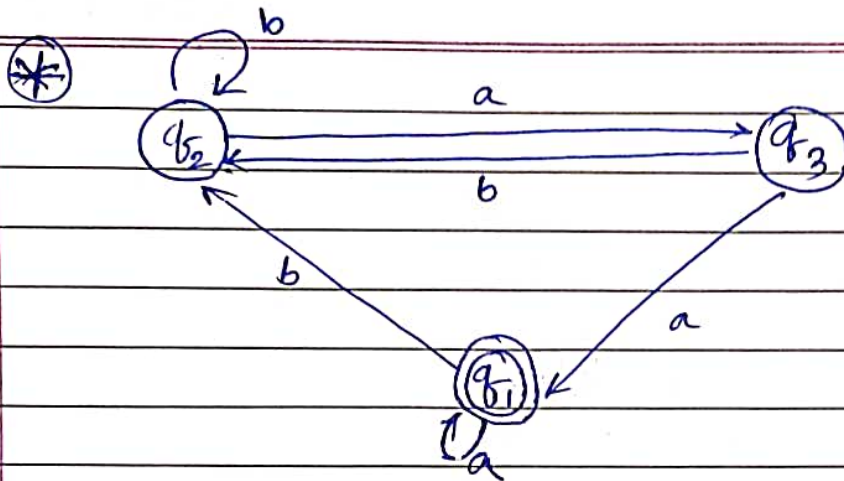


# Assignment - TOC

Name: Zishmendu Sarker  
Roll: 2K19/20/450

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Here, the initial state and final state is  $q_1$ .  
The equation for the three state is  $q_1, q_2, q_3$ , are.

$$q_1 = q_1 a + q_3 a + \epsilon \quad [\epsilon \text{ more is because } q_1 \text{ is the initial state}]$$

$$q_2 = q_1 b + q_2 b + q_3 b$$

$$q_3 = q_2 a$$

Now, we solve these three equations -

$$q_2 = q_1 b + q_2 b + q_3 b$$

$$= q_1 b + q_2 b + (q_2 a) b \quad (\text{substituting value of } q_3)$$

$$= q_1 b + q_2 (b + ab)$$

$$= q_1 b (b + ab)^* \quad (\text{Applying Arden's Theorem})$$

$$q_1 = q_1 a + q_3 a + \epsilon$$

$$= q_1 a + q_1 b (b + ab)^* a + \epsilon \quad (\text{substituting value of } q_3)$$

$$= q_1 a + q_1 b (b + ab)^* a a + \epsilon \quad (\text{substituting value of } q_2)$$

$$\begin{aligned}
 q_i &= q_i (a + b(b + ab)^* aa)^* + \epsilon \\
 &= \epsilon (a + b(b + ab)^* aa)^* \\
 &= (a + b(b + ab)^* aa)^*
 \end{aligned}$$

so, the regular expression is  $(a + b(b + ab)^* aa)^*$ .

← ○ →