

Data Structures and Algorithms

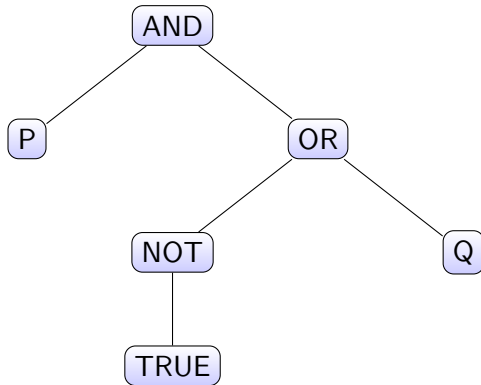
Assignment 3

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A PLTreeNode tree

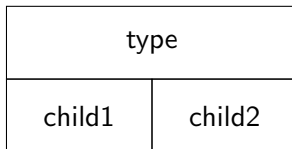


Prefix: $\text{AND}(\text{P}, \text{OR}(\text{NOT}(\text{TRUE}), \text{Q}))$

Infix: $((P) \wedge ((\neg T) \vee (Q)))$

Reverse Polish: $[\text{P}, \text{TRUE}, \text{NOT}, \text{Q}, \text{OR}, \text{AND}]$

A single PLTreeNode Object



- Make sure that your code **ALWAYS** maintains the invariant:
`type.getArity() == 0 → child1 == null && child2 == null`
`type.getArity() == 1 → child1 != null && child2 == null`
`type.getArity() == 2 → child1 != null && child2 != null`
EITHER test if child is null OR get the arity
- Change the type simply by assigning to it (but make sure you correct the children if necessary to preserve the invariant)
- Within PLTreeNode, don't use setters and getters to access type, child1 and child2: just assign to or from them

Recursion: Preorder Recursion

```
myMethod()  
{  
    // do something to this node here  
  
    if (child1 != null)  
        child1.myMethod();  
  
    if (child2 != null)  
        child2.myMethod();  
}
```

Recursion: Inorder Processing

```
myMethod()  
{  
    if (child1 != null)  
        child1.myMethod();  
  
    // do something to this node here  
  
    if (child2 != null)  
        child2.myMethod();  
}
```

Recursion: Postorder Processing

```
myMethod()  
{  
    if (child1 != null)  
        child1.myMethod();  
  
    if (child2 != null)  
        child2.myMethod();  
  
    // do something to this node here  
  
}
```

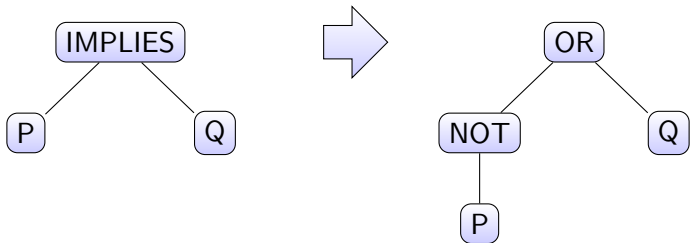
Processing Order Choice

The choice of processing order is sometimes a free choice, sometimes dictated by the situation.

- If the recursion does not modify the tree, then the recursion is just gathering information
 - Choose the order so that the information is available when it is needed
 - Sometimes some recursion can be avoided if you are careful
 - e.g. if you find the necessary information in the left sub-tree, it may not be necessary to recurse down the right
- If the recursion does modify the tree, then you may need a specific order
 - If you are recursing to find and modify a pattern in the tree, then making that modification may introduce that pattern in other places: make sure that the process order will catch those newly introduced patterns

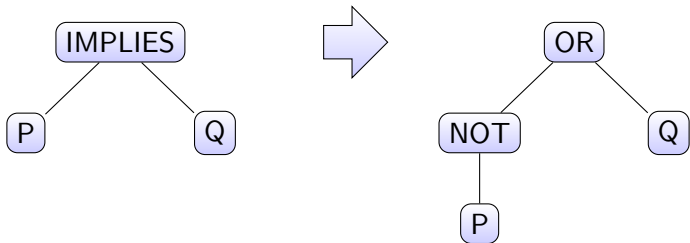
eliminateImplies()

Should have called it `replaceImplies()`



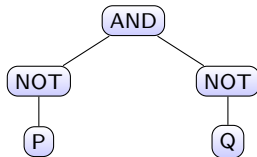
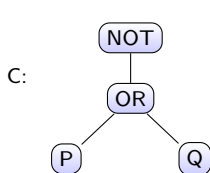
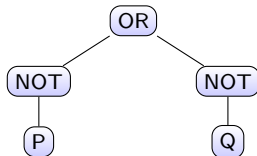
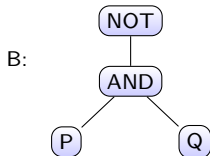
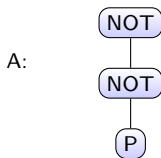
eliminateImplies()

Should have called it `replaceImplies()`

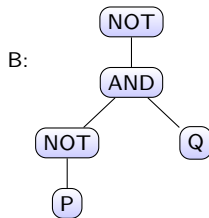
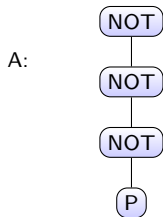


- Doesn't introduce new Left Hand Side (LHS) patterns so no problems with processing order choice

pushNotDown()

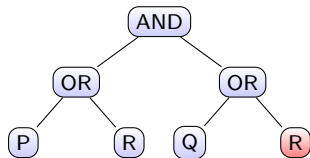
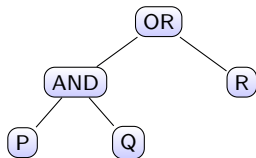


`pushNotDown()`: can produce new LHS patterns

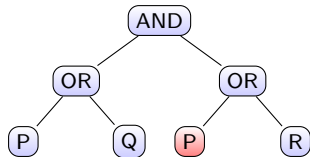
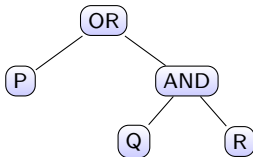


pushOrBelowAnd()

A:

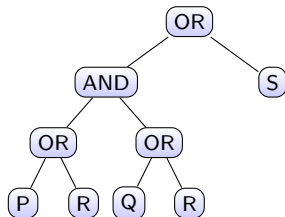
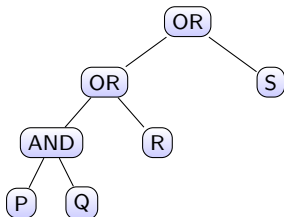


B:

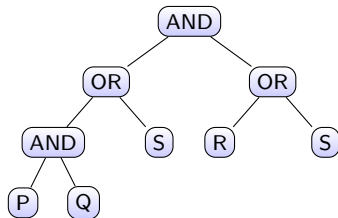
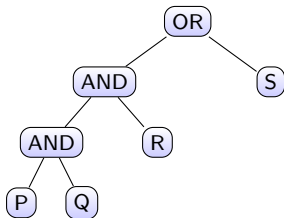


pushOrBelowAnd(): Issues

A:

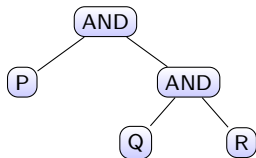
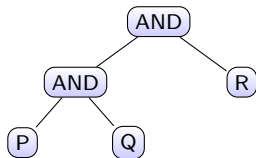


B:

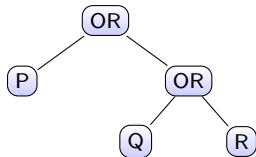
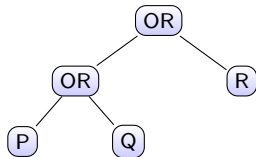


makeAndOrRightDeep()

A:



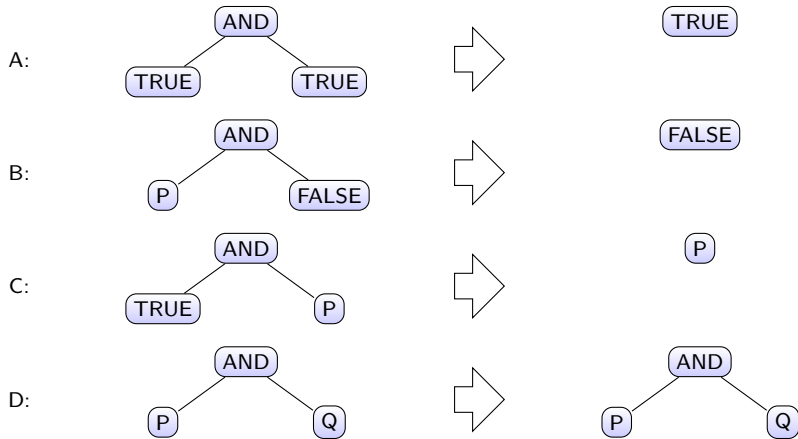
B:



evaluateConstantSubtrees()

A	B	$A \wedge B$	$A \vee B$	$A \rightarrow B$	$\neg B$
\top	\top	\top	\top	\top	\perp
\top	\perp	\perp	\top	\perp	\top
\top	N	B	\top	B	N
\perp	\top	\perp	\top	\top	
\perp	\perp	\perp	\perp	\top	
\perp	N	\perp	B	\top	
N	\top	A	\top	\top	
N	\perp	\perp	A	$\neg A$	
N	N	N	N	N	

evaluateConstantSubtrees(): some cases



evaluateConstantSubtrees(): Preorder or postorder?

Try (manually!) seeing what the difference is if you recurse before or after processing the node in this example:

