

3 Computation of the HW95 tidal potential catalogue

Our catalogue HW95 of the Earth tide generating potential has been computed by using an expansion of the form

$$V(t) = \sum_{\ell=1}^{\ell=\ell_{\max}} \sum_{m=0}^{m=\ell} \left(\frac{r}{a}\right)^{\ell} \bar{P}_{\ell m}(\cos \theta) \sum_i [C_i^{\ell m}(t) \cos(\alpha_i(t)) + S_i^{\ell m}(t) \sin(\alpha_i(t))] \quad (5)$$

The time dependent tidal potential coefficients are given by

$$C_i^{\ell m}(t) = C0_i^{\ell m} + t \cdot C1_i^{\ell m} \quad (6)$$

$$S_i^{\ell m}(t) = S0_i^{\ell m} + t \cdot S1_i^{\ell m} \quad (7)$$

where the potential coefficients $C0_i^{\ell m}$ and $S0_i^{\ell m}$ have the dimension m^2/s^2 and the linear drift coefficients $C1_i^{\ell m}$ and $S1_i^{\ell m}$ have the dimension $m^2/s^2/J.cy$. The arguments $\alpha_i(t)$ are computed from

$$\alpha_i(t) = m \cdot \lambda + \sum_{j=1}^{j=11} k_{ij} \cdot arg_j(t) \quad \text{with } k_{i1} = m. \quad (8)$$

The integer coefficients k_{ij} are given in our catalogue, while the eleven astronomical arguments $arg_j(t)$ (τ = mean local lunar time, s = mean lunar longitude, h = mean solar longitude, p = mean longitude of lunar perigee, N' = negative mean longitude of the lunar ascending node, p_s = mean longitude of solar perigee, L_{Mer} = mean longitude of Mercury, L_{Ven} = mean longitude of Venus, L_{Mar} = mean longitude of Mars, L_{Jup} = mean longitude of Jupiter, L_{Sat} = mean longitude of Saturn) can be computed from polynomials in time, given

Table 12: Fundamental frequencies in °/hour after Simon et al. (1994) at J2000

| j | argument | symbol | frequency [°/hour] |
|-----|---|-----------|--------------------|
| 1. | mean local lunar time | τ | 14.492 052 120 18 |
| 2. | mean lunar longitude | s | 0.549 016 519 73 |
| 3. | mean solar longitude | h | 0.041 068 639 91 |
| 4. | mean longitude of lunar perigee | p | 0.004 641 813 41 |
| 5. | negative mean longitude of lunar ascending node | N' | 0.002 206 406 87 |
| 6. | mean longitude of solar perigee | p_s | 0.000 001 961 51 |
| 7. | mean longitude of Mercury | L_{Mer} | 0.170 515 710 90 |
| 8. | mean longitude of Venus | L_{Ven} | 0.066 757 030 52 |
| 9. | mean longitude of Mars | L_{Mar} | 0.021 836 295 20 |
| 10. | mean longitude of Jupiter | L_{Jup} | 0.003 463 726 64 |
| 11. | mean longitude of Saturn | L_{Sat} | 0.001 395 746 14 |

Table 13: Polynomial coefficients for astronomical arguments after Simon et al. (1994), units are: ° and °/1000 yrs

| j | Constant | t | t^2 | t^3 | t^4 |
|-----|--------------------|------------------------|---------------|---------------|---------------|
| 1. | 242.149 804 529 99 | 127 037 328.885 530 56 | 0.176 961 11 | -0.001 831 40 | 0.000 088 24 |
| 2. | 218.316 645 629 99 | 4 812 678.811 957 50 | -0.146 638 89 | 0.001 851 40 | -0.000 153 55 |
| 3. | 280.466 450 160 02 | 360 007.697 488 06 | 0.030 322 22 | 0.000 020 00 | -0.000 065 32 |
| 4. | 83.353 243 119 98 | 40 690.136 352 50 | -1.032 172 22 | -0.012 491 68 | 0.000 526 55 |
| 5. | 234.955 444 990 00 | 19 341.362 619 72 | -0.207 561 11 | -0.002 139 42 | 0.000 165 01 |
| 6. | 282.937 340 980 01 | 17.194 576 67 | 0.045 688 89 | -0.000 017 76 | -0.000 033 23 |
| 7. | 252.250 905 519 99 | 1 494 740.721 722 33 | 0.030 349 84 | 0.000 018 11 | -0.000 065 32 |
| 8. | 181.979 800 850 00 | 585 192.129 533 30 | 0.031 013 95 | 0.000 014 90 | -0.000 065 32 |
| 9. | 355.432 999 580 02 | 191 416.963 702 97 | 0.031 051 87 | 0.000 015 64 | -0.000 065 32 |
| 10. | 34.351 518 740 03 | 30 363.027 748 48 | 0.022 329 72 | 0.000 037 01 | -0.000 052 14 |
| 11. | 50.077 444 300 00 | 12 235.110 686 22 | 0.051 907 83 | -0.000 029 85 | -0.000 097 40 |

Table 11: IERS 1992 numerical constants used for the HW95 catalogue

| Item | Numerical value | Comment |
|---------------|--|---|
| f | 1 / 298.2564219846 | flattening of the Earth's ellipsoid |
| a | 6378136.3 m | semi-major axis of the Earth's ellipsoid |
| $J_{2\oplus}$ | $1.0826362 \cdot 10^{-3}$ | 2nd degree zonal harmonic coeff. of the Earth's gravity field |
| GM | $3.986004418 \cdot 10^{14} \text{ m}^3/\text{s}^2$ | geocentric gravitational constant |
| M/Ea | 0.012300034 | ratio of mass of Moon to that of the Earth |
| S/Me | 6023600 | ratio of mass of Sun to that of the Mercury |
| S/Ve | 408523.71 | ratio of mass of Sun to that of the Venus |
| S/Ea | 332946.045 | ratio of mass of Sun to that of the Earth |
| S/Ma | 3098708. | ratio of mass of Sun to that of the Mars |
| S/Ju | 1047.3486 | ratio of mass of Sun to that of the Jupiter |
| S/Sa | 3497.90 | ratio of mass of Sun to that of the Saturn |

Example for tidal potential catalogue:

Listing of those 45 waves with amplitudes exceeding $1 \cdot 10^{-2} \text{ m}^2/\text{s}^2$:

| number | 1 | m | k | k | k | k | k | k | k | k | k | frequency | CO | SO | C1 | S1 nam |
|--------|----|---|---|----|----|----|----|----|----|----|------------|-------------------------|----|--------------|-----------|--------------|
| | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | (deg/hour) | | | | | |
| C***** | | | | | | | | | | | | | | | | |
| 1 | MO | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.00000000-594428666. | | 0. | -1935360. | 0. MO |
| 3 | SU | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.00000000-2751200919. | | 0. | -890704. | 0. SO |
| 23 | MO | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0.00220641 771788513. | | 0. | -325040. | 0. |
| 194 | SU | 2 | 0 | 0 | 1 | 0 | 0 | -1 | 0 | 0 | 0 | 0.04106668 -137899524. | | 0. | 306581. | 0. SA |
| 358 | SU | 2 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0.08213728 -855082729. | | 0. | 885919. | 0. SSA |
| 799 | MO | 2 | 0 | 1 | -2 | 1 | 0 | 0 | 0 | 0 | 0 | 0.47152105 -185961196. | | 0. | -64233. | 0. MSM |
| 946 | MO | 2 | 0 | 1 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 0.54437471 -972501389. | | 0. | -322767. | 0. MM |
| 984 | MO | 3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.54901652 | 0. | -103721679. | 0. | 22110. |
| 1325 | MO | 2 | 0 | 2 | -2 | 0 | 0 | 0 | 0 | 0 | 0 | 1.01589576 -161326507. | | 0. | -56860. | 0. MSF |
| 1512 | MO | 2 | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1.09803304-1841041825. | | 0. | 1939970. | 0. MF |
| 1529 | MO | 2 | 0 | 2 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1.10023945 -763323862. | | 0. | 324410. | 0. |
| 1989 | MO | 2 | 0 | 3 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 1.64240775 -352500762. | | 0. | 370294. | 0. MTM |
| 2001 | MO | 2 | 0 | 3 | 0 | -1 | 1 | 0 | 0 | 0 | 0 | 1.64461415 -146096331. | | 0. | 62177. | 0. |
| 3876 | MO | 2 | 1 | -3 | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 12.85428619 | 0. | 129857156. | 0. | -86007. 2Q1 |
| 3979 | MO | 2 | 1 | -3 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 12.92713984 | 0. | 156593207. | 0. | -60053. SIG1 |
| 4251 | MO | 2 | 1 | -2 | 0 | 1 | -1 | 0 | 0 | 0 | 0 | 13.39645449 | 0. | 185063773. | 0. | 44599. |
| 4263 | MO | 2 | 1 | -2 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 13.39866089 | 0. | 981305656. | 0. | -510204. Q1 |
| 4388 | MO | 2 | 1 | -2 | 2 | -1 | 0 | 0 | 0 | 0 | 0 | 13.47151455 | 0. | 186260860. | 0. | -76093. R01 |
| 4664 | MO | 2 | 1 | -1 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 13.94082919 | 0. | 966886565. | 0. | 220455. |
| 4681 | MO | 2 | 1 | -1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 13.94303560 | 0. | 5125256711. | 0. | -2762670. 01 |
| 5059 | MO | 2 | 1 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 14.48741031 | 0. | -144896357. | 0. | 63561. |
| 5110 | MO | 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 14.49669393 | 0. | -402872065. | 0. | 161257. M1 |
| 5525 | SU | 2 | 1 | 1 | -3 | 0 | 0 | 1 | 0 | 0 | 0 | 14.91786468 | 0. | 139201619. | 0. | -415011. PI1 |
| 5653 | SU | 2 | 1 | 1 | -2 | 0 | 0 | 0 | 0 | 0 | 0 | 14.95893136 | 0. | 2380313224. | 0. | -1207214. P1 |
| 5946 | MO | 2 | 1 | 1 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 15.03886223 | 0. | 142689589. | 0. | -141064. |
| 5958 | MO | 2 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 15.04106864 | 0. | -4925288540. | 0. | 1908945. K1 |
| 5961 | SU | 2 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 15.04106864 | 0. | -2279779400. | 0. | 875007. K1 |
| 5978 | MO | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 15.04327505 | 0. | -977663900. | 0. | -226210. |
| 6244 | SU | 2 | 1 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 15.12320592 | 0. | -102392652. | 0. | 159986. FI1 |
| 6738 | MO | 2 | 1 | 2 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 15.58544335 | 0. | -403016900. | 0. | 187668. J1 |
| 7106 | MO | 2 | 1 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 16.13910168 | 0. | -220445439. | 0. | 349751. 001 |
| 7112 | MO | 2 | 1 | 3 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 16.14130809 | 0. | -141251705. | 0. | 150453. |
| 8628 | MO | 2 | 2 | -2 | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 27.89535483 313070026. | | 0. | 8483. | 0. 2N2 |
| 8720 | MO | 2 | 2 | -2 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 27.96820848 377850712. | | 0. | 2561. | 0. MI2 |
| 8976 | MO | 2 | 2 | -1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 28.43972953 2365821950. | | 0. | 40182. | 0. N2 |
| 9082 | MO | 2 | 2 | -1 | 2 | -1 | 0 | 0 | 0 | 0 | 0 | 28.51258319 449404707. | | 0. | -2587. | 0. NI2 |
| 9323 | MO | 2 | 2 | 0 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 28.98189783 -461038339. | | 0. | 258211. | 0. |
| 9337 | MO | 2 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 28.9841042412356348081. | | 0. | 130692. | 0. M2 |
| 9622 | MO | 2 | 2 | 1 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 29.52847895 -349288916. | | 0. | -1547. | 0. L2 |
| 9947 | SU | 2 | 2 | 2 | -3 | 0 | 0 | 1 | 0 | 0 | 0 | 29.95893332 335581352. | | 0. | -823253. | 0. T2 |
| 10068 | SU | 2 | 2 | 2 | -2 | 0 | 0 | 0 | 0 | 0 | 0 | 30.00000000 5738394275. | | 0. | 138617. | 0. S2 |
| 10303 | MO | 2 | 2 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 30.08213728 1067392061. | | 0. | -1036988. | 0. K2 |
| 10306 | SU | 2 | 2 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 30.08213728 494523165. | | 0. | -563232. | 0. K2 |
| 10318 | MO | 2 | 2 | 2 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 30.08434369 465420663. | | 0. | -184316. | 0. |
| 12022 | MO | 3 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 43.47615636 -149687399. | | 0. | 993. | 0. M3 |