Assignment 1 Base R 1: Vectors

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1. Create the vectors:
(a) (1, 2, 3, , 19, 20)
1:20
[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
(b) $(20, 19, \ldots, 2, 1)$
20:1
[1] 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1
(c) (1, 2, 3, , 19, 20, 19, 18, , 2, 1)
c(1:20,19:1)
[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 19 18 17 ## [24] 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1
(d) assign vector $c(4, 6, 3)$ variable name tmp
Use tmp for parts (e), (f) and (g)
$tmp \leftarrow c(4,6,3)$
(e) (4, 6, 3, 4, 6, 3, , 4, 6, 3) where there are 10 occurrences of 4.
a <- rep(tmp, length = 30) a
[1] 4 6 3
[1] 10
(f) (4, 6, 3, 4, 6, 3, , 4, 6, 3, 4) where there are 11 occurrences of 4, 10 occurrences of 6 and 10 occurrences of 3.

```
b \leftarrow rep(tmp, length = 31)
## [1] 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4
sum(b == 4)
## [1] 11
sum(b == 6)
## [1] 10
sum(b == 3)
## [1] 10
       (g) (4, 4, \ldots, 4, 6, 6, \ldots, 6, 3, 3, \ldots, 3) where there are 10 occurrences of 4, 20 occurrences of 6 and
                     30 occurrences of 3.
rep(tmp, times=c(10,20,30))
 \hbox{ \#\# } \hbox{ [1] } \hbox{ 4 } \hbox{ 6 } \hbox{ 
2. Create a vector of the values of
e^x \cos(x) at x = 3, 3.1, 3.2, \dots, 6.
# reset value of tmp
tmp < - seq(3,6, by = .01)
tmp1 <- exp(tmp)*cos(tmp)</pre>
head(tmp1, n = 30)
## [1] -19.88453 -20.11200 -20.34000 -20.56850 -20.79745 -21.02684 -21.25660
## [8] -21.48672 -21.71714 -21.94784 -22.17875 -22.40986 -22.64110 -22.87244
## [15] -23.10384 -23.33524 -23.56660 -23.79788 -24.02902 -24.25998 -24.49070
## [22] -24.72113 -24.95123 -25.18093 -25.41019 -25.63894 -25.86714 -26.09472
## [29] -26.32163 -26.54780
```

3. Create the following vectors:

To keep the listing shorter

(a) $(0.1^30.1^1, 0.1^60.2^4, ..., 0.1^{36}0.234)$

```
a \leftarrow seq(3,36, by = 3)
b < - seq(1,34, by = 3)
c <- 0.1^{(a)}*0.2^{(b)}
head(c, n = 12)
   [1] 2.000000e-04 1.600000e-09 1.280000e-14 1.024000e-19 8.192000e-25
    [6] 6.553600e-30 5.242880e-35 4.194304e-40 3.355443e-45 2.684355e-50
## [11] 2.147484e-55 1.717987e-60
 (b) (2, \frac{2^2}{2}, \frac{2^3}{3}, ..., \frac{2^{25}}{25})
(2^{(1:25)})/(1:25)
    [1] 2.000000e+00 2.000000e+00 2.666667e+00 4.000000e+00 6.400000e+00
    [6] 1.066667e+01 1.828571e+01 3.200000e+01 5.688889e+01 1.024000e+02
## [11] 1.861818e+02 3.413333e+02 6.301538e+02 1.170286e+03 2.184533e+03
## [16] 4.096000e+03 7.710118e+03 1.456356e+04 2.759411e+04 5.242880e+04
## [21] 9.986438e+04 1.906502e+05 3.647221e+05 6.990507e+05 1.342177e+06
4. Calculate the following:
 (a) \sum_{i=10}^{100} (i^3 + 4i^2)
sum((10:100)^3+4*(10:100)^2)
## [1] 26852735
 (b) \sum_{i=1}^{25} \left( \frac{2^i}{i} + \frac{3^i}{i^2} \right)
 tmp = 1:25
 sum((2^tmp)/tmp + 3^tmp/(tmp^2))
## [1] 2129170437
```

- 5. Use the function paste() to create the following character vectors of length 30:
 - (a) ("label 1", "label 2",, "label 30"). Note that there is a single space between label and the number following.

```
paste("label", 1:30, sep=" " )

## [1] "label 1" "label 2" "label 3" "label 4" "label 5" "label 6"

## [7] "label 7" "label 8" "label 9" "label 10" "label 11" "label 12"

## [13] "label 13" "label 14" "label 15" "label 16" "label 17" "label 18"

## [19] "label 19" "label 20" "label 21" "label 22" "label 23" "label 24"

## [25] "label 25" "label 26" "label 27" "label 28" "label 29" "label 30"

(b) ("fn1", "fn2", ..., "fn30").

In this case, there is no space between fn and the number following. *****

paste("fn", 1:30, sep="")

## [1] "fn1" "fn2" "fn3" "fn4" "fn5" "fn6" "fn7" "fn8" "fn9" "fn10"

## [11] "fn11" "fn12" "fn13" "fn14" "fn15" "fn16" "fn17" "fn18" "fn19" "fn20"

## [21] "fn21" "fn22" "fn23" "fn24" "fn25" "fn26" "fn27" "fn28" "fn29" "fn30"
```

6. Execute the following lines which create two vectors of random integers which are chosen with replacement from the integers $0, 1, \ldots, 999$. Both vectors have length 250.

```
set.seed(50)
xVec <- sample(0:999, 250, replace=T)
yVec <- sample(0:999, 250, replace=T)</pre>
xVec
     [1] 708 437 200 767 513 44 699 646 42 107 390 269 640 77 277 676 835
##
    [18] 364 74 168 616 193 710 842 309 650 577 257 324 368 358 408 437 618
   [35] 222 627 121 701 373 458 363 836 278
                                              93
                                                 55 700 954 458 713 803 996
   [52] 765 639 299 358 425 715 525 511 266 578 655 197 585 129
                                                                   38 724
   [69] 136 944 507 995 661 74 967 148 657 956 652 956 543
                                                              17 339 469 544
## [86] 19
               1 680 537 645 691 688 828 760
                                               48 294
                                                       69 807 311 668 505 964
## [103] 632
                  24 862 10 614 840 353 878
                                               72 193 113
                                                          82 322 91 789 444
               8
                                               76 256 359 189 807 457
## [120] 986 624 18 537 554 515 460 263
                                          42
## [137] 543 324 176 477 541 160 260 174
                                          48 415 707 625 530 407 216 224 395
## [154] 977 828 461 148 293 660
                                 38 137 224 852 743 683 545 353 371 866 452
## [171] 811 768 339 203 478 49
                                  20 880 480 996 894 357 900 603 667 787 972
## [188] 457 467 324 928 109 365 987 572 280 113 702 963 405
                                                              63 621 517 446
## [205] 533 190 638 275 865 435 501 669 124
                                               14 920 308
                                                          84 523
                                                                    5 863 860
## [222] 120 206 399   29 256 678   59 497 188 127 258 376 171 781 870 110 957
## [239] 285 382 34 403 631 197 179 545 123 760 238 178
Suppose x = (x_1, x_2, ..., x_n) denotes the vector xVec and y = (y_1, y_2, ..., y_n) denotes the vector yVec.
```

(a) Create the vector $(y_2 - x_1, ..., y_n - x_{n-1})$.

```
tmp1 <- yVec[-1] - xVec[-length(xVec)]
head(tmp1, n = 250)</pre>
```

```
##
      [1]
           163 -122
                       317 -146
                                  417
                                        393
                                              249 -489
                                                         741
                                                                           402 -549
                                                                                      338
                                                                      81
                                                     36
                            217
                                                                            48
                                                                                397
##
    [15]
           583 -403
                       -67
                                  307 -121 -269
                                                        -706 -563
                                                                     102
                                                                                      297
##
    [29]
           -45 -152
                       497
                            405
                                  339
                                       -400
                                              499
                                                   -89
                                                         211 -670
                                                                      87
                                                                            74
                                                                                554
                                                                                      149
    [43]
                 612
                       193
                           -453
                                  -70
                                              127 -709
                                                        -708 -722
                                                                     -64
                                                                           388
                                                                                     -212
##
          -183
                                       -141
                                                                               -184
##
    [57]
           242
                 430
                       275
                            672 -150
                                        275
                                              -96
                                                  -255
                                                         512
                                                               577
                                                                     264
                                                                           439
                                                                                149
                                                                                     -916
           374
                -889
                                        394
                                                         345
                                                                           100
##
    [71]
                      -332
                            324
                                 -553
                                              -87
                                                   -75
                                                              -735
                                                                     -55
                                                                                -40
                                                                                       15
##
    [85]
           279
                 409
                       790 -547 -487
                                       -399
                                             -619 -168
                                                        -185
                                                                19
                                                                     645
                                                                           551
                                                                                227
                                                                                     -366
##
    [99]
           242
                 147
                       247
                           -499
                                 -614
                                        758
                                               63 -227
                                                         247
                                                               379
                                                                    -472
                                                                           566
                                                                               -762
                                                                                      152
##
   Γ1137
           493
                 360
                        69
                            190
                                  544
                                       -176
                                              216
                                                  -676
                                                        -205
                                                               782
                                                                    -109
                                                                           189
                                                                               -233
                                                                                      505
                            487
                                                         704
##
   [127]
          -219
                 288
                      -57
                                  256
                                        300 -192
                                                  -263
                                                               674
                                                                     217
                                                                           280
                                                                                 17
                                                                                      -68
   [141]
           259
                 612
                     -127
                               1
                                  545
                                       -231
                                            -191
                                                  -338
                                                         333
                                                               495
                                                                     -21
                                                                            -4
                                                                                294
                                                                                     -668
   [155]
                 420
                       793
                            631
                                        655
                                                        -220
                                                                    -285
                                                                           327
                                                                                523
          -814
                                  -67
                                              143
                                                   611
                                                              -518
                                                                                      -13
         -679 -241
   [169]
                        39
                            193
                                  342
                                        588
                                              469
                                                     68
                                                         895
                                                              -658
                                                                     232
                                                                         -331
                                                                                 27
                                                                                      441
##
                                                                         -974
   [183] -733 -182
                     -399
                              79
                                 -469
                                        371
                                              475
                                                   265
                                                        -407
                                                               211
                                                                      59
                                                                                -90
                                                                                      218
           396 -486
                           -327
                                  425
                                        220
                                              128
                                                         294 -107 -365
   [197]
                     -963
                                                   235
                                                                           146
                                                                               -588
                                                                                      449
   [211]
          -434
                 221
                       846
                            386
                                 -910
                                        161
                                              206
                                                   109
                                                         712
                                                              -334
                                                                    -434
                                                                             7
                                                                                640 -350
                 353
                            225
##
   [225]
           923
                     -579
                                  327
                                        410
                                              568
                                                  -195
                                                         -83
                                                               154
                                                                    -486 -195
                                                                                667 -144
   [239]
                 410
                            380
                                 -559
                                        414
                                                   193
                                                         222
                                                               -92
                                                                     553
           272
                       546
                                              674
```

(b) Create the vector $(\frac{\sin(y_1)}{\cos(x_2)}, \frac{\sin(y_2)}{x_3}, ..., \frac{y_{n-1}}{\cos(x_n)})$.

```
tmp1 <- sin(yVec[-length(yVec)])/cos(xVec[-1])
head(tmp1, n = 250)</pre>
```

```
##
     [1]
           0.88603405
                         -1.44184825
                                        0.82807258
                                                     -1.61591717
                                                                    -0.86017343
##
     [6]
           20.26356465
                         -0.79930406
                                        1.72414444
                                                     -0.08094240
                                                                    -0.74895634
##
    [11]
           -2.59866958
                         -0.37361045
                                       31.11471579
                                                      0.12355916
                                                                   -0.35925226
##
    [16]
           -0.90743608
                          0.34374436
                                        5.78205917
                                                     -2.57418558
                                                                    -0.78661325
##
    [21]
           -0.59855406
                          0.98936263
                                        0.33042931
                                                     -1.75124647
                                                                    -0.59435547
    [26]
##
            1.05374692
                          0.65497397
                                       -0.11596582
                                                     -0.97176537
                                                                     0.57180267
                                                                   -3.77616264
##
    [31]
                         -0.49259143
                                       -0.99433357
           0.75799030
                                                      0.05377148
##
    [36]
           20.54902944
                          0.77784817
                                        1.28146891
                                                     -0.51650728
                                                                     6.66902699
##
    [41]
           -0.92970072
                        -10.93066299
                                       -3.13102962
                                                     30.87943423
                                                                    -1.14281543
##
    [46]
           0.36757630
                          1.18479716
                                        0.94594159
                                                      0.93339520
                                                                     0.93632658
##
    [51]
         -11.05384468
                          2.76893270
                                        0.97488334
                                                     -0.08932225
                                                                    -1.33616578
##
    [56]
           -3.30065552
                          0.62663162
                                       -1.96486337
                                                      0.08653876
                                                                     0.56695489
                                                                   -0.13860882
##
    [61]
           44.07630714
                         -1.11764853
                                        0.11230330
                                                     -0.46073106
##
    [66]
            0.84026052
                          2.64708780
                                       -1.63174570
                                                     -9.63022830
                                                                    -2.15553419
##
    [71]
           -0.42770826
                          3.24955062
                                       -4.23453154
                                                      0.93067452
                                                                    -0.88388390
                                       -8.22082884
##
    [76]
           0.69339350
                          1.72841015
                                                       1.69276461
                                                                     1.02074555
##
    [81]
                         -0.90739226
                                        1.11331935
           -3.21968328
                                                      0.59579467
                                                                     0.19571363
##
    [86]
           -0.17975474
                          4.38929818
                                        0.64431266
                                                     -1.54509170
                                                                    -0.26536991
##
    [91]
           -0.81679156
                          1.34164181
                                       -1.03400420
                                                     -1.33639979
                                                                    -0.4444499
##
    [96]
           0.96777754
                         -0.09545121
                                       -0.63686070
                                                     -2.30844090
                                                                    -0.11384497
   [101]
##
            1.08800453
                          1.06851885
                                       -0.30428029
                                                     -1.77044888
                                                                    -1.45269351
##
   [106]
           0.97943716
                         -2.15021752
                                        1.56128032
                                                      0.61018741
                                                                     5.59692239
##
   [111]
           -1.03020002
                         -1.14632240
                                       -0.81548097
                                                      0.95359082
                                                                    74.12815803
                                                                    -0.68385723
   [116]
           -0.20329495
                         -0.08875385
                                       -0.76023984
                                                     -0.42372635
##
   [121]
            1.28860542
                          0.94117702
                                        1.89561343
                                                      0.69369539
                                                                     4.15021756
##
   [126]
           -1.08026240
                          1.26615554
                                        0.02147428
                                                      3.32694398
                                                                     0.22930300
## [131]
            1.14217476
                          0.73847767
                                        8.72339712 -17.15727240
                                                                     0.90435970
```

```
## [136]
           1.07791792
                         0.75391899
                                      -0.26297571
                                                     0.83894657
                                                                  -1.22542984
## [141]
          -0.57277292
                        -1.22429033
                                       2.10719833
                                                    -1.35745285
                                                                  -0.84117115
## [146]
          -0.69663176
                        -0.99207337
                                      -1.17363312
                                                    -5.50814669
                                                                  -1.12309426
                                                    -4.42251048
## [151]
           0.60767585
                         0.32903697
                                      -0.08845387
                                                                  -1.31360561
## [156]
          -1.05268827
                        -1.45007537
                                      -1.03184453
                                                     0.38034305
                                                                   2.06381128
## [161]
          -1.64568068
                         0.47938401
                                      46.18666528
                                                     1.75988821
                                                                  14.03349520
## [166]
           1.99884446
                        -1.02170635
                                       1.02445028
                                                    -0.15250370
                                                                  -1.11793279
## [171]
          -4.12228606
                         1.02355677
                                       0.89546497
                                                     0.74732250
                                                                  -2.09533197
## [176]
          -2.40630344
                        -0.73530615
                                       0.90759126
                                                    -0.87474163
                                                                  -4.22536917
## [181]
          -2.04450866
                        -7.41320483
                                       0.03607946
                                                    -0.85674969
                                                                  -0.85648584
## [186]
           2.58973778
                         8.68248704
                                      -0.74202802
                                                     1.07347586
                                                                   1.37638585
## [191]
           1.73104746
                        -0.57596355
                                      -0.49915725
                                                     0.11786229
                                                                  -0.45584137
## [196]
          -0.97726281
                        -6.86428063
                                      -0.60929448
                                                    -0.72132361
                                                                   0.0000000
## [201]
           1.00734878
                         4.20789995
                                                                  10.00784534
                                      -0.81616263
                                                    -1.72455176
## [206]
                         8.77005056
                                      -0.64297796
                                                     0.24086573
           0.71310632
                                                                  -6.12424634
## [211]
           0.94848253
                         9.22132979
                                      -5.85933168
                                                    -0.77292827
                                                                  -0.85749485
## [216]
           0.80000340 -10.45187777
                                       2.91489552
                                                     0.86914823
                                                                   0.93956496
## [221]
           1.15020196
                        -4.25009579
                                      -0.97278301
                                                     1.05669698
                                                                  23.96919924
## [226]
          -0.11659711
                         0.58615433
                                      -1.23512544
                                                     1.08111948
                                                                   3.37846777
## [231]
           0.96204558
                        -1.18727215
                                       0.77801767
                                                     2.39161655
                                                                   1.01270315
## [236]
           0.30508064
                        -1.13987140
                                       1.35085069
                                                     2.13213714
                                                                   0.95034702
## [241]
           0.48941676
                        -1.03804260
                                       1.11768517
                                                    -0.25446052 -15.07630921
## [246]
           1.12429826
                         0.28067653
                                      -0.75125301
                                                    -1.91160477
```

(c) Create the vector $(x_1 + 2x_2 - x_3, x_2 + 2x_3 - x_4, ..., x_{x-2} + 2x_{n-1} - x_n)$

```
last <- length(xVec)
second_last <- length(xVec) - 1
third_last <- length(xVec) - 2

tmp1 <- xVec[1:third_last] + 2*xVec[2:second_last] - xVec[3:last]
head(tmp1, n = 250)</pre>
```

```
##
     [1] 1382
                 70 1221 1749
                               -98
                                     796 1949
                                                623 -134
                                                           618
                                                                288 1472
                                                                           517
                                                                                -45
##
          794 1982 1489
                          344 -206 1207
                                          292
                                                771 2085
                                                           810 1032 1547
                                                                           767
                                                                                537
    [15]
##
    [29]
          702
                676
                     737
                          664 1451
                                     435 1355
                                                168 1150
                                                           989
                                                                926
                                                                     348 1757 1299
##
    Γ431
          409 -497
                     501 2150 1157 1081 1323 2030 1887 1744
                                                                879
                                                                     590
                                                                           493
                                                                               1330
##
    [57] 1254 1281
                     465
                          767 1691
                                     464 1238
                                                805 -519 1425
                                                                710 -611 1517
##
    [71] 1836 2243 -158 1860
                                606
                                     506 1917 1304 2021 2025
                                                                238
                                                                     226
                                                                           733 1538
                     824 1109 1136 1339 1239 1584 2300
                                                                567 -375 1372
    [85]
          581
              -659
                                                           562
##
    [99] 1142
                714 1801 2220
                                624
                                    -806 1738
                                                268
                                                     398 1941
                                                                668 2037
                                                                           829
                                                                                345
##
   Γ1137
          337
                -45
                     635 -285 1225
                                     691 1792 2216
                                                     123
                                                           538 1130 1124 1172
                                                                                944
##
   [127]
          271
                -62
                     229
                          785
                                -70 1346 1622
                                                381
                                                     104 1036 1015
                                                                     199
                                                                           589 1399
  [141]
          601
                506
                     560 -145
                                171 1204 1427 1278 1128
                                                           615
                                                                269
                                                                       37 1521 2172
## [155] 1602
                      74 1575
                                599
                                      88 -267 1185 1655 1564 1420
                                                                     880
                464
                                                                           229 1651
   [169]
          959 1306 2008 1243
                                267 1110
                                          556 -791 1300
                                                          844 1578 2427
                                                                           708 1554
   [183] 1439 1150 1269 2274 1419 1067
                                                     781 -148 1767 1851 1019 -196
                                          187 2071
  [197]
          554 2223 1710
                          -90
                                788
                                    1209
                                          876 1322
                                                     275 1191
                                                                323
                                                                    1570 1234
                                                                                768
  [211] 1715
                903
                    -768 1546 1452
                                     -47 1125
                                               -330
                                                     871
                                                         2463
                                                                894
                                                                     133
                                                                           975
                                                                                201
                          865
                                     184
## [225]
         -137 1553
                     299
                                746
                                          267
                                                839
                                                     -63
                                                           863 2411
                                                                     133 1739 1145
## [239] 1015
                 47
                     209 1468
                                846
                                      10 1146
                                                 31 1405 1058
```

(d) Calculate $\sum_{i=1}^{n-1} \frac{e^{-x_{i+1}}}{x_i+10}$

```
last <- length(xVec)
sum(exp((-1)*xVec[-1])/(xVec[-last]+10))
## [1] 0.01269872
```

7. This question uses the vectors xVec and yVec created in the previous question and the functions sort,

order, mean, sqrt, sum, and abs.

(a) Pick out the values in yVec which are > 600. ******

```
yVec[yVec>600]
```

```
## [1] 709 871 621 930 948 783 878 671 860 768 698 974 855 813 776 721 917 ## [18] 985 705 884 840 687 957 955 786 938 930 641 615 988 881 881 997 823 ## [52] 965 743 615 615 803 948 760 604 800 772 863 902 689 881 941 924 693 ## [69] 835 632 872 876 850 961 681 791 947 915 712 665 921 798 866 828 942 ## [86] 841 645 681 827 884 890 970 632 717 846 952 609 824 695 675 777 813 ## [103] 792 783 611 853 738 668 791
```

(b) What are the index positions in yVec of the values which are > 600?

```
which(yVec>600)
```

```
##
     [1]
                    5
                                        13
                                                 18
                                                     27
                                                         28
                                                                  33
                                                                               42
                                10
                                    11
                                             16
                                                              32
##
    [18]
          43
               45
                   48
                       50
                           55
                                58
                                    59
                                        60
                                                 63
                                                     66
                                                         67
                                                              68
                                                                  72
##
    [35]
          88
                   95
                           97 101 102 105 107 109 111 114 118 119 120 123 125
              94
                       96
    [52] 127 131 132 134 136 137 138 139 142 143 150 151 154 157 158 159
    [69] 163 164 167 168 172 173 174 175 176 178 180 181 182 183 187 189
    [86] 203 204 205 206 211 213 214 219 220 224 226 227 230 232 237 238 239
  [103] 241 243 245 246 247 249 250
```

(c) What are the values in xVec which correspond to the values in yVec which are > 600? (By correspond, we mean at the same index positions.)

```
xVec[which(yVec>600)]
```

```
[1] 708 437 513
                      44 646 107 390 640 676 364 577 257 408 437 618 627 836
##
    [18] 278
             55 458 803 358 525 511 266 578 197
                                                  38 724
                                                          61 995 652 956
    [35] 680 760
                  48 294
                          69 505 964
                                      24
                                          10 840 878 113 789 444 986 537 515
    [52] 263 359 189 457 274 543 324 176 160 260 407 216 977 148 293 660 137
##
    [69] 852 743 353 371 768 339 203 478
                                         49 880 996 894 357 900 972 467 324
```

```
## [86] 517 446 533 190 501 124 14 5 863 399 256 678 188 258 110 957 285 ## [103] 34 631 179 545 123 238 178
```

(d) Create the vector $(|x_1 - \bar{x}|^{1/2}, |x_2 - \bar{x}|^{1/2}, ..., |x_n - \bar{x}|^{1/2})$

```
sqrt(abs(xVec - mean(xVec)))
```

```
[1] 16.0044994 3.8543482 15.8699716 17.7522956 7.8194629 20.1954450
    [7] 15.7208142 13.9335566 20.2449006 18.5702989 7.8648585 13.5224258
##
##
    [13] 13.7165593 19.3611983 13.2233127 14.9714395 19.5740645 9.3731532
   [19] 19.4385185 16.8480266 12.8118695 16.0890025 16.0668603 19.7520632
##
    [25] 11.9522383 14.0763632 11.1867779 13.9590831 11.3073427 9.1572922
   [31] 9.6879306 6.6223863 3.8543482 12.8896858 15.1610026 13.2341981
   [37] 18.1894475 15.7842960 8.8800901 2.4787093 9.4263461 19.5995918
##
   [43] 13.1854465 18.9434949 19.9212449 15.7525871 22.4085698 2.4787093
    [49] 16.1599505 18.7388367 23.3268943 17.6958752 13.6800585 12.3634947
##
##
   [55] 9.6879306 5.1822775 16.2217138 8.5524266 7.6905136 13.6329014
##
   [61] 11.2313846 14.2528594 15.9642100 11.5388041 17.9681941 20.3434510
   [67] 16.4967876 19.7700784 17.7723381 22.1843188 7.4259006 23.3054500
##
    [73] 14.4618118 19.4385185 22.6967839 17.4314658 14.3228489 22.4531512
   [79] 14.1472259 22.4531512 9.5469367 20.8532012 10.6233705 4.1405314
##
   [85] 9.5991666 20.8051917 21.2333700 15.1044364 9.2273506 13.8976257
##
   [91] 15.4642814 15.3669776 19.3944322 17.5540309 20.0961688 12.5640758
   [97] 19.5667064 18.8452647 11.8682770 14.7018366 7.2899931 22.6305988
## [103] 13.4217734 21.0678903 20.6846803 20.2520122 21.0203711 12.7335777
## [109] 19.7013705 9.9426355 20.6432556 19.4898948 16.0890025 18.4080417
## [115] 19.2316406 11.3954377 18.9962101 18.3614814 2.8028557 23.1115556
## [121] 13.1203658 20.8292103 9.2273506 10.1066315 7.9463199 2.8537694
## [127] 13.7424889 20.2449006 19.3870060 13.9948562 9.6361818 16.2128344
## [133] 18.8452647 2.2680388 18.7844617 13.3362663 9.5469367 11.3073427
## [139] 16.6089133 5.0143793 9.4416100 17.0837935 13.8512093 16.6690132
## [145] 20.0961688 6.0709143 15.9732276 13.1584194 8.8399095
                                                              6.6974622
## [151] 15.3576040 15.0948998 7.5402918 22.9160206 19.3944322
                                                             3.0239048
## [157] 17.4314658 12.6038089 14.4271965 20.3434510 17.7441821 15.0948998
## [163] 20.0035997 17.0629423 15.2034207 9.6511139 9.9426355
## [169] 20.3505282 0.3794733 18.9510950 17.7804387 10.6233705 15.7751704
## [175] 5.1131204 20.0712730 20.7811453 20.6916408 5.3050919 23.3268943
## [181] 21.0272205 9.7394045 21.1694119 12.2940636 14.6677878 18.3069386
## [187] 22.8066657 2.2680388 3.8915293 11.3073427 21.8207241 18.5163711
## [193] 9.3196566 23.1331796 10.9610219 13.1093860 18.4080417 15.8159413
## [199] 22.6084940 6.8451443 19.7194320 13.0055373 8.0711833
## [205] 9.0079964 16.1819653 13.6434600 13.2987217 20.3259440 4.1056059
        7.0102782 14.7358067 18.1067943 20.9250090 21.6366356 11.9939985
## [211]
## [223] 15.6797959 7.2702132 20.5634627 13.9948562 15.0380850 19.8205953
## [229] 6.7189285 16.2436449 18.0237621 13.9232180 8.7095350 16.7587589
## [235] 18.1423262 20.4485696 18.4893483 22.4754088 12.9172753
                                                              8.3579902
## [241] 20.4415264 6.9897067 13.3844686 15.9642100 16.5183534 9.6511139
## [247] 18.1343872 17.5540309 14.6238162 16.5485951
```

⁽e) How many values in yVec are within 200 of the maximum value of the terms in yVec?

```
difference <- abs(yVec - max(yVec))</pre>
length(yVec[difference <= 200])</pre>
## [1] 57
 (f) How many numbers in xVec are divisible by 2? (Note that the modulo operator is denoted \%%.)
length(xVec[xVec %% 2 == 0])
## [1] 124
 (g) Sort the numbers in the vector xVec in the order of increasing values in yVec.
 xVec[order(yVec)]
                                                    42 616
     [1] 405 842 308 572 461
                                8 256 507 373 639
                                                             29 645 376 669 688
    [18] 197
              63 638 862
                           77 996
                                   93
                                        59
                                          585 661
                                                    72
                                                        339
                                                             20 206 537
##
          42 603 425
                       48 707 452 477
                                        99 224 811 715 358 963 222 395 543
    [52] 193 683 710 691 954 700 614 787 835 275 435
                                                       309
                                                            368
                                                                224 460
    [69] 530 765 523 171 870 807 469 828 624
                                               200 713
                                                        365
                                                            781
                                                                 74 129
##
                                                                          76
##
    [86]
         760 193 866 353 168 967 545 920 541 650 148 277
                                                             18 667
                                                                    865 987
   [103] 655
                1 554 699 311 458 632
                                        84 269
                                                82 280 544
                                                             17 621 807
   [120]
         457
             702
                   91 625
                          767 828 109 860 363 121 657
                                                        668 324
                                                                382
             928 415
                         127 176 678 179 444 724 189
   [137]
          74
                       38
                                                        457 513
                                                                743
                                                                             789
   Γ154]
          38 760 446 986 894 238 640 110 203 533 113 358 977
                                                                294 137
          55 708 996 863 627 123 515 359 964 324
                                                    24 364 260 618 957
  [188] 631 266 680 478 178
                               34 900 537 160 274 437 285 505
                                                                 19 188 190
## [205] 852 803 517
                       69 399 768 545 408 676 407 972 437 353 371 390 995
## [222] 148 458 501 124 216 880 836 878 357 660
                                                    44 197 578 293 324
## [239] 543 256 511 525 339 263
                                   14 257 278
                                                61 840 956
 (h) Pick out the elements in yVec at index positions 1, 4, 7, 10, 13, . . .
yVec[seq(1,250,by=3)]
    [1] 709 517 437 783 671 860 581 347 279 974 216 776 538 460 985 248 317
        288 687 957 938 101 615 285 106 414 881 488 484 791 246 643 845 553
   [18]
        465
             87 993 116 473 635 310 428 965
                                               19 489 803 604 800 175 516 902
        689 881 593 835 398 358 850 791 915 665 167 866 942 320 482 216
```

8. By using the function cumprod or otherwise, calculate

[69] 681 273 884 970 469 717 127 952 284 695 325 777 792

$$1 + \frac{2}{3} + (\frac{2}{3}\frac{4}{5}) + (\frac{2}{3}\frac{4}{5}\frac{6}{7} + \dots + (\frac{2}{3}\frac{4}{5}\dots\frac{38}{39}))$$

72 738 791

```
sum(cumprod(seq(2,38,by=2))/cumprod(seq(3,39,by=2))) + 1
```

[1] 6.976346