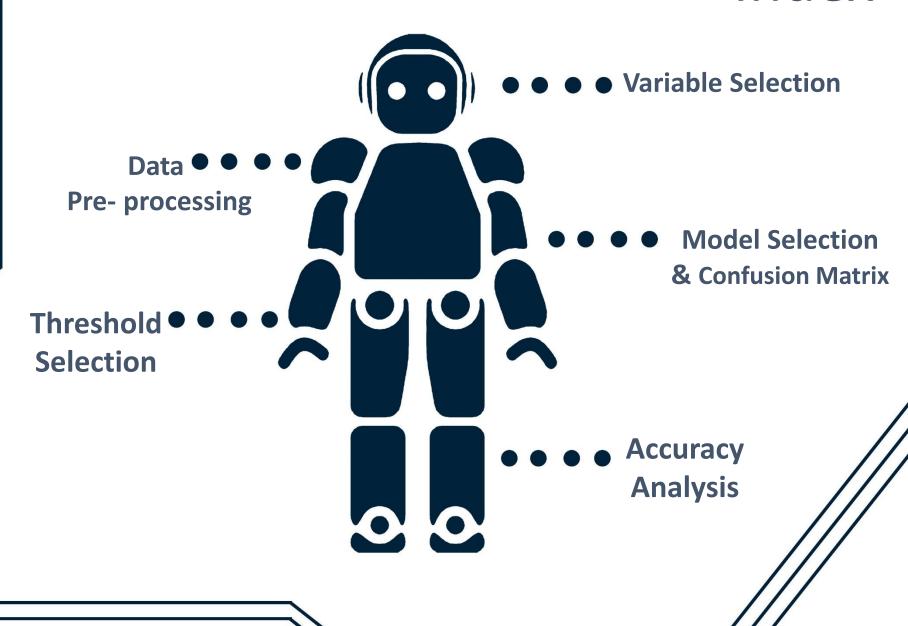
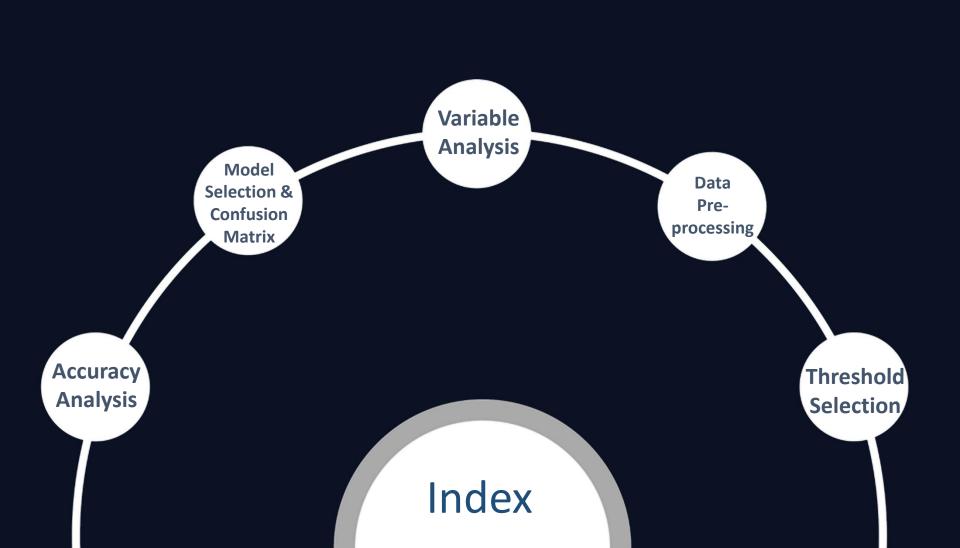
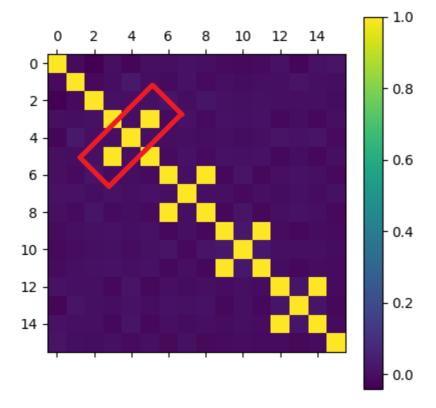


Index



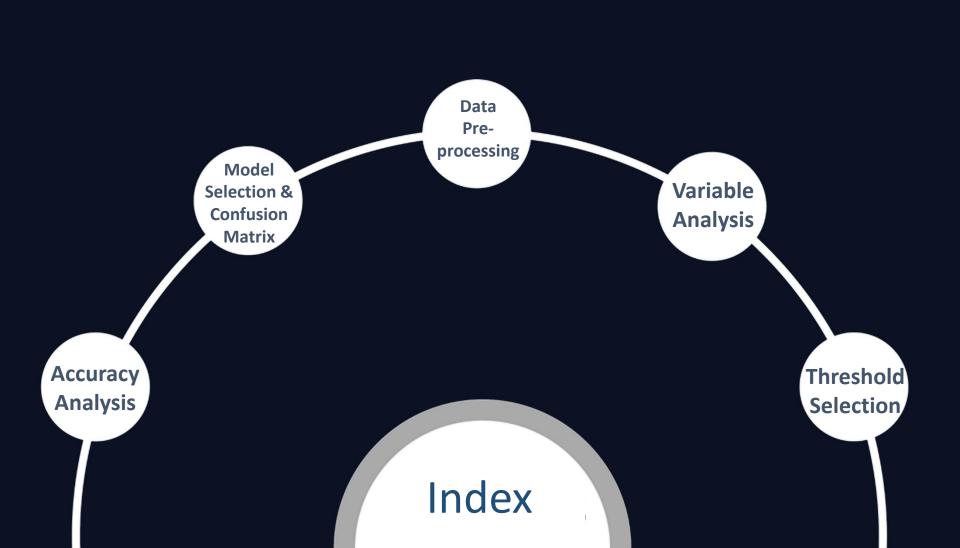


Variable Analysis



- High Correlation between certain equally spaced variables was observed
- •These variables were identified to be total_*_minutes and Total_*_charges

We derived one feature out of these two using Principal Component Analysis(PCA)



Data Pre-processing

- •After the variable selection and normalization of some features was done to match the scale.
- •We converted some features which were in string format('yes/no') into Boolean(1/0).
- •Removing of variables like area_code, phone_number, state & id.

S	S				
total_intl_calls	total_e	ve_min	utes		
3			197.4	— Large	e Differe
3			195.5		
5			121.2		
7			61.9		
3			148.3		

Dataset Split

The Dataset was split into

Train Data: Used to train the different models

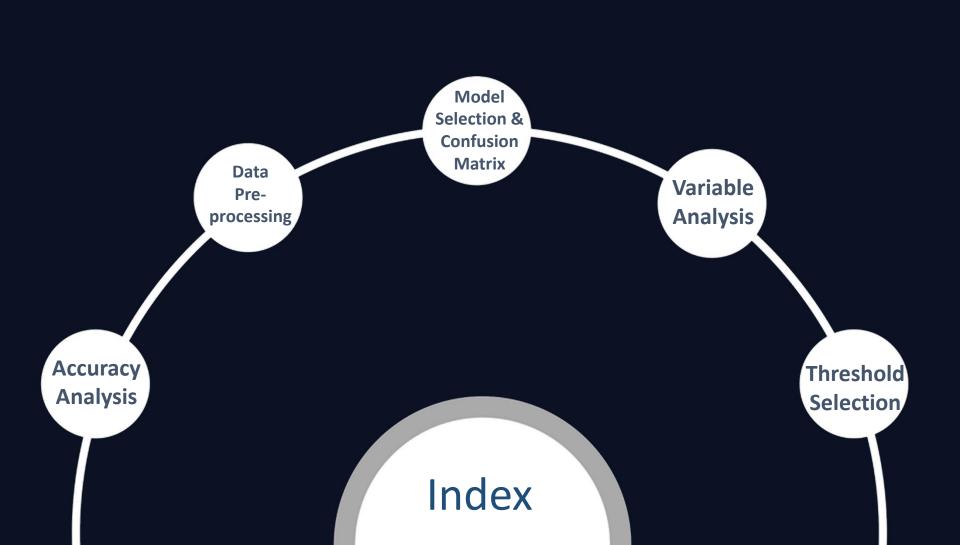
•Validation Data: Used to test the different models and find respective Area Under ROC Curve, sensitivity, specificity and precision. Threshold selection was done using this.

•Test Data: Separate Dataset strata on which the validated model was tested upon to find the various parameters. This dataset can be thought of as an unknown Dataset on which the model can be applied.

The total Dataset of 5000 was split into 3500:750:750 for Train, Validation and Test data respectively.

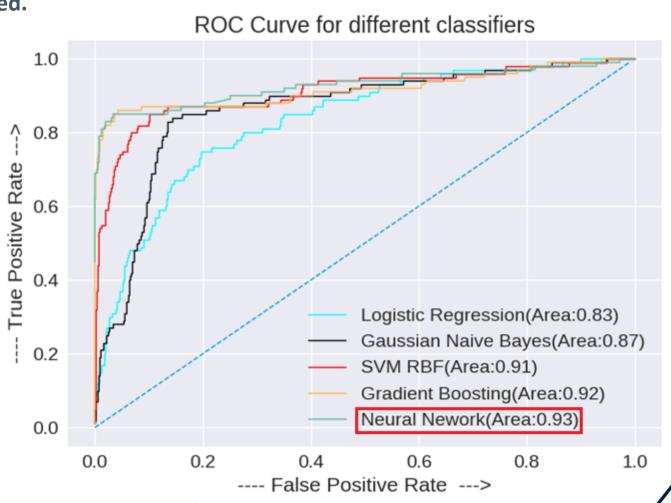
Churn percentage in full data: 14.14%
Churn percentage in training set: 14.51%
Churn percentage in validation set: 13.33%
Churn percentage in test set: 13.20%

Difference between full data and test data is 0.94%



Model Selection

We decided to go with Area under ROC curve parameter. Classifiers were tested and the classifier with the highest Area Under ROC Curve (AUC-ROC) was selected.



Logistic Regression

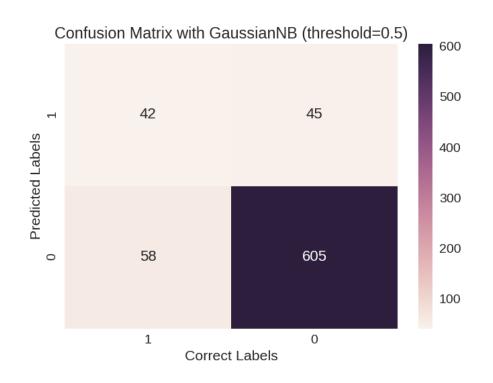


AUC: 0.833

Specificity: 0.98

Sensitivity/Recall: 0.22

Naive Bayes'



AUC: 0.865

Specificity: 0.93

Sensitivity/Recall: 0.42

SVM Classifier



AUC: 0.911

Specificity: 0.99

Sensitivity/Recall: 0.55

Precision: 0.86

Gradient Boosting



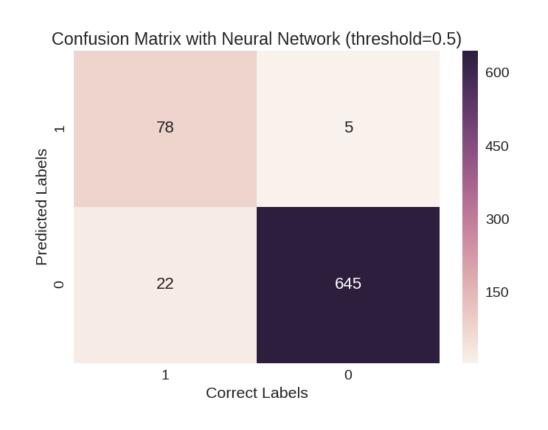
AUC: 0.917

Specificity: 0.99

Sensitivity/Recall: 0.73

Neural Network

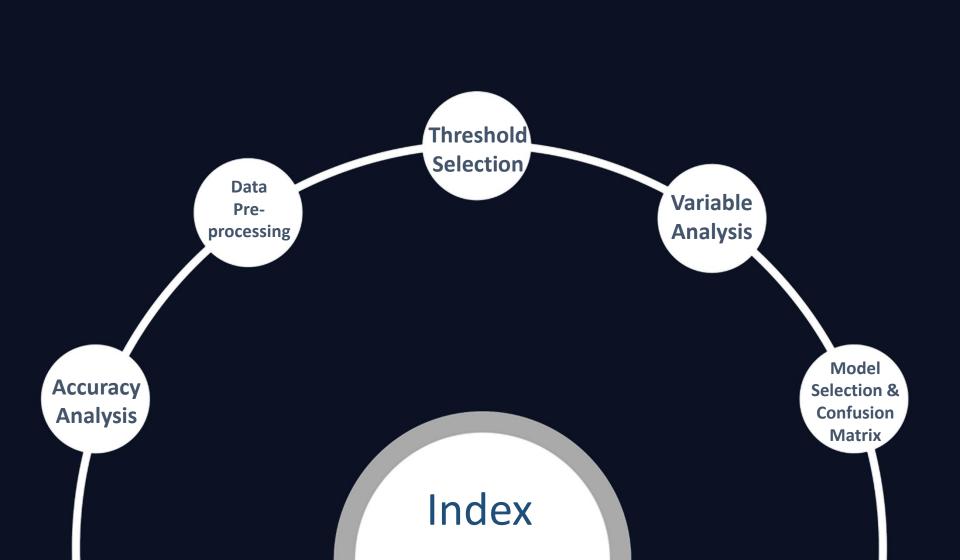
Selected Model



AUC: 0.927

Specificity: 0.99

Sensitivity/Recall: 0.78



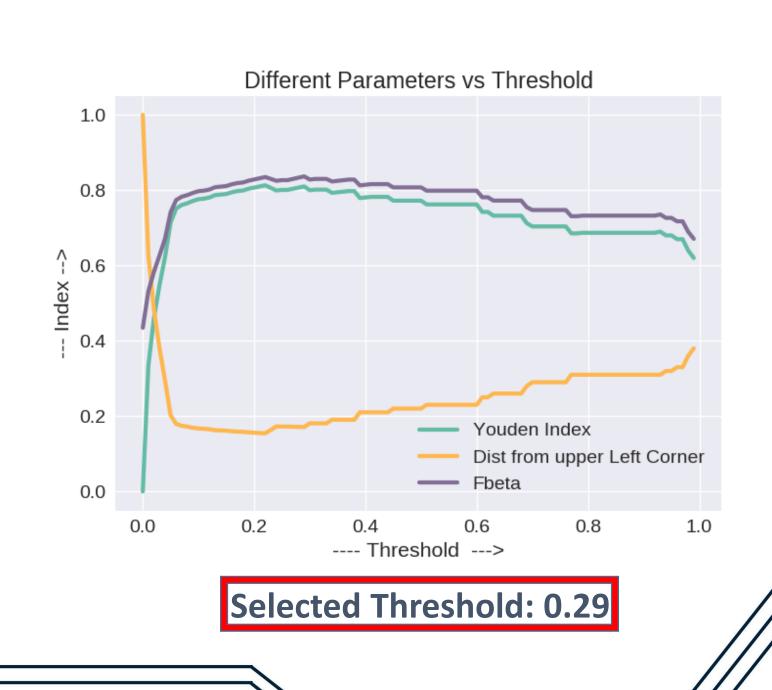
Threshold Selection

As we saw at the threshold value of 0.5, we have high precision, however, Recall value is low.

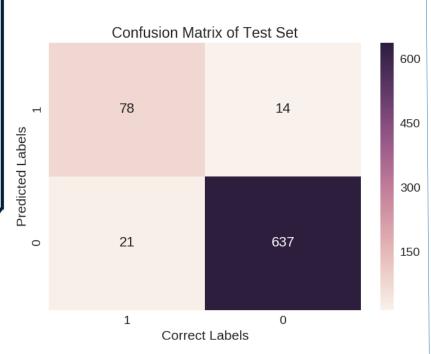
To choose the right threshold value for classification we plotted different parameters like :

- •Youden Index: (Sensitivity + Specificity 1)
- •Distance of the point from the upper left corner on the ROC curve
- •F-Beta value: : 2/(Fbeta)= (1/(beta*Recall)) + (1/(precision))

against varying thresholds



Confusion Matrix



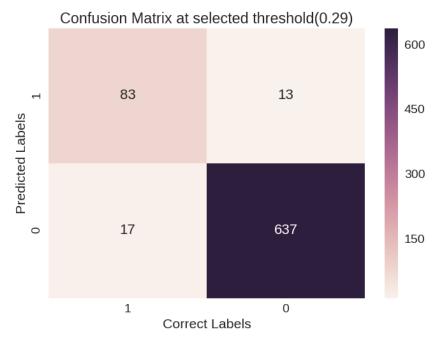
Test Data

Specificity: 0.98

Sensitivity/Recall: 0.81

Precision: 0.85Test

AUC: 0.903233564524



Validation Data

Specificity: 0.98

Sensitivity/Recall: 0.83

Precision: 0.86

val AUC: 0.927284615385

val. Accuracy: 0.96



We analyzed the impact of each variable by omitting them and then observing the Area Under ROC Curve.

We reached to the conclusion that following had the most impact:

- •total_day_charge
- •number_customer_service_calls
- •international_plan

Variables like account_lenght has minimal effect. Finally, we observed that we had the highest Area Under ROC Curve when all the features(prepared dataset after variable analysis) were taken into consideration.

Alternative Approach

Cost Analysis

For a Company, in order to balance to the budget along with the Retention and Acquisition costs, their balance of Recall and Precision can be dependent on cost of acquisition and cost of retention.

Approach Taken

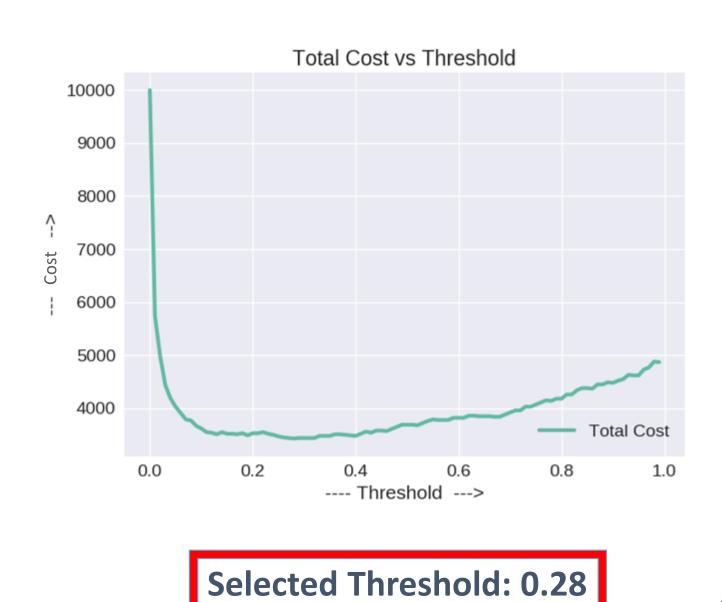


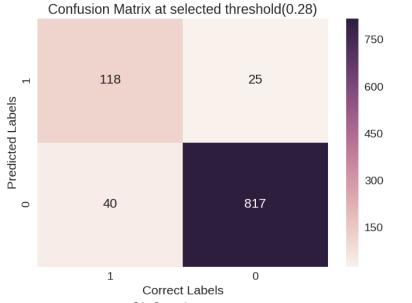
Using our model, we would get the total number of customers leaving as TP+ FP so, we would be spending Cost of Retention on them.

While we would be spending Cost of Acquisition on FN number of customers.

Cost of Retention: Rs. 10/ person Cost of Acquisition: Rs. 50/ person

Cost= 10(TP+ FP)+ 50(FN)





Validation Data

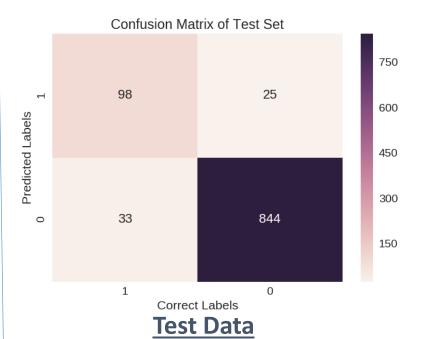
Specificity: 0.97

Sensitivity/Recall: 0.75

Precision: 0.83

val AUC: 0.882809916113 | Training AUC: 0.966490499186

val. Accuracy: 0.935



Specificity: 0.97

Sensitivity/Recall: 0.75

Precision: 0.8

Test AUC: 0.88829399415 | Test Accuracy: 0.942

Appendix

```
import numpy as np
    from sklearn import preprocessing, cross_validation, svm
    from sklearn.linear_model import LogisticRegression
    from sklearn.ensemble import GradientBoostingClassifier
    from sklearn.naive bayes import GaussianNB
    from sklearn.neural network import MLPClassifier
    import pandas as pd
    from sklearn import metrics
    import matplotlib.pyplot as plt
    import seaborn as sn
    plt.style.use('seaborn-darkgrid')
    plt.rcParams['axes.facecolor'] = '#f7f1eb'
    df = pd.read csv('newccd.csv')
    df.drop(['Id'], 1, inplace=True)
    X = df.drop(['churn'],1)
    y = list(df.churn)
    print "Churn percentage in full data:",np.sum(1*(np.array(y)==1))/5000.0
28 X train, X test, y train, y test = cross validation.train test split(X,y,test size=0.3)
    X val, X test, y val, y test = cross validation.train test split(X test,y test,test size=0.5)
    print "Churn percentage in training data:",np.sum(1*(np.array(y train)==1))/float(len(y train))
    print "Churn percentage in val data:",np.sum(1*(np.array(y val)==1))/float(len(y val))
    print "Churn percentage in test data:",np.sum(1*(np.array(y_test)==1))/float(len(y_test))
    print "\nLogistic Regression Analysis:"
    clf = LogisticRegression(solver='sag', max iter=500)
    clf.fit(X train, y train)
    prob = clf.predict proba(X val)[:,1]
    fpr1, tpr1, thresholds = metrics.roc curve(np.array(y val), prob, pos label=1)
    AUC1 = metrics.auc(fpr1, tpr1)
    print "AUC: ", AUC1
```

```
43 AUC1 = metrics.auc(fpr1, tpr1)
     print "AUC: ", AUC1
     pred = (prob>=0.5)*1
      tn, fp, fn, tp = metrics.confusion_matrix(np.array(y_val), pred).ravel()
conf_matrix = np.array([[tp,fp],[fn,tn]])
     sensitivity = tp/float(fn+tp)
specificity = tn/float(fp+tn)
precision = tp/float(tp+fp)
df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
print "Confusion Matrix at default Threshold=0.5"
      print df cm
     print "Specificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2),"\n"
sn.set(font_scale=1.4)
     sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
plt.title("Confusion Matrix with Log Reg (threshold="+str(0.5)+")")
     plt.xlabel("Correct Labels")
plt.ylabel("Predicted Labels")
     plt.show()
    print "\nGaussian Naive Bayes Analysis:"
     clf = GaussianNB()
69 clf.fit(X_train, y_train)
70 prob = clf.predict_proba(X_val)[:,1]
     fpr2, tpr2, thresholds = metrics.roc_curve(np.array(y_val), prob, pos_label=1)
     AUC2 = metrics.auc(fpr2, tpr2)
     print "AUC : ", AUC2
     pred = (prob \ge 0.5)*1
     tn, fp, fn, tp = metrics.confusion_matrix(np.array(y_val), pred).ravel()
      conf matrix = np.array([[tp,fp],[fn,tn]])
     sensitivity = tp/float(fn+tp)
specificity = tn/float(fp+tn)
     precision = tp/float(tp+fp)
df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
print "Confusion Matrix at default Threshold=0.5"
      print df cm
     print "Specificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2),"\n"
sn.set(font_scale=1.4)
      sn.heatmap(df cm. annot=True.annot kws={"size": 16}.fmt='a')
```

```
85 print "Specificity:", np.round(specificity,2)," | Sensitivity/Recall:", np.round(sensitivity,2)," | Precision:",np.round(precision,2),"\n"
 86 sn.set(font scale=1.4)
 87 sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
 88 plt.title("Confusion Matrix with GaussianNB (threshold="+str(0.5)+")")
 89 plt.xlabel("Correct Labels")
 90 plt.ylabel("Predicted Labels")
     plt.show()
 94 print "\nSVM Analysis:"
 95 clf = svm.SVC(probability=True, kernel='rbf')
 97 clf.fit(X train, y train)
     prob = clf.predict proba(X val)[:,1]
    fpr3, tpr3, thresholds = metrics.roc curve(np.array(y val), prob, pos label=1)
100 AUC3 = metrics.auc(fpr3, tpr3)
    print "AUC : ", AUC3
103 pred = (prob>=0.5)*1
    tn, fp, fn, tp = metrics.confusion_matrix(np.array(y_val), pred).ravel()
     conf matrix = np.array([[tp,fp],[fn,tn]])
107   sensitivity = tp/float(fn+tp)
108   specificity = tn/float(fp+tn)
109   precision = tp/float(tp+fp)
110 df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
111 print "Confusion Matrix at default Threshold=0.5"
    print df cm
print "Specificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2),"\n"
114 sn.set(font_scale=1.4)
sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
plt.title("Confusion Matrix with SVM (threshold="+str(0.5)+")")
117 plt.xlabel("Correct Labels")
118 plt.ylabel("Predicted Labels")
119 plt.show()
123 print "\nGradient Boosting Analysis:"
124 clf = GradientBoostingClassifier()
126 clf.fit(X_train, y_train)
    prob = clf.predict_proba(X_val)[:,1]
128 fpr4, tpr4, thresholds = metrics.roc curve(np.array(y_val), prob, pos_label=1)
     AUC4 = metrics.auc(fpr4. tpr4)
```

```
123 print "\nGradient Boosting Analysis:"
124 clf = GradientBoostingClassifier()
126 clf.fit(X train, y train)
     prob = clf.predict_proba(X_val)[:,1]
128 fpr4, tpr4, thresholds = metrics.roc curve(np.array(y val), prob, pos label=1)
129 AUC4 = metrics.auc(fpr4, tpr4)
     print "AUC: ", AUC4
     pred = (prob \ge 0.5)*1
tn, fp, fn, tp = metrics.confusion_matrix(np.array(y_val), pred).ravel()
     conf matrix = np.array([[tp,fp],[fn,tn]])
136 sensitivity = tp/float(fn+tp)
     specificity = tn/float(fp+tn)
138 precision = tp/float(tp+fp)
139 df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
    print "Confusion Matrix at default Threshold=0.5"
141 print df cm
142 print "Specificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2),"\n"
143 sn.set(font_scale=1.4)
     sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
144
145 plt.title("Confusion Matrix with Gradient Boosting (threshold="+str(0.5)+")")
146 plt.xlabel("Correct Labels")
     plt.ylabel("Predicted Labels")
148 plt.show()
152 print "\nNeural Network Analysis:"
clf = MLPClassifier(solver='lbfqs', alpha=le-5, hidden layer sizes=(10,), random state=1,activation='relu',max iter=300)
155 clf.fit(X train, y_train)
     prob = clf.predict_proba(X_val)[:,1]
     fpr5, tpr5, thresholds = metrics.roc_curve(np.array(y_val), prob, pos_label=1, drop_intermediate=False)
158 AUC5 = metrics.auc(fpr5, tpr5)
     print "AUC : ", AUC5,"\n"
     pred = (prob \ge 0.5)*1
tn, fp, fn, tp = metrics.confusion_matrix(np.array(y val), pred).ravel()
     conf matrix = np.array([[tp,fp],[fn,tn]])
165 sensitivity = tp/float(fn+tp)
```

```
152 print "\nNeural Network Analysis:"
clf = MLPClassifier(solver='lbfgs', alpha=le-5, hidden layer sizes=(10,), random state=1,activation='relu',max iter=300)
     clf.fit(X train, y train)
     prob = clf.predict proba(X val)[:,1]
     fpr5, tpr5, thresholds = metrics.roc_curve(np.array(y_val), prob, pos_label=1,drop_intermediate=False)
     AUC5 = metrics.auc(fpr5, tpr5)
     print "AUC : ", AUC5,"\n"
     pred = (prob \ge 0.5)*1
     tn, fp, fn, tp = metrics.confusion matrix(np.array(y val), pred).ravel()
     conf matrix = np.array([[tp,fp],[fn,tn]])
     sensitivity = tp/float(fn+tp)
166 specificity = tn/float(fp+tn)
     precision = tp/float(tp+fp)
168 df cm = pd.DataFrame(conf matrix, index=["1","0"],columns=["1","0"])
     print "Confusion Matrix at default Threshold=0.5"
     print df cm
     print "Specificity:", np.round(specificity,2)," | Sensitivity/Recall:", np.round(sensitivity,2)," | Precision:",np.round(precision,2),"\n
172 sn.set(font scale=1.4)
     sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
plt.title("Confusion Matrix with Neural Network (threshold="+str(0.5)+")")
175 plt.xlabel("Correct Labels")
     plt.ylabel("Predicted Labels")
     plt.show()
     x = np.arange(0.0, 1.0, 0.01)
plt.plot(x,x,'--',color="#00a2d9",linewidth=1)
     plt.plot(fpr1,tpr1,label="Logistic Regression(Area:"+str(round(AUC1,2))+")", color="cyan",linewidth=1)
     plt.plot(fpr2,tpr2,label="Gaussian Naive Bayes(Area:"+str(round(AUC2,2))+")", color="black",linewidth=1)
     plt.plot(fpr3,tpr3,label="SVM RBF(Area:"+str(round(AUC3,2))+")", color="red",linewidth=1)
     plt.plot(fpr4,tpr4,label="Gradient Boosting(Area:"+str(round(AUC4,2))+")", color="#ffb74d",linewidth=1)
     plt.plot(fpr5,tpr5,label="Neural Nework(Area:"+str(round(AUC5,2))+")", color="#62bba4",linewidth=1)
     plt.legend(loc='lower right')
     plt.title("ROC Curve for different classifiers")
     plt.xlabel("---- False Positive Rate --->")
    plt.ylabel("---- True Positive Rate --->")
194 plt.show()
```

```
x = np.arange(0.0, 1.0, 0.01)
     print "Choosing threshold at point closer to upper left corner in ROC curve:"
     YIndexList = []
    dList = []
     fb = []
     Highest YIndex=0 # Initializing it to zero
     Lowest \overline{d} = 1
     highest Fbeta=0
     for threshold in x:
          pred = (prob>=threshold)*1
          tn, fp, fn, tp = metrics.confusion matrix(np.array(y val), pred).ravel()
          sensitivity = tp/float(fn+tp)
          specificity = tn/float(fp+tn)
          d = np.sqrt(np.power(1-sensitivity,2)+np.power(1-specificity,2))
          YIndex=specificity+sensitivity-1
          fbeta = metrics.fbeta score(y val, pred,beta=2)
          if fbeta>=highest Fbeta:
              highest Fbeta=fbeta
              selected threshold=threshold
          YIndexList.append(YIndex)
          dList.append(d)
          fb.append(fbeta)
     plt.plot(x,YIndexList,color='#62bba4',label="Youden Index",linewidth=3)
     plt.plot(x,dList,color='#ffb74d',label="Dist from upper Left Corner",linewidth=3)
     plt.plot(x, fb,color='#816E94',label="Fbeta",linewidth=3)
     plt.legend(loc='lower right')
     plt.title("Different Parameters vs Threshold")
     plt.xlabel("---- Threshold --->")
     plt.ylabel("--- Index -->")
     plt.show()
     pred = (prob>=selected threshold)*1
    tn, fp, fn, tp = metrics.confusion matrix(np.array(y val), pred).ravel()
     conf matrix = np.array([[tp,fp],[fn,tn]])
     df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
     print "Confusion Matrix at selected threshold=", selected threshold
     print df cm
     sn.set(font scale=1.4)
238 sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
239 plt.xlabel("Correct Labels")
240 plt.vlabel("Predicted Labels")
```

210

```
print df cm
    sn.set(font scale=1.4)
238 sn.heatmap(df cm, annot=True,annot kws={"size": 16},fmt='g')
     plt.xlabel("Correct Labels")
     plt.ylabel("Predicted Labels")
240
    plt.title("Confusion Matrix at selected threshold("+str(selected threshold)+")")
     plt.show()
     sensitivity = tp/float(fn+tp)
246 specificity = tn/float(fp+tn)
     precision = tp/float(tp+fp)
     acc = (tp+tn)/float(tp+tn+fn+fp)
248
     prob = clf.predict proba(X train)[:,1]
     fpr, tpr, thresholds = metrics.roc curve(np.array(y train), prob, pos label=1)
     Training AUC = metrics.auc(fpr, tpr)
    print "\nSpecificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2)
    print "val AUC:",AUC5," | Training AUC:",Training AUC," | val. Accuracy:",acc
    print "\nTest set Analysis:"
     prob = clf.predict proba(X test)[:,1]
    fpr, tpr, thresholds = metrics.roc curve(np.array(y test), prob, pos label=1)
    Val AUC = metrics.auc(fpr, tpr)
    pred = (prob>=selected threshold)*1
    tn, fp, fn, tp = metrics.confusion matrix(np.array(y test), pred).ravel()
265 conf matrix = np.array([[tp,fp],[fn,tn]])
266 df_cm = pd.DataFrame(conf_matrix, index=["1","0"],columns=["1","0"])
     print "Confusion Matrix of Test Set:"
    print df_cm
270 sn.set(font scale=1.4)
271 sn.heatmap(df_cm, annot=True,annot_kws={"size": 16},fmt='g')
272 plt.xlabel("Correct Labels")
    plt.ylabel("Predicted Labels")
    plt.title("Confusion Matrix of Test Set")
    plt.show()
    sensitivity = tp/float(fn+tp)
278 specificity = tn/float(fp+tn)
279 precision = tp/float(tp+fp)
```

```
plt.title("Confusion Matrix of Test Set")
275 plt.show()
     sensitivity = tp/float(fn+tp)
278 specificity = tn/float(fp+tn)
     precision = tp/float(tp+fp)
280 acc = (tp+tn)/float(tp+tn+fn+fp)
281 print "\nSpecificity:", np.round(specificity,2),"| Sensitivity/Recall:", np.round(sensitivity,2),"| Precision:",np.round(precision,2)
     print "Test AUC:", Val AUC, " | Test Accuracy:", acc
285 x = np.arange(0.0, 1.0, 0.01)
286 print "Threshold selection:"
287 YIndexList = []
288 dList = []
289 fb = []
290 cost list = []
291 Highest YIndex=0 # Initializing it to zero
     Lowest d = 1
     highest Fbeta=0
294 tn, fp, fn, tp = metrics.confusion_matrix(np.array(y val), (prob>=0.01)*1).ravel()
295 ratio = 5
     lowest cost = 10*(tp+fp)+ratio*10*fn
     for threshold in x:
         pred = (prob>=threshold)*1
         tn, fp, fn, tp = metrics.confusion matrix(np.array(v val), pred).ravel()
         sensitivity = tp/float(fn+tp)
         specificity = tn/float(fp+tn)
         d = np.sqrt(np.power(1-sensitivity,2)+np.power(1-specificity,2))
         YIndex=specificity+sensitivity-1
         fbeta = metrics.fbeta score(y val, pred,beta=2)
         cost = 10*(tp+fp)+ratio*10*fn
         if cost<=lowest cost:</pre>
             lowest cost=cost
             selected threshold=threshold
         YIndexList.append(YIndex)
         dList.append(d)
         fb.append(fbeta)
         cost list.append(cost)
     cost list=np.array(cost list)
313
```