

Unit - 6

DATE: ___/___/___
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Web security

Web security refers to the protective measures and protocols that organization adopt to protect the organization from cyber criminals and threats that use the web channel.

Top web security threats

- Cross-site scripting (XSS)
- SQL Injection
- Phishing
- Ransomware
- Code Injection
- Viruses & worms
- Spyware
- Denial of service.

Security Measures

- Updated softwares
- Be aware of SQL Injection
- Cross-site Scripting (XSS)
- Error Messages
- Data validations
- Password

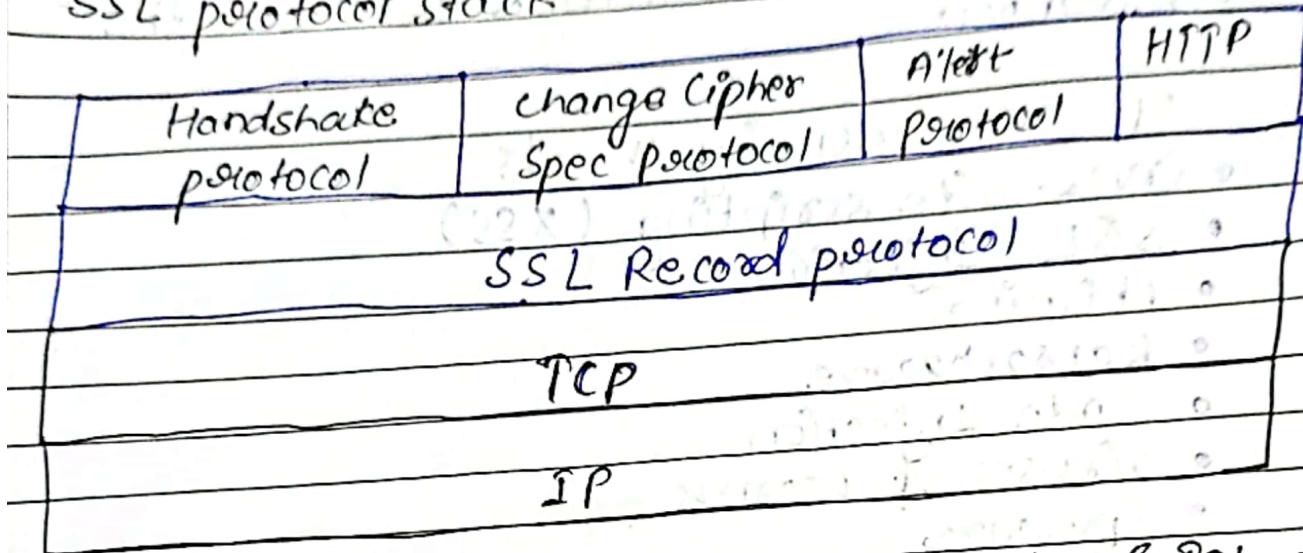
Secure Socket Layer (SSL)

SSL provides security to the data that is transferred between web browser and web server.

It encrypts the link between a web server & browser and which ensures that all data passed between them remain private and free from attack.

→ lies between application layer and transport layers of TCP/IP

SSL protocol stack



SSL Record protocol (Confidentiality & Integrity)

It has two services

- Confidentiality (done by encryption)
- Message Integrity (done by MAC)

Working:-

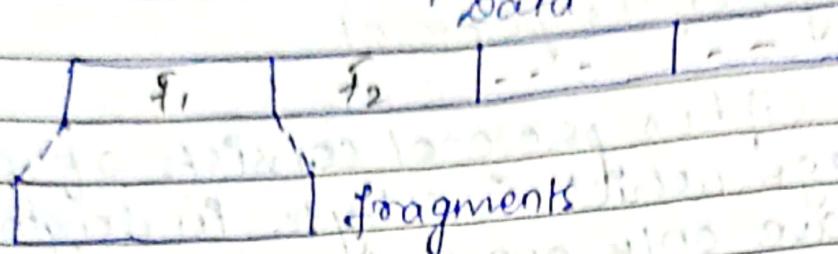
Application data is divided into fragments. The fragments is compressed and then encrypted. MAC (Message Authentication code) generated by SHA algo, and MD5 (Message digest) is appended.

At last SSL header is appended to the data.

block size or
fragment size = 2¹⁴ bytes

DATE: _____
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Application
Data



(compression (optional))

MAC

(calculation & addition of
MAC)

compre-
ssion
+
MAC

encryption

SSL
Header

Handshake Protocol

It is used to establish sessions. This protocol allows client & server to authenticate each other by sending a series of messages to each other. Handshake protocol uses four phases to complete its cycle.

- Ensure Authentication
- most complicated part in SSL
- key exchange between client & server

Working

- connection establishment with server
- key exchange from server to client
- Handshake done from server
- key exchange from client to server
- Handshake done from server.

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• SSL change Cipher protocol

Change cipher protocol consists of a single message which is 1 byte in length and can have only one value.

1 byte

→ copies the pending state into current state.

* SSL Alert protocol

This protocol is used to convey SSL-related alerts to the peer entity. Each message in this protocol contains 2 bytes

[level
(1 byte)] [Alert
(1 byte)]

Level is further classified into two parts.

Warning (level=1)

Bad certificate

No certificate

Certificate expired

Certificate unknown

Close notify

fatal error (level=2)

Handshake failure

Decompression failure

Illegal parameters

Bad record MAC

Unexpected message

Features of SSL

- Can be tailored to the specific needs of the given application.
- Originated by netscape.
- Designed to make use of TCP to provide reliable, end-to-end secure service.
- This is two layered protocol.

Versions of SSL

SSL 1 - Never released because of high insecurity.

SSL 2 - Released in 1995

SSL 3 - Released in 1996

TLS 1.0 - Released in 1998

|| 1.1 " " 2006

1.2 " " 2008

1.3 " " 2018

Transport Layer Security

- defined in RFC 5246 (Req. for comments)
- for providing security in transport layer.
- derived from SSL
- ensures that no 3rd party may eavesdrop or tampers with any message.

Benefits of TLS

Encryption

Interoperability

Algorithm flexibility

Ease of Deployment

Ease of Use

Working

Uses client server handshake mechanism.

1. Key exchange b/w client and server

(by Diffie Hellman key Exchange Algo)

2. Now TLS protocol will open an encryption channel.

(by RC4 / IDEA / DES Algorithm)

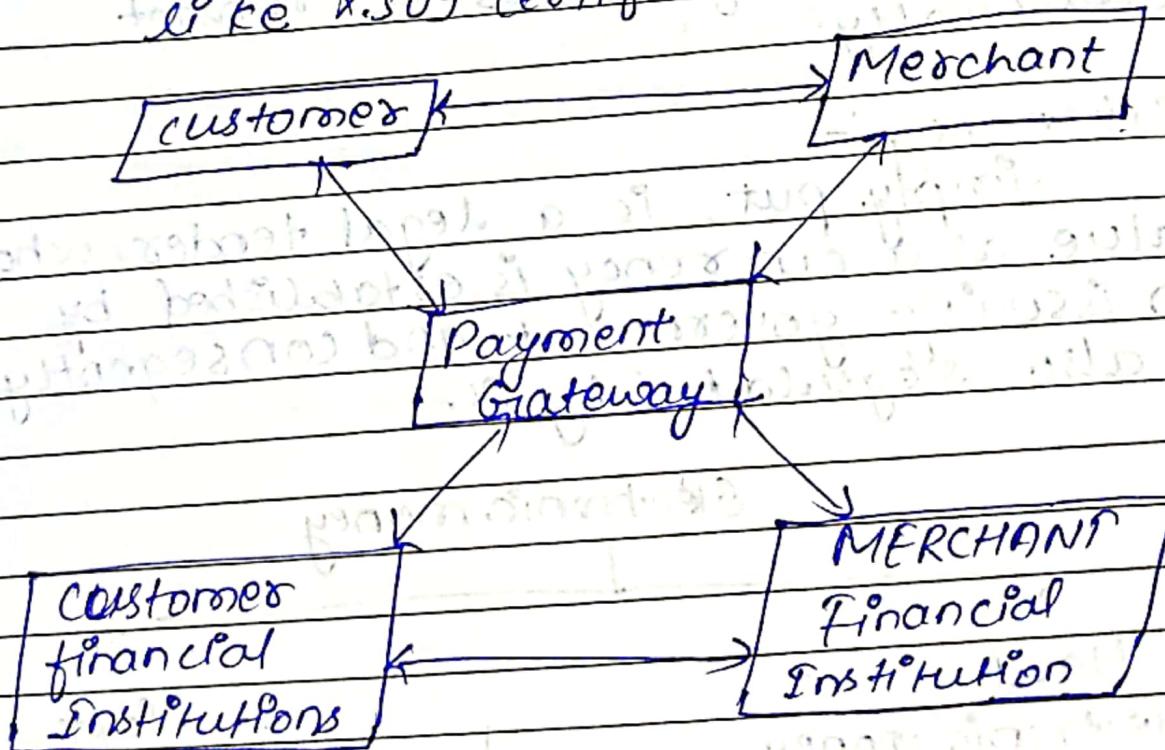
3. It also ensures that message are not altered,

(by MD5 / SHA Algo)

* RFC 5246 is similar to SSL V3

Secure Electronic Transaction

- ensures security & integrity of the electronic transactions done using credit cards, debit cards, UPF, netbanking
- uses different encryptions & hashing techniques to secure payments.
- Set protocol restricts the revealing of credit card details to merchants (amazon, flipkart) thus keeping hackers and thieves at bay.
- implemented using digital certificates like X.509 certificate.



Requirement that SFT protocol need to meet

- Mutual Authentication
- confidentiality of (PJ and OI)
- Period Integrity
- interoperability and security mechanism.

Participant in SET

Card holder

Customer bank

Merchant

Acquirer

Certificate authority

Electronic Money:-

Electronic money refers to the currency electronically stored on electronic systems and digital database, as opposed to physical paper and coin money and is used to make it easier for users to transact electronically.

Fiat money:-

simply put, is a legal tender, whose value as a currency is established by an issuing government and consequently is also regulated by it.

Electronic money

Hard

electronic money

that is used for irreversible transactions,

highly secured &

more or less procedural in nature.

Soft

electronic money used for reversible or flexible transactions

canceling a transaction or modifying the payment profile.

Features of E-money

- o Store of value :-
- o Medium of exchange
- o Unit of Account
- o Standard of deferred payment.

Advantage of electronic money

- o Increased flexibility and convenience
- o Historical record
- o prevents fraudulent activities
- o Instantaneous
- o Increased security

Disadvantages of electronic money

- o Necessity of certain infrastructure.
- o Possible security breaches/hacks
- o Online scam.

study material - time at station
and transportation grant is difficult to get
money to travel around using ATM

study material - time at station
and transportation grant is difficult to get

study material - time at station
and transportation grant is difficult to get

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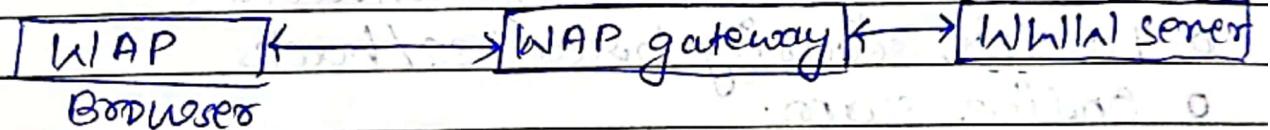
WAP security

It is a specification for a set of communication protocols to standardize the way wireless devices such as mobile phones & radio transceivers, can be used for internet access (including email, the web, newsgroups and instant messaging).

Wireless Markup Language was used to create pages that can be delivered using WAP.

How the WAP work?

WAP Architecture



WAP model & layers

Similar to client - server model but uses an additional WAP gateway as an intermediary between client & server.

WAP protocol stack

wireless Application Environment

wireless session protocol

wireless transaction protocol

wireless transport layer security

wireless datagram protocol

Use of WAP

- wireless network of mobile phone operators.
- Content providers
- End Users

Not much famous in all countries because of widespread HTML compatibility in mobile phones.

firewall design principles

A firewall is a hardware or software to prevent a private computer or network of computers from unauthorized access, it acts as a filter to avoid unauthorized users from accessing private computers & networks.

Principles

- Developing Security policy
Without it, there is increase in risks as there will not be a proper implementation of security solutions.
- Simple Solution Design:-
If the design of solution is complex then it will be difficult to implement, maintain and upgrade by analysing new possible threats, efficiency keeping in mind yet simple in structure.

o Choosing right device:

If the outdated device is used for designing firewall, it exposes the network to risk and is almost useless.

o Layered defence

A network defence must be multi-layered because it gives an edge to the security design and finally neutralize the attack on the system.

o Consider Internal threats

Sometimes internal threats ~~can~~ be neglected which makes the network weaker and vulnerable. Filtering them adds a new layer in security point of view.

Need & Importance

Different requirements

Outlining policies

Identifying policies

Setting restrictions

Identify Deployment locations

Value of security is reflected by deployment of security devices.

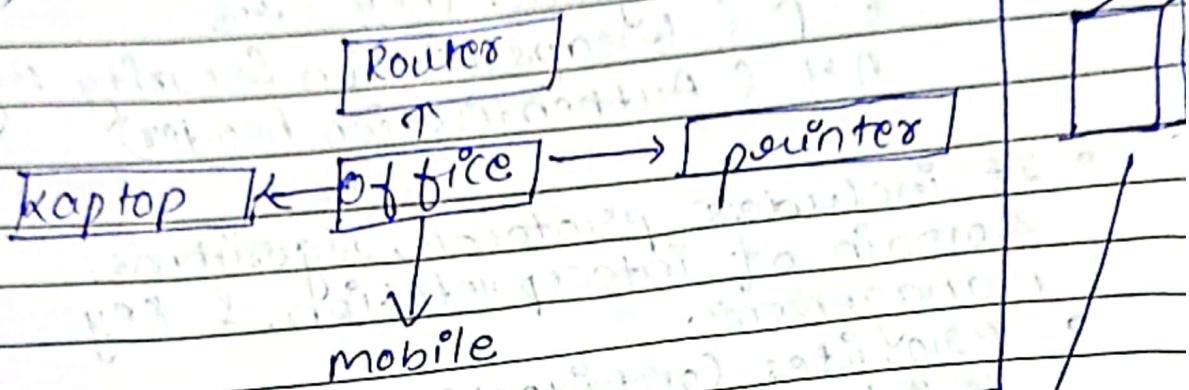
Deployment of security devices depends on the nature of organization.

Deployment of security devices depends on the nature of organization.

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Virtual private Networks Security
It is a way to extend a private network using a public network such as internet.

(E)

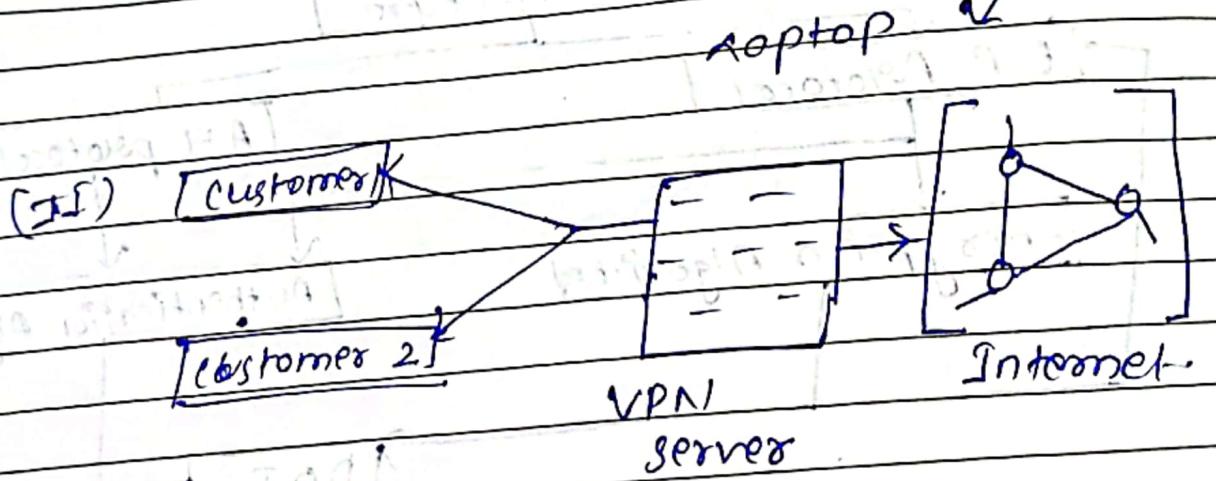


A

(B)

VPN
server

(C)



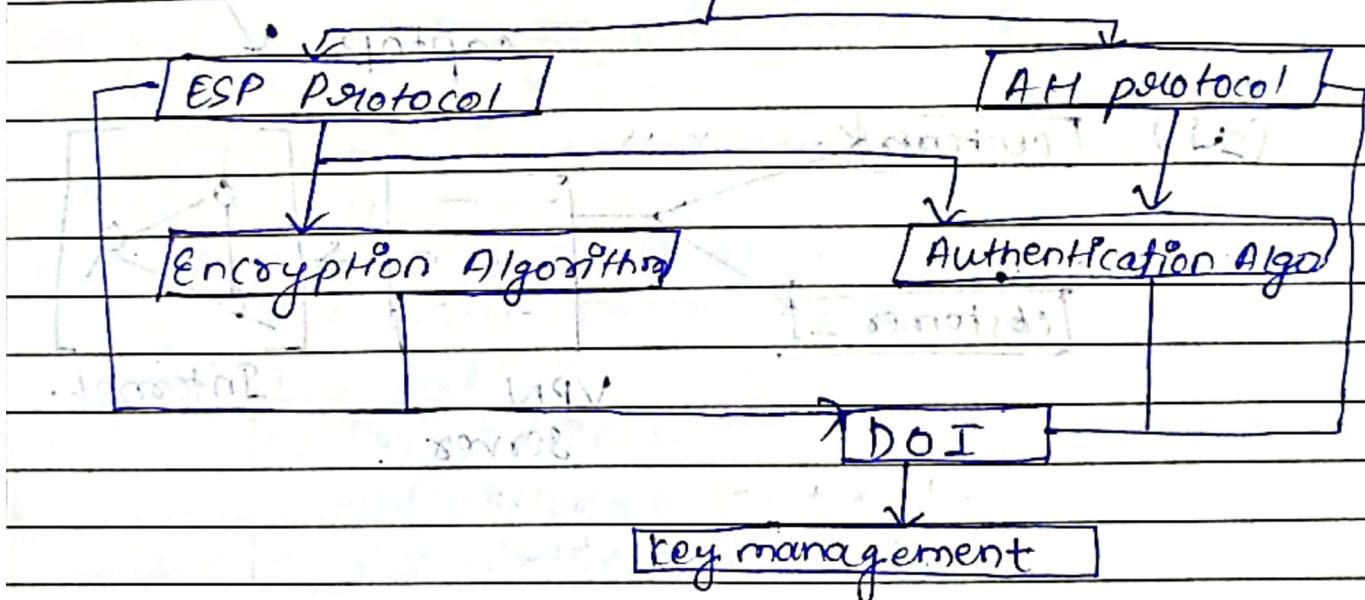
IP Security

It is a framework for protecting communication over IP.

1) Architecture

- It uses two protocols to secure the traffic or data flow. They are
ESP (Encapsulation Security Payload)
AH (Authentication header)
- It includes protocols, algorithms, domain of interpretation, & key management.
- Provides confidentiality, authentication & integrity.

(a) [Architecture]



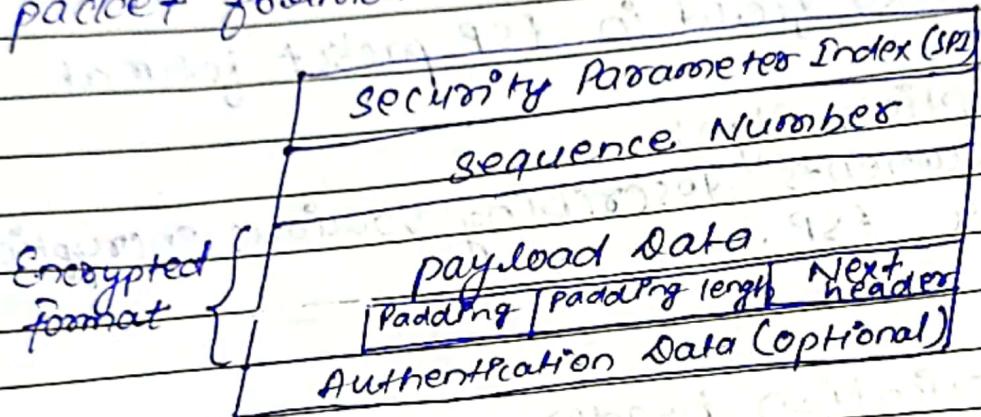
Architecture covers the general concepts, definitions, protocols, algo. and security requirements of IP Security technology.

2) ESP protocol

provides a confidentiality service.
Implemented either two ways:

ESP with optional Authentication
ESP with Authentication

packet format



Security parameter index (SPI)

used by security association to give unique number to the connection built between the client & server.

sequence number

are allotted to every packet so that on the receiver side packets can be arranged properly.

payload Data:-

It's an actual data that are encrypted for confidentiality purpose.

padding:

Extra bits of space are added to the original message in order to ensure confidentiality.

Next header: means next payload or next actual data.

Authentication data:

optional field in ESP packet format.

3) Encryption Algo:

documents describing various encryption

also for ESP.

4) Authentication header:

provides authentication and integrity service.

Implemented as Authentication with Integrity.

Next header	Payload length	Reserved
Security Parameter Index	Index	
Sequence Number		
Authentication Data (Integrity Checksum)		

It covers the packet format and general issue related to the use of AH for packet authentication & integrity.

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5. Authentication Algo:-

contains the set of documents that describe the authentication algorithm used for AH & for the authentication option of ESP.

6. DOI

Identified that supports both AH & ESP protocol and contains values needed for documentation related to each other.

7. Key Management:-

contains the document that describes how the keys are exchanged between sender and receiver.

confidentiality (IPsec) - IPsec

nonrepudiation (NRI)

authentication (A) - IPsec

key exchange (KE) - IPsec

Integrity (I) - IPsec

confidentiality (IPsec) - IPsec

Electronic mail security

It is the process of ensuring the availability, integrity and authenticity of email communications by protecting against the risk of email threats.

PGP (Pretty Good Privacy)

- * invented by phil zimmermann in 1991
- * New security concept which provide email-security.
- * It is an encryption that provides cryptographic privacy and integrity also authentication for data communication
- * PGP is used for signing, encryption and decrypting texts, emails, files, directories and to increase the security of email communications.

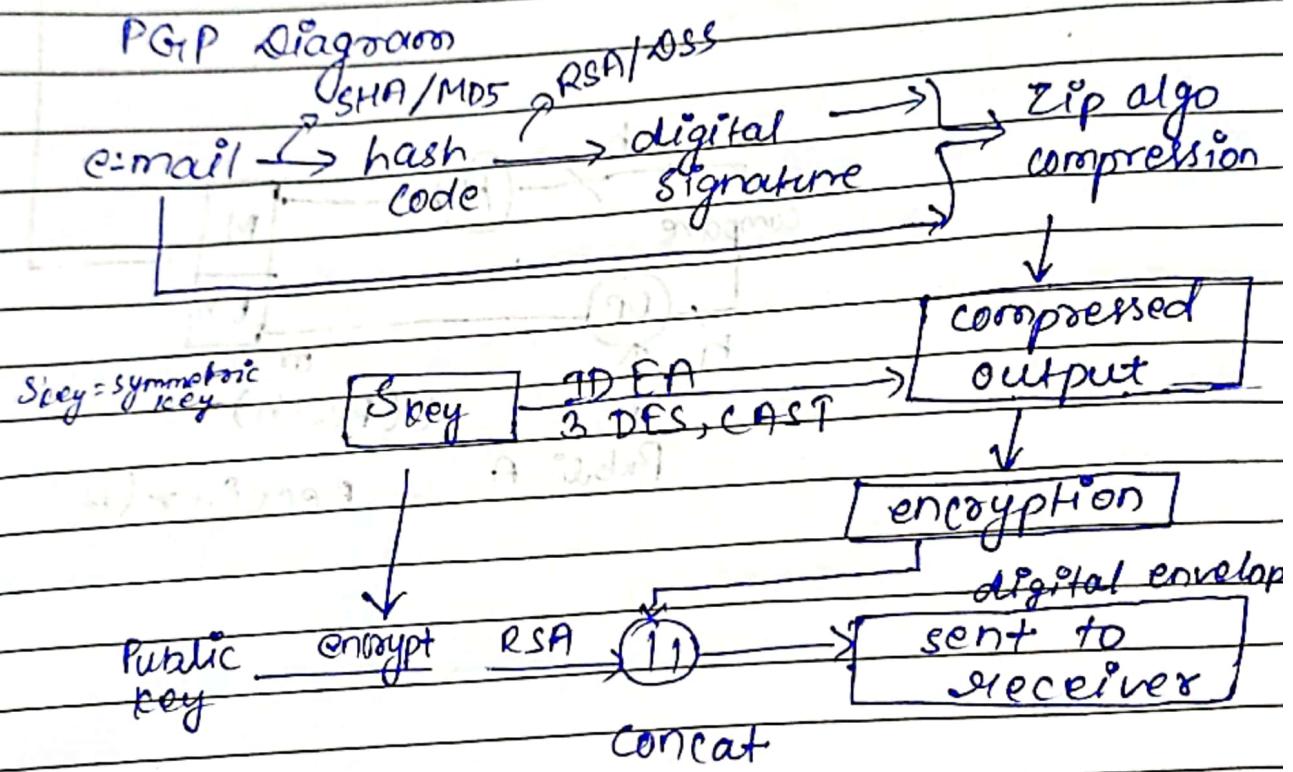
PGP encryption uses a serial combination of

- (i) Hashing
- (ii) Data compression
- (iii) Symmetric key Cryptograph
- (iv) asymmetric key cryptography

and each step uses one of the several supported algorithm like RSA, IDEA, SHA etc.

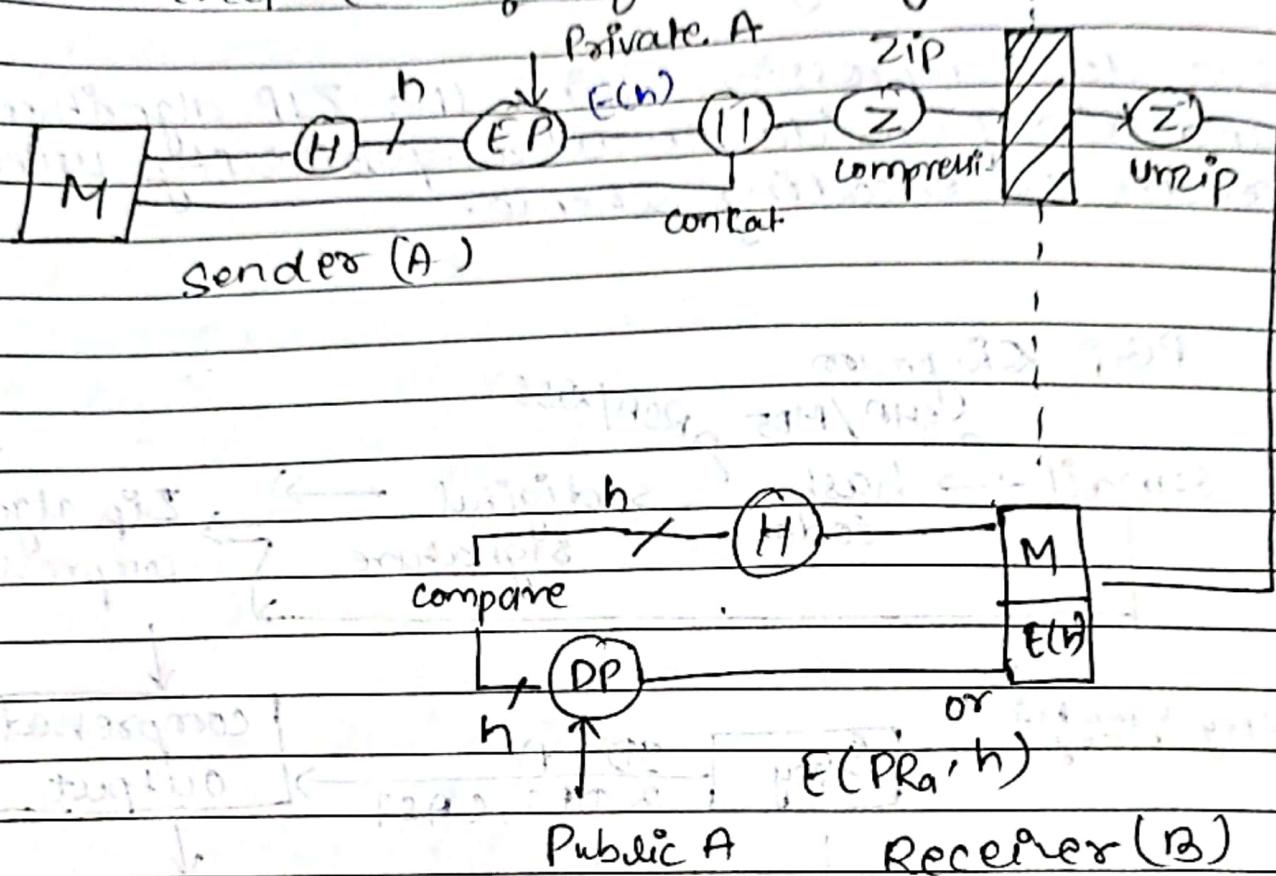
- Services provided by PGP
- * authentication (using digital signature)
 - * confidentiality

We do compression using the ZIP algorithm and also provide email compatibility using radix-64 encoding scheme.

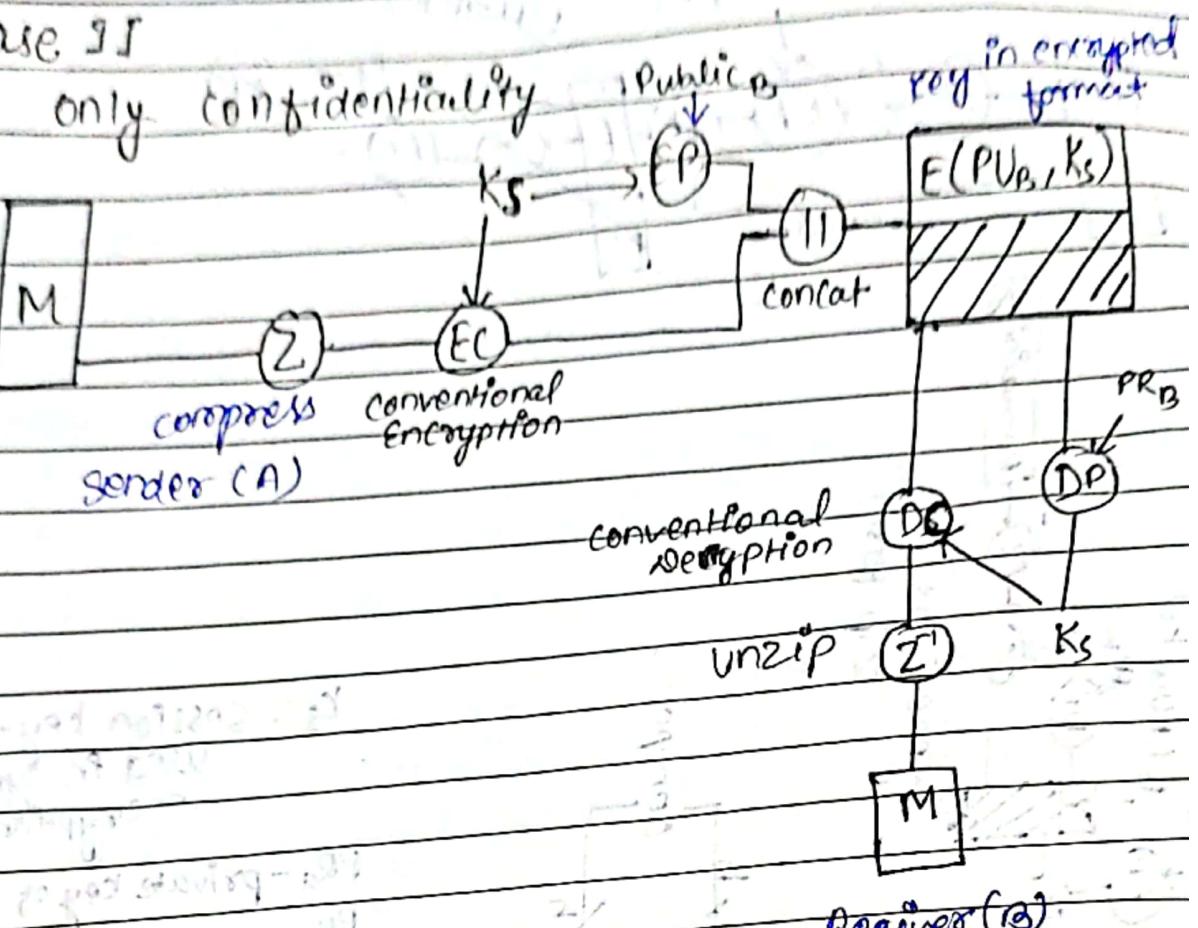


Case-J

authentication + digital signature
achieved (No confidentiality)



Case 3.5



Here we are not using private key of sender to encrypt the message. So that's why authentication is not achieved here.

Message = S

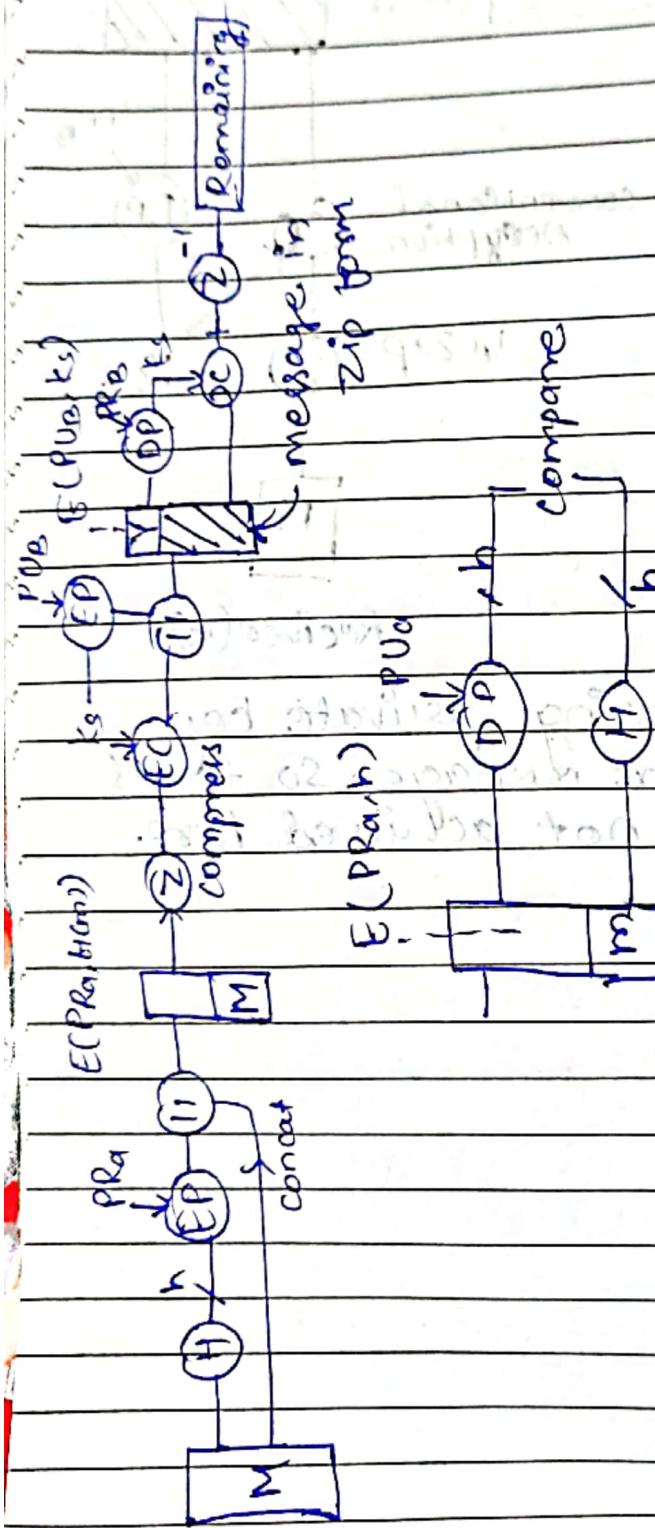
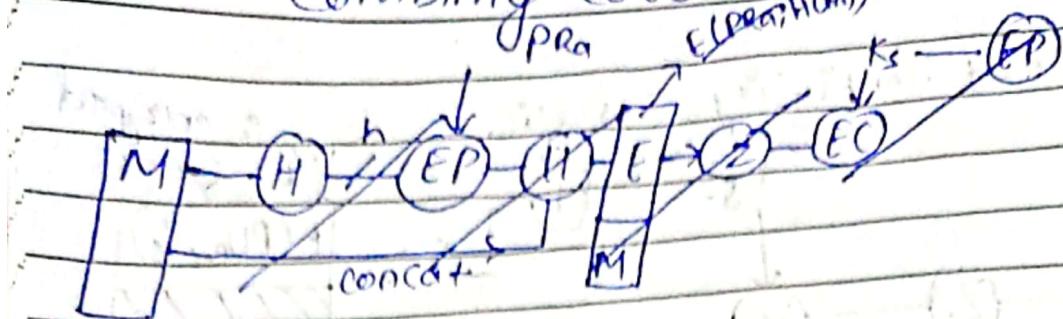
Key = K

IV = I

IV

DATE: / /
PAGE: / /

Combining case 1 and case 1'



k_s = session key
used in symmetric encryption.

PRa - private key of user A

PVa - public " " " "

EP - public key encryption

DP - public key decryption

EC - conventional symmetric encryption

DC - conventional symmetric decryption.

h = hash code

H = hash function

Z = compression algo

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MIME (Multipurpose Internet Mail Extension)

* MIME is a standard which was proposed by Bell Communication in 1991 in order to expand the limited capabilities of email.

Email has a simple structure
Email can send messages only in
ASCII 7-bit ascii format.

In short, MIME is a supplementary protocol
or a add which allows non ascii data
to be sent through email using SMTP.

It allows users to exchange different kinds
of data files on the internet like audio
video, images etc.

MIME is an extension to the Internet Email
protocol.

Email with mime formatting are
typically transmitted with standard
protocols like SMTP (simple mail transfer
protocol), POP (post offices protocol) and
the IMAP (Internet Message Access protocol).

Although MIME was designed mainly for SMTP
its content types are also important in other
communication protocols.

e.g.) In HTTP protocol for the world wide web
Good Write Servers insert a MIME header field

at the beginning of any web transaction.

Limitations of SMTP (need of MIME)

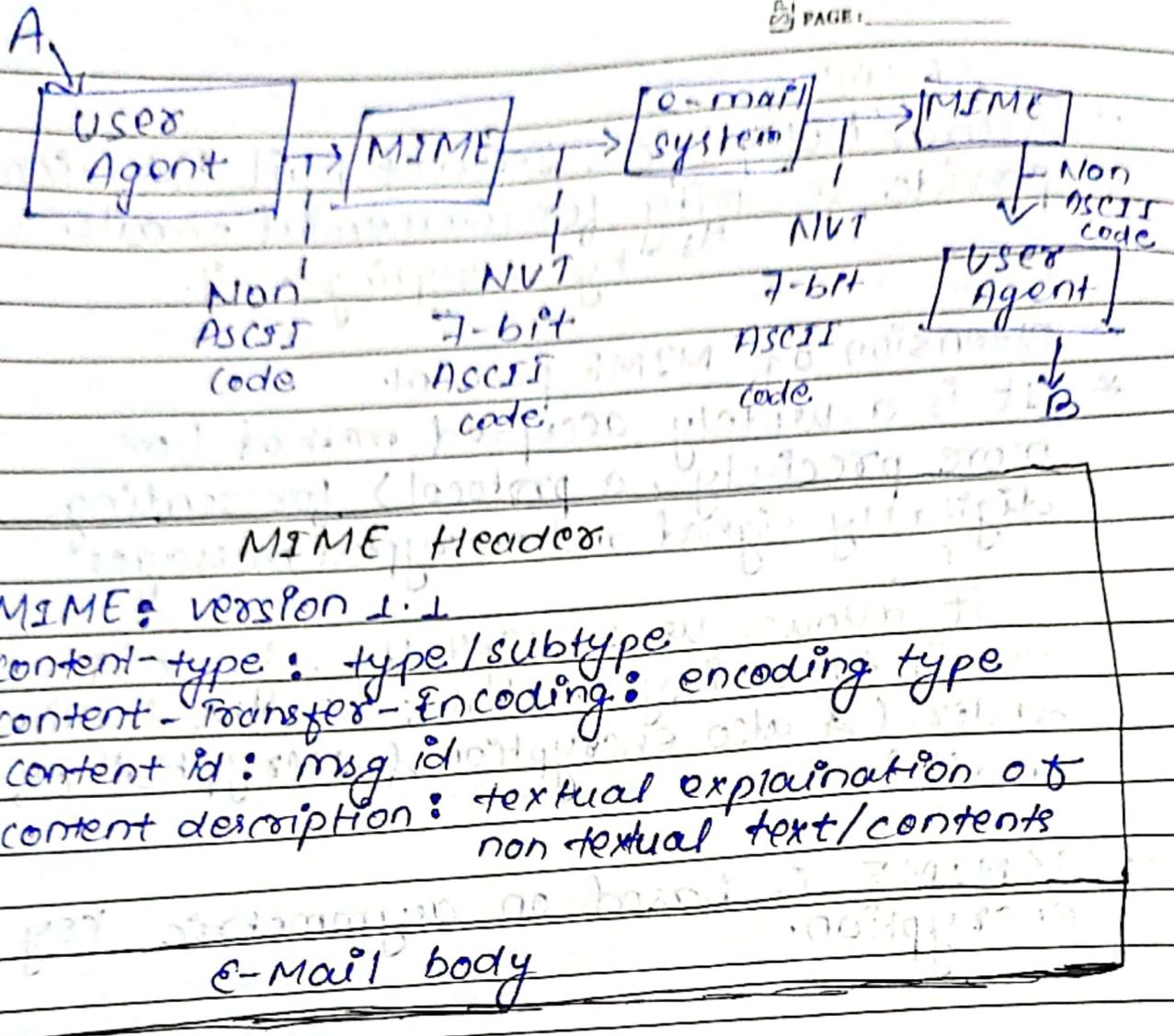
- I) SMTP has a very simple structure.
- II). can only send messages in NVT 7-bit ASCII format.
- III) cannot be used for languages that do not support 7-bit ASCII format such as French, German etc. So in order to make SMTP more broad, we use MIME.
- IV) cannot be used to send binary files or video or audio data.

MIME header

added to the original email header section to define transformation.

There are 5 headers which we add to the original header.

- 1) MIME Version - (currently 1.1)
- 2) Content Type - defines type of data used in msg like audio, video etc.
- 3) Content Transfer-Encoding - tells method used for encoding (eg 8 bit encoding)
- 4) Content Id - helps in uniquely identifying the message.
- 5) Content description - it defines whether the body is actually image, video or audio.



MIME v2 and additions

Content-Transfer-Encoding (I)
Content-Type (II)
Content-ID (III)
Content-Description (IV)
Content-Location (V)
Content-Transfer-Encoding (VI)

headers of basic bootstrapping in v2

headers for basic bootstrapping in v2

S/MIME

- * Secure / Multipurpose Internet Mail Extension.
- * provide security for commercial emails.

by encrypting mail.

- * extension of MIME protocol.

It is a widely accepted method (or more precisely, a protocol) for sending digitally signed and encrypted messages.

i.e.
it allows us to digitally sign our email to verify ourselves as the legitimate sender. (& also encryption & decryption of mails)

- * S/MIME is based on asymmetric key encryption.

Function provided by S/MIME

- Authentication
- Message integrity
- Non-repudiation of origin (using digital signature)
- Privacy
- Data security (using encryption)

In short

S/MIME is a protocol used to encrypt emails & digitally signed them.

1st version of S/MIME → 1995
2nd → 1998
3rd → 1999

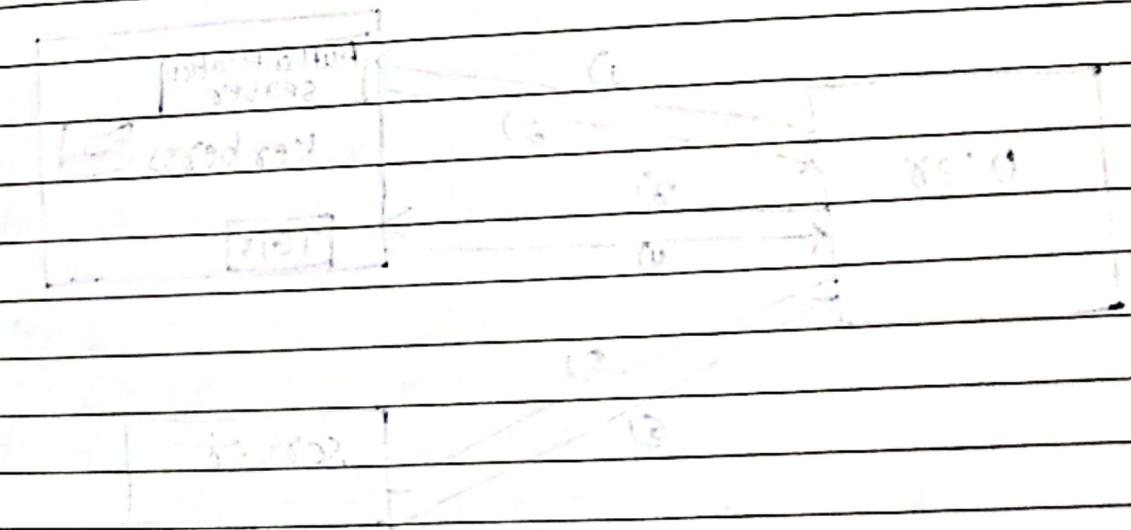
3rd version is supported in the following.

- Microsoft Outlook 2000
- Microsoft Exchange 5.5 & later.

* What does S/MIME do?

It provides

- i) Digital signature
(provides authentication + nonrepudiation)
- ii) msg encryption
(provides confidentiality + data integrity)



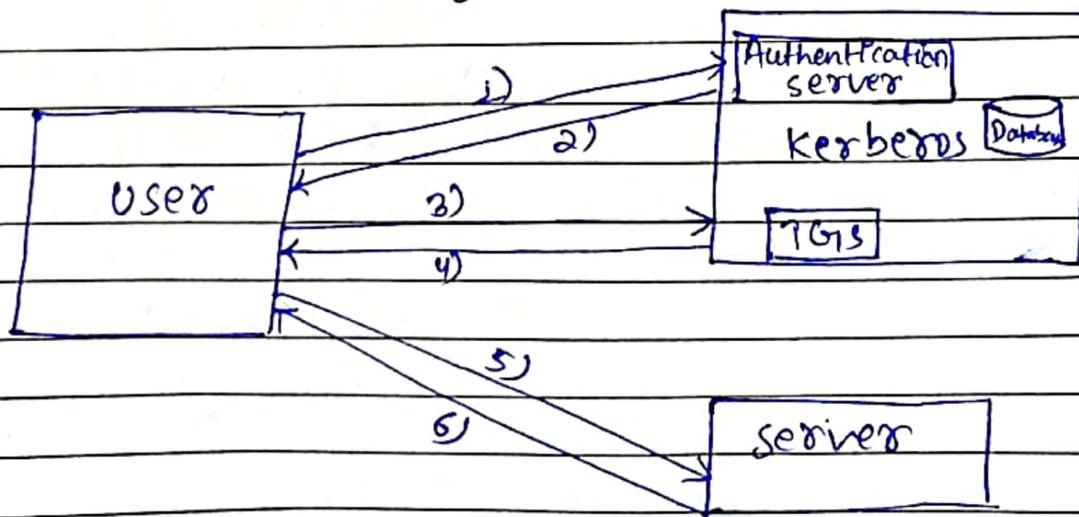
Authentication Applications

Kerberos provides a centralized authentication server whose function is to authenticate users to servers & servers to users.

- client server architecture.
- It runs as a 3rd party trusted server known as Key Distribution Center (KDC).
- Symmetric key.

Main components of Kerberos are:-

- Authentication Server (AS)
performs the initial authentication & ticket for ticket granting service.
- Database:
AS verifies the access rights of users in the database.
- Ticket Granting Server (TGS)
issue ticket for server.



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Step 1:-

User login and request services on the host.
Thus user requests for ticket-granting service.

Step 2:-

Authentication Server verifies user's access right using database and then gives ticket granting-ticket and session key. Results are encrypted using the password of the user.

Step 3:-

The decryption of the message is done using the password then send the ticket to TGS. The ticket contains authenticators like user name, network addresses.

Step 4:-

Ticket Granting Server decrypts the ticket sent by user and authenticator verifies the request then creates the ticket for requesting services from the server.

Step 5:-

The user sends the Ticket and Authenticator to the server.

Step 6:-

The server verifies the Ticket and authenticator then generate access to the service. After this user can access the services.

Kerberos Limitations

- does not work well in timeshare environment.
- Secured Kerberos Server
- Scalability.
- May result in cascading loss of trust.
- Assumes work stations are secure.

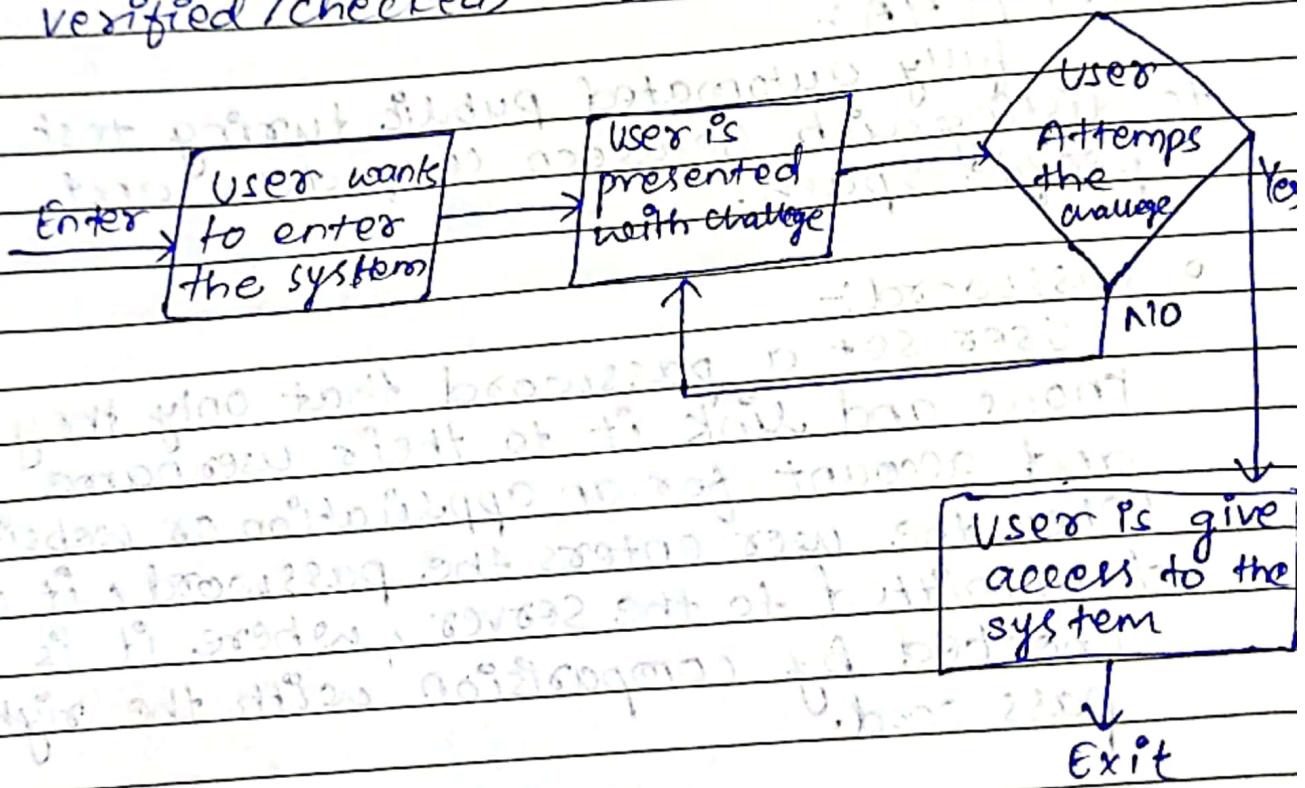
X.509

- digital signature certificate accepted internationally.
- does not generate any keys but provides a way to access public keys.
- There are several elements in X509 certificate. It has 3 versions

Version 1	Version 2	Version 3
version	version	version
Serial Number	serial number	serial number
Signature Algorithm Identifier	signature algorithm identifier	signature algorithm identifier
Issuer Name	issuer name	issuer name
Validity period	validity period	validity period
Subject Name	subject name	subject name
Public key Information	public key information	public key information
Issue unique ID	issue unique ID	issue unique ID
Subject unique ID	subject unique ID	subject unique ID
Extension	extension	extension

Challenge Response Authentication

- It is most popular method for authenticating operations.
- They are a collection of protocols in which one side issues a challenge (to be addressed) and the other side is required to respond with the right response (to be verified/checked) in order to be authenticated.



* challenge question comes in two flavours

- o Static question:

→ Security question that you have saved as a part of account set up

- o Dynamic question:-

The tasks are chosen at random with assumption that user is genuine one.

Methods of authentication:-

Broadly they are of 3 types. They are:-

knowledge based :- pin, password so on
property based :- key, smartcard so on
Biology based :- facial, iris, and so on

Other additional and

- CAPTCHA:-

fully automated public turing test
to distinguish between computers and
people spam.

- Password:-

User set a password that only they
know and link it to their user name
and account for an application or website.

When the user enters the password, it is
transmitted to the server, where it is
checked by comparison with the right
password.

- Biometrics

Every time a user wishes to verify himself
he must provide his unique biometric
information to authenticating system
for verification.

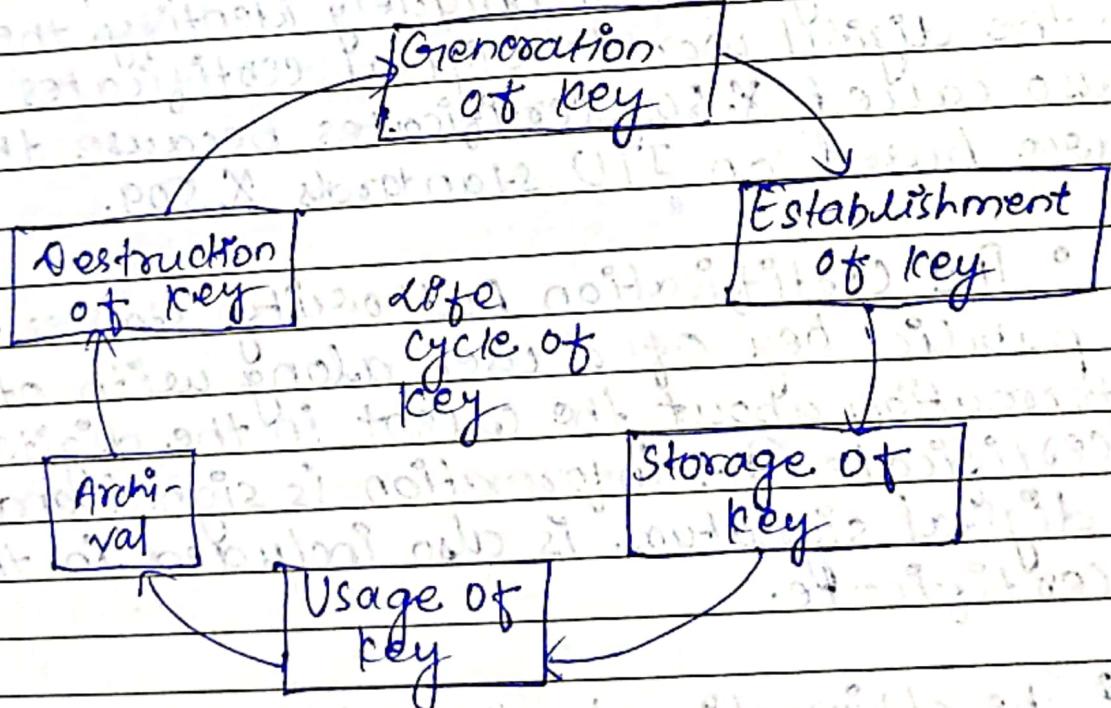
Public key Infrastructure

PKI is the governing body behind issuing digital certificate to protect confidential data and give unique identities to users and systems.

Managing key (key management)

Security of cryptosystem relies on its key. The 3 main areas of key management are as follows:

- A cryptographic key is a piece of data that must be managed by secure administration.



• public key management: further requires

- keeping the private key secret.
- assuring the public key.

components of public key Infrastructure

- Digital certificate
- Private key token
- Registration authority
- Certification Authority
- CMS or Certification management system
(explain)

Digital certificate

Digital certificates are issued to people and electronic systems to uniquely identify them in the digital world. Digital certificates are also called X.509 certificates because they are based on ITU standards X.509.

- The certification Authority stores the public key of a user along with other information about the client in the digital certificate. The information is signed and a digital signature is also included in the certificate.
- The affirmation for the public key then thus be retrieved by validating the signature using public key of certification authority.

private key token

while the public key of a client is stored on the certificate, the associated secret private key can be stored on the key owner's computer. If an attacker gains access to the computer, he can easily gain access to the private key. For this reason, a private key is stored on secure removable storage tokens access to which is protected through a password.

Digital Signature

Certifying Authority (CA)

- The CA issues certificate to client and assists other users to verify the certificate.
- They take responsibility for identifying correctly the identity of the client asking for a certificate to be issued and ensures that the information contained within the certificate is correct and digitally signs it.

function of CA:-

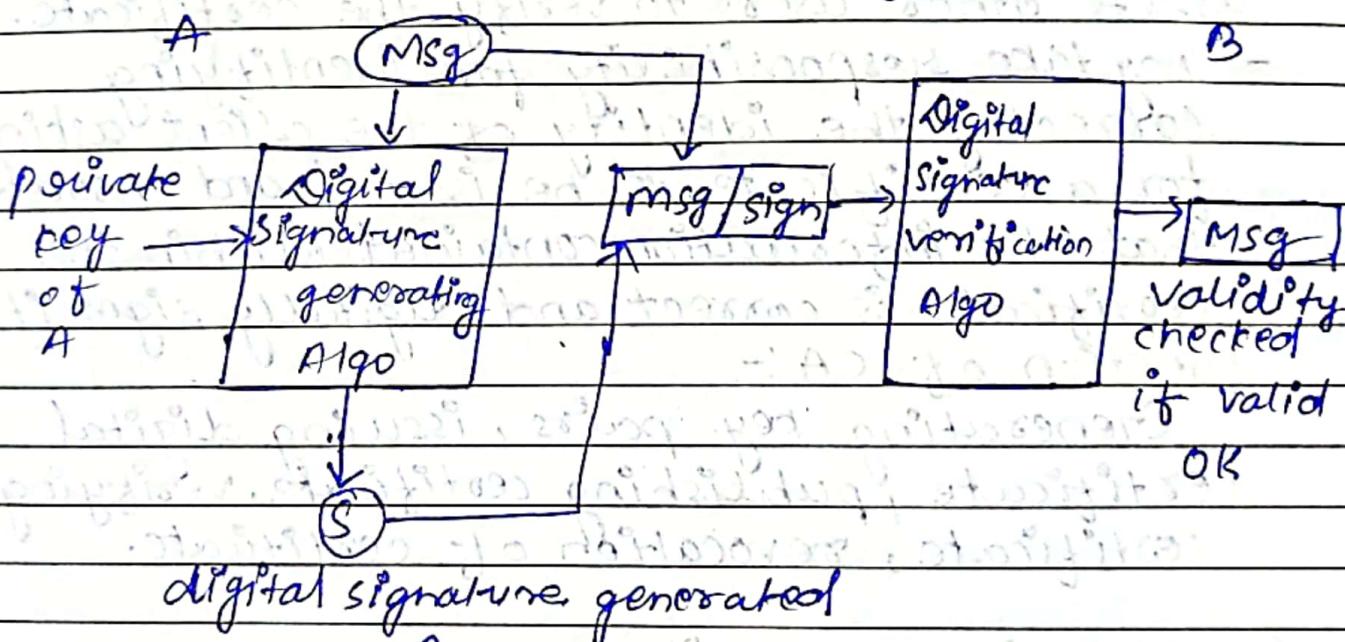
Generating key pairs, issuing digital certificate, publishing certificate, verifying certificate, revocation of certificate.

Registration Authority (RA)

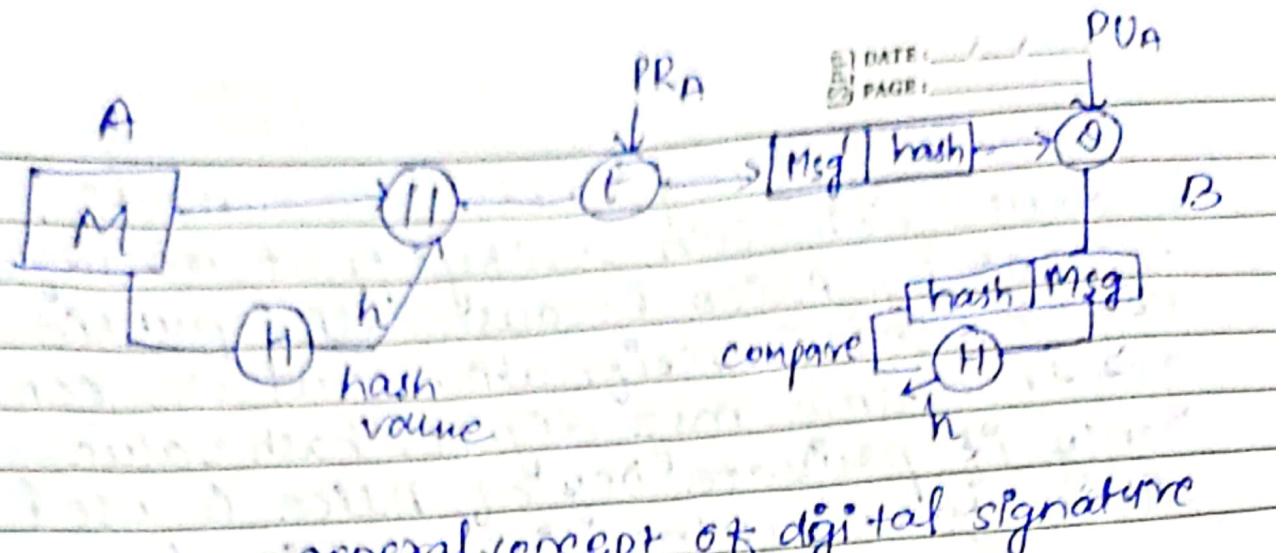
CA may use a third party registration authority to perform the necessary checks on the person or company requesting the certificate to confirm their identity. The RA may appear to the client as a CA, but they do not digitally sign the certificate that is issued.

Digital Signature

- It is a mathematical technique used to validate the authenticity & integrity of a message, software or digital document.
- digital equivalent of a hand written signature or stamped seal, but it offers far more inherent security.
- based on asymmetric key
- use for msg authentication & non-repudiation & msg integrity
- not used for confidentiality.



→ also provides message integrity because if message changed then at receiver side, we will not get exact message achieved using hashing concept using Good msg digest & hash value.



general concept of digital signature

Note → The signature uses some info unique to the sender to prevent both forgery and denial of service.

Sender sends two documents → msg & signature.

It must be easy to produce digital signature.

It must be easy to verify & recognize.

We need (i) key generation algo → to generate private key.

(ii) signing algo i/p → M and private key
o/p digital signature.

(iii) verifying algo → using public key and sign.

We are getting message authentication because bob can verify that message is sent by Alice because Alice public key is used in verification and we can get the same msg. digest/hash value only if private key of Alice is used. Therefore, authenticity achieved.

message Integrity

If the message is changed between anywhere then, receiver will not get the same hash value/msg digest so if hash value/msg digest not same then message changed.

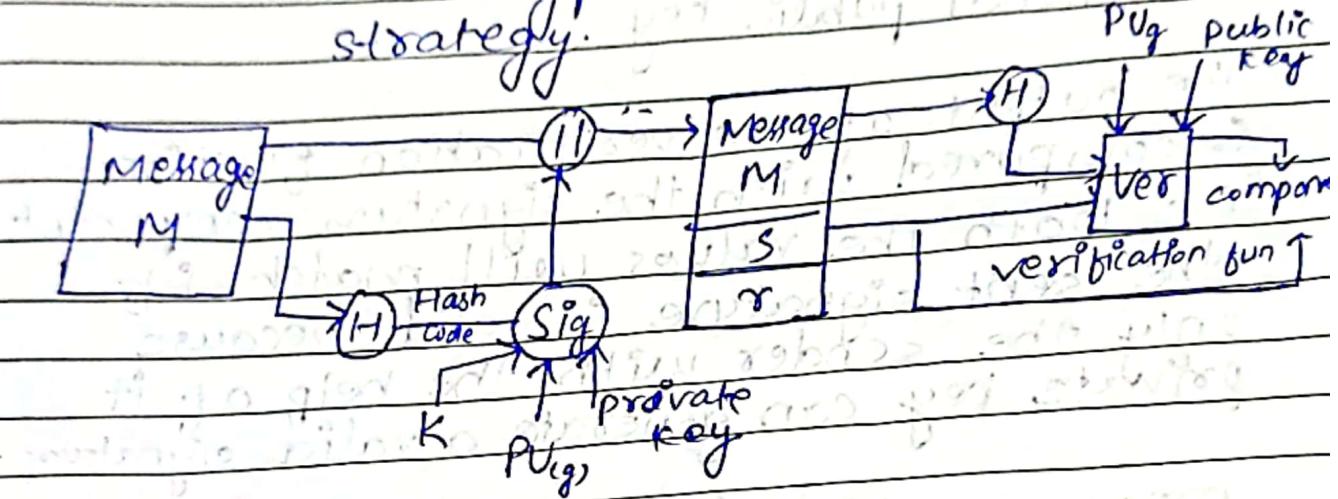
Hash function helps in preserving the integrity of message

Non-repudiation:-
achieved by using a trusted 3rd party.

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Digital Signature Standard (DSS)

It is a federal information processing standard (FIPS) which defines algorithms that are used to generate digital signature with the help of (SHA) for authentication of electronic documents. It provides digital signature algorithm no encryption or key exchange strategy.



Sender side

hash code is generated out of message and following inputs are given to the signature function.

- 1) The hash code
- 2) random number ' k ' generated for particular number
- 3) The private key of sender - $PR_{(as)}$
- 4) global public key i.e. $Pu_{(g)}$

These input to the function will provide us with the output signature containing two components - ' s ' and ' g '. Therefore, the original message concatenated with signature

Receiver side

At the receiver end, verification of the sender is done. There is a verification function which takes the following inputs

- 1) The hash code generated by the receiver
- 2) Signature components 's' & 'r'
- 3) Public key of sender.
- 4) Global public key.

The output of the verification function is compared with the signature component 'r'. Both the values will match if the sent signature is valid because only the sender with the help of its private key can generate a valid signature.

Proof of digital signature Algorithm

Downloaded doc for it: www.cs.vt.edu/~shankar/courses/cs5441/lectures/digital-signatures.pdf

Every file is different at step 1
A third certificate string at step 2
Last part of the file is changing each time
Good Write *can have specimen for so many examples of the same thing*

MD5

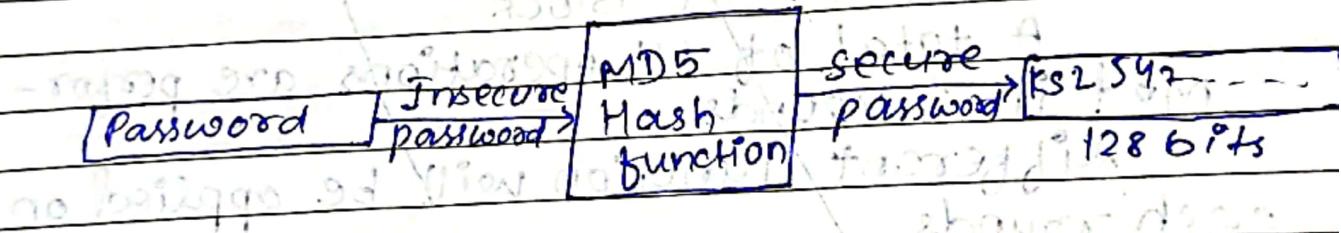
Message digest algorithm

- developed by Rivest
- Fast and produces 128 bit message digests

It's a hashing algorithm, is one-way cryptographic function that accepts a message of any length as input and returns as output a fixed-length digest value to be used for authenticating the original message.

Use of MD5

- used for file authentication
- used for security purpose in a web application.
- can store our password in 128 bits format



Working of the MD5 algorithm

1) Append Padding bits

(We add padding bits in the original message in such a way that:

$$\text{length (original message + padding bits)} = 512 \times i - 64$$

2) Append length Bits!

We add the length bit in output of first step.

Output of 1st step = $512 \times n - 64$

length bits = 64

After adding both we will get $512 \times n$ i.e. the exact multiple of 512.

3) Initialize MD buffers:-

Here we use 4 bit buffer i.e. J, K, L and M. The size of each buffer is 82 bits.

$$J = 0x67425301$$

$$K = 0xEDFCBAP45$$

$$L = 0x98CBADEF$$

$$M = 0x13DCE476$$

4) Process Each 512-bit Block

A total of 64 operations are performed in 4 rounds.

A different function will be applied on each rounds

$$f(K, L, M) = (K \text{ AND } L) \text{ OR } (\text{NOT } K \text{ AND } M)$$

$$g(K, L, M) = (K \text{ AND } L) \text{ OR } (\text{NOT } L \text{ AND } M)$$

$$h(K, L, M) = K \text{ XOR } L \text{ XOR } M$$

$$i(K, L, M) = L \text{ XOR } (K \text{ OR } \text{NOT } M)$$

In each bit position, f act as conditional

If K then Y else M. The function f can have been represented using + instead of v since

Good Work
Xpand

Difference between digital signature & certificate.
Difference between SHA & MD5

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KL and not K(M) will never have
1's in the similar bit position.

Step 5 Output

The message digest created an output including A, B, C, D. The output from the final round is the 128-bit hash result or message digest it can be acquired after it has been incrementally processed all 512-bit block of the message.

Secure Hash function

invented by national security agency.

In 1993, NSA introduced a new process which developed the 16-word message block input to the compression function to an 80-word block between other things.

Algo:-

Step 1: Append padding bits:

(Left side) The original message is padded and its duration is congruent to $448 \bmod 512$. Padding includes a single 1 followed by essential numbers of zeros.

Step 2: Append length

(Right side) 64-bit blocks is added to original length of message to make Good complete length equal to multiple of 512.

Step 3: Initialize buffer

buffer includes 5 registers of 32 bits each. They are initialized as,

$$A = 67\ 45\ 23\ 01$$

$$B = ef\ cd\ ab\ 89$$

$$C = 98\ ba\ dc\ 0fe$$

$$D = 10\ 32\ 54\ 76$$

$$E = 3\ d2\ e1\ f0$$

Same as MD5, but is SHA, these values are saved in big-endian format which defines that most essential byte of the word is located in the low-address byte position.

Step 4: Process message in 512-bit block

The compression function is divided into 20 sequential steps. It includes four rounds of processing, where each round is made up of 20 steps.

The four rounds are structurally same as one another with the only difference that each round need a different Boolean function which it can define as, t_1 , t_2 , t_3 , t_4 and one of the four multiple additive constants k_t ($0 \leq t \leq 9$) which is based on the step under consideration.

Output:-

After processing the final 512 bit message block t_0 (considering that the message is divided into t_0 512-bit block), and it can obtain 160-bit message.

Good Writelgic!!

Message Authentication and Hash function:

Authentication Requirement

- Revelation
- Analysis of traffic
- Deception
- Modification in the content
- Modification in the sequence
- Modification in the timings
- Source Refusal
- Destination refusal

Message Authentication function

Based on two functionality level

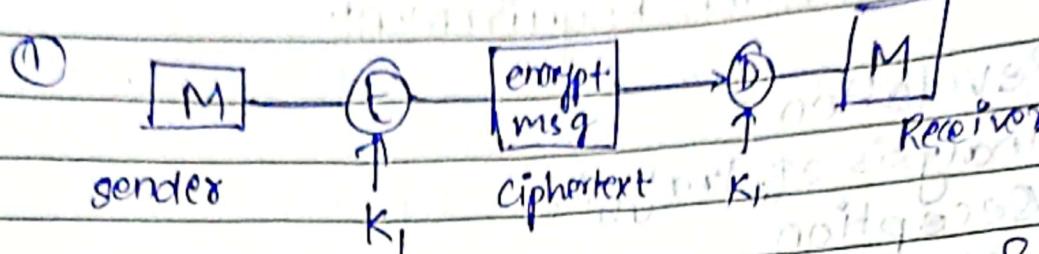
- lower level
 - there is a need for a function that produces an authenticator, which is the value that will further help in authentication of messages.
- higher level
 - lower level function is used in order to help receiver verify the authenticity of messages.

An authenticator must be there to authenticate the message.

Types of authentication function

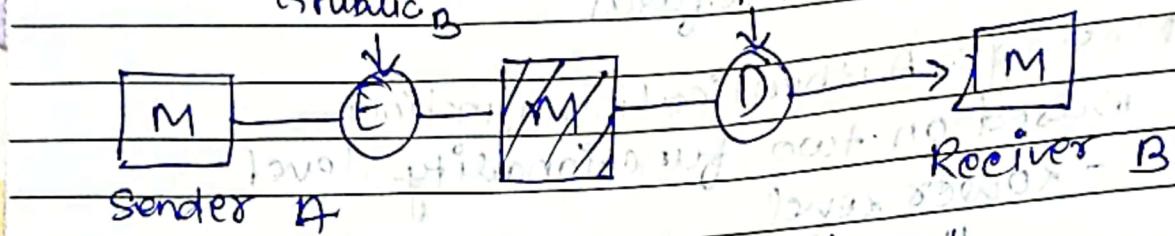
- I) Message encryption
- II) Message Authentication Code
- III) Hash function

(i) Message encryption:-
cipher-text act as authenticator



key K_1 is shared between sender & receiver.

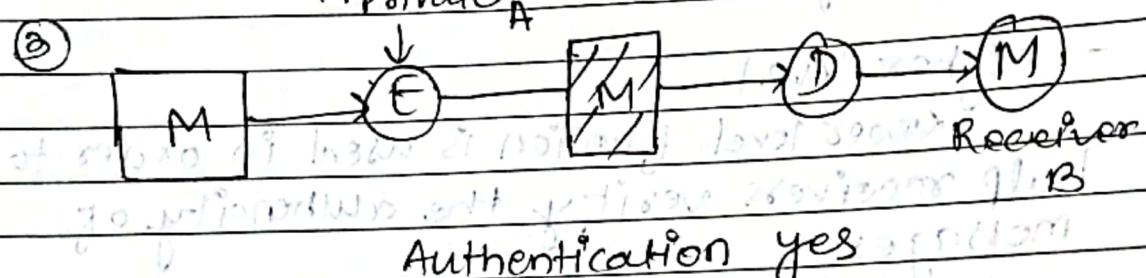
② for asymmetric encryption:



Asymmetric Authentication is not

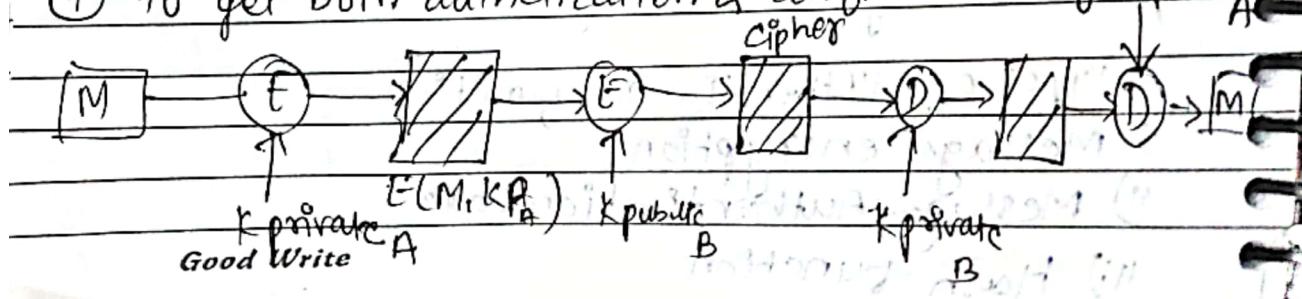
Confidentiality yes

Authenticaton & Confidentiality



Confidentiality No

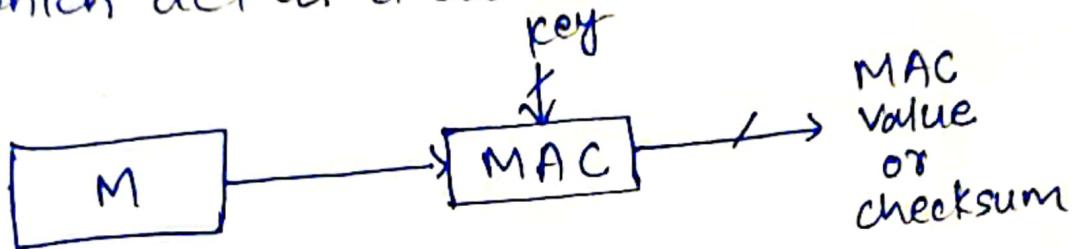
④ To get both authentication & confidentiality Kpublic



• Message authentication code
ciphertext + key = MAC

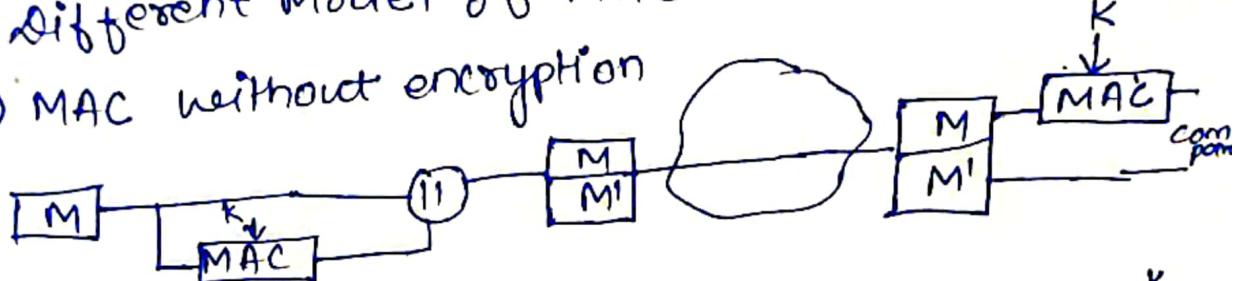
We will have some authentication function and we apply them on plain text along with the key which produces a fixed length code called MAC

$C(M, K)$ = fixed length code
which act as a authenticator here.

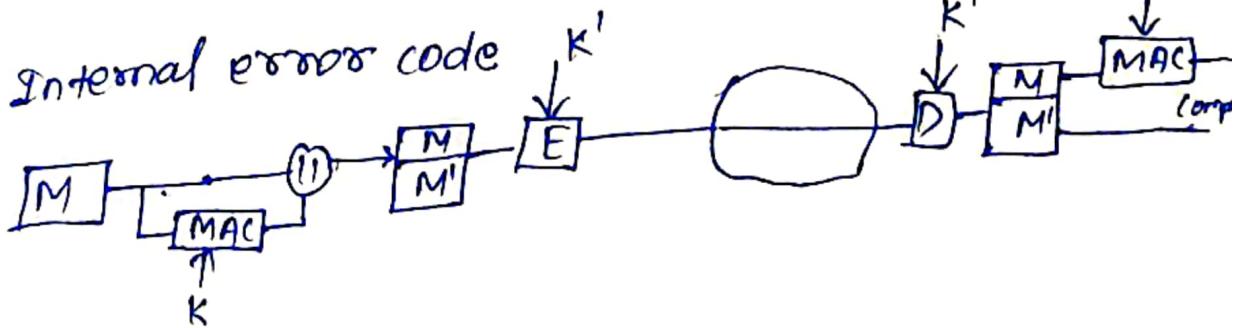


Different Model of MAC

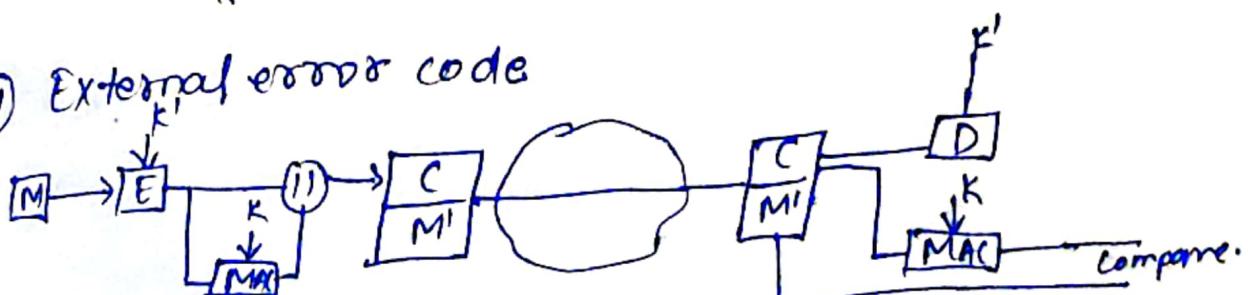
I) MAC without encryption



II) Internal error code



III) External error code



(iii) Hash function

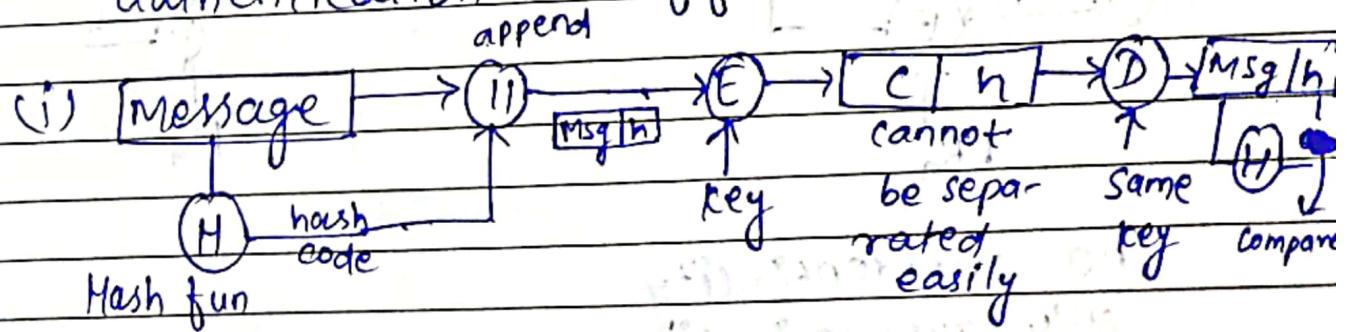
- similar to MAC (Message authentication code) but it does not use a key.
- takes in variable size message and produce a fixed output called Hash code / Hash value / message digest
- The only input is message
- A hash value 'h' is generated by function H as,

$$H(M) = \text{fixed length code, } h$$

 variable length message.

They are also called as compression function.

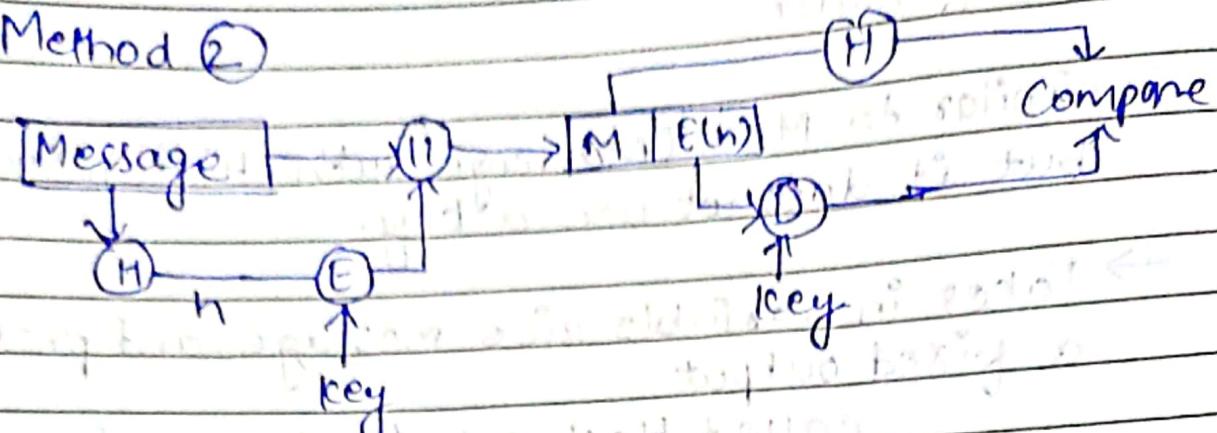
There are different methods to provide authentication in different situations.



authentication + confidentiality
 if both hash codes
 equal in the end
 because only A & B share
 the secret key

maintained because
 msg was encrypted
 before sending

Method ②

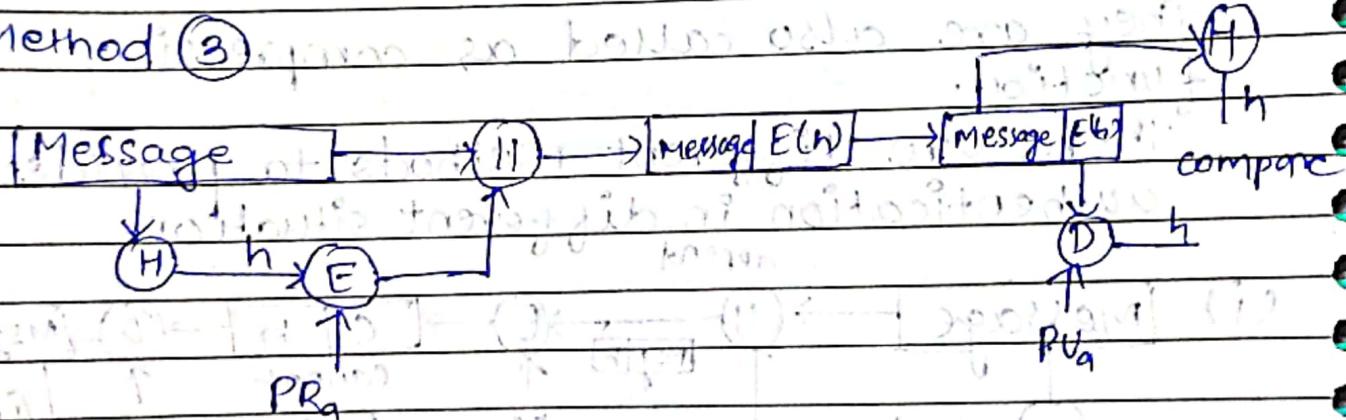


only authenticity
not confidentiality

because only hash code is encrypted not
the message as whole.

we can use this method if the message
is not private, because it will take
less processing time since we are not
encrypting message.

Method ③

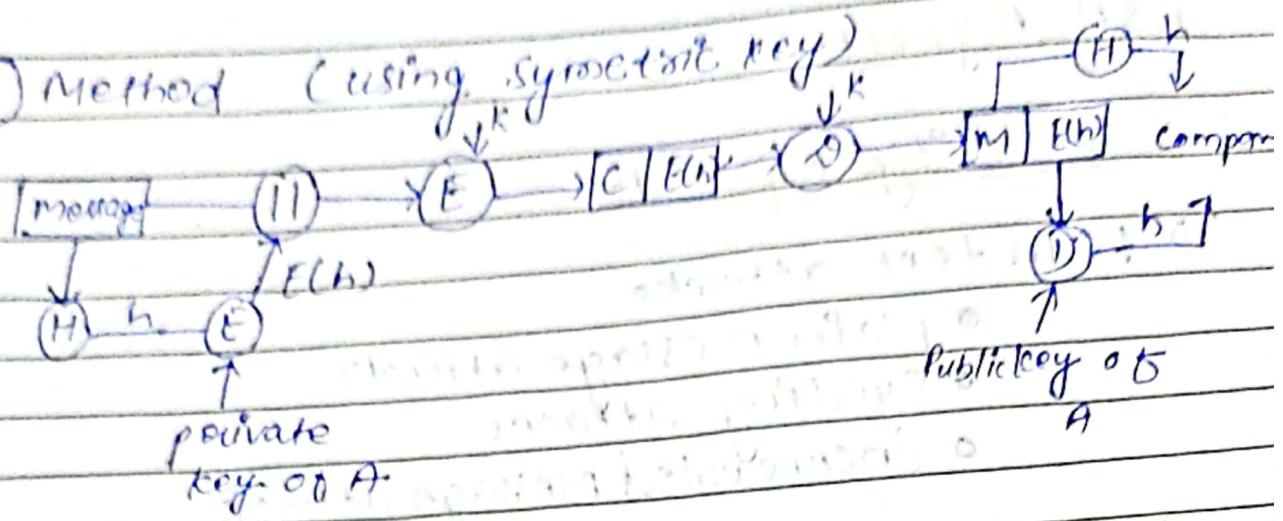


no confidentiality
only authentication

processing time will be less as the message
is not encrypted.

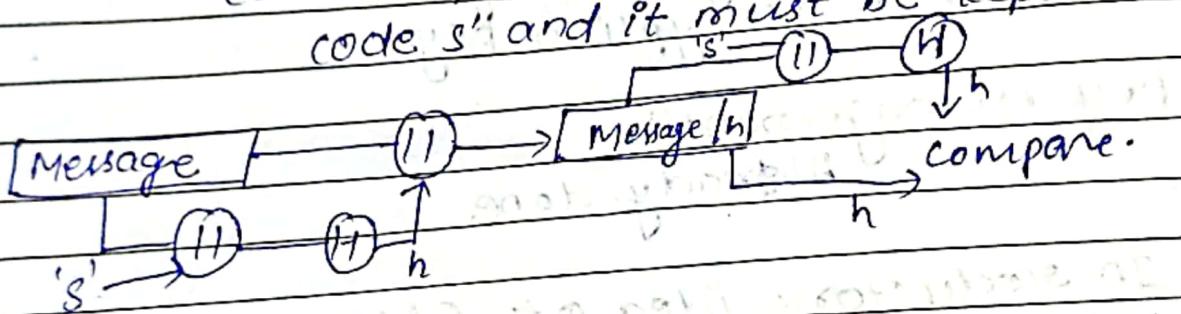
Good Write

(4) Method (using symmetric key)



Method-5

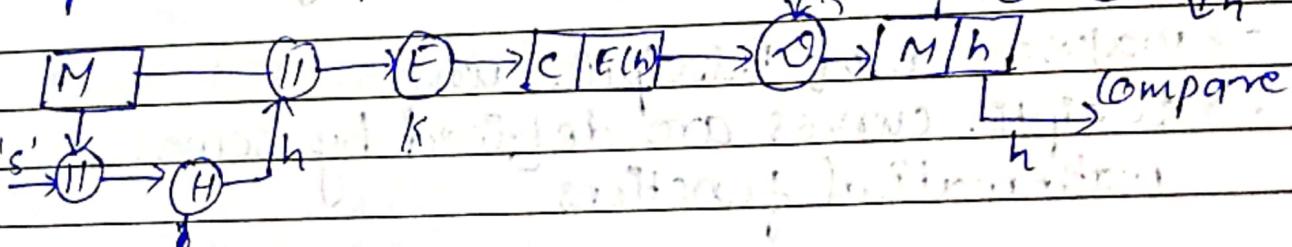
(sender & receiver will have a secret code 's' and it must be kept secret)



No ~~confidentiality~~ confidentiality (we get in method 6)
 only authentication.

Method-6

confidentiality can be added to the previous approach by encrypting the message



RSA Algorithm

Security of RSA

1) Plain text attacks

- plain message attacks

- cycling attacks

- Unconcealed Message attack

2) Chosen cipher attack

3) Factorization attack

4) Attack on Encryption key

5) Attack on decryption key

Key management:

Already done

Introductory idea of Elliptic curve cryptography:-

→ It is asymmetric / public key ecosystem.

→ It provides equal security with smaller key size (eg:- as compared to RSA)

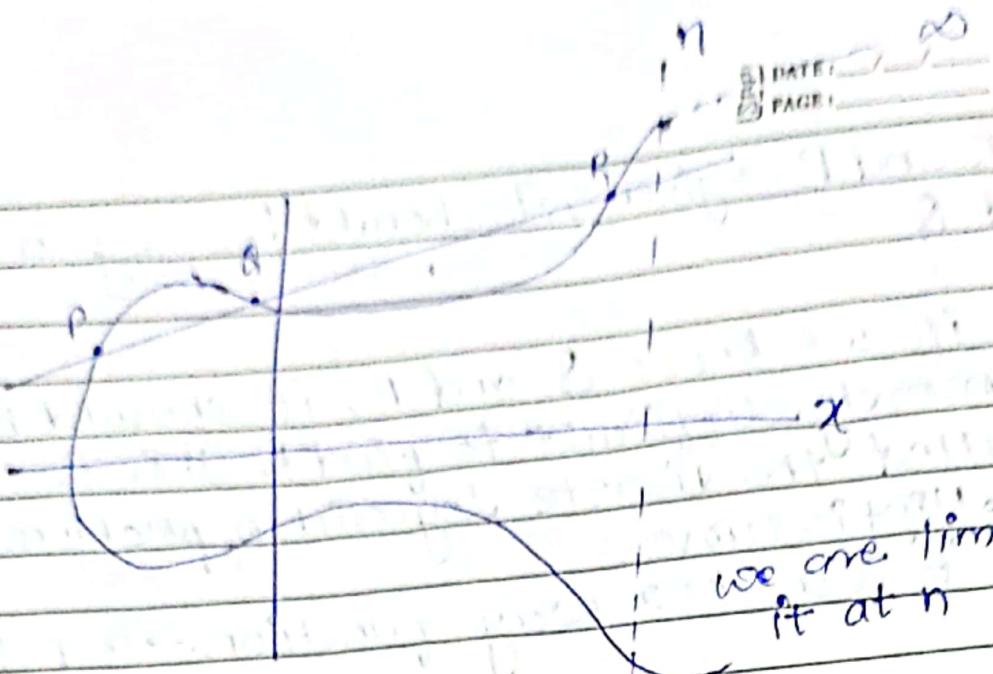
Small size + high security

→ makes use of Elliptic curve

→ Elliptic curves are defined by some mathematical functions

$$\text{Eg } y^2 = x^3 + ax + b$$

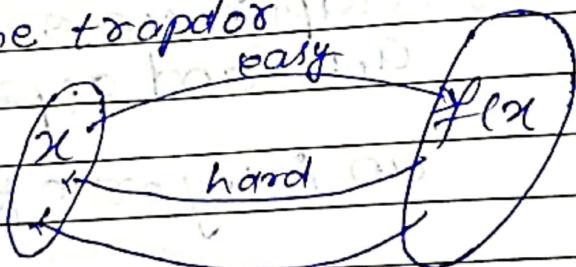
equation of degree 3



→ symmetric to x -axis

→ If we draw a line, it will touch a max of 3 points.

A Trapdoor function is a function that is easy to compute in one direction, yet difficult to compute in opposite direction (finding its inverse) without special info called the trapdoor



easy if given $f(x)$

"t" → trapdoor value

- Let $E_p(a, b)$ be the elliptic curve

- Consider the equation $Q = kP$

where $Q, P \rightarrow$ points on curve
and $k \leq n$

if K and $P \rightarrow$ given, it should be easy to find Q

- but if we know Q and P , it should be extremely difficult to find K . This is called the discrete logarithm problem for elliptic curve.
ie it is a one way function. \rightarrow Trap fun

$A \rightarrow B$ easy to compute

$B \rightarrow A$ very difficult.

Algo is somewhat same to Diffie-Hellman
~~but~~

ECC key exchange

Global public elements.

$E_q(a, b)$: elliptic curve with parameters a, b and q (prime no or

an integer of form 2^m)

G_1 : point on the curve whose order is larger value of n .

User A key generation

Select private key $n_{A1}, n_{A2} < n$

calculate Public key $P_A = n_{A1}G_1$

Good Write

User B key generation:

Select private key $n_B \in \mathbb{N}$

calculate public key $P_B = n_B \times G$

calculation of secret key by User A

$$K_A = n_A \times P_B$$

calculation of secret key by User B

$$K_B = n_B \times P_A$$

Here secret key has been exchanged.

ECC encryption

Let the message be M

- First encode this message M into a point on elliptic curve.

• Let this point be P_M

Now this point P_M is encrypted

for encryption, chose a random positive integer K

The cipher text will be

$$C_M = \{ K G_1, P_M + K P_B \}$$

for encryption
private key of
B used

This point is sent to the receiver.

Decryption

For decryption, multiply 1st point in the pair with receiver's secret key.

i.e $K_G * n_B$ || for decryption private key of B is used.

Then subtract it from 2nd point / coordinate in the pair

$$\text{i.e } P_m + K_P_B - (K_G * n_B)$$

but we know $P_B = n_B \times G_1$

so,

$$P_m + K_P_B - K_P_B$$

$\Rightarrow P_m$ (Original point)

So, receiver gets the same point.

Now, after decoding it. The receiver will get the message.

Elgamal encryption

- is a public key cryptosystem (asymmetric key concept is used)

→ This cryptosystem is based on the difficulty of finding discrete logarithm in a cyclic group that is even if we know g^a and g^k , it is extremely difficult to compute g^{ak} .

Idea of Elgamal encryption decryption.

suppose Alice wants to communicate with Bob

1. Bob generates public and private keys:

- Bob chooses a very large number q and a cyclic group \mathbb{F}_q .

- From the cyclic group \mathbb{F}_q , he chooses any element g and an element 'a' such that $\gcd(a, q) = 1$.

- Then he computes $h = g^a$

- Bob publishes \mathbb{F}_q , $h = g^a$, q and g as his public key and retains 'a' as a private key.

Elgamal Encryption

- is a public key cryptosystem (asymmetric key concept P is used)

→ This cryptosystem is based on the difficulty of finding discrete logarithm in a cyclic group that is even if we know g^a and g^k , it is extremely difficult to compute g^{ak} .

Idea of Elgamal encryption decryption.

Suppose Alice wants to communicate with Bob

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- From the cyclic group \mathbb{F}_q , he chooses any element g and an element 'a' such that $\gcd(a, q) = 1$.
- Then he computes $h = g^a$.
- Bob publishes f , $h = g^a$, q and g as his public key and retains a as a private key.

2. Alice encrypts data using Bob's public key

- Alice encrypts data

- Alice selects an elements k from cyclic group \mathbb{Z}_q^*

$$\gcd(k, q) = 1$$

- Then, compute

$$P = g^k \text{ and } s = h^k = g^{ak}$$

- Multiplies with

- Then she sends $(P, M*s)$

$$(g^k, M*s)$$

3. Bob decrypt the message

- Bob calculate $s' = p^a = g^{ak}$

- He divides $M*s$ by s' to

$$M \text{ obtained } M = s^{-1} * s' = s^{-1} * s = 1$$

B Unit

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Introduction to group, ring and field

Group:

A group is a set G_1 which is CLOSED under an operation * and satisfies the given four or following properties

- 1) A₁ - closure $a, b \in G_1$, then $(a * b) \in G_1$
- 2) A₂ - Associative $a * (b * c) = (a * b) * c$ for all $a, b, c \in G_1$
- 3) A₃ - Identity $(a * e) = (e * a) = e$ for all $a, e \in G_1$
- 4) Inverse element $(a * a') = (a' * a) = e$ for all $a, a' \in G_1$

The group is said to be Abelian group if it satisfies
A5 - commutative $(a * b) = (b * a)$ for all $a, b \in G$

Rings

A ring denoted by $\{R, +, *\}$ is a set of elements with two binary operations, called addition and multiplication such that for all $a, b, c \in R$ the following axioms are obeyed

* Group (A1-A4); Abelian group (A5)
Under addition.

(2) Associative of multiplication (X)

for every $a, b, c \in R$

$$a * (b * c) = (a * b) * c$$

(3) Distributive properties

$$a * (b + c) = ab + ac \text{ for all } a, b, c \in R.$$

$$(a + b)c = ac + bc "$$

(4) closure property.

for all $a, b \in R$

$a * b$ also belong to R .

Note

commutative Ring

A ring is said to be commutative if it

satisfies additional conditions

Commutativity of Multiplication

$$\text{i.e. } a * b = b * a \text{ for all } a, b \in R$$

field

A field is a set F which is closed under two operation $+$ and $*$ such that

1) F is an abelian group under $+$

2) $F - \{0\}$ (the set F without the additive

Good Write identity 0) is an abelian group under $*$.

★ Prime Numbers:

If N is a prime number then the divisors are 1 and N .

A prime number is a number greater than 1 with only two factors - itself and one.

why we use prime numbers in Cryptography

- Used by many encryption algo.
- Very fast multiplication
- Extremely computer-intensive to do reverse.
- factoring very large prime numbers is very hard i.e. take computers a long time.

Relative Prime Number

Two prime numbers are said to be relatively prime, if they have no prime factor in common and their only common factor is 1.

$$\text{if } \gcd(a, b) = 1$$

then a, b are co-prime

Ex: 13 & 17 are co-prime

13 & 17 are co-prime

Modular Arithmetic

① Mod

$$7 \bmod 4 = 3$$

$$② -x \bmod y = y - (x \bmod y)$$

$$\begin{aligned} -11 \bmod 7 &= 7 - (11 \bmod 7) \\ &= 7 - 4 \\ &= 3 \end{aligned}$$

if $x \bmod y = 0$, then this formula fails.

* Congruent Modulo

Two integers a and b are said to be congruent modulo n if

$$(a \bmod n) \equiv (b \bmod n)$$

e.g.: $73 \equiv (4 \bmod 23)$ means.

$$73 \bmod 23 = 4 \bmod 23$$

properties of congruency

(i) $a \equiv b \pmod{n}$ if $n \mid (a-b)$

(ii) $a \equiv b \pmod{n}$ implies $b \equiv a \pmod{n}$

(iii) if $a \equiv b \pmod{n}$ & $b \equiv c \pmod{n}$

then $a \equiv c \pmod{n}$

Modular arithmetic operations / properties

$$① (a+b) \text{ mod } n = [(a \text{ mod } n) + (b \text{ mod } n)] \text{ mod } n$$

$$② (a-b) \text{ mod } n = [(a \text{ mod } n) - (b \text{ mod } n)] \text{ mod } n$$

$$③ (a \times b) \text{ mod } n = [a(\text{mod } n) * b(\text{mod } n)] \text{ mod } n$$

e.g.: let $a=11$, $b=15$, $n=8$

$$(11 \times 15) \text{ mod } 8 = (3 \times 7) \text{ mod } 8 \\ 5 = 5$$

Note: Exponentiation is performed by repeated multiplication, as in ordinary arithmetic.

Given

$$11^7 \text{ mod } 13$$

To find it we will proceed as

$$11^2 \equiv 121 \equiv 4 \pmod{13}$$

$$11^4 = (11^2)^2 \equiv 4^2 \pmod{13} \equiv 16 \pmod{13} \\ \equiv 3$$

$$11^7 = (11 \times 4 \times 3) \pmod{13} \\ = 132 \pmod{13} \\ \equiv 2$$

④ if $x \equiv y \pmod{n}$ and $a \equiv b \pmod{n}$

$$(x+a) \equiv (y+b) \pmod{n}$$

$$17 \equiv 4 \pmod{13}, \quad 42 \equiv 3 \pmod{13}$$

$61 + 59 \equiv 7 \pmod{13}$, which is true.

⑤ if $x \equiv y \pmod{n}$ and $a \equiv b \pmod{n}$ then

$$(x-a) \equiv (y-b) \pmod{n}$$

the answer will be 49 + 37 = 86

Fermat's and Euler's theorem

Euler's theorem ($\phi(n)$)

Euler's totient $\phi(n)$ is defined as the no. of the integers less than n that are co-prime to n .

Now

when $n \rightarrow \text{prime}$

$$\phi(n) = n - 1$$

Also,

$$\phi(a+b) = \phi(a) * \phi(b) // a \text{ and } b \\ \text{should be co-prime}$$

$$\text{eg } \phi(35) = \phi(7) * \phi(5)$$

$$= 6 * 4 = 24$$

Euler's theorem is also called as Fermat-Euler's theorem or Euler's theorem

Euler's theorem state that if x and n are co-prime positive integers, then

$$x^{\phi(n)} \equiv 1 \pmod{n} / x \pmod{n} = 1 \pmod{n}$$

where $\phi(n) \rightarrow$ Euler's totient function

* This is a generalized version of Fermat's theorem.

Let $x = 11$, $n = 10$; both are co-prime

we can represent x as

$$\phi(10)$$

$$11 \equiv 1 \pmod{10}$$

$$11^4 \equiv 1 \pmod{10}$$

$$\phi(20) = \phi(5) \times \phi(2)$$

$$= 4 \times 1$$

$$= 4$$

$$14641 \equiv 1 \pmod{10} \text{ which is true}$$

$$14640 \equiv 1 \pmod{10}$$

Note:

$$x^{\phi(n)} \equiv 1 \pmod{n}$$

$a = \text{any multiple of } \phi(n)$ it will

give the same result.

Fermat's theorem

→ special case of Euler's theorem.

If n is prime and n is a positive integer, not divisible.

$$x^{n-1} \equiv 1 \pmod{n}$$

$n \rightarrow$ prime number

$x \rightarrow$ is not divisible by n

$$\text{eg } x = 3, n = 5$$

$$3^{n-1} \equiv 1 \pmod{n}$$

$$3^{5-1} \equiv 1 \pmod{5}$$

$$3^4 \equiv 1 \pmod{5}$$

$$81 \equiv 1 \pmod{5}$$

Another form of Fermat's theorem.

$$x^n \equiv x \pmod{n}$$

$$x = 3, n = 5$$

$$3^5 \equiv 3 \pmod{5}$$

$$243 \equiv 3$$

$$243 \pmod{5} \equiv 3 \pmod{5}$$

$$2 \equiv 3$$

proved.

Euclidean / Euclidian Algorithm

used to find gcd of two positive integers (basically large numbers)

$$\gcd(a, b) \leftarrow \gcd(b, a \bmod b)$$

$$\gcd(a, 0) = a$$

$$\gcd(a, b)$$

$$a + b = 1025$$

$$b = 35$$

$$\gcd(1025, 35)$$

$$= \gcd(35, 1025 \bmod 35)$$

$$= \gcd(35, 10)$$

$$= \gcd(10, 35 \bmod 10)$$

$$= \gcd(10, 5)$$

$$= \gcd(5, 10 \bmod 5)$$

$$= \gcd(5, 0)$$

$$= 5$$

example 2:

$$\gcd(11, 7) \equiv \gcd(a, b)$$

$$\equiv \gcd(7, 11 \bmod 7)$$

$$\equiv \gcd(7, 4)$$

$$\equiv \gcd(4, 7 \bmod 4)$$

$$\equiv \gcd(4, 3)$$

$$\equiv \gcd(3, 4 \bmod 3)$$

$$\equiv \gcd(3, 1)$$

$$\equiv \gcd(1, 3 \bmod 1)$$

$$= \gcd(1, 0)$$

Therefore they are co-prime, mutually relative or relative prime.

Good Write

Chinese Remainder Theorem

Chinese Remainder theorem states that there always exist an 'X' that satisfies the given congruence.

$$x \equiv \text{rem}[0] \pmod{\text{num}[0]}$$

$$x \equiv \text{rem}[1] \pmod{\text{num}[1]}$$

- - and $(\text{num}[0], \text{num}[1], \dots, \text{num}[m-1])$
 i.e. must be co-prime to one another

Algorithm

$$\text{if } x \equiv a_1 \pmod{m_1}$$

$$x \equiv a_2 \pmod{m_2}$$

$$(1) \quad x \equiv a_3 \pmod{m_3}$$

$$(i) \quad \gcd(m, m_2) = \gcd(m_2, m_3) = \gcd(m, m_3) \\ \geq 1$$

(m, m_2, m_3) all should be co-prime.

$$(ii) \quad x = (M_1 x_1 a_1 + M_2 x_2 a_2 + M_3 x_3 a_3 + \dots + M_n x_n a_n) \pmod{M}$$

$$M = m_1 * m_2 * m_3 * \dots * m_n$$

$$M_i = M/m_i \text{ e.g. } M_1 = M/m_1$$

$$\frac{m_1 m_2 m_3}{m_1} = m_1 m_2 m_3$$

$$m_1 + m_2 + m_3 = m_1 m_2 m_3$$

$$M_1 = m_2 m_3$$

$$M_2 = m_1 m_3$$

$$M_3 = m_1 m_2$$

To calculate x_i

$$M_i x_i \equiv 1 \pmod{m_i}$$

↳ multiplicative inverse of M_i

$$M_i x_i \equiv 1 \pmod{m_i}$$

example

$$x \equiv 1 \pmod{5}$$

$$x \equiv 1 \pmod{7}$$

$$x \equiv 3 \pmod{11}$$

we can find the value of x as,

$$x = (M_1 x_1 a_1 + M_2 x_2 a_2 + M_3 x_3 a_3) \pmod{M}$$

Here, from question,

$$a_1 = 1$$

$$m_1 = 5$$

$$a_2 = 1$$

$$m_2 = 7$$

$$a_3 = 3$$

$$m_3 = 11$$

co-primes

Using Chinese remainder theorem

$$M_1 = m_2 \cdot m_3$$

$$= 7 \times 11 = 77$$

$$M_2 = m_1 \times m_3$$

$$= 7 \times 5 = 35$$

$$M_3 = m_1 \times m_2$$

$$= 7 \times 5 = 35$$

$$M = m_1 \times m_2 \times m_3 = 7 \times 11 \times 5 = 385$$

Now, we will calculate x_i value.

for x_1

$$M_1 x_1 \equiv 1 \pmod{m_1}$$

$$77 x_1 \equiv 1 \pmod{5}$$

$$\text{or } M_1 x_1 \pmod{m_1} \equiv 1 \pmod{5}$$

$$\therefore 77 x_1 \pmod{5} \equiv 1 \pmod{5}$$

$$77 x_1 \pmod{5} \equiv 1 \pmod{5}$$

putting $x_1 = 3$

$$6 \pmod{5} = 1$$

$$\therefore x_1 = 3$$

Similarly,

$$M_2 X_2 \pmod{m_2} = 1$$

$$55 X_2 \pmod{7} = 1$$

$$6 X_2 \pmod{7} = 1$$

when we put $X_2 = 6$

then,

$$6 \times 6 \pmod{7} = 1 \text{ true}$$

$$\therefore X_2 = 6$$

Also,

$$M_3 X_3 \pmod{m_3} = 1$$

~~$$35 X_3 \pmod{11} = 1$$~~

$$2 X_3 \pmod{11} = 1$$

$$X_3 = 6$$

$$\therefore 12 \pmod{11} = 1$$

Now,

$$x = (77 \times 8 \times 1 + 55 \times 6 \times 1 + 35 \times 6 \times 9) \pmod{385}$$

$$= 1191 \pmod{385}$$

$$\approx 36$$

discrete logarithms

$5^x \bmod 17$ = equally distributed.

If x is given then $5^x \bmod 17$ is easy to calculate but if

$5^x \bmod 17 = 12$ (is given) and we are asked to compute x , then its tough to do so.

Its easy on one way but difficult in reverse way.

if we are going to compute

$$g^x \bmod p$$

$$2^x \bmod 7 = 4, x = 2, 5, \text{ etc.} \times P$$

here g is the primitive root of prime number p . and x can be any number

for smaller value of p it may be easy to find x

* If p is very large then find x will be hard.

* time & effort will be more to find it.

* Strength of one way & how much time it takes to break it.

Numerical

Solve $\log_2 9 \pmod{11}$

Here, $p=11$, $g=2$, $x=9$

$$\log_g x \equiv n \pmod{p}$$

$$x \equiv g^n \pmod{p}$$

$$9 \equiv 2^n \pmod{11}$$

Try $n=1, 2, 3, 4, 5, 6$

when $n=6$

then,

$$9 \equiv 2^6 \pmod{11} \text{ true.}$$

$$2^6 \pmod{7} = 4$$

$x=2, 4$ then solved.

* Principles of public key cryptosystem

The approach of public key cryptosystem derivative from an attempt to attack two of the most complex problem related to symmetric encryption:

- i) key distribution

The two basic principles of any crypto-system

- I) confidentiality;
- II) Authenticity.

problem associated with confidentiality
problems associated with authentication.