Convolutional neural network layers

In this notebook, we will build the convolutional neural network layers. This will be followed by a spatial batchnorm, and then in the final notebook of this assignment, we will train a CNN to further improve the validation accuracy on CIFAR-10.

```
In [1]:
          1 ## Import and setups
          3
            import time
          5 import numpy as np
          6 import matplotlib.pyplot as plt
          7 | from nndl.conv_layers import *
          8 from utils.data utils import get CIFAR10 data
          9 from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
         10 from utils.solver import Solver
         11
         12 %matplotlib inline
         13 | plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         14 | plt.rcParams['image.interpolation'] = 'nearest'
         15 | plt.rcParams['image.cmap'] = 'gray'
         17 # for auto-reloading external modules
         18 | # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
         19 %load_ext autoreload
         20 %autoreload 2
         21
         22 | def rel_error(x, y):
              """ returns relative error """
         23
         24
              return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

Implementing CNN layers

Just as we implemented modular layers for fully connected networks, batch normalization, and dropout, we'll want to implement modular layers for convolutional neural networks. These layers are in nnd1/conv_layers.py.

Convolutional forward pass

Begin by implementing a naive version of the forward pass of the CNN that uses for loops. This function is conv_forward_naive in nndl/conv_layers.py. Don't worry about efficiency of implementation. Later on, we provide a fast implementation of these layers. This version ought to test your understanding of convolution. In our implementation, there is a triple for loop.

After you implement conv_forward_naive, test your implementation by running the cell below.

```
In [14]:
           1 | x_shape = (2, 3, 4, 4)
           2 \text{ w\_shape} = (3, 3, 4, 4)
           3 \mid x = np.linspace(-0.1, 0.5, num=np.prod(x_shape)).reshape(x_shape)
           4 | w = np.linspace(-0.2, 0.3, num=np.prod(w_shape)).reshape(w_shape)
           5 b = np.linspace(-0.1, 0.2, num=3)
           7 | conv_param = {'stride': 2, 'pad': 1}
           8 out, _ = conv_forward_naive(x, w, b, conv_param)
             correct_out = np.array([[[[-0.08759809, -0.10987781],
           9
          10
                                         [-0.18387192, -0.2109216]
          11
                                        [[ 0.21027089, 0.21661097],
                                         [ 0.22847626, 0.23004637]],
          12
                                        [[0.50813986, 0.54309974],
          13
                                         [ 0.64082444, 0.67101435]]],
          14
          15
                                        [[[-0.98053589, -1.03143541],
                                         [-1.19128892, -1.24695841]],
          16
          17
                                         [[ 0.69108355, 0.66880383],
          18
                                         [ 0.59480972, 0.56776003]]
          19
                                         [[ 2.36270298, 2.36904306],
                                          [ 2.38090835, 2.38247847]]]])
          20
          21
             # Compare your output to ours; difference should be around 1e-8
          22
             print('Testing conv forward naive')
          23
             print('difference: ', rel_error(out, correct_out))
```

Testing conv_forward_naive difference: 2.2121476417505994e-08

Convolutional backward pass

Now, implement a naive version of the backward pass of the CNN. The function is <code>conv_backward_naive</code> in <code>nndl/conv_layers.py</code>. Don't worry about efficiency of implementation. Later on, we provide a fast implementation of these layers. This version ought to test your understanding of convolution. In our implementation, there is a quadruple <code>for loop</code>.

After you implement conv_backward_naive, test your implementation by running the cell below.

```
In [15]:
           1 \mid x = np.random.randn(4, 3, 5, 5)
           2 \mid w = np.random.randn(2, 3, 3, 3)
           3 b = np.random.randn(2,)
           4 | dout = np.random.randn(4, 2, 5, 5)
           5 | conv_param = {'stride': 1, 'pad': 1}
           7 out, cache = conv_forward_naive(x,w,b,conv_param)
           8
           9
             dx_num = eval_numerical_gradient_array(lambda x: conv_forward_naive(x, w, b, conv_param)[0], x, dout)
          10 dw num = eval_numerical_gradient_array(lambda w: conv_forward_naive(x, w, b, conv_param)[0], w, dout)
          db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, conv_param)[0], b, dout)
          12
          13 | out, cache = conv_forward_naive(x, w, b, conv_param)
          14 dx, dw, db = conv_backward_naive(dout, cache)
          15
          16 # Your errors should be around 1e-9'
          17 | print('Testing conv_backward_naive function')
          18 print('dx error: ', rel_error(dx, dx_num))
          19 print('dw error: ', rel_error(dw, dw_num))
          20 print('db error: ', rel_error(db, db_num))
```

Testing conv_backward_naive function dx error: 2.8364612219207357e-09 dw error: 7.414473932941124e-10 db error: 1.7963277570556685e-10

Max pool forward pass

In this section, we will implement the forward pass of the max pool. The function is <code>max_pool_forward_naive</code> in <code>nndl/conv_layers.py</code>. Do not worry about the efficiency of implementation.

After you implement <code>max_pool_forward_naive</code> , test your implementation by running the cell below.

```
In [16]:
           1 | x_shape = (2, 3, 4, 4)
           2 \mid x = np.linspace(-0.3, 0.4, num=np.prod(x_shape)).reshape(x_shape)
             pool_param = {'pool_width': 2, 'pool_height': 2, 'stride': 2}
           5
             out, _ = max_pool_forward_naive(x, pool_param)
           6
           7
              correct_out = np.array([[[[-0.26315789, -0.24842105],
           8
                                        [-0.20421053, -0.18947368]],
           9
                                       [[-0.14526316, -0.13052632],
                                        [-0.08631579, -0.07157895]],
          10
                                       [[-0.02736842, -0.01263158],
          11
          12
                                        [ 0.03157895, 0.04631579]]],
          13
                                      [[[ 0.09052632, 0.10526316],
                                        [ 0.14947368, 0.16421053]],
          14
          15
                                       [[ 0.20842105, 0.22315789],
          16
                                        [ 0.26736842, 0.28210526]],
          17
                                       [[0.32631579, 0.34105263],
                                        [ 0.38526316, 0.4
          18
                                                                  ]]]])
          19
          20 | # Compare your output with ours. Difference should be around 1e-8.
          21 | print('Testing max_pool_forward_naive function:')
          22 print('difference: ', rel_error(out, correct_out))
```

Testing max_pool_forward_naive function: difference: 4.1666665157267834e-08

Max pool backward pass

In this section, you will implement the backward pass of the max pool. The function is <code>max_pool_backward_naive</code> in <code>nndl/conv_layers.py</code>. Do not worry about the efficiency of implementation.

After you implement <code>max_pool_backward_naive</code> , test your implementation by running the cell below.

Testing max_pool_backward_naive function:
dx error: 3.27562860627328e-12

Fast implementation of the CNN layers

Implementing fast versions of the CNN layers can be difficult. We will provide you with the fast layers implemented by utils. They are provided in utils/fast_layers.py.

The fast convolution implementation depends on a Cython extension ('pip install Cython' to your virtual environment); to compile it you need to run the following from the utils directory:

```
python setup.py build_ext --inplace
```

NOTE: The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation.

You can compare the performance of the naive and fast versions of these layers by running the cell below.

You should see pretty drastic speedups in the implementation of these layers. On our machine, the forward pass speeds up by 17x and the backward pass speeds up by 840x. Of course, these numbers will vary from machine to machine, as well as on your precise implementation of the naive layers.

```
In [2]:
          1 from utils.fast_layers import conv_forward_fast, conv_backward_fast
          2 | from time import time
          4 \times = \text{np.random.randn}(100, 3, 31, 31)
          5 | w = np.random.randn(25, 3, 3, 3)
          6 \mid b = np.random.randn(25,)
          7 | dout = np.random.randn(100, 25, 16, 16)
          8 conv_param = {'stride': 2, 'pad': 1}
          9
         10 | t0 = time()
         11 | out_naive, cache_naive = conv_forward_naive(x, w, b, conv_param)
         12 | t1 = time()
         13 | out_fast, cache_fast = conv_forward_fast(x, w, b, conv_param)
         14 | t2 = time()
         15
         16 | print('Testing conv_forward_fast:')
         17 print('Naive: %fs' % (t1 - t0))
         18 | print('Fast: %fs' % (t2 - t1))
         19 | print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         20 print('Difference: ', rel_error(out_naive, out_fast))
         21
         22 \mid t0 = time()
         23 dx_naive, dw_naive, db_naive = conv_backward_naive(dout, cache_naive)
         24 | t1 = time()
         25 | dx_fast, dw_fast, db_fast = conv_backward_fast(dout, cache_fast)
         26 \mid t2 = time()
         27
         28 print('\nTesting conv_backward_fast:')
         29 print('Naive: %fs' % (t1 - t0))
         30 print('Fast: %fs' % (t2 - t1))
         31 print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         32 print('dx difference: ', rel_error(dx_naive, dx_fast))
         33 print('dw difference: ', rel_error(dw_naive, dw_fast))
         34 | print('db difference: ', rel_error(db_naive, db_fast))
```

Testing conv_forward_fast:
Naive: 7.493805s
Fast: 0.009972s
Speedup: 751.495397x
Difference: 6.31060443914836e-11

Testing conv_backward_fast:
Naive: 9.539863s
Fast: 0.012964s
Speedup: 735.886398x
dx difference: 2.802491524250478e-11
dw difference: 1.782169596108106e-11

```
In [3]:
          1 from utils.fast_layers import max_pool_forward_fast, max_pool_backward_fast
          3 \times = \text{np.random.randn}(100, 3, 32, 32)
          4 | dout = np.random.randn(100, 3, 16, 16)
          5 | pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
          7 \mid t0 = time()
          8 out_naive, cache_naive = max_pool_forward_naive(x, pool_param)
          9 t1 = time()
         10 | out_fast, cache_fast = max_pool_forward_fast(x, pool_param)
         11 | t2 = time()
         12
         13 print('Testing pool_forward_fast:')
         14 print('Naive: %fs' % (t1 - t0))
         15 | print('fast: %fs' % (t2 - t1))
         16 | print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         17 | print('difference: ', rel_error(out_naive, out_fast))
         18
         19 t0 = time()
         20 dx_naive = max_pool_backward_naive(dout, cache_naive)
         21 | t1 = time()
         22 | dx_fast = max_pool_backward_fast(dout, cache_fast)
         23 | t2 = time()
         25 print('\nTesting pool_backward_fast:')
         26 print('Naive: %fs' % (t1 - t0))
         27 print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         28 | print('dx difference: ', rel_error(dx_naive, dx_fast))
```

Testing pool_forward_fast:
Naive: 0.490292s
fast: 0.008982s
speedup: 54.587811x
difference: 0.0

Testing pool_backward_fast:
Naive: 1.525969s
speedup: 109.350225x
dx difference: 0.0

Implementation of cascaded layers

We've provided the following functions in nnd1/conv_layer_utils.py : - conv_relu_forward - conv_relu_backward - conv_relu_pool_forward - conv_relu_pool_backward

These use the fast implementations of the conv net layers. You can test them below:

```
In [4]:
          1 | from nndl.conv_layer_utils import conv_relu_pool_forward, conv_relu_pool_backward
          3 \mid x = np.random.randn(2, 3, 16, 16)
          4 \mid w = np.random.randn(3, 3, 3, 3)
          5 \mid b = np.random.randn(3,)
          6 | dout = np.random.randn(2, 3, 8, 8)
          7 | conv_param = {'stride': 1, 'pad': 1}
          8 | pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
         10 out, cache = conv_relu_pool_forward(x, w, b, conv_param, pool_param)
         11 | dx, dw, db = conv_relu_pool_backward(dout, cache)
         12
         dx_num = eval_numerical_gradient_array(lambda x: conv_relu_pool_forward(x, w, b, conv_param, pool_param)[0], x, dout
         14 | dw_num = eval_numerical_gradient_array(lambda w: conv_relu_pool_forward(x, w, b, conv_param, pool_param)[0], w, dout
         15 db_num = eval_numerical_gradient_array(lambda b: conv_relu_pool_forward(x, w, b, conv_param, pool_param)[0], b, dout
         17 print('Testing conv_relu_pool')
         18 print('dx error: ', rel_error(dx_num, dx))
         print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

Testing conv_relu_pool dx error: 1.3196552481431648e-08 dw error: 5.59037405866879e-10

db error: 7.92375991508291e-12

```
1 | from nndl.conv_layer_utils import conv_relu_forward, conv_relu_backward
In [5]:
          2
          3 \times = \text{np.random.randn}(2, 3, 8, 8)
         4 w = np.random.randn(3, 3, 3, 3)
          5 b = np.random.randn(3,)
          6 | dout = np.random.randn(2, 3, 8, 8)
          7 conv_param = {'stride': 1, 'pad': 1}
          9 out, cache = conv_relu_forward(x, w, b, conv_param)
         10 dx, dw, db = conv_relu_backward(dout, cache)
         11
         12 dx_num = eval_numerical_gradient_array(lambda x: conv_relu_forward(x, w, b, conv_param)[0], x, dout)
         dw_num = eval_numerical_gradient_array(lambda w: conv_relu_forward(x, w, b, conv_param)[0], w, dout)
         | db_num = eval_numerical_gradient_array(lambda b: conv_relu_forward(x, w, b, conv_param)[0], b, dout)
         15
         16 print('Testing conv_relu:')
         17 print('dx error: ', rel_error(dx_num, dx))
         18 print('dw error: ', rel_error(dw_num, dw))
         19 print('db error: ', rel_error(db_num, db))
```

Testing conv_relu:

dx error: 8.249377854023348e-08
dw error: 2.0776994406872497e-09
db error: 3.356044237571737e-10

What next?

We saw how helpful batch normalization was for training FC nets. In the next notebook, we'll implement a batch normalization for convolutional neural networks, and then finish off by implementing a CNN to improve our validation accuracy on CIFAR-10.