COSE474-2024F: Deep Learning HW1

2022320017 Youjin Kim

** Discussions & exercises are at the bottom of each chapter

2. Preliminaries

2.1. Data Manipulation

2.1.1. Getting Started

```
In [ ]: import torch
In [ ]: x = torch.arange(12, dtype=torch.float32)
Out[]: tensor([0., 1., 2., 3., 4., 5., 6.,
                                                  7., 8., 9., 10., 11.])
In [ ]: x.numel()
Out[]: 12
In [ ]: x.shape
Out[]: torch.Size([12])
In []: X = x.reshape(3,4)
Out[]: tensor([[ 0., 1.,
                           2., 3.],
                [ 4., 5., 6., 7.],
                [8., 9., 10., 11.]])
In [ ]: torch.zeros((2,3,4))
Out[]: tensor([[[0., 0., 0., 0.],
                 [0., 0., 0., 0.],
                 [0., 0., 0., 0.]
                [[0., 0., 0., 0.],
                 [0., 0., 0., 0.],
                 [0., 0., 0., 0.]]
In [ ]: torch.ones((2,3,4))
```

```
[1., 1., 1., 1.],
                 [1., 1., 1., 1.]],
                [[1., 1., 1., 1.],
                 [1., 1., 1., 1.],
                 [1., 1., 1., 1.]])
In [ ]: | torch.randn(3,4)
Out[]: tensor([[-1.0557, 0.8418, 0.4618, -0.8704],
                [0.7211, -1.4905, -0.5259, -0.9298],
                [0.7455, -0.0146, 0.8335, -0.4199]])
In []: torch.tensor([[2,1,4,3],[1,2,3,4],[4,3,2,1]])
Out[]: tensor([[2, 1, 4, 3],
                [1, 2, 3, 4],
                [4, 3, 2, 1]])
        2.1.2. Indexing and Slicing
In []: X[-1], X[1:3]
Out[]: (tensor([8., 9., 10., 11.]),
         tensor([[ 4., 5., 6., 7.],
                 [8., 9., 10., 11.]]))
In []: X[1,2] = 17
        Χ
Out[]: tensor([[ 0.,
                       1., 2., 3.],
                       5., 17., 7.],
                [ 4.,
                       9., 10., 11.]])
                [ 8.,
In []: X[:2, :] = 12
        Χ
Out[]: tensor([[12., 12., 12., 12.],
                [12., 12., 12., 12.]
                [8., 9., 10., 11.]])
        2.1.3. Operations
In [ ]: # example of unary scalar operators (taking one input)
        torch.exp(x)
Out[]: tensor([162754.7969, 162754.7969, 162754.7969, 162754.7969, 162754.7969,
                162754.7969, 162754.7969, 162754.7969,
                                                        2980.9580,
                                                                      8103.0840,
                 22026.4648, 59874.1406])
In [ ]: # example of binary scalar operators (taking a pair of inputs)
        # inputs should be the same shape
        x = torch.tensor([1.0, 2, 4, 8])
        y = torch.tensor([2,2,2,2])
```

Out[]: tensor([[[1., 1., 1., 1.],

```
x+y, x-y, x*y, x/y, x**y
Out[]: (tensor([ 3.,
                      4., 6., 10.]),
         tensor([-1.,
                       0., 2., 6.]),
         tensor([ 2., 4., 8., 16.]),
         tensor([0.5000, 1.0000, 2.0000, 4.0000]),
         tensor([ 1., 4., 16., 64.]))
In [ ]: # concatenating multiple tensors
        X = torch.arange(12, dtype=torch.float32).reshape((3,4))
        Y = torch.tensor([[2.0, 1, 4, 3], [1, 2, 3, 4], [4, 3, 2, 1]])
        torch.cat((X,Y), dim=0), torch.cat((X,Y), dim=1)
Out[]: (tensor([[ 0.,
                        1., 2., 3.],
                        5., 6., 7.],
                 [ 4.,
                 [ 8.,
                        9., 10., 11.],
                 [ 2.,
                            4.,
                                  3.],
                        1.,
                 [ 1.,
                        2.,
                             3.,
                                  4.],
                 [ 4.,
                        3.,
                             2.,
                                  1.]]),
         tensor([[ 0., 1.,
                                  3., 2., 1., 4.,
                            2.,
                                                 3.,
                       5., 6., 7., 1., 2.,
                 [ 4.,
                                                      4.],
                 [8., 9., 10., 11., 4., 3.,
                                                 2.,
In [ ]: # binary tensor via logical statements
        X == Y
Out[]: tensor([[False, True, False, True],
                [False, False, False, False],
                [False, False, False, False]])
In [ ]: # summing all elemtents in the tensor
        X.sum()
Out[]: tensor(66.)
        2.1.4. Broadcasting
In [ ]: a = torch.arange(3).reshape((3,1))
        b = torch.arange(2).reshape((1,2))
        a,b
Out[]: (tensor([[0],
                 [1].
                 [2]]),
         tensor([[0, 1]]))
In []: \# a(3x1) and b(1x2) have different shape
        # broadcasting produces a larger 3x2 matrix by replicating 'a' along the
        a + b
Out[]: tensor([[0, 1],
                [1, 2],
                [2, 3]])
```

2.1.5. Saving Memory

```
In []: before = id(Y)
    Y = Y+X # id(Y) changes because we dereference original Y and instead poi
    id(Y) == before

Out[]: False

In []: # in-place operations : assign result of an operation to a previously all
    Z = torch.zeros_like(Y)
    print('id(Z):',id(Z))
    Z[:] = X+Y
    print('id(Z):',id(Z))
    id(Z): 6066767328
    id(Z): 6066767328

In []: before = id(X)
    X += Y # or X[:] = X+Y
    id(X) ==before

Out[]: True
```

2.1.6. Conversion of Other Python Objects

```
In []: A = X.numpy() # converting torch to numpy
B = torch.from_numpy(A) # converting NumPy to torch
type(A), type(B)

Out[]: (numpy.ndarray, torch.Tensor)

In []: a = torch.tensor([3.5])
a, a.item(), float(a), int(a) # converting a size-1 tensor to scalar

Out[]: (tensor([3.5000]), 3.5, 3.5, 3)
```

2.1.7. Summary

2.1.8. Exercises

```
In [ ]: X, Y, X==Y, X<Y, X>Y
```

```
Out[]: (tensor([[ 2., 3., 8., 9.],
                  [ 9., 12., 15., 18.],
                  [20., 21., 22., 23.]]),
         tensor([[ 2., 2., 6., 6.],
                  [5., 7., 9., 11.],
                  [12., 12., 12., 12.]
         tensor([[ True, False, False, False],
                  [False, False, False, False],
                  [False, False, False, False]]),
         tensor([[False, False, False, False],
                  [False, False, False, False],
                  [False, False, False, False]]),
         tensor([[False, True, True,
                                       True],
                  [ True,
                         True,
                                 True,
                                        True],
                  [ True, True,
                                 True,
                                        True]]))
In []: a = torch.arange(4).reshape((4,1))
        b = torch.arange(3).reshape((1,3))
        a+b, a-b, a*b, a/b, a**b
Out[]: (tensor([[0, 1, 2],
                  [1, 2, 3],
                  [2, 3, 4],
                  [3, 4, 5]]),
         tensor([[0, -1, -2],
                  [1, 0, -1],
                  [2, 1, 0],
                  [3, 2, 1]]),
         tensor([[0, 0, 0],
                  [0, 1, 2],
                  [0, 2, 4],
                  [0, 3, 6]]),
         tensor([[
                    nan, 0.0000, 0.0000],
                    inf, 1.0000, 0.5000],
                     inf, 2.0000, 1.0000],
                     inf, 3.0000, 1.5000]]),
         tensor([[1, 0, 0],
                  [1, 1, 1],
                  [1, 2, 4],
                  [1, 3, 9]]))
```

2.2. Data Preprocessing

2.2.1. Reading the Dataset

```
In []: import os

os.makedirs(os.path.join('.', 'data'), exist_ok=True)
data_file = os.path.join('.', 'data', 'house_tiny.csv')
with open(data_file, 'w') as f:
    f.write('''NumRooms,RoofType,Price
NA,NA,127500
2,NA,106000
4,Slate,178100
```

```
In [ ]: import pandas as pd
        data = pd.read csv(data file)
        print(data)
          NumRooms RoofType
                              Price
                        NaN 127500
               NaN
               2.0
                        NaN 106000
       1
               4.0
       2
                      Slate 178100
               NaN
                        NaN 140000
        2.2.2. Data Preparation
In [ ]: ## Separating out columns corresponding to input verses target values
        # we can select columns either by name or via integer-location based inde
        ## Handling missing values
        # imputation : replaces missing values w/ estimates
        # deletion : discards either rows/columns w/ missing values
        # imputation technique(1) : treating NaN as a category
        inputs, targets = data.iloc[:, 0:2], data.iloc[:, 2]
        inputs = pd.get_dummies(inputs, dummy_na=True)
        print(inputs)
          NumRooms
                    RoofType_Slate RoofType_nan
               NaN
                             False
                                            True
       0
       1
               2.0
                             False
                                            True
       2
                                           False
               4.0
                              True
       3
               NaN
                             False
                                            True
In []: # imputation technique(2): replace NaN entries w/ mean value of the colu
        inputs = inputs.fillna(inputs.mean())
        print(inputs)
          NumRooms
                    RoofType_Slate RoofType_nan
       0
               3.0
                             False
                                            True
       1
               2.0
                             False
                                            True
       2
               4.0
                              True
                                           False
       3
               3.0
                             False
                                            True
        2.2.3. Conversion to the Tensor Format
In [ ]: import torch
        X = torch.tensor(inputs.to_numpy(dtype=float))
        y = torch.tensor(targets.to_numpy(dtype=float))
        X, y
Out[]: (tensor([[3., 0., 1.],
```

[2., 0., 1.], [4., 1., 0.],

[3., 0., 1.]], dtype=torch.float64),

tensor([127500., 106000., 178100., 140000.], dtype=torch.float64))

NA, NA, 140000''')

2.2.5. Exercises

```
In []: #1. Loaded datasets. No missing values. All attributes except 'sex' is nu
         abalone_data = pd.read_csv("./data/abalone.data",
                                     names = [
                                          "sex", "length", "diameter", "height",
                                          "whole_weight", "shucked_weight",
                                          "viscera_weight", "shell_weight",
                                          "rings"
                                     1
                                    )
         print(abalone_data)
                  length
                          diameter
                                     height
                                             whole_weight shucked_weight \
             sex
       0
              М
                   0.455
                              0.365
                                      0.095
                                                    0.5140
                                                                     0.2245
       1
               Μ
                   0.350
                              0.265
                                      0.090
                                                    0.2255
                                                                     0.0995
       2
               F
                   0.530
                              0.420
                                      0.135
                                                    0.6770
                                                                     0.2565
       3
               Μ
                   0.440
                              0.365
                                      0.125
                                                    0.5160
                                                                     0.2155
       4
               Ι
                   0.330
                              0.255
                                      0.080
                                                    0.2050
                                                                     0.0895
       . . .
              . .
                     . . .
                                . . .
                                        . . .
                                                        . . .
                                                                         . . .
                   0.565
                              0.450
                                                    0.8870
                                                                     0.3700
       4172
              F
                                      0.165
       4173
              М
                   0.590
                              0.440
                                      0.135
                                                    0.9660
                                                                     0.4390
                              0.475
       4174
              Μ
                   0.600
                                      0.205
                                                    1.1760
                                                                     0.5255
       4175
               F
                   0.625
                              0.485
                                      0.150
                                                    1.0945
                                                                     0.5310
                              0.555
       4176
                   0.710
                                      0.195
                                                    1.9485
                                                                     0.9455
              М
              viscera_weight shell_weight
                                              rings
       0
                      0.1010
                                     0.1500
                                                 15
       1
                                                  7
                      0.0485
                                     0.0700
       2
                                                  9
                      0.1415
                                     0.2100
       3
                                     0.1550
                                                 10
                      0.1140
       4
                      0.0395
                                     0.0550
                                                  7
       . . .
                          . . .
                                         . . .
                                                . . .
       4172
                      0.2390
                                     0.2490
                                                 11
       4173
                      0.2145
                                     0.2605
                                                 10
                                                  9
       4174
                      0.2875
                                     0.3080
       4175
                                                 10
                      0.2610
                                     0.2960
                                                 12
       4176
                      0.3765
                                     0.4950
       [4177 rows x 9 columns]
In []: #2. selecting columns by name
```

abalone_data[["sex", "length", "height"]][:10]

```
Out[]: sex length height
        0
            Μ
              0.455
                     0.095
        1
            M 0.350
                     0.090
        2
            F 0.530
                     0.135
            M 0.440
                     0.125
        3
        4
            I 0.330
                     0.080
            1 0.425
                     0.095
        6
            F 0.530
                     0.150
        7
                     0.125
            F 0.545
                     0.125
        8
            M 0.475
               0.550
                      0.150
In [ ]: #3. Depends on RAM. If the dataset if too large, it cannot be handled at
        #4. For large categories, we can reduce them based on the similarities of
        #5. pandas / NumPy, Pillow, ...
       2.3. Linear Algebra
        2.3.1. Scalars
In []: x = torch.tensor(3.0)
        y = torch.tensor(2.0)
        x+y, x*y, x/y, x**y
Out[]: (tensor(5.), tensor(6.), tensor(1.5000), tensor(9.))
        2.3.2. Vectors
In []: x = torch.arange(3)
Out[]: tensor([0, 1, 2])
In []: x[2]
Out[]: tensor(2)
```

In []: len(x)

In []: x.shape

Out[]: 3

```
Out[]: torch.Size([3])
        2.3.3. Matrices
In []: A = torch.arange(6).reshape(3,2)
Out[]: tensor([[0, 1],
                [2, 3],
                [4, 5]])
In [ ]: A.T
Out[]: tensor([[0, 2, 4],
                [1, 3, 5]])
In []: A = torch.tensor([[1,2,3],[2,0,4],[3,4,5]])
        A == A.T
Out[]: tensor([[True, True, True],
                [True, True, True],
                [True, True, True]])
        2.3.4. Tensors
In []:
       torch.arange(24).reshape(2,3,4)
Out[]: tensor([[[ 0,
                       1, 2, 3],
                 [ 4,
                      5, 6, 7],
                 [8,
                      9, 10, 11]],
                [[12, 13, 14, 15],
                 [16, 17, 18, 19],
                 [20, 21, 22, 23]])
        2.3.5. Basic Properties of Tensors Arithmetic
In [ ]: A = torch.arange(6, dtype=torch.float32).reshape(2,3)
        B = A.clone()
        A, A+B
Out[]: (tensor([[0., 1., 2.],
                 [3., 4., 5.]]),
         tensor([[ 0., 2., 4.],
                 [ 6., 8., 10.]]))
In [ ]: A*B # elementwise product
Out[]: tensor([[ 0., 1., 4.],
                [ 9., 16., 25.]])
```

In []: | a = 2

X = torch.arange(24).reshape(2,3,4)

```
Out[]: (tensor([[[2, 3, 4, 5],
                       7, 8,
                               9],
                  [ 6,
                  [10, 11, 12, 13]],
                 [[14, 15, 16, 17],
                  [18, 19, 20, 21],
                  [22, 23, 24, 25]]]),
         torch.Size([2, 3, 4]))
        2.3.6. Reduction
In []: x = torch.arange(3, dtype=torch.float32)
        x, x.sum()
Out[]: (tensor([0., 1., 2.]), tensor(3.))
In [ ]: A.shape, A.sum()
Out[]: (torch.Size([2, 3]), tensor(15.))
In [ ]:
        A.shape, A.sum(axis=0).shape
Out[]: (torch.Size([2, 3]), torch.Size([3]))
In [ ]:
        A.shape, A.sum(axis=1).shape
Out[]:
        (torch.Size([2, 3]), torch.Size([2]))
        A.sum(axis=[0,1]) == A.sum() # same as A.sum()
In [ ]:
Out[]: tensor(True)
In []:
        A.mean(), A.sum()/A.numel()
Out[]: (tensor(2.5000), tensor(2.5000))
In []: A.mean(axis=0), A.sum(axis=0)/A.shape[0]
Out[]: (tensor([1.5000, 2.5000, 3.5000]), tensor([1.5000, 2.5000, 3.5000]))
        2.3.7. Non-Reduction Sum
In [ ]: # keepdims=True : keep # of axes unchanged when invoking function
        sum_A = A.sum(axis=1, keepdims=True)
        sum_A, sum_A.shape
Out[]: (tensor([[ 3.],
                 [12.]]),
         torch.Size([2, 1]))
In [ ]: # create a matrix where each row sums up to 1
```

a+X, (a*X).shape

```
A / sum_A
Out[]: tensor([[0.0000, 0.3333, 0.6667],
                 [0.2500, 0.3333, 0.4167]])
In [ ]: # calculate the cumulative sum of elements of A along the axis
        A.cumsum(axis=0)
Out[]: tensor([[0., 1., 2.],
                [3., 5., 7.]])
        2.3.8. Dot Products
In [ ]: y = torch.ones(3, dtype = torch.float32)
        x, y, torch.dot(x, y)
Out[]: (tensor([0., 1., 2.]), tensor([1., 1., 1.]), tensor(3.))
In [ ]: torch.sum(x*y) # same as dot product
Out[]: tensor(3.)
        2.3.9. Matrix-Vector Products
In [ ]: print(A, A.shape)
        print(x, x.shape)
        print(torch.mv(A,x))
        print(A@x)
       tensor([[0., 1., 2.],
               [3., 4., 5.]]) torch.Size([2, 3])
       tensor([0., 1., 2.]) torch.Size([3])
       tensor([ 5., 14.])
       tensor([ 5., 14.])
        2.3.10. Matrix-Matrix Multiplication
In []: B = torch.ones(3,4)
        print(torch.mm(A,B))
        print(A@B)
       tensor([[ 3., 3., 3., 3.],
               [12., 12., 12., 12.]])
       tensor([[ 3., 3., 3., 3.],
               [12., 12., 12., 12.]])
        2.3.11. Norms
In [ ]: |# L2 norm
        u = torch.tensor([3.0, -4.0])
        torch.norm(u)
Out[]: tensor(5.)
```

```
In []: # L1 norm (manhattan distance)
torch.abs(u).sum()

Out[]: tensor(7.)

In []: # Frobenius norm
torch.norm(torch.ones((4,9)))

Out[]: tensor(6.)
```

2.5. Automatic Differentiation

2.5.1. A Simple Function

```
In []: x = torch.arange(4.0)
Out[]: tensor([0., 1., 2., 3.])
In []: x.requires\_grad\_(True) # equal to x = torch.arange(4.0, requires\_grad=Tru)
        x.grad # gradient is none by default
In []: y = 2 * torch.dot(x,x)
Out[]: tensor(28., grad_fn=<MulBackward0>)
In [ ]: | # take gradient of y w.r.t. x by calling its backward method
        # we can access the gradient via x's grad attribute
        y.backward()
        x.grad
Out[]: tensor([0., 4., 8., 12.])
In []: x.grad == 4*x
Out[]: tensor([True, True, True, True])
In [ ]: x.grad.zero_() # reset the gradient buffer
        # define another function & take its gradient
        y = x.sum()
        y.backward()
        x.grad
Out[]: tensor([1., 1., 1., 1.])
```

2.5.2. Backward for Non-Scalar Variables ***

```
In []: x.grad.zero_()
```

```
y = x * x
        y.backward(gradient=torch.ones(len(y))) # Faster : y.sum().backward()
Out[]: tensor([0., 2., 4., 6.])
        2.5.3. Detaching Computation
In [\ ]: # we want to focus on the direct influence of x on z, rather than the inf
        x.grad.zero_()
        y = x * x
        u = y.detach() # takes the same value as y but its provenance has been wi
        z = u * x
        z.sum().backward()
        x.grad == u
Out[]: tensor([True, True, True, True])
In [ ]: x.grad.zero ()
        y.sum().backward() # we can still calculate gradient y w.r.t. x because c
        x.grad == 2 * x
Out[]: tensor([True, True, True, True])
        2.5.4. Gradients and Python Control FLow
In [ ]: def f(a):
            b = a * 2
            while b.norm() < 1000:
                b = b * 2
            if b.sum() > 0:
                c = b
            else:
                c = 100 * b
            return c
In []: a = torch.randn(size=(), requires_grad=True)
        d = f(a)
        d.backward()
In []: a.grad == d / a
```

2.6. Discussion

Out[]: tensor(True)

In the last code of section 2.5.4, why is a grad == d/a?

Function f(a) simply outputs various multiples of a. * b = 2^n * a (n is an integer) * c = b or 100b Therefore, d is a scalar multiplication of a. Since d is a scalar multiplication

of a, its gradient becomes a scalar. d.backward() calculates the gradient of d w.r.t. a and stores it in a.grad. Therefore, a.grad is logically equal to d/a.

3. Linear Neural Networks for Regression

3.1. Linear Regression

```
In []: import math
  import time
  import numpy as np
  import torch
  from d2l import torch as d2l
```

3.1.1. Basics

Given features of a training dataset X and corresponding(=known) labels y, the goal of linear regression is to find the weight vector w and the bias term b such that, given features of a new data example sampled from the same distribution as X, the new example's label will (in expectation) be predicted with the smallest error.

For searching the best model parameters w and b, we need 2 more things: (1) measure of the quality of some given model = Loss Function (2) procedure for updating the model to improve its quality = Optimization Alg.

3.1.2. Vectorization for Speed

```
In []: n = 10000
    a = torch.ones(n)
    b = torch.ones(n)

In []: # using for-loop
    c = torch.zeros(n)
    t = time.time()
    for i in range(n):
        c[i] = a[i] + b[i]
    f'{time.time() - t:.5f} sec'

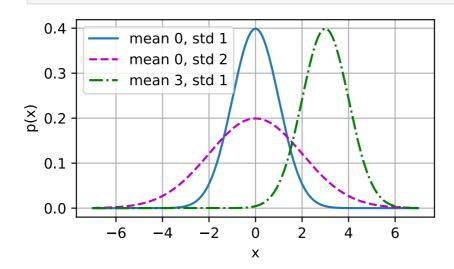
Out[]: '0.05815 sec'

In []: # using vectorization
    t = time.time()
    d = a + b
    f'{time.time() - t:.5f} sec'

Out[]: '0.00124 sec'
```

3.1.3. The Normal Distribution and Squared Loss

legend=[f'mean {mu}, std {sigma}' for mu, sigma in params])



3.1.4. Linear Regression as a Neural Network

We can think of linear regression as a single-layer fully connected network.

3.1.6. Exercises

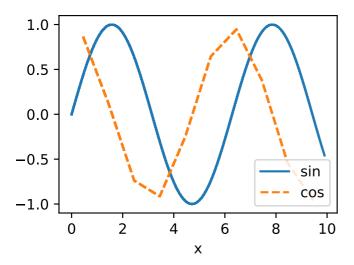
3.2. Object-Oriented Design for Implementation

```
In []: import time
  import numpy as np
  import torch
  from torch import nn
  from d2l import torch as d2l
```

3.2.1. Utilities

```
In []: def add_to_class(Class): #@save
    """Register functions as methods in created class."""
    def wrapper(obj):
        setattr(Class, obj.__name__, obj)
    return wrapper
```

```
In [ ]: | # we plan to implement a class A with a method do.
        class A: #class A
            def init (self):
                self.b = 1
        a = A() #instance a
In [ ]: @add_to_class(A) # decorate method do by add_to_class w/ class A as argum
        def do(self):
            print('Class attribute "b" is', self.b)
        a.do()
       Class attribute "b" is 1
In []: # utility class that saves all algruments in a class's __init__ method as
        # this allows us to extend constructor call signatures implicitly w/o add
        class HyperParameters: #@save
            """The base class of hyperparameters"""
            def save_hyperparameters(self, ignore=[]):
                raise NotImplemented
In []: # call the fully-implemented HyperParameters class saved in d2l
        class B(d2l.HyperParameters):
            def __init__(self, a, b, c):
                self.save_hyperparameters(ignore=['c'])
                print('self.a=', self.a, 'self.b=', self.b)
                print('Thre is no self.c =', not hasattr(self, 'c'))
        b = B(a=1, b=2, c=3)
       self.a= 1 self.b= 2
       Thre is no self.c = True
In []: # this allows us to plot experiment progress interactively while it is go
        class ProgressBoard(d2l.HyperParameters): #@save
            """The board that plots data points in animation"""
            def __init__(self, xlabel=None, ylabel=None, xlim=None, ylim=None,
                         xscale='linear', yscale='linear',
                         ls=['-','--','-.',':'], colors=['C0','C1','C2','C3'],
                         fig=None, axes=None, figsize=(3.5,2.5), display=True):
                self.save_hyperparameters()
            def draw(self, x, y, label, every_n=1): # plots a point in the figure
                raise NotImplemented
In [ ]: board = d2l.ProgressBoard('x')
        for x in np.arange(0, 10, 0.1):
            board.draw(x, np.sin(x), 'sin', every_n=1)
            board.draw(x, np.cos(x), 'cos', every_n=10)
```



3.2.2. Models

```
In [ ]: # __init__ : stores learnable parameters
        # training_step method : accepts a data batch to return the loss value
        # configure_optimizers : retruns the optimization method used to updated
        # validation_step : report the evaluation megsures
        class Module(nn.Module, d2l.HyperParameters): #@save
            """The base class of models."""
            def __init__(self, plot_train_per_epoch=2, plot_valid_per_epoch=1):
                super().__init__()
                self.save_hyperparameters()
                self.board = ProgressBoard()
            def loss(self, y_hat, y):
                raise NotImplementedError
            def forward(self, X):
                assert hasattr(self, 'net'), 'Neural Network is defined'
                return self.net(X)
            def plot(self, key, value, train):
                """Plot a point in animation"""
                assert hasattr(self, 'trainer'), 'Trainer is not inited'
                self.board.xlabel='epoch'
                if train:
                    x = self.trainer.train_batch_idx / \
                        self.trainer.num_train_batches
                    n = self.trainer.num_train_batches / \
                        self.plot_train_per_epoch
                else:
                    x = self.trainer.epoch + 1
                    n = self.trainer.num_val_batches / \
                        self.plort_valid_per_epoch
                self.board.draw(x, value.to(d2l.cpu()).detach().numpy(),
                                 ('train_' if train else 'val_') + key,
                                 every_n=int(n))
            def training_step(self, batch):
                l = self.loss(self(*batch[:-1]), batch[-1])
                self.plot('loss', l, train=True)
```

```
return l

def validation_step(self, batch):
    l = self.loss(self(*batch[:-1]), batch[-1])
    self.plot('loss', l, train=False)

def configure_optimizers(self):
    raise NotImplementedError
```

3.2.3. Data

```
In []:
    class DataModule(d2l.HyperParameters): #@save
        """The base class of data."""
    def __init__(self, root='../data', num_workers=4):
        self.save_hyperparameters()

    def get_dataloader(self, train):
        raise NotImplementedError

    def train_dataloader(self):
        return self.get_dataloader(train=True)

    def val_dataloader(self):
        return self.get_dataloader(train=False)
```

3.2.4. Training

```
In [ ]: class Trainer(d21.HyperParameters): #@save
            """The base class for training models with data."""
            def __init__(self, max_epochs, num_gpus=0, gradient_clip_val=0):
                self.save_hyperparameters()
                assert num_gpus==0, 'No GPU support yet'
            def prepare data(self, data):
                self.train_dataloader = data.train_dataloader()
                self.val_dataloader = data.val_dataloader()
                self.num_train_batches = len(self.train_dataloader)
                self.num_val_batches = (len(self.val_dataloader) if self.val_data
            def prepare_model(self, model):
                model.trainer = self
                model.board.xlim = [0, self.max_epochs]
                self.model = model
            def fit(self, model, data):
                self.prepare_data(data)
                self.prepare model(model)
                self.optim = model.configure_optimizers()
                self.epoch = 0
                self.train_batch_idx = 0
                self.val_batch_idx = 0
                for self.epoch in range(self.max_epochs):
                    self.fit_epoch()
```

```
def fit_epoch(self):
    raise NotImplementedError
```

3.4. Linear Regression Implementation from Scratch

```
In []: %matplotlib inline
   import torch
   from d2l import torch as d2l
```

3.4.1. Defining the Model

```
In []: class LinearRegressionScratch(d2l.Module): #@save
    """The linear regression model implemented from scratch."""
    def __init__(self, num_inputs, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
        self.w = torch.normal(0, sigma, (num_inputs, 1), requires_grad=Tr
        self.b = torch.zeros(1, requires_grad=True) # bias is 0
In []: @d2l.add_to_class(LinearRegressionScratch) #@save
    def forward(self, X):
        return torch.matmul(X, self.w) + self.b
```

3.4.2. Defining the Loss Function

```
In []: @d2l.add_to_class(LinearRegressionScratch)
    def loss(self, y_hat, y):
        l = (y_hat - y)**2 / 2
        return l.mean() # avg of squared loss value among all examples in the
```

3.4.3. Defining the Optimization Algorithm

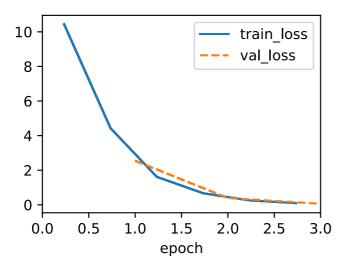
```
In [ ]: @d2l.add_to_class(LinearRegressionScratch) #@save
    def configure_optimizers(self): # returns an instance of the SGD class
        return SGD([self.w, self.b], self.lr)
```

3.4.4. Training

- in each epoch: iterate through the entire training dataset & pass once through ever example
- in each iteration : grap a minibatch of training examples & compute its loss through the model's training_step method
- compute the gradients w.r.t. each parameter
- call the optimization algorithm to update the model parameters

```
In [ ]: @d2l.add_to_class(d2l.Trainer) #@save
        def prepare_batch(self, batch):
            return batch
        @d2l.add_to_class(d2l.Trainer) #@save
        def fit_epoch(self):
            self.model.train()
            for batch in self.train_dataloader:
                loss = self.model.training_step(self.prepare_batch(batch))
                self.optim.zero grad()
                with torch.no_grad():
                    loss.backward()
                    if self.gradient_clip_val > 0:
                         self.clip_gradients(self.gradient_clip_val, self.model)
                    self.optim.step()
                self.train_batch_idx += 1
            if self.val dataloader is None:
                return
            self.model.eval()
            for batch in self.val_dataloader:
                with torch.no_grad():
                    self.model.validation_step(self.prepare_batch(batch))
                self.val_batch_idx += 1
```

```
In []: model = LinearRegressionScratch(2, lr=0.03)
  data = d2l.SyntheticRegressionData(w=torch.tensor([2, -3.4]),b=4.2)
  trainer = d2l.Trainer(max_epochs=3)
  trainer.fit(model, data)
```



```
in []:
    with torch.no_grad():
        print(f'error in estimating w: {data.w - model.w.reshape(data.w.shape
        print(f'error in estimating b: {data.b - model.b}')

error in estimating w: tensor([ 0.1149, -0.1927])
    error in estimating b: tensor([0.2631])
```

3.5. Discussion

What are the differences between gradient descent, stochastic gradient descent and minibatch stochastic gradient descent algorithm? Discuss each algorithm and compare their advantages/disadvantages.

GD, SGD, Mini-batch SGD are all optimization algorithms used to minimize a loss function by updating model parameters. They differ in how much of the training data is used to compute the gradient during each update step.

1. Gradient Descent [GD]

- computes the gradient of the loss function using the entire training dataset. also called 'batch' gradient descent [BGD]
- advantages : provides a precise & stable gradient b/c it uses all data
- disadvantages: SLOW(in each step) for large datasets, requires a lot of memory
- 2. Stochastic Gradient Descent [SGD]
 - computes the gradient using only one random data point(one sample)
 from the training dataset at each update. introduces randomness into the parameter updates
 - advantages: requires less memory than full-batch. can escape local optima due to its noisy updates. FAST(in each step)
 - disadvantages: may take longer to converge (may never reach the exact optima due to its noise). b/o moving data from main memory to processor ache is slower than multiplication/addition, it can take a lot longer to process one sample at a time compared to a full batch.
- 3. Mini-batch Stochastic Gradient Descent [Mini-batch SGD]
 - computes the gradient using a small subset(mini-batch) of the training data at each update. The specific size of the mini-batch depends on many factors such as amt of memory, # of accelerators, layers, dataset size.
 - advantages: more stable than SGD b/c averaging over a mini-batch reduces the noise in the gradient estimation. takes advantage of vectorized operations on GPUs.
 - disadvantages: requires careful tuning of the batch size. requires more memory than SGD

4. Linear Neural Networks for Classification

4.1. Softmax Regression

4.1.1. Classification

Simple image classification problem

- input : 2x2 grayscale image -> 4 features (1 pixel = 1 scalar)
- output : label (cat, chicken, dog)

One-hot encoding: simple way to represent categorical data!

- cat = (1,0,0)
- chicken = (0,1,0)
- dog = (0,0,1)

Since we have 4 features and 3 possible output categories, we need 12 scalars to represent the weights (w w/ subscripts) and 3 scalars to represent the biases (b w/ subscripts).

Softmax: transform output values so that they are nonnegative and add up to 1

4.1.2. Loss Function

Now that we learned a mapping from features x to probabilities y_hat, we ened a way to optimize the accuracy of this mapping.

The vector y_hat returned by softmax can be interpreted as the extimated conditional probabilities of each class, given any input x. Since maximizing the product of terms is awkward, we take the negative logarithm to obtain the equivalent problem of minimizing the negative log-likelihood. -> Cross-Entropy Loss

4.1.3. Information Theory Basics

Information theory deals w/ the problem of encoding, decoding, transmitting, and manipulating information(data)

- One of the fundamental theorems of information theory states that in order to encode data drawn randomly from the distribution, we need at least H[P] "nats" to encode it
- Easy to predict = easy to compress
- If we cannot perfectly predict every event-> surprised. Our surprise is greater when an event is assigned lower probability.
- Entropy = level of surprise experienced by someone who knows the true

probability.

• Cross-entropy = expected surprisal of an observer w/ subject probabilities Q upon seeing data that was actually generated according to probabilities P.

Cross-entropy classification obejctive

- maximizing the likelihood of the observed data
- minimizing our surprisal required to communicate the labels

4.2. The Image Classification Dataset

```
In []: %matplotlib inline
import time
import torch
import torchvision
from torchvision import transforms
from d2l import torch as d2l

d2l.use_svg_display()
```

4.2.1. Loading the Dataset

```
In []: # Fashion-MNIST : 10 class, 6000 img for each class in training dataset,
data = FashionMNIST(resize=(32,32))
len(data.train), len(data.val)
```

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-images-idx3-ubyte.gz

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/tra in-images-idx3-ubyte.gz to ../data/FashionMNIST/raw/train-images-idx3-ubyt e.gz

100.0%

Extracting ../data/FashionMNIST/raw/train-images-idx3-ubyte.gz to ../data/FashionMNIST/raw

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-labels-idx1-ubyte.qz

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-labels-idx1-ubyte.gz to ../data/FashionMNIST/raw/train-labels-idx1-ubyte.gz

100.0%

Extracting ../data/FashionMNIST/raw/train-labels-idx1-ubyte.gz to ../data/FashionMNIST/raw

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10 k-images-idx3-ubyte.gz

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10 k-images-idx3-ubyte.gz to ../data/FashionMNIST/raw/t10k-images-idx3-ubyte.gz

100.0%

Extracting ../data/FashionMNIST/raw/t10k-images-idx3-ubyte.gz to ../data/FashionMNIST/raw

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10 k-labels-idx1-ubyte.gz

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10 k-labels-idx1-ubyte.gz to ../data/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz

100.0%

Extracting ../data/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz to ../data/FashionMNIST/raw

```
Out[]: (60000, 10000)
```

```
In []: # c, h, w = # of color channels, height, width
data.train[0][0].shape
```

Out[]: torch.Size([1, 32, 32])

4.2.2. Reading a Minibatch

```
In []: # let's load a minibatch of images by invoking train_dataloader method
    # it contains 64 images
    X, y = next(iter(data.train_dataloader()))
    print(X.shape, X.dtype, y.shape, y.dtype)

    torch.Size([64, 1, 32, 32]) torch.float32 torch.Size([64]) torch.int64

In []: tic = time.time()
    for X,y in data.train_dataloader():
        continue
    f'{time.time() - tic:.2f} sec'

Out[]: '2.63 sec'

4.2.3. Visualization

In []: def show_images(imgs, num_rows, num_cols, titles=None, scale=1.5): #@save
```

```
In []: def show_images(imgs, num_rows, num_cols, titles=None, scale=1.5): #@save
    """Plot a list of images"""
    raise NotImplementedError

In []: @d2l.add_to_class(FashionMNIST) #@save
    def visualize(self, batch, nrows=1, ncols=8, labels=[]):
        X,y = batch
        if not labels:
            labels = self.text_labels(y)
        d2l.show_images(X.squeeze(1), nrows, ncols, titles=labels)

batch = next(iter(data.val_dataloader()))
    data.visualize(batch)
```



4.3. The Base Classification Model

4.3.1. The Classifier Class

```
In []: class Classifier(d2l.Module): #@save
    """The base class of classification models."""
    def validation_step(self, batch): # report loss value & classificatio
        Y_hat = self(*batch[:-1])
        self.plot('loss', self.loss(Y_hat, batch[-1], train=False))
        self.plot('acc', self.accuracy(Y_hat, batch[-1], train=False))

In []: # By default we use a stochastic gradient descent optimizer
@d2l.add to class(d2l.Module) #@save
```

```
def configure_optimizers(self):
    return torch.optim.SGD(self.parameters(), lr=self.lr)
```

4.3.2. Accuracy

```
In []: @d2l.add_to_class(Classifier) #@save
    def accuracy(self, Y_hat, Y, averaged=True):
        """Compute the number of correct predictions."""
        Y_hat = Y_hat.reshape((-1, Y_hat.shape[-1]))
        preds = Y_hat.argmax(axis=1).type(Y.dtype) # obtain the predicted cla
        compare = (preds == Y.reshape(-1)).type(torch.float32) # compare pred
        return compare.mean() if averaged else compare # tensor containing en
```

4.4. Softmax Regression Implementation from Scratch

4.4.1. The Softmax

```
In []: X = \text{torch.tensor}([[1.0, 2.0, 3.0], [4.0, 5.0, 6.0]])
        X.sum(axis=0, keepdims=True), X.sum(axis=1, keepdims=True)
Out[]: (tensor([[5., 7., 9.]]),
         tensor([[ 6.],
                  [15.]]))
In [ ]: ## computing softmax requires 3 steps :
        # (1) exponentiation of each term
        # (2) a sum over each row to compute the normalization constant for each
        # (3) division of each row by its normalization constant
        def softmax(X):
            X_{exp} = torch.exp(X)
             partition = X_exp.sum(1, keepdims=True)
             return X_exp / partition # broadcasting mechinism applied here
In []: X = torch.rand((2,5))
        X_{prob} = softmax(X)
        X_prob, X_prob.sum(1)
Out[]: (tensor([[0.1816, 0.2600, 0.1207, 0.2546, 0.1830],
                  [0.2637, 0.1306, 0.2260, 0.2101, 0.1696]]),
          tensor([1.0000, 1.0000]))
```

4.4.2. The Model

```
In []: # raw data : 28x28 pixel images
# output data : 10 classes -> dimension of 10

# softmax regression
class SoftmaxRegressionScratch(d2l.Classifier):
    def __init__(self, num_inputs, num_outputs, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
```

```
In []: @d2l.add_to_class(SoftmaxRegressionScratch)
    def forward(self, X):
        X = X.reshape((-1, self.W.shape[0])) # flatten 28x28 img into a vecto
        return softmax(torch.matmul(X, self.W) + self.b)
```

4.4.3. The Cross-Entropy Loss

```
In []: y = torch.tensor([0,2])
    y_hat = torch.tensor([[0.1, 0.3, 0.6], [0.3, 0.2, 0.5]])
    y_hat[[0,1], y]
    # first element comes from row 0, col y[0]
    # second element comes from row 1, col y[1]

Out[]: tensor([0.1000, 0.5000])

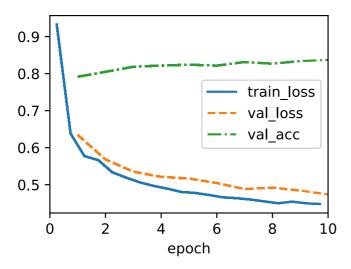
In []: def cross_entropy(y_hat, y):
        return -torch.log(y_hat[list(range(len(y_hat))), y]).mean()
        cross_entropy(y_hat, y)

Out[]: tensor(1.4979)

In []: @d2l.add_to_class(SoftmaxRegressionScratch)
        def loss(self, y_hat, y):
            return cross_entropy(y_hat, y)
```

4.4.4. Training

```
In []: # use fit method to train the model w/ 10 epochs
   data = d2l.FashionMNIST(batch_size=256)
   model = SoftmaxRegressionScratch(num_inputs=784, num_outputs=10, lr=0.1)
   trainer = d2l.Trainer(max_epochs=10)
   trainer.fit(model, data)
```



4.4.5. Prediction

```
In [ ]: | X, y = next(iter(data.val_dataloader()))
         preds = model(X).argmax(axis=1)
         preds.shape
Out[]: torch.Size([256])
In [ ]: # we are more interested in the imgs we label "incorrectly"
         wrong = preds.type(y.dtype) != y
         X, y, preds = X[wrong], y[wrong], preds[wrong]
         labels = [a+'\n'+b \text{ for } a, b \text{ in } zip(
             data.text_labels(y), data.text_labels(preds))]
         data.visualize([X,y], labels=labels)
                                        pullover
                                                                      ankle boot
          sneaker
                                                         sandal
                           coat
          sandal
                                          shirt
                                                        sneaker
                                                                        sandal
                           shirt
```

4.5. Discussion

What are the disadvantages of one-hot encoding? Compare with other encoding methods. When the number of output labels is large, which encoding method is appropriate?

- High dimensionality: Since one-hot encoding creates a sparse vector with a
 dimension equal to the number of categories, the results can be very highdimensional and sparse vectors if there are many categories. This can lead to
 increased memory usage and computational complexity.
- Compared to ordinal encoding which leverages the order of categories, one-hot encoding cannot capture any relationship between categories. Also, using

target/mean encoding which replaces each category with the mean of the target variable, dimensionality can be reduced.

5. Multilayer Perceptrons

5.1. Multilayer Perceptrons

5.1.1 Hidden Layers

Limitations of Linear Models

- Linearity in affine transformations is a **strong** assumption
- Monotinicity (any increase in feature must either always cause an increase/decrease in our model's output): In reality, the output depends in complex ways on its context.
- Studies on nonlinearity
 - sequence of binary decisions in decision trees (Quinlan, 1993)
 - kernel methods(Aroszajn, 1950)

...

Incorporating Hidden Layers: MLP

- easiest way to overcome limitations of linear models: stacking many fullyconnected layers on top of one another
- every input influences every neuron in the hidden layer, an each of these in turn influences every neuron in the output layers

From Linear to Nonlinear

• a nonlinear activation function σ is applied to each hidden unit.

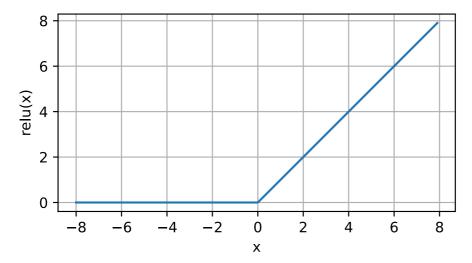
Universal Approximators

- even with a single-hidden-layer network, given enough nodes (possibly absurdly many), and the right set of weights, we can model any function
- However, just because a single-hidden-layer network can learn any function does not mean that you should try to solve all of your problems with one.
- In this case, kernel methods are way more effective, since they are capable of solving the problem exactly even in **infinite dimensional spaces** (Kimeldorf and Wahba, 1971, Schölkopf et al., 2001)
- We can approximate many functions much more compactly by using deeper(rather than wider) networks (Simonyan and Zisserman, 2014)

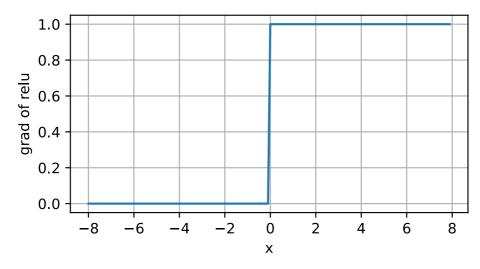
5.1.2. Activation Functions

$$ReLU(x) = max(x, 0)$$

```
In []: # ReLU : rectified linear unit
x = torch.arange(-8.0, 8.0, 0.1, requires_grad=True)
y = torch.relu(x)
d2l.plot(x.detach(), y.detach(), 'x', 'relu(x)', figsize=(5, 2.5))
```

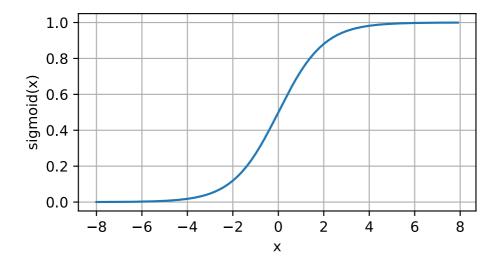


```
In []: # gradient of ReLU : backpropagation
    y.backward(torch.ones_like(x), retain_graph=True)
    d2l.plot(x.detach(), x.grad, 'x', 'grad of relu', figsize=(5,2.5))
```

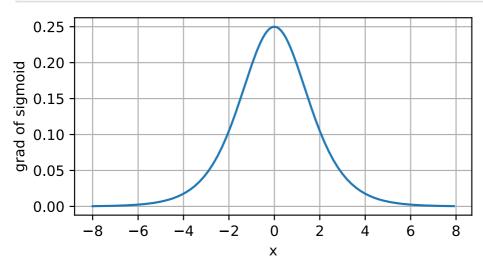


$$\operatorname{sigmoid}(x) = \frac{1}{1 + \exp(-x)}$$

```
In []: y = torch.sigmoid(x)
d2l.plot(x.detach(), y.detach(), 'x', 'sigmoid(x)', figsize=(5,2.5))
```



```
In []: x.grad.data.zero_()
    y.backward(torch.ones_like(x), retain_graph=True)
    d2l.plot(x.detach(), x.grad, 'x', 'grad of sigmoid', figsize=(5,2.5))
```



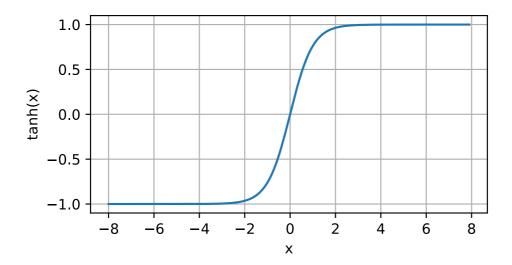
Largest gradient is 0.25 in sigmoid.

If we have many layers, the value will get small as we multiply 0.25 several times, so we prefer ReLU more in this case.

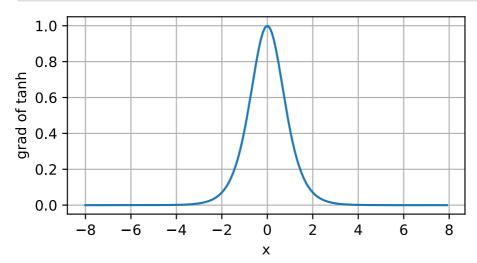
Gradient Vanishing Problem

$$\tanh(x) = \frac{1 - \exp(-2x)}{1 + \exp(-2x)}$$

```
In []: y = torch.tanh(x)
d2l.plot(x.detach(), y.detach(), 'x', 'tanh(x)', figsize=(5,2.5))
```



```
In []: x.grad.data.zero_()
    y.backward(torch.ones_like(x), retain_graph=True)
    d2l.plot(x.detach(), x.grad, 'x', 'grad of tanh', figsize=(5,2.5))
```



5.2. Implementation of Multilayer Perceptrons

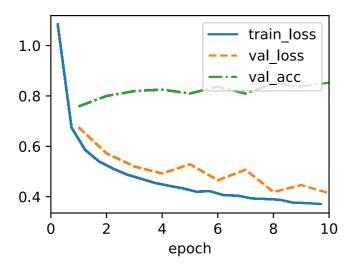
```
In []: import torch
from torch import nn
from d2l import torch as d2l
```

5.2.1. Implementation from Scratch

```
In [ ]: def relu(X):
```

```
a = torch.zeros_like(X)
             return torch.max(X,a)
In [ ]: @d2l.add_to_class(MLPScratch)
        def forward(self, X):
            X = X.reshape((-1, self.num_inputs))
            H = relu(torch.matmul(X, self.W1) + self.b1)
             return torch.matmul(H, self.W2) + self.b2
        model = MLPScratch(num_inputs=784, num_outputs=10, num_hiddens=256, lr=0.
        data = d2l.FashionMNIST(batch_size=256)
        trainer = d2l.Trainer(max_epochs=10)
        trainer.fit(model, data)
                                    train loss
       1.2
                                    val loss
                                    val_acc
       1.0
       8.0
       0.6
       0.4
                  2
           0
                         4
                                6
                                       8
                                             10
                          epoch
```

5.2.2. Concise Implementations



5.3. Forward Propagation, Backward Propagation and Computational Graphs

Forward propagation(forward pass): calculation and storage of intermediate variables (including outputs) for a NN in order from the input layer to the output layer.

Backpropagation: calculating the gradient of NN parameters.

- traverses the network in reverse order, from the output to the input layer, according to the chain rule
- stores any intermediate variables (partial derivatives) required while calculating the gradient w.r.t. some parameters

Whan training NN, forward and backward propagation depend on each other. For forward propagation, we traverse the computational graph in the direction of dependencies and compute all variables on its path. These are then used for backpropagation where the compute order on the graph is reversed.

- Note that backpropagation reuses the stored intermediate values from forward propagation to avoid duplicate calculations.
- Besides, the size of such intermediate values is roughly proportional to the number of network layers and the batch size. Thus, training deeper networks using larger batch sizes more easily leads to out-of-memory errors.

5.4. Discussion&Exercises

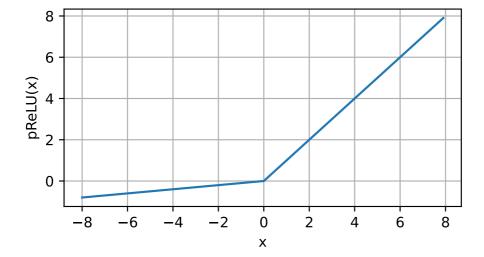
5.1.2.1 (Exercise) My own exercise/experiment

implementing parameterized ReLU:

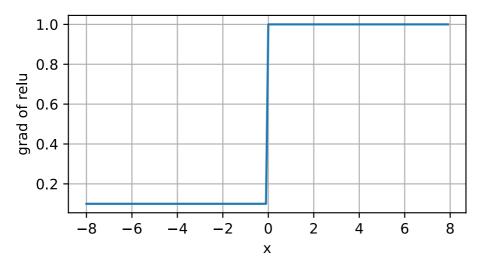
$$pReLU(x) = \max(0, x) + \alpha \min(0, x).$$

```
In []: # pReLU : adds a linear term to ReLU so that some info still gets through
pReLU = lambda x, a: torch.max(torch.tensor(0), x) + a * torch.min(torch.
```

```
In []: y = pReLU(x=x, a=0.1)
    d2l.plot(x.detach(), y.detach(), 'x', 'pReLU(x)', figsize=(5,2.5))
```



```
In []: # gradient of pReLU
x.grad.data.zero_() # set gradient to 0 (이거 안넣으면 gradient 누적됨)
y.backward(torch.ones_like(x), retain_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of relu', figsize=(5,2.5))
```



5.1.2.3. (Exercise)

Show that sigmoid and tanh are very similar

•
$$\tanh(x) + 1 = \frac{1 - \exp(-2x)}{1 + \exp(-2x)} + 1 = \frac{2}{1 + \exp(-2x)}$$

•
$$2 \operatorname{sigmoid}(2x) = \frac{2}{1 + \exp(-2x)}$$

5.2.4 (Exercise)

Try adding a hidden layer to see how it affects the results.

```
In [ ]: model = my_MLP(num_outputs=10, num_hiddens=256, lr=0.1)
    trainer.fit(model,data)
```

