Problem 1

In [2]:

(1, 8) (12, 5) (16, 5) (4, 9) (5, 5) (11, 5) (9, 3) (15, 4) (8, 4) (20, 6) (10, 7) (3, 2) (2, 5) (14, 5) (7, 7) (6, 2) (17, 6) (13, 6) (18, 3) (19, 3)

Problem 2

In [4]:

```
def count_values_1(dic):
   vs = dic.values()
   vs = list(vs)
   count = dict()
   for i in vs:
       if i in count:
           count[i] = count[i] + 1
        else:
            count[i] = 1
   return len(count)
def count_values_2(dic):
   vs = dic.values()
   vs = set(vs)
   return len(vs)
temp = {'red' : 1, 'green' : 1, 'blue' : 2}
print(count_values_1(temp))
print(count_values_2(temp))
```

Problem 3

In [5]:

```
def normal_to_sparse(vec):
    sps = dict()
    for i in range(0, len(vec)):
        if vec[i] == 0 : continue
        else:
             sps[i] = vec[i]
    return sps
def change_sign(dic):
    keys = dic.keys()
    for i in keys:
        dic[i] = -dic[i]
    return dic
def add_vector(dic1, dic2):
    rdic = dict()
    for i in dic1.keys():
        for j in dic2.keys():
             if(i == j):
                 rdic[i] = dic1[i] + dic2[i]
    for i in dic1.keys():
        if i not in rdic:
             rdic[i] = dic1[i]
    for i in dic2.keys():
        if i not in rdic:
             rdic[i] = dic2[i]
    return rdic
def minus_vector(dic1, dic2):
    return add_vector(dic1, change_sign(dic2))
vec = [1,0,0,0,0,0,3,0,0,0]
print(normal_to_sparse(vec))
print(change_sign(normal_to_sparse(vec)))
print(add_vector({0:1, 6:3}, {1:2, 6:3}))
print(minus_vector({0:1, 6:3}, {1:2, 6:3}))
{0: 1, 6: 3}
{0: -1, 6: -3}
{6: 6, 0: 1, 1: 2}
{6: 0, 0: 1, 1: -2}
```