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TOC Test-02

Answer to the ques. no: 1

Ambiguous CFG:

A CFG is said to be ambiguous if there exists more than one derivation tree for the given input string i.e. more than one Left Most - Derivation Tree (LMDT) or Right Most Derivation Tree (RMDT).

If the grammar is said to be ambiguous or it has ambiguity, then it is not good for compiler construction. No method can automatically detect and remove ambiguity by re-writing the whole grammar without ambiguity.

Let, $G = (V, T, P, S)$ is a CFG is said to be ambiguous if and only if there exist a string in T^* that has more than one parse tree.

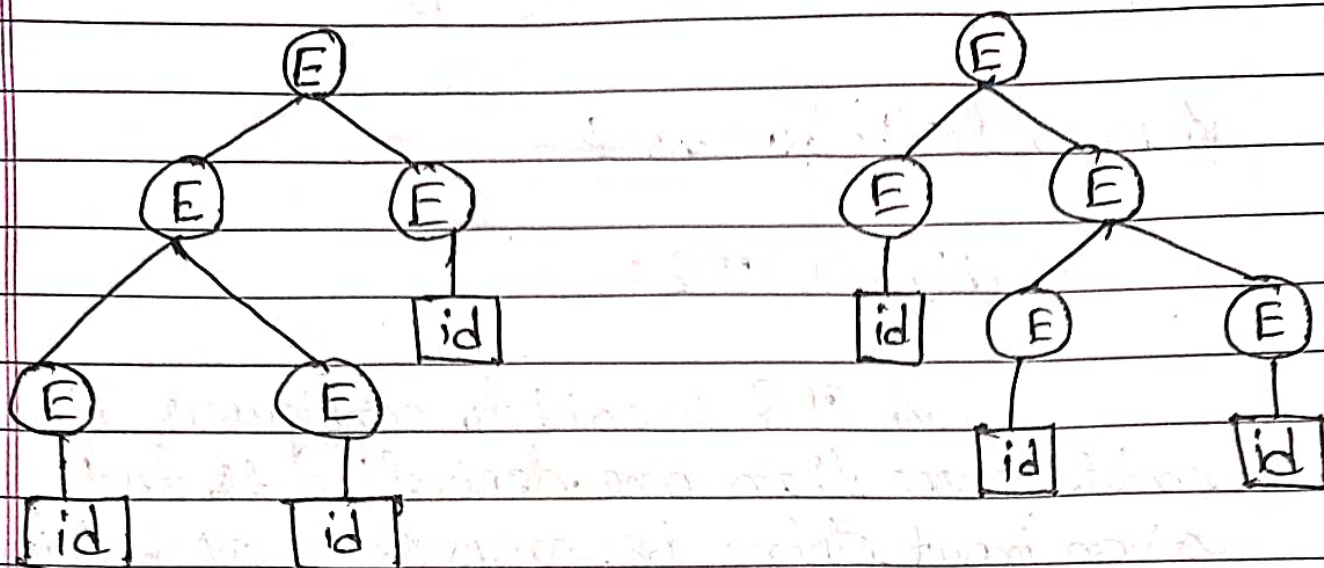
Here, V is a finite set of variables.

T is a finite set of terminals

P is a finite set of production of the form, $A \rightarrow \alpha$, where A is a variable and $\alpha \in (V \cup T)^*$ is a designated variable called the start symbol.

Ex. $E \rightarrow E + E \mid id$

We can create two parse tree from this grammar to obtain a string $id + id + id$:



Inherently Ambiguous CFG:

Ⓐ If every context-free grammar G with language $L = L(G)$ is ambiguous, then L is said to be inherently ambiguous language. Ambiguity is a property of grammar not language.

For example,

$$L = \{a^n b^n c^m\} \cup \{a^n b^m c^m\}$$

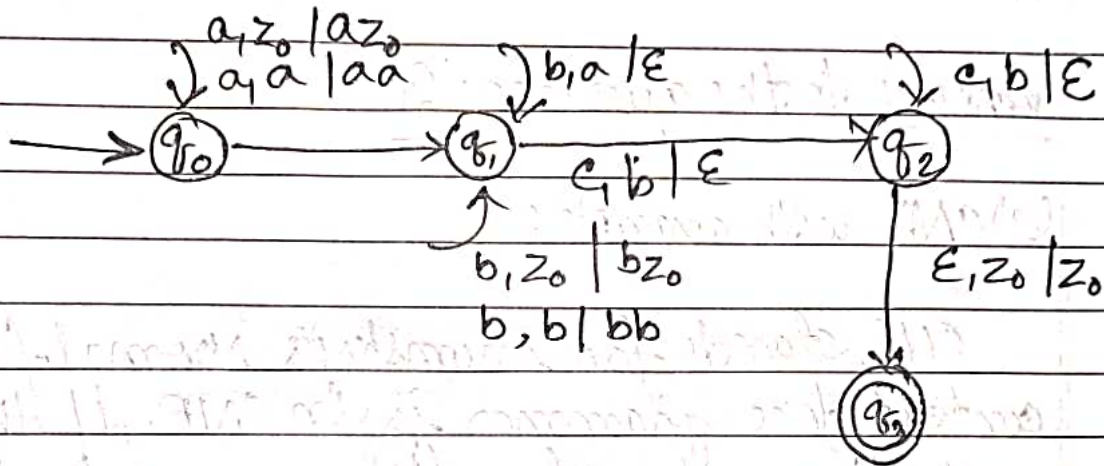
Q. 4.)

(i) Given that,

$$L = \{a^n b^{n+m} c^m : n \geq 1, m \geq 1\}$$

$$= a^n b^n b^m c^m$$

$$\alpha = \{abbc, a^2b^4b^2c^2, a^4b^4b^4c^4, \dots\}$$

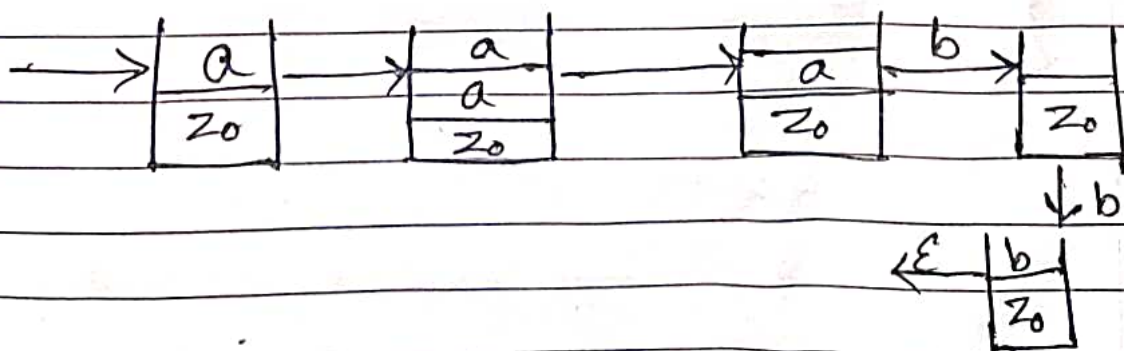


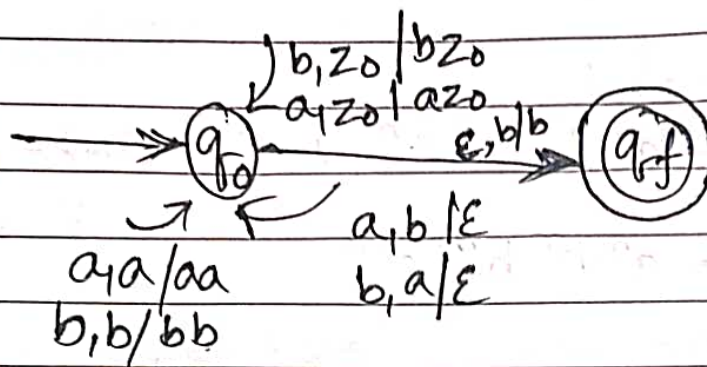
(ii) Given that,

$$L = \{w : n_a(w) < n_b(w)\}$$

$$= \{b, abb, aabbb, \dots\}$$

Logic: b should remain at the top of stack at the end of string. (ε is input).
push a or push b, if top = a, input = b, pop. If top = b, input = a, pop.





Answer to the ques. no. 3

(a) CNF with example:

CNF stands for Chomsky's Normal form. A context free grammar is in CNF. If the production rules satisfy one of the following conditions.

- If there is start symbol generating ϵ .
Ex. $A \rightarrow \epsilon$.

- If a non-terminal generates two non-terminals. Ex. $S \rightarrow AB$.

- If a non-terminal generates a terminal
Ex. $S \rightarrow a$.

CNF Example:

Let,

$$A = \{w \mid w \in \{a, b\}^* \text{ and } w = w^R\}$$

CNF in CNF

Derivation of baaab

$$S \rightarrow AU \mid BU \mid a \mid b \mid \epsilon$$

$$S \Rightarrow BV$$

$$T \rightarrow AU \mid BV \mid a \mid b$$

$$\Rightarrow bV$$

$$U \rightarrow TA$$

$$\Rightarrow bTB$$

$$A = a$$

$$\Rightarrow bAUB$$

$$B = b$$

$$\Rightarrow baUB$$

$$\Rightarrow baTAB$$

$$\Rightarrow baaAB$$

$$\Rightarrow baaaB$$

$$\Rightarrow baaab.$$

(b) GNF with example:

GNF stands for Greibach normal form. A CFG is in GNF. If all the production rules satisfy one of the following conditions.

- A start symbol generating ϵ .

$$\text{Ex. } S \rightarrow \epsilon.$$

- A non-terminal generating a terminal

$$\text{Ex. } A \rightarrow a.$$

- A non-terminal generating a terminal which is followed by one or more non-terminals

of non-terminals.
Ex. $S \rightarrow aASB$.

GNF Example:

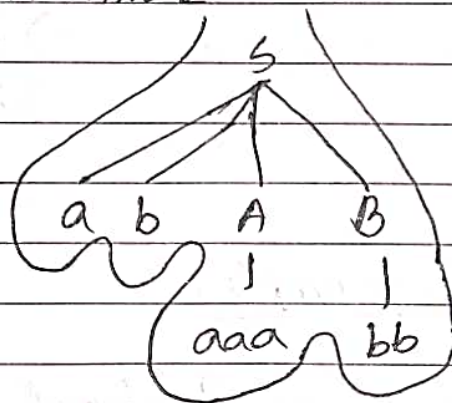
$G_1 = \{ S \rightarrow aB | aB, A \rightarrow aA | a, B \rightarrow bB | b \}$

$G_2 = \{ S \rightarrow aAB | aB, A \rightarrow aA | \epsilon, B \rightarrow bB | \epsilon \}$

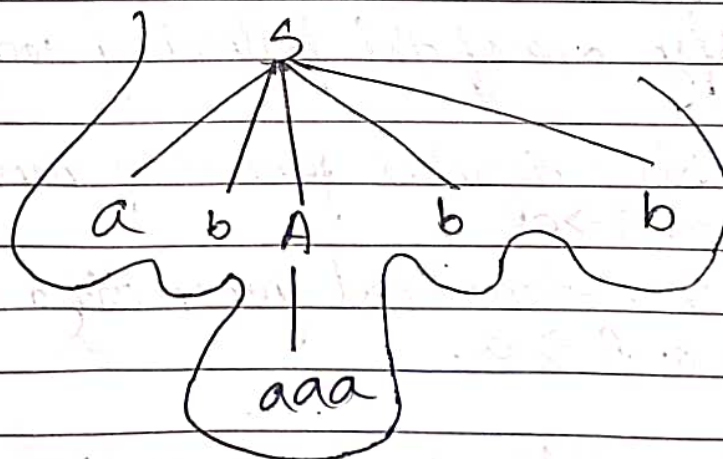
Answer to the ques. no: 2

\rightarrow $abaaabb$ this generate both Grammar

①



②



so both are equal