



HUS.HAD

Hanoi University of Science

Mục lục

1 Miscellaneous

2 Mathematics

2.1 Data structure

2.2 Number Theory

2.3 Numerical

3 String

3.1 Data Structures

4 Data Structures

4.1 Trees

5 Graph

5.1 Shortest Path

1 Miscellaneous

1.0.1 Commands on Shell

```
1 # compile
2 g++ $1.cpp --std=c++17 -Wall -Wextra -O2 -o $1
3 diff output.txt answer.txt
4 # before running shell file
5 chmod 700 any_shell_file.sh
```

1.0.2 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 /*
4 #include <ext/pb_ds/assoc_container.hpp>
5 #include <ext/pb_ds/tree_policy.hpp>
6 using namespace __gnu_pbds;
7 typedef tree<int, null_type, less<int>, rb_tree_tag,
8     ↳ tree_order_statistics_node_update> ordered_set;
9 */
10 typedef long long ll;
11 typedef long double ld;
12 template<class T>using PQMax=priority_queue<T>;
13 template<class T>using PQMin=priority_queue<T, vector<T>,
14     ↳ greater<T>>;
15 template<class T1, class T2>
```

```
16 void minimize(T1 &a, T2 b){ if (b < a) a = b; }
17 template<class T> void read(T &number) {
18     bool negative = false; register int c;
19     number = 0; c = getchar();
20     while (c!='-' && !isalnum(c)) c = getchar();
21     if (c=='-') negative = true, c = getchar();
22     for (; (c>47 && c<58); c=getchar())
23         number = number*10 + c-48;
24     if (negative) number *= -1;
25 }
26 template<class T, class ...Ts>
27 void read(T &a, Ts&... args){
28     read(a); read(args...);
29 }
30
31 #define fi first
32 #define se second
33 #define FOR(type,i,a,b) for(type i=(a); i<=(b); i++)
34 #define REV(type,i,b,a) for(type i=(b); i>=(a); i--)
35 #define EFOR(type,i,a,b) for(type i=(a); i<(b); i++)
36 #define EREV(type,i,b,a) for(type i=(b); i>(a); i--)
37 #define testBit(n, bit) ((n) >> (bit)) & 1
38 #define flipBit(n, bit) ((n) ^ (1ll << (bit)))
39 #define cntBit(n) __builtin_popcount(n)
40 #define cntBitll(n) __builtin_popcountll(n)
41 #define log2(n) (31 - __builtin_clz(n))
42 #define log2ll(n) (63 - __builtin_clzll(n))
43 #define CURRENT_TIMESTAMP
44     ↳ chrono::steady_clock::now().time_since_epoch().count()
45 #define randomize mt19937_64 mt(CURRENT_TIMESTAMP)
46
47 // remember to fill in:
48 // #define MAX ???
49 // #define MOD ???
50 // int main()
51 // {ios_base::sync_with_stdio(0);cin.tie(0);}
```

2 Mathematics

2.1 Data structure

2.1.1 Modulo

```
1 typedef unsigned long long ull;
2 struct modint{
3     inline static /*const*/ ll MOD = 998244353;
4     int v;
5     static inline ll mod(ll num) {
6         ll val=num-ull((__uint128_t(-1ULL/MOD)*num)>>64)*MOD;
7         return val-(val>=MOD)*MOD;
8     }
9     modint inv() const{
10         ll answer = 1, a = v, n = MOD - 2;
11         while (n) {
12             if (n & 1) answer = mod(answer * a);
```

```
13         a = mod(a * a); n >>= 1;
14     }
15     return answer;
16 }
17
18 modint(ll a = 0)
19 { v=(a<0)?(MOD-mod(-a)):mod(a);v-=(v>=MOD)*MOD; }
20 inline modint& operator += (modint b)
21 { v+=b.v; v-=(v>=MOD)*MOD; return *this; }
22 inline modint& operator -= (modint b)
23 { v+=MOD-b.v; v-=(v>=MOD)*MOD; return *this; }
24 inline modint& operator *= (modint b)
25 { v = mod(1ll * v * b.v); return *this; }
26 inline modint& operator /= (modint b)
27 { return (*this)*=b.inv(); }
28 inline modint& operator ^= (ll n) {
29     modint a = v; v = 1;
30     while (n) {if (n & 1) *this *= a; a *= a, n >>= 1;}
31     return *this;
32 }
33 };
34 #define NEWOP(op, op2) inline modint operator op\
35     (modint a, modint b) {return a op2 b;}
36 NEWOP(+,+=);NEWOP(-,=-);NEWOP(*,*=);NEWOP(/,/=);
37 #undef NEWOP
38 #define NEWCMP(op) inline bool operator op\
39     (modint a, modint b) {return a.v op b.v;}
40 NEWCMP(==);NEWCMP(!=);NEWCMP(<);NEWCMP(>);NEWCMP(<=);NEWCMP(>=);
41 #undef NEWCMP
42 inline modint operator - (modint a){return -a.v;}
43 inline modint operator ^ (modint a, ll n){return a^=n;}
44 inline istream& operator >> (istream& s, modint &i)
45 { ll tmp; s >> tmp; i = tmp; return s; }
46 inline ostream& operator << (ostream& s, modint i)
47 {return s << i.v;}
```

2.1.2 BigInteger

```
1 #include "../miscellaneous/template.hpp"
2 #include "../math/numerical/ntt.hpp"
3
4 // potential MLE in reserve() && resize()
5 class bigint {
6     using vc = vector<char>;
7     private:
8         bool neg = false;
9         vc ds;
10         inline bigint&flipNega(){neg=!neg;return *this;}
11         inline void reformat() {
12             while ((int)ds.size() > 1 && *(ds.rbegin()) == 0)
13                 ↳ ds.pop_back();
14             if (ds.size() == 1 && ds[0] == 0) neg = false; }
15         inline bigint& _pD(const bigint&num, int p10=0) {
16             resize(max(size(), num.size() + p10)); bool nho = 0;
17             EFOR(int, i, p10, num.size() + p10) {
18                 ds[i] += nho + num.ds[i-p10];
19                 nho = ds[i] > 9; ds[i] -= 10 * nho; }
```

```

19     EFOR(int, i, num.size() + p10, size()) {
20         ds[i] += nho; nho = ds[i] > 9; ds[i] -= 10 * nho;
21         if (nho == 0) break; }
22     if (nho) push_back(nho); return *this; }
23 inline bool ltAbs(const bigint& oth, bool xV, bool
    ↪ eqV) const {
24     if (size() != oth.size()) return size() < oth.size();
25     REV(int, i, size() - 1, 0) if (ds[i] != oth.ds[i])
26         return (ds[i] < oth.ds[i]) xor xV;
27     return eqV; }
28 inline bigint& _mD(const bigint& num) {
29     bool flip = ltAbs(num, false, false);
30     const vc *big = &(flip ? num.ds : ds),
31         *small = &(flip ? ds : num.ds);
32     resize(big->size());
33
34     bool nho = 0;
35     EFOR(int, i, 0, small->size()) {
36         ds[i] = (*big)[i] - (nho + (*small)[i]);
37         nho = ds[i] < 0; ds[i] += 10 * nho; }
38     EFOR(int, i, small->size(), size()) {
39         ds[i] = (*big)[i] - nho; nho = ds[i] < 0;
40         ds[i] += 10 * nho; if (nho == 0) break; }
41     if (nho or flip) flipNeg();
42     if (nho) push_back(nho); else reformat();
43     return *this; }
44
45 public:
46     inline static string _I;
47     /* constructors */
48     bigint() { ds = {0}; }
49     bigint(ll num) {
50         if (num == 0) { ds = {0}; return; } ds.reserve(18);
51         while (num) ds.push_back(num % 10), num /= 10; }
52     bigint(string s) {
53         ds.reserve(s.size());
54         REV(int, j, (int)s.size() - 1, 0)
55             if (s[j] != '-') ds.push_back(s[j] - '0');
56         else neg = true;
57         reformat(); }
58     bigint(vc &ds, bool neg) : ds(ds), neg(neg) { reformat(); }
59     bigint(vc &&ds, bool neg) : ds(ds), neg(neg) { reformat(); }
60     /* access data */
61     inline bool isN() const { return neg; }
62     inline char& operator[] (int idx) { return ds[idx]; }
63     /* copy vector api */
64     inline int size() const { return ds.size(); }
65     inline bool empty() const { return ds.empty(); }
66     inline void pop_back() { ds.pop_back(); }
67     inline void reserve(int sz) { ds.reserve(sz); }
68     inline void resize(int sz) { ds.resize(sz); }
69     inline void push_back(char c) { ds.push_back(c); }
70     /* comparator */
71     inline bool operator == (const bigint& oth) const {
72         if (isN() != oth.isN() || size() != (int) oth.size()) return 0;
73         REV(int, i, size() - 1, 0) if (ds[i] != oth.ds[i]) return false;
74         return true; }

```

```

75     inline bool operator < (const bigint& oth) const
76     { return (isN() != oth.isN()) ? isN() : ltAbs(oth, isN(), 0); }
77     inline bool operator <= (const bigint& oth) const
78     { return (isN() != oth.isN()) ? isN() : ltAbs(oth, isN(), 1); }
79     inline bool operator != (const bigint& num) const
80     { return not operator==(num); }
81     inline bool operator >= (const bigint& num) const
82     { return not operator<(num); }
83     inline bool operator > (const bigint& num) const
84     { return not operator<=(num); }
85     // fix rvalue error/improve performance by:
86     // inline bool operator ... (bigint &&num) const
87     // { return operator ... (num); }
88
89     /* operator + - * / */
90     inline bigint operator - () const
91     { return bigint(*this).flipNeg(); }
92     inline bigint& operator += (const bigint& num)
93     { return (num.isN() == isN()) ? _pD(num) : _mD(num); }
94     inline bigint& operator -= (const bigint& num)
95     { return (num.isN() == isN()) ? _mD(num) : _pD(num); }
96     inline bigint operator + (const bigint& num)
97     { bigint res(*this); res += num; return res; }
98     inline bigint operator - (const bigint& num)
99     { bigint res(*this); res -= num; return res; }
100    inline bigint operator * (const bigint& num) const {
101        if (*this == 0 || num == 0 || empty() || num.empty()) return 0;
102        if (size() == 1 or num.size() == 1) {
103            const vector<char> &D = (size() == 1) ? num.ds : ds;
104            char mul = (size() == 1) ? ds[0] : num.ds[0];
105            bigint ans; ans.resize(D.size()); char nho = 0;
106            EFOR(int, i, 0, D.size()) {
107                ans[i] = D[i] * mul + nho; nho = ans[i] / 10;
108                ans[i] -= 10 * nho;
109            }
110            if (nho) ans.push_back(nho);
111            if (isN() xor num.isN()) ans.flipNeg();
112            return ans;
113        }
114        /* FFT */
115        FFT::buildRoot();
116        vector<int> a(ds.begin(), ds.end());
117        vector<int> b(num.ds.begin(), num.ds.end());
118        vector<modint> newAns = FFT::multiply(a, b);
119        bigint ans; ans.resize(newAns.size());
120        int nho = 0;
121        EFOR(int, i, 0, ans.size()) {
122            int tmp = newAns[i].v + nho;
123            nho = tmp / 10;
124            ans[i] = tmp - nho * 10;
125        }
126        while (nho > 0) { ans.push_back(nho % 10); nho /= 10; }
127        /* Karatsuba */
128        // int mSz = max(size(), num.size()), B = mSz / 2;
129        // bigint a0(vector<char>(ds.begin(), ds.begin() +
    ↪ min(B, size())), false),

```

```

130     // a1(vector<char>(ds.begin() + min(B, size()), ds.end()
    ↪ ), false),
131     // b0(vector<char>(num.ds.begin(),
    ↪ num.ds.begin() + min(B, num.size())), false),
132     // b1(vector<char>(num.ds.begin() + min(B, num.size()),
    ↪ num.ds.end()), false);
133     // ans = a0 * b0; bigint
    ↪ z2 = a1 * b1, z1 = (a0 + a1) * (b0 + b1) - (z2 + ans);
134     // ans._pD(z2, B * 2)._pD(z1, B);
135     if (isN() xor num.isN()) ans.flipNeg();
136     ans.reformat(); return ans;
137 }
138 friend istream& operator >> (istream& inp, bigint& num)
139     { inp >> bigint::_I; num = bigint(bint::_I); return inp; }
140 friend ostream& operator << (ostream& out, const bigint& num) {
141     if (num.isN()) out << '-';
142     REV(int, i, (int) num.size() - 1, 0) out << char(num
    ↪ .ds[i] + '0');
143     return out;
144 }
145 };

```

2.2 Number Theory

2.2.1 Mildly-optimized sieve(Factorable)

```

1 // remember to call sieve() before any factorize()
2 namespace Eratos_Factorable {
3     constexpr ll MAX = 100000000;
4     constexpr ll EST = 53000000; // 1.1 * MAX / ln(MAX)
5     int smallDiv[MAX + 1] = {};
6     int primes[EST], cntPrime = 0;
7     inline void sieve(int size = MAX) {
8         memset(smallDiv, false, sizeof(smallDiv));
9         primes[++cntPrime] = 2; primes[++cntPrime] = 3;
10        for (int i = 2; i <= size; i += 2) smallDiv[i] = 2;
11        for (int i = 3; i <= size; i += 6) smallDiv[i] = 3;
12        for (int mul = 1; 6 * mul - 1 <= size; mul++) {
13            bool pass = false;
14            for (int i : {6 * mul - 1, 6 * mul + 1}) if (!smallDiv[i]) {
15                primes[++cntPrime] = i; smallDiv[i] = i;
16                for (ll j = 11 * i; j <= size; j += i * 2)
17                    if (not smallDiv[j]) smallDiv[j] = i;
18                if (11 * i * i > size) pass = true;
19            }
20            if (pass) break;
21        }
22    }
23    inline vector<int> factorize(ll number) {
24        vector<int> ans;
25        while (number > 1) {
26            int d = smallDiv[number];
27            while (number % d == 0)
28                ans.push_back(d), number /= d;
29        }
30        return ans;
31    }

```

```
32 }
```

2.2.2 Primality check

```
1 #define MAX 1000001
2 #define MOD 1000000007
3
4 namespace MillerRabin{
5     typedef __int128_t i128;
6     constexpr int SMALL_PRIMES[12] =
7         ↪ {2,3,5,7,11,13,17,19,23,29,31,37};
8
9     inline ll _power(ll a, ll n, ll mod) {
10         ll ans = 1;
11         while (n) {
12             if (n & 1) ans = (i128)ans * a % mod;
13             a = (i128)a * a % mod; n >>= 1;
14         }
15         return ans;
16     }
17     inline bool _fermatCheck(ll n, ll a, ll pw, int p2) {
18         ll num = _power(a, pw, n);
19         if (num == 1 || num == n - 1) return true;
20         FOR(int, i, 1, p2-1) {
21             num = (i128) num * num % n;
22             if (num == n - 1) return true;
23         }
24         return false;
25     }
26     inline bool checkPrime(const ll n) {
27         if (n == 2 || n == 3 || n == 5 || n == 7) return true;
28         if (n < 11 || (n & 1) == 0) return false;
29         ll d = n-1; int p2 = 0;
30         while ((d & 1) == 0) d >>= 1, p2++;
31         for (int a: SMALL_PRIMES)
32             if (n == a) return true;
33             else if (not _fermatCheck(n, a, d, p2))
34                 return false;
35         return true;
36     }
37 }
```

2.2.3 Prime factorization

```
1 #include "millerrabin.hpp"
2 randomize;
3 namespace Pollards{
4     typedef __int128_t i128;
5     #define sqp1(a, b, mod) (((i128(a)*(a)+(b)))%(mod))
6     #define rand(mt)%1'000'000'000 + 1)
7     inline vector<ll> rho(ll n) {
8         if (n == 1) return {};
9         if (MillerRabin::checkPrime(n)) return {n};
10        vector<ll> ans;
11        if (n % 2 == 0) {
12            while (n % 2 == 0) ans.push_back(2), n /= 2;
```

```
13        vector<ll> others = rho(n);
14        ans.insert(ans.end(), others.begin(), others.end());
15        return ans;
16    }
17    ll x = 2, y = 2, g = 1, b = 1;
18    while (g == 1) {
19        x=sqp1(x,b,n); y=sqp1(y,b,n); y=sqp1(y,b,n);
20        g = __gcd(abs(x-y), n);
21        if (g == n) x=y=rand, b=rand, g=1;
22    }
23    vector<ll> tmp1 = rho(g), tmp2 = rho(n / g);
24    ans.insert(ans.end(), tmp1.begin(), tmp1.end());
25    ans.insert(ans.end(), tmp2.begin(), tmp2.end());
26    return ans;
27 }
28 }
```

2.2.4 Gauss

```
1 #include "../miscellaneous/template.hpp"
2 #include "../ds/modint.hpp"
3 #define MAX 500
4 namespace Gaussian {
5     struct Equation {
6         vector<modint> cf; modint sum; // cf coef
7         void div(modint d){ for(modint&num:cf)num/=d;sum/=d; }
8         void minus(Equation &eq, modint mul) {
9             FOR(int,i,0,(int)cf.size()-1)cf[i]==eq.cf[i]*mul;
10            sum -= eq.sum * mul; } };
11    struct Elimination{
12        int SZ=0;Elimination(){}Elimination(int SZ):SZ(SZ){}
13        Equation eqs[MAX]; int cnt = 0; int col[MAX];
14
15        void add(Equation eq) { eqs[cnt++] = eq; }
16        int size() {return SZ;} int count() {return cnt;}
17        pair<vector<modint>, vector<vector<modint>>> solve() {
18            int ln = 0;
19            FOR(int, i, 0, size()-1) {
20                int ptr = ln;
21                while (ptr < count() and eqs[ptr].cf[i] == 0) ptr++;
22                if (ptr==count())continue; swap(eqs[ln],eqs[ptr]);
23                eqs[ln].div(eqs[ln].cf[i]);
24                FOR(int, j, 0, count()-1) if (j != ln)
25                    eqs[j].minus(eqs[ln], eqs[j].cf[i]);
26                col[ln++] = i; }
27            FOR(int,i,ln,count()-1) if(eqs[i].sum!=0) return{};
28            vector<modint> sol(SZ); vector<vector<modint>> basis;
29            REV(int, i, size()-1, 0) {
30                if (i != col[ln-1]) {
31                    vector<modint> cur(SZ); cur[i] = 1;
32                    FOR(int,row,0,ln-1)cur[col[row]]-=eqs[row].cf[i];
33                    basis.push_back(cur); continue; }
34            sol[i] = eqs[i].sum; }
35            return {sol, basis}; } };
```

2.3 Numerical

2.3.1 FFT

```
1 #include "../miscellaneous/template.hpp"
2
3 #define MAX 1000001
4 #define MOD 1000000007
5
6 typedef complex<ld> cd;
7 namespace FFT{
8     const ld TAU = acos(-1) * 2;
9     // 3.14159'26535'89793'23846'26433'83279'50288'41971
10    // '69399'37510'58 * 2;
11
12    constexpr int BIT = 20, MAX_LEN = 1 << BIT;
13    vector<int> _rev[BIT + 1];
14    cd _root[MAX_LEN + 1];
15    void buildRoot() {
16        _root[0] = _root[MAX_LEN] = 1;
17        for (int i=BIT-1, dist=1<<(BIT-1); i>=0; i--,
18            ↪ dist>>=1) {
19            cd w = polar(ld(1.0), TAU * dist / MAX_LEN);
20            for (int pos = 0; pos < MAX_LEN; pos += 2 * dist)
21                _root[pos + dist] = _root[pos] * w;
22        }
23        _rev[0] = {0};
24        for (int bit=1, len=2; len<=MAX_LEN; bit++, len*=2) {
25            _rev[bit].resize(len, 0);
26            for (int i = 0; i < len; i++)
27                _rev[bit][i]=((i&1)<<(bit-1))|_rev[bit-1][i/2];
28        }
29        void dft(vector<cd> &poly, bool invert = false) {
30            assert((cntBit((int)poly.size()) == 1));
31            const int n = poly.size(), coef = MAX_LEN / n;
32            for (int dist=n/2, span=n; dist>0; dist/=2, span/=2)
33                for (int pos = 0; pos < dist; pos++)
34                    for (int i=pos, k=0; i<n; i+=span, k+=dist) {
35                        int len = log2(n / span);
36                        int newK = _rev[span][k / dist] * dist;
37                        int tmp = (invert ? (n - newK) : newK) * coef;
38                        cd a = poly[i], b = _root[tmp] * poly[i + dist];
39                        poly[i] = a + b, poly[i + dist] = a - b;
40                    }
41            if (invert) for (cd &x: poly) x /= n;
42        }
43        template<class T>vector<T>conv(vector<T>_a,vector<T>_b){
44            int len = int(_a.size() + _b.size()) - 1;
45            int bit = log2(len)+(cntBit(len)>1); len=1<<bit;
46            vector<cd> a(len);
47            for (int i = 0; i < len; i++)
48                a[i] = cd((i < _a.size())?_a[i]:0,
49                    ↪ (i<_b.size())?_b[i]:0);
49            dft(a, false);
50            for (int i = 0; i < len; i++)
51                if (i < _rev[bit][i]) swap(a[i], a[_rev[bit][i]]);
```

```

52   for (int i = 0; i < len; i++) a[i] *= a[i];
53   vector<cd> b(a.begin(), a.end());
54   for (int i = 0; i < len; i++)
55       b[i] = a[i] - conj(a[-i & (len-1)]); //(n-i)%n
56   dft(b, true);
57   for (int i = 0; i < len; i++)
58       if (i < _rev[bit][i]) swap(b[i], b[_rev[bit][i]]);
59
60   while (len > 0 && b[len - 1].imag() < 1e-9) len--;
61   vector<T> ans(len);
62   FOR(int, i, 0, len-1) ans[i]=round(b[i].imag()/4.0);
63   return ans;
64 }
65 }

```

2.3.2 NTT

k -th root of unity, mod p : ω_k satisfies
$$\begin{cases} \omega_k^k \equiv 1 \\ \omega_k^i \not\equiv \omega_k^j & (i \neq j) \end{cases}$$

$p = c \times 2^k + 1 \Rightarrow w_{2^k} = g^c$ w/ any $g : \gcd(g, p) = 1$
only works for p with big k (e.g. 998244353 w/ $k = 23$ below)

```

1  #include "../math/ds/modint.hpp"
2
3  // MOD=998244353=c*2^k+1 => ROOT=g^c, any g: gcd(g,MOD)=1
4  namespace FFT{
5      constexpr int K_MOD = 23, BIT = 22, MAX_LEN = 1 << BIT;
6      constexpr int ROOT = 15311432;
7
8      modint _root[MAX_LEN + 1];
9      vector<int> _rev[BIT + 1];
10     bool _built = false;
11     void buildRoot() {
12         if (_built) return; _built = true;
13         _root[0] = 1; modint mul=ROOT;
14         FOR(int, i, 1, K_MOD-BIT) mul*=mul;
15         FOR(int, i, 1, MAX_LEN) _root[i] = _root[i-1] * mul;
16         for (int bit=0, len=1; len<=MAX_LEN; bit++, len*=2) {
17             _rev[bit].resize((1 << bit), 0);
18             for (int i = 1; i < (1 << bit); i++)
19                 _rev[bit][i]=((i&1)<<(bit-1))|_rev[bit-1][i/2];
20         }
21     }
22
23     void transform(vector<modint> &v, bool invert){
24         const int len = v.size(), coef = MAX_LEN / len;
25         const int bit = log2(len);
26         FOR(int, i, 0, len-1) if (i < _rev[bit][i])
27             swap(v[i], v[_rev[bit][i]]);
28
29         for (int jmp=1, span=2; span<=len; jmp*=2, span*=2)
30             for (int beg = 0; beg < len; beg += span)
31                 for (int i = 0; i < jmp; i++) {
32                     int k=coef*len/jmp*i/2; if (invert) k=MAX_LEN-k;
33                     modint a = v[beg+i], b = _root[k] * v[beg+i+jmp];

```

```

34         v[beg + i] = a + b; v[beg + i + jmp] = a - b;
35     }
36     if (invert) FOR(int, i, 0, len-1) v[i] /= len;
37 }
38 template<class T>
39 vector<modint> multiply(vector<T> &a, vector<T> &b) {
40     int len = int(_a.size() + _b.size()) - 1;
41     len = 1 << (log2(len) + (cntBit(len) > 1));
42     vector<modint> a(_a.begin(), _a.end()); a.resize(len, 0);
43     vector<modint> b(_b.begin(), _b.end()); b.resize(len, 0);
44     transform(a, false); transform(b, false);
45     FOR(int, i, 0, len - 1) a[i] *= b[i];
46     transform(a, true); return a;
47 }
48 }

```

3 String

3.1 Data Structures

3.1.1 HashStr

```

1  class Hash {
2      #define op operator
3  private:
4      inline static constexpr int SZ = 2, MOD[6] = {
5          (int) 1e9+7, (int) 1e9+20041203, (int) 1e9+2277,
6          (int) 1e9+5277, (int) 1e9+8277, (int) 1e9+9277,
7      };
8      int val[SZ] = {};
9      static ll pw(ll a, ll n, ll mod) {
10         ll answer = 1;
11         for (; n > 0; a = a * a % mod, n >>= 1)
12             if (n & 1) answer = answer * a % mod;
13         return answer;
14     }
15 public:
16     Hash(ll num){EFOR(int,i,0,SZ)val[i]=num%MOD[i];}
17     Hash(): Hash(0) {}
18     int& op[] (int idx) {return val[idx];}
19     bool op == (const Hash &oth) const {
20         EFOR(int,i,0,SZ)if(oth.val[i]!=val[i])return false;
21         return true;
22     }
23     bool op < (const Hash &oth) const {
24         EFOR(int,i,0,SZ)
25             if(oth.val[i]!=val[i]) return val[i]<oth.val[i];
26         return false;
27     }
28     bool op <= (const Hash &oth) const {
29         EFOR(int, i, 0, SZ)
30             if(oth.val[i]!=val[i])return val[i]<oth.val[i];
31         return true;
32     }
33     bool op != (const Hash&oth)const{return not op==(oth);}
34     bool op > (const Hash&oth)const{return not op<=(oth);}

```

```

35     bool op >= (const Hash&oth)const{return not op<(oth);}
36     Hash& op += (Hash &oth) {
37         EFOR(int,i,0,SZ)val[i]=(val[i]+oth[i])%MOD[i];
38         return *this;
39     }
40     Hash& op -= (Hash &oth) {
41         EFOR(int,i,0,SZ)val[i]=(val[i]+MOD[i]-oth[i])%MOD[i];
42         return *this;
43     }
44     Hash& op *= (Hash &oth) {
45         EFOR(int,i,0,SZ)val[i]=(1ll*val[i]*oth[i])%MOD[i];
46         return *this;
47     }
48     Hash inv() const {
49         Hash ans; EFOR(int, i, 0, SZ)
50             ans[i] = pw(val[i], MOD[i]-2, MOD[i]);
51         return ans;
52     }
53     Hash& op/=(const Hash&oth){return op*=(oth.inv());}
54     Hash& op+=(Hash&oth){ return op+=(oth);}
55     Hash& op-=(Hash&oth){ return op-=(oth);}
56     Hash& op*=(Hash&oth){ return op*=(oth);}
57     Hash& op/=(Hash&oth){ return op/=(oth);}
58     friend Hash op+(Hash a,Hash b){return(a += b);}
59     friend Hash op-(Hash a,Hash b){return(a -= b);}
60     friend Hash op*(Hash a,Hash b){return(a *= b);}
61     friend Hash op/(Hash a,Hash b){return(a /= b);}
62     friend ostream& op << (ostream& out, const Hash &num) {
63         out << "(";
64         EFOR(int,i,0,SZ)out<<num.val[i]<<","; "[i==SZ-1];
65         return out;
66     }
67 };
68
69 class HashString {
70 private:
71     inline static constexpr int MAX = 1e6, BASE = 311;
72     inline static Hash _p[MAX + 1], _i[MAX + 1];
73     Hash *sF, *sB; int len;
74     inline static bool _init = false;
75 public:
76     static void init() {
77         _init = true; _p[0] = 1;
78         FOR(int, i, 1, MAX) _p[i] = _p[i-1] * BASE;
79         _i[MAX] = _p[MAX].inv();
80         REV(int, i, MAX-1, 0) _i[i] = _i[i + 1] * BASE;
81         FOR(int, i, 0, MAX) assert(_i[i] * _p[i] == 1);
82     }
83     HashString(string s = "") {
84         if (not _init) init(); len = s.size();
85         sF=new Hash[len+1],sB=new Hash[len+2];
86         sF[0]=sB[len+1]=0;
87         FOR(int,i,1,len)sF[i]=sF[i-1]+s[i-1]*_p[i];
88         REV(int,i,len,1)sB[i]=sB[i+1]+_p[len-i+1]*s[i-1];
89     }
90     ~HashString() {}

```



```

91
92 int getLength() const {return len;}
93 Hash getF(int l,int r){return (sF[r]-sF[l-1])*_i[l-1];}
94 Hash getB(int l,int r){return (sB[l]-sB[r+1])*_i[len-r];}
95 Hash getF(int idx) {return sF[idx];}
96 Hash getB(int idx) {return sB[idx];}
97 };

```

4 Data Structures

4.1 Trees

4.1.1 Persistent Segment Tree

```

1 namespace Persistent{
2 template<class T> struct Node {
3     Node *l, *r; T val;
4     Node(): Node(T()) {}
5     Node(T val): Node(val, nullptr, nullptr) {}
6     Node(T val, Node* l, Node* r): l(l), r(r), val(val) {}
7 };
8 struct Range{
9     inline static int N; int l, r, mid;
10    inline static void init(int N) {Range::N = N;}
11    Range(): Range(N) {} Range(int n): Range(1, n){}
12    Range(int l, int r): l(l), r(r) {mid = (l+r)/2;}
13    inline bool isSingle() {return l == r;}
14    inline bool contains(int x) {return l<=x&&x<=r;}
15    inline bool isInside(int L, int R) {return L<=l&&r<=R;}
16    inline bool noRelate(int L, int R) {return r<L || R<l;}
17    inline Range L() {return {l, mid};}
18    inline Range R() {return {mid+1, r};}
19 };
20 template<class T> struct SegTree {
21     static const T DEF_VAL;
22     inline static T process(T a, T b);
23     vector<Node<T>*> trees;
24     SegTree() {}
25     template<class T2>
26     Node<T>* _buildTree(T2 *arr, Range rng) {
27         if (rng.isSingle())
28             return new Node<T>(arr[rng.l]);
29         Node<T>* l = _buildTree(arr, rng.L());
30         Node<T>* r = _buildTree(arr, rng.R());
31         return new Node<T>(process(l -> val, r -> val), l, r);
32     }
33     Node<T>* _newRoot(Node<T>* root) {
34         return new Node<T>(*root);
35     }
36     Node<T>* _update(Range rng, Node<T>* node, int pos, T
37         ↪ val) {
38         if (rng.isSingle())
39             return new Node<T>(val);
40         Node<T>* l = node -> l, *r = node -> r;
41         if (rng.L().contains(pos))
42             l = _update(rng.L(), l, pos, val);

```

```

42     else
43         r = _update(rng.R(), r, pos, val);
44     return new Node<T>(process(l -> val, r -> val), l, r);
45 }
46 T _get(Range rng, Node<T>* node, int L, int R) {
47     if (rng.noRelate(L, R)) return DEF_VAL;
48     if (rng.isInside(L, R)) return node -> val;
49     return process(
50         _get(rng.L(), node -> l, L, R),
51         _get(rng.R(), node -> r, L, R)
52     );
53 }
54
55 template<class T2>void buildTree(T2* arr) {
56     trees = {_buildTree(arr, Range())};
57 }
58 void addTree(int from) {
59     assert(from < (int)trees.size());
60     trees.push_back(_newRoot(trees[from]));
61 }
62 void update(int from, int pos, T val) {
63     assert(from < (int)trees.size());
64     trees[from] = _update(Range(), trees[from], pos, val);
65 }
66 T get(int from, int L, int R) {
67     assert(from < (int)trees.size());
68     return _get(Range(), trees[from], L, R);
69 }
70 };
71
72 // remember to declare:
73 // template<> const T Persistent::SegTree<T>::DEF_VAL
74 // template<> T Persistent::SegTree<T>::process(T a, T b)

```

5 Graph

5.1 Shortest Path

5.1.1 SPFA

Somehow this passed yosupo's Library Checker.

```

1 #define MAX 1000001
2 struct Node
3 {
4     int node, len;
5     Node() {node = len = 0;}
6     Node(int node, int len) {this -> node = node, this ->
7         ↪ len = len;}
8 };
9 namespace SPFA{
10 int n; vector<Node> graph[MAX];
11 constexpr ll oo = (1e18+1);
12 bool in[MAX]; int cnt[MAX];
13 ll d[MAX], trace[MAX];
14 deque<int> q;
15 randomize;

```

```

15
16 void spfa(int root, bool detect){
17     FOR(int, i, 0, n)
18         shuffle(graph[i].begin(), graph[i].end(), mt);
19     memset(d, 0x3f, sizeof(d));
20
21     d[root] = 0; q.push_back(root);
22     ll qSum = 0;
23     while (!q.empty()) {
24         while (d[q.front()] > d[q.back()])
25             { q.push_back(q.front()); q.pop_front(); }
26         int node = q.front(); q.pop_front();
27         in[node] = false;
28         const int LIM = sqrt(n);
29         qSum -= d[node];
30         for (Node ch: graph[node]) {
31             int child=ch.node;
32             ll chDist=(d[node]==-oo) ? -oo : (d[node]+ch.len);
33             if (chDist >= d[child]) continue;
34             qSum=max(-oo,qSum+chDist-in[child]*d[child]);
35             d[child] = chDist, trace[child] = node;
36             if (in[child]) continue;
37             if (++cnt[child] == n) {
38                 if (not detect) break;
39                 d[child] = chDist = -oo;
40             }
41             in[child] = true;
42             if (cnt[child] > LIM or d[child] * q.size() > qSum)
43                 q.push_back(child);
44             else if (q.empty() or d[child] <= d[q.front()])
45                 q.push_front(child);
46             else
47                 q.push_back(child);
48         }
49     }
50 }
51 }

```