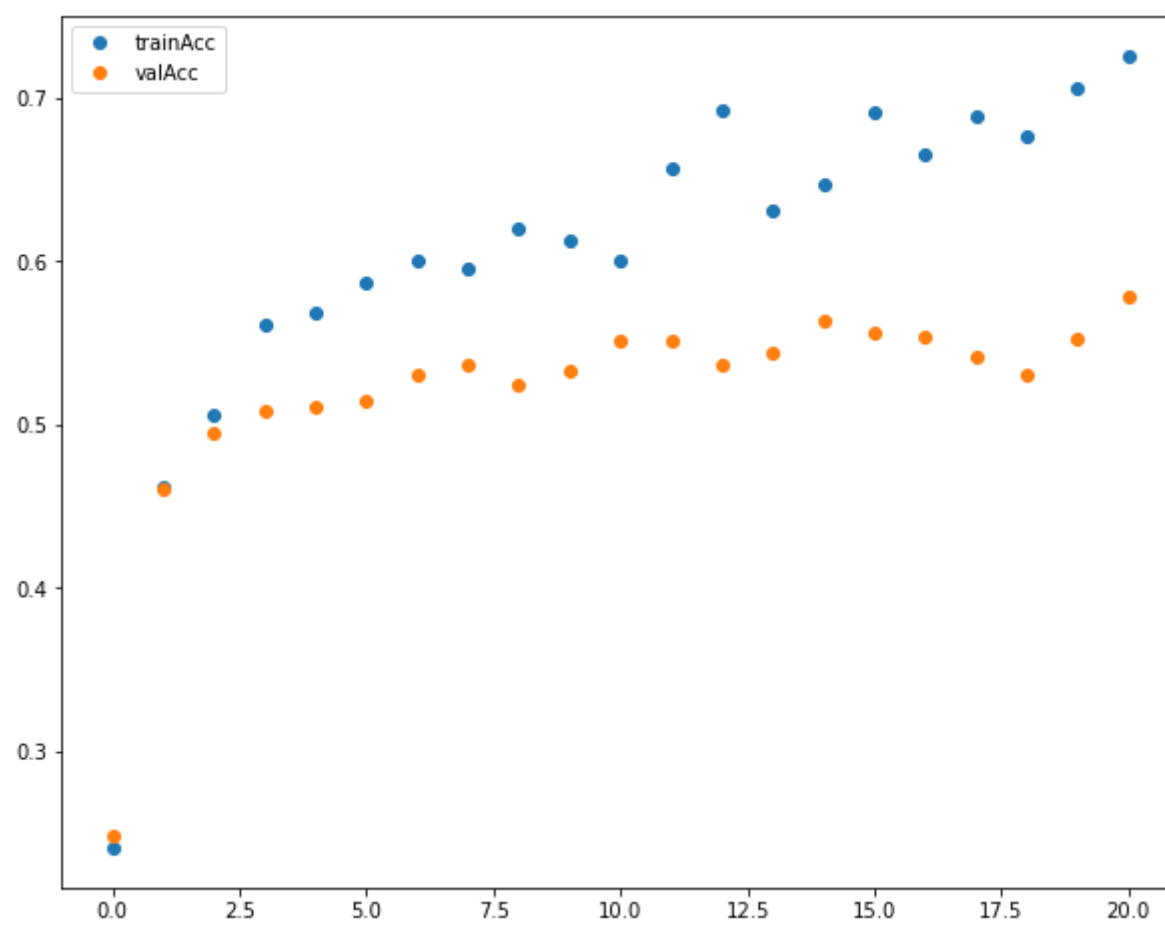
```

[200]
0.7
3
0.001
0

```

```
In [26]: 1 plt.figure()
2         plt.plot(solver.train_acc_history, 'o', label="trainAcc")
3         plt.plot(solver.val_acc_history, 'o', label="valAcc")
4         plt.legend()
```

Out[26]: <matplotlib.legend.Legend at 0x1ab242f3370>



```
In [31]: 1 solver.val_acc_history[-1]
```

Out[31]: 0.534