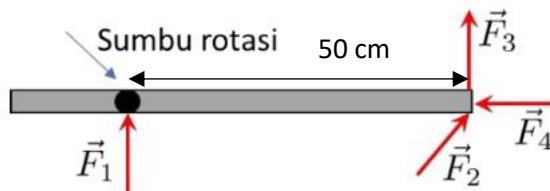




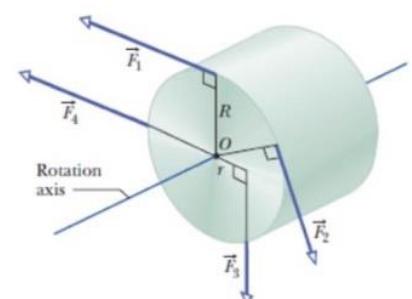
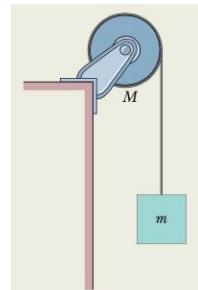
3rd STUDENT ASSIGNMENT SHEET ELEMENTARY PHYSICS IA (FI-1101)
Semester 1 Year 2023-2024
TOPIC: RIGID BODY I

For all problems air resistance can be ignored; use $g = 9,8 \text{ m/s}^2$.

1. A wheel of 10 cm radius rotates with a constant angular speed ω of p rad/s.
 - a. If at $t = 2 \text{ s}$, a point on the edge of the wheel is at an angle $= 30^\circ$ to the positive x-axis, determine its position at $t = 5 \text{ s}$.
 - b. Determine the magnitude of the velocity $t = 2 \text{ s}$.
 - c. Plot the position, angular velocity, and angular acceleration as a function of time.
2. In the following figure you can see a rod and its axis of rotation which is perpendicular to the image plane. If in this position four forces are applied to the rod with the magnitude of each force, $F_1=2 \text{ N}$, $F_2=5 \text{ N}$, $F_3=7 \text{ N}$ and $F_4=10 \text{ N}$, and the force F_2 forms an angle of 60° with the rod:
 - a. Calculate the torque exerted by each force.
 - b. If the mass of the rod is 2 kg (evenly distributed) and the distance from the axis of rotation to the left end of the rod is 20 cm, calculate the magnitude of the rod's angular acceleration.
 - c. Calculate the rod's angular velocity when the rod forms an angle of 30° to its initial position.



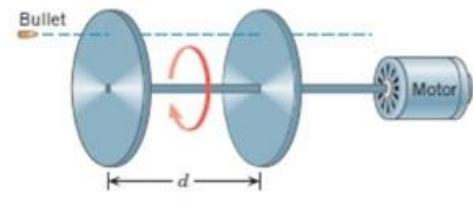
3. A pulley of uniform mass, $M = 2 \text{ kg}$ and radius $R = 10 \text{ cm}$, is mounted on a fixed horizontal shaft, as shown in the following figure. A block of mass $m = 1 \text{ kg}$ is suspended from a massless rope wrapped around the edge of a pulley. Calculate (Assume the rope does not slip, and there is no friction on the pulley shaft):
 - a. acceleration of falling block
 - b. angular acceleration of the pulley
 - c. tension of the rope.
4. Angular acceleration of a wheel $\alpha = 5t^4 - 6t^2 \text{ rad/s}^2$. At $t = 0\text{s}$, the wheel has an angular velocity $\omega = 2 \text{ rad/s}$ and position $\theta = 1.5 \text{ rad}$. Find:
 - a. angular velocity equation ω (in rad/s) as a function of time t .
 - b. angular position θ (in rad) as a function of time t .
 - c. plot the angular velocity ω and angular position θ as a function of time t .
5. In the following figure, a 1.5 kg cylinder is rotating about its main axis which passes through point O. Some forces which magnitudes are: $F_1 = 4 \text{ N}$, $F_2 = 3 \text{ N}$, $F_3 = 2 \text{ N}$, and $F_4 = 5 \text{ N}$ works on the cylinder in the direction as shown in the figure. If $r = 4 \text{ cm}$ and $R = 10 \text{ cm}$, and the relative angle of each force with respect to the cylinder does not change when the cylinder rotates, calculate:
 - a. the magnitude of total torque
 - b. the magnitude of angular acceleration
 - c. angular acceleration direction
 - d. moment of inertia when cylinder rotates about an axis passing through capture point of F_3 and parallel with the rotation axis.
 - e. the magnitude of angular acceleration of problem d.



6. There are four particles with masses and coordinates as follows: $m_1 = 25 \text{ g}$, $x_1 = 2 \text{ cm}$, $y_1 = 2 \text{ cm}$; $m_2 = 50 \text{ g}$, $x_2 = 0 \text{ cm}$, $y_2 = 4 \text{ cm}$; $m_3 = 30 \text{ g}$, $x_3 = -3 \text{ cm}$, $y_3 = -3 \text{ cm}$; and $m_4 = 25 \text{ g}$, $x_4 = -2 \text{ cm}$, $y_4 = 4 \text{ cm}$. Determine the moment of inertia of the particle system if the axis of rotation is:

- a. $y = 1$
- b. $x = 1$
- c. z -axis.

7. In the following picture you can see a tool for determining the speed of a fired bullet. This tool consists of two discs, which can rotate on their axis with an angular speed of 100.0 rad/s , which are separated by a distance of $d = 0.5 \text{ m}$. If a bullet penetrates the left disk first before penetrating the right disk, and the difference in the angular positions of the bullet holes in the two disks is $\theta = 0.25 \text{ rad}$, determine the speed of the bullet.



8. An object rotates about a fixed axis, and the angular position of a reference line on the object is given by $q = 0.4 e^{2t} \text{ rad/s}$. Consider a point on the object that is 4 cm from the axis of rotation. At $t = 0\text{s}$, determine the magnitudes of:

- a. angular velocity
- b. tangential acceleration component
- c. radial acceleration component.