

Sampling and Coverage

GOV 1010

Pre-Election Polls

A Sample of Problems



1936 Presidential Election

Franklin Delano Roosevelt (D) is
first-term incumbent

Elected in 1932 with 57.4% of
vote

Alf Landon (R) , Kansas
Governor, is challenger

“People’s Budget” vs Balanced Budget



Pre Election
Polls in
1936

Literary Digest and Gallup

- Literary Digest
 - Weekly Newsmagazine
 - Founded in 1890
 - Polls since 1916
 - 136 million mailings 1916 – 1932
 - Predicted Roosevelt victory within 1% in 1932
 - “Uncanny accuracy”
- Methodology
 - Mail surveys
 - Large sample sizes
 - **Mailed 10 million surveys in 1936**
 - Auto owners / telephone directories
- George Gallup Ph.D.
 - Advertising Measurement specialist
 - “American Institute of Public Opinion”
 - New nationally syndicated newspaper column
 - Money-back guarantee (more accurate)
- Methodology
 - Face-to-face surveys with quota sampling
 - Also some mail polls



**SECRET BALLOT—No Signature—No Condition—
No Obligation—Just Mark Your Choice—Mail at Once**

CANDIDATES FOR PRESIDENT OFFICIALLY NOMINATED
(Names Arranged Alphabetically)

Put a Cross ☒ in Square Before the
Name of Presidential Candidate You Prefer

<input type="checkbox"/> John W. Aldrich (Republican)	<input type="checkbox"/> Charles McNary (Unionist)
<input type="checkbox"/> Earl Browder (Communist)	<input type="checkbox"/> Franklin D. Roosevelt (Democratic)
<input type="checkbox"/> Hiram Colvin (Prohibitionist)	<input type="checkbox"/> Norman Thomas (Socialist)
<input type="checkbox"/> Alfred M. Landon (Republican)	<input type="checkbox"/> _____

Mark How You Voted For President in 1932

☐ Did Not Vote

☐ Under Legal Age

☐ Other Reasons

This is important and will reveal the significant drift from one party to another.

To assist in tabulation please write name of your State here: _____

For Recording
The **Literary Digest**

Popular Vote			Electoral Vote		
Dem.	Rep.	Other	Dem.	Rep.	Other
7,645	16,056	967			

Popular Vote			Electoral Vote		
Dem.	Rep.	Other	Dem.	Rep.	Other
33423	4190	5387	34	165	0

Popular Vote			Electoral Vote		
Dem.	Rep.	Other	Dem.	Rep.	Other
298	153	360	62	166	0

1932 RESULTS		Electoral Votes	STATES	FINAL 1936 POLL—L.D.			ACTUAL VOTES 1936 ELECTION		
ROOSEVELT	HOOVER			Dem.	Rep.	Other	Dem.	Rep.	Other
207,910	34,675	11	Alabama						
79,264	36,104	3	Arizona						
189,602	28,467	9	Arkansas						
1,324,157	847,902	22	California						
250,877	189,617	6	Colorado						
281,632	288,420	8	Connecticut						
54,319	57,073	3	Delaware						
206,307	69,170	7	Florida						
234,118	19,863	12	Georgia						
109,479	71,312	4	Idaho						
1,882,304	1,432,756	29	Illinois						
862,054	677,184	14	Indiana						
598,019	414,433	11	Iowa						
424,204	349,498	9	Kansas						
580,574	394,716	11	Kentucky						
249,418	18,853	10	Louisiana						

Literary Digest versus Gallup Forecasts

	Literary Digest	Gallup	Election
Roosevelt	43%	56%	62%
Landon	57%	43%	37%
Roosevelt Electoral Votes	161	315+	523
Sample Size	2,376,523	40,000 MAX	

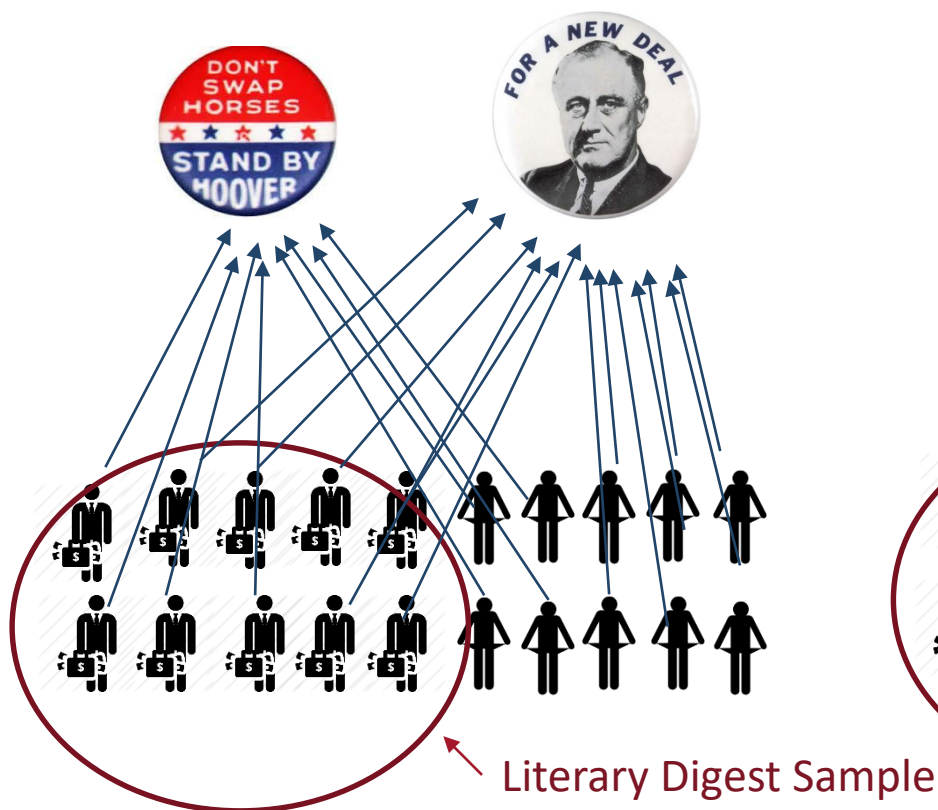


Discussion

Differences Between 1932 and 1936

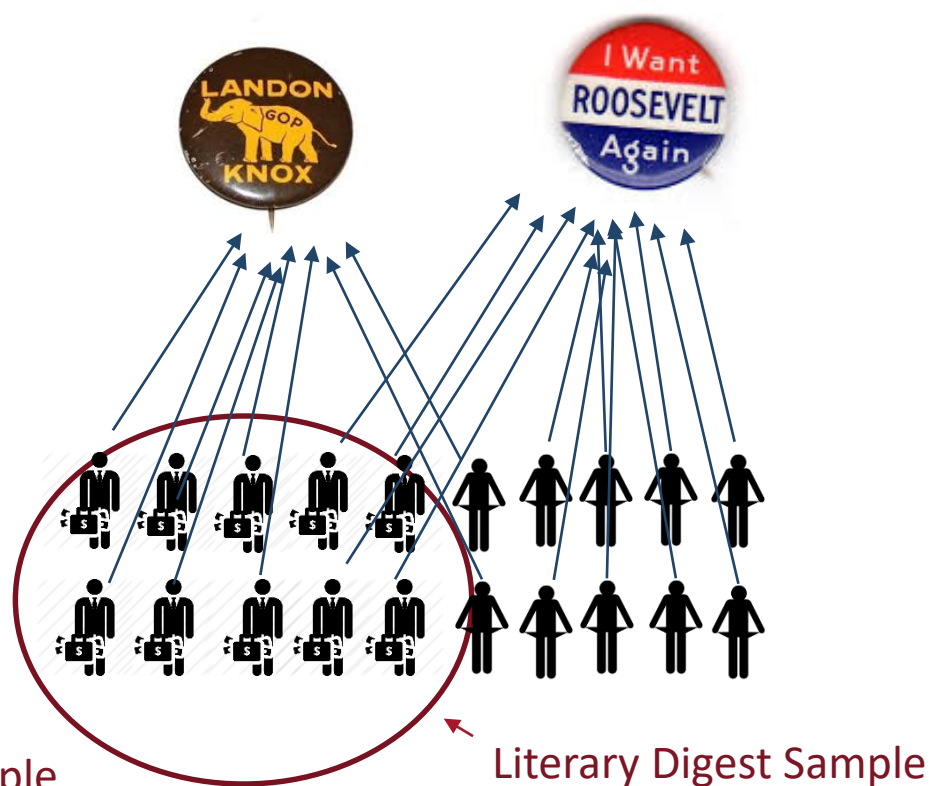
1932

Few Differences on Vote by Income

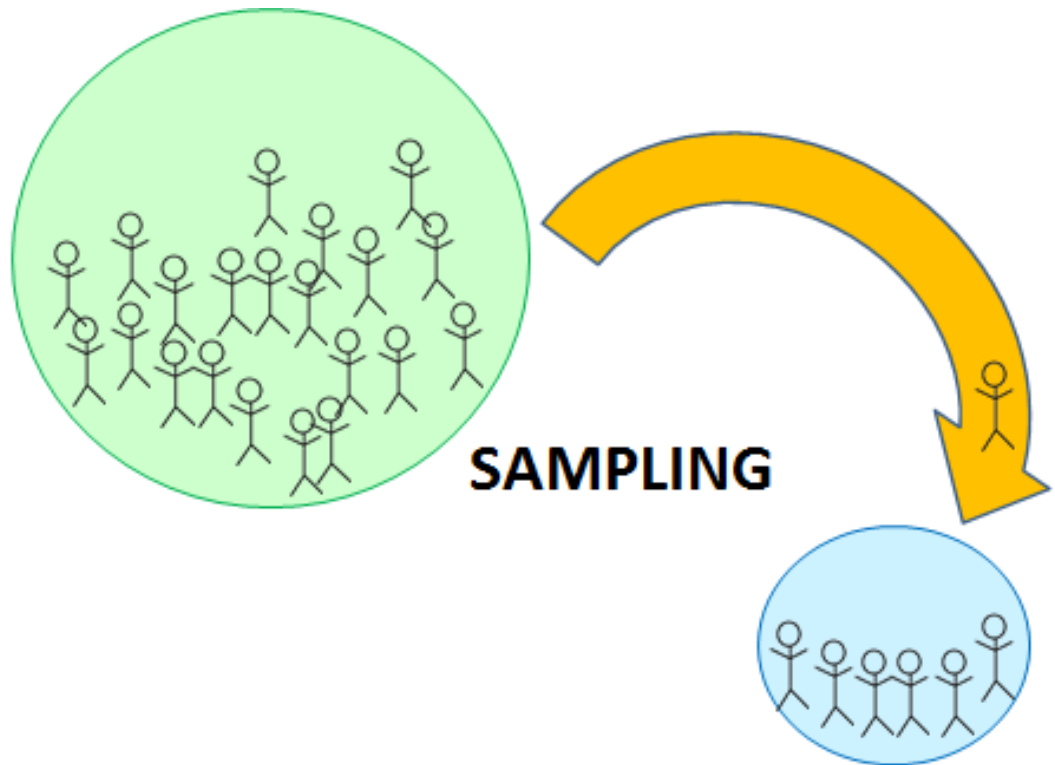


1936

Large Differences on Vote by Income



Inference in Scientific Samples



Populations in Surveys

Population of Inference

- The general set of persons to whom one wishes to generalize results.
- This population may be infinite

Target Population

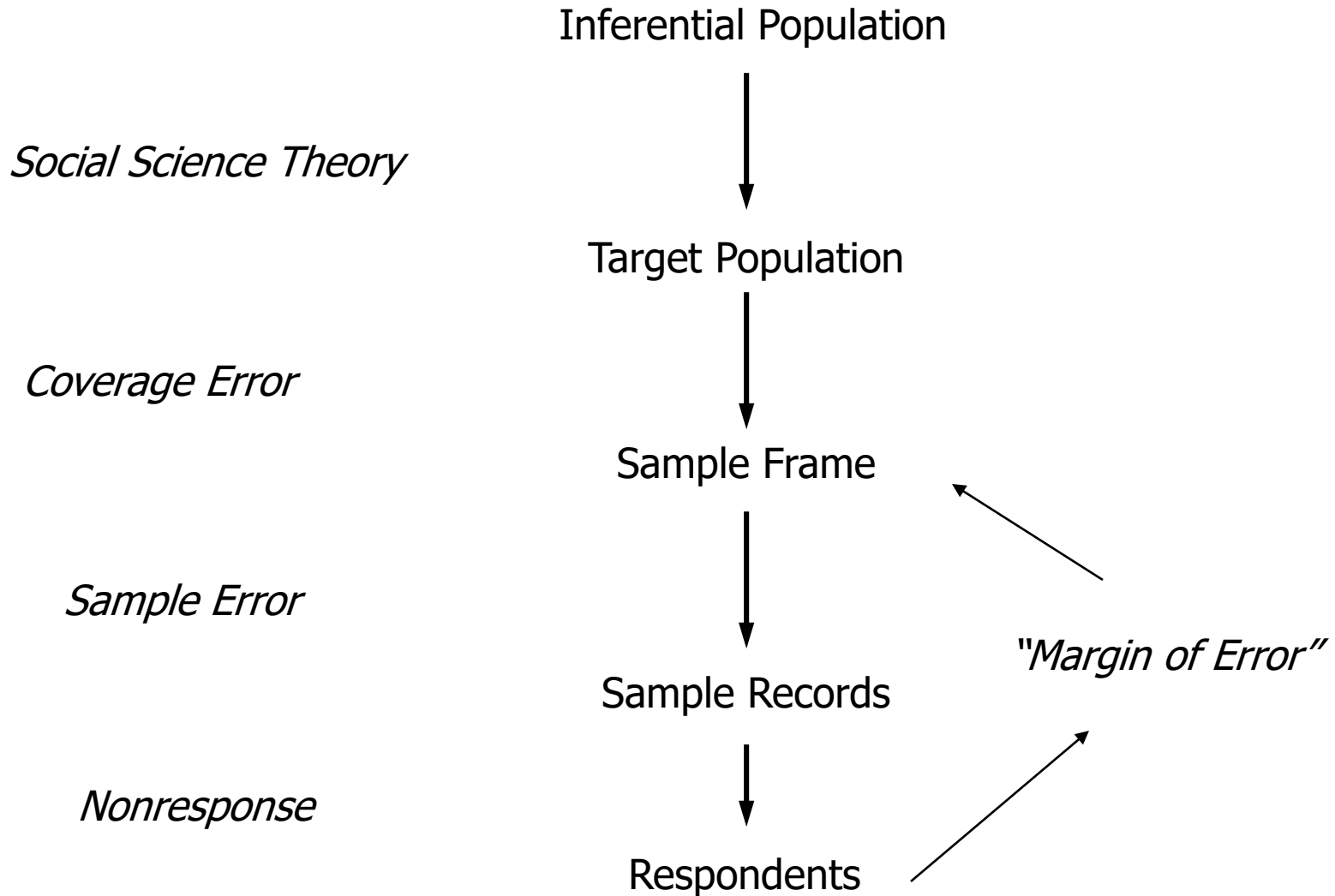
- The inferential population as operationalized by the researcher.
- Bounded by time
- Observable (i.e. can be reached)

Frame Population

- Population that could be measured by the sample frame
- Generally, all members of the frame
- Or... all members who could be enumerated by the sample frame

Survey Population:

- The set of people who can be reached through your sample frame as implemented in the survey



All Americans



Social Science Theory

All American Adults Home at Some Point Aug 19 – Aug 20, 2018



Coverage Error

Americans with Domestic Telephone Service



Sample Error

Approximately 5,000 (valid) Telephone Numbers Sampled



Nonresponse

1,001 Americans who Responded to Survey

Sample Frames



List, or



Set of procedures



Sometimes requires two or more stages of selection



Designed to cover target population

Sampling Harvard Graduates





Sampling People at Burning Man Festival (Black Rock City)



Ideal Sample Frame

- Simple list
- Available and accessible
- All Members of target population are on list
- All members of list are eligible respondents
- Contact information available for all elements of frame

Example of Typical Sample Frame

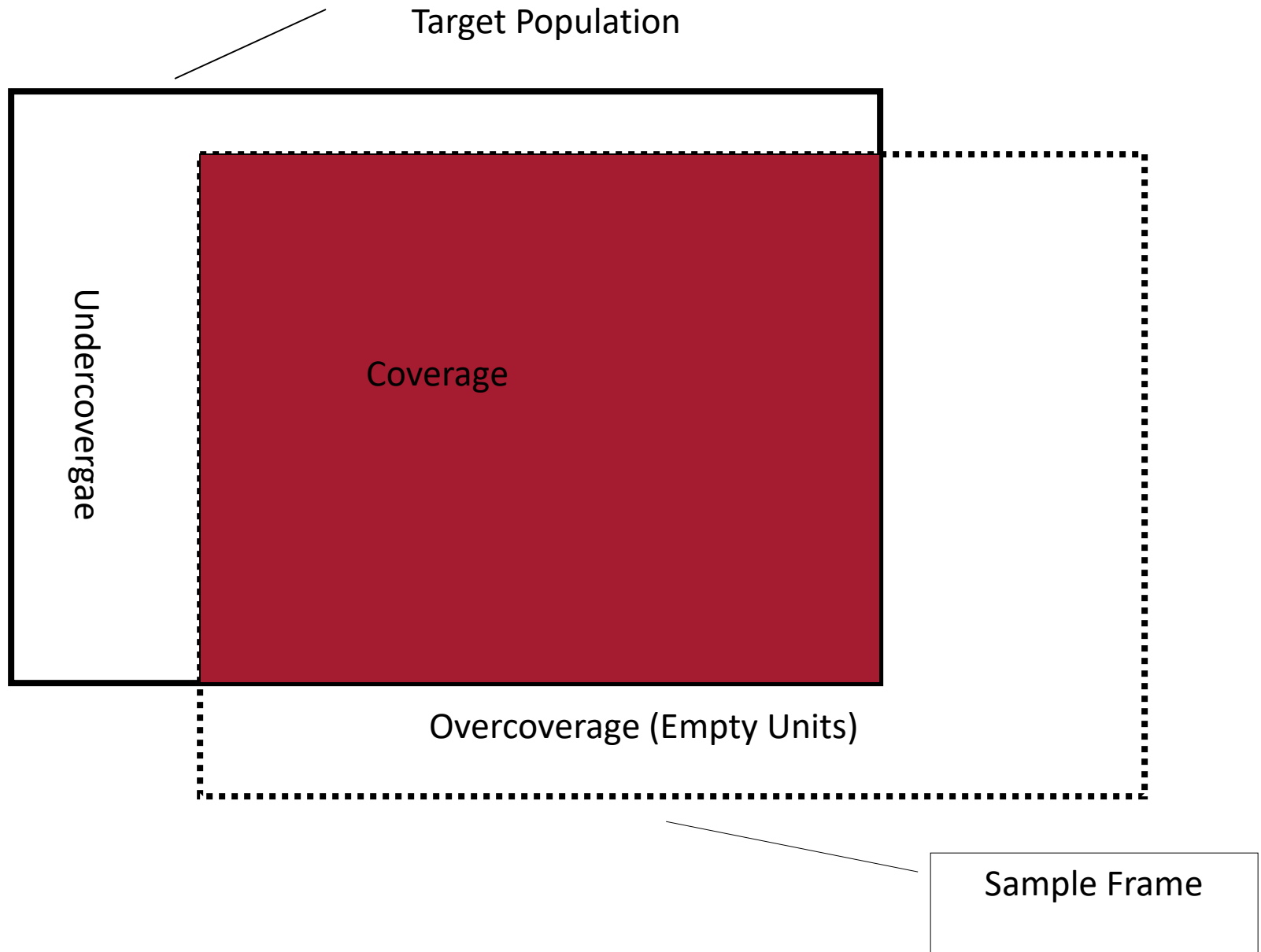
Population		Sample
<i>Ed Ash</i>	→	617-555-1234
<i>Peggy Birch</i>	→	617-555-1235
<i>Tony Birch</i>	↗	
<i>Marie Chestnut</i>	→	617-555-1236
	↘	617-555-1237
<i>Philip Elm</i>		(No telephone)
<i>(Not Assigned)</i>		617-555-1238

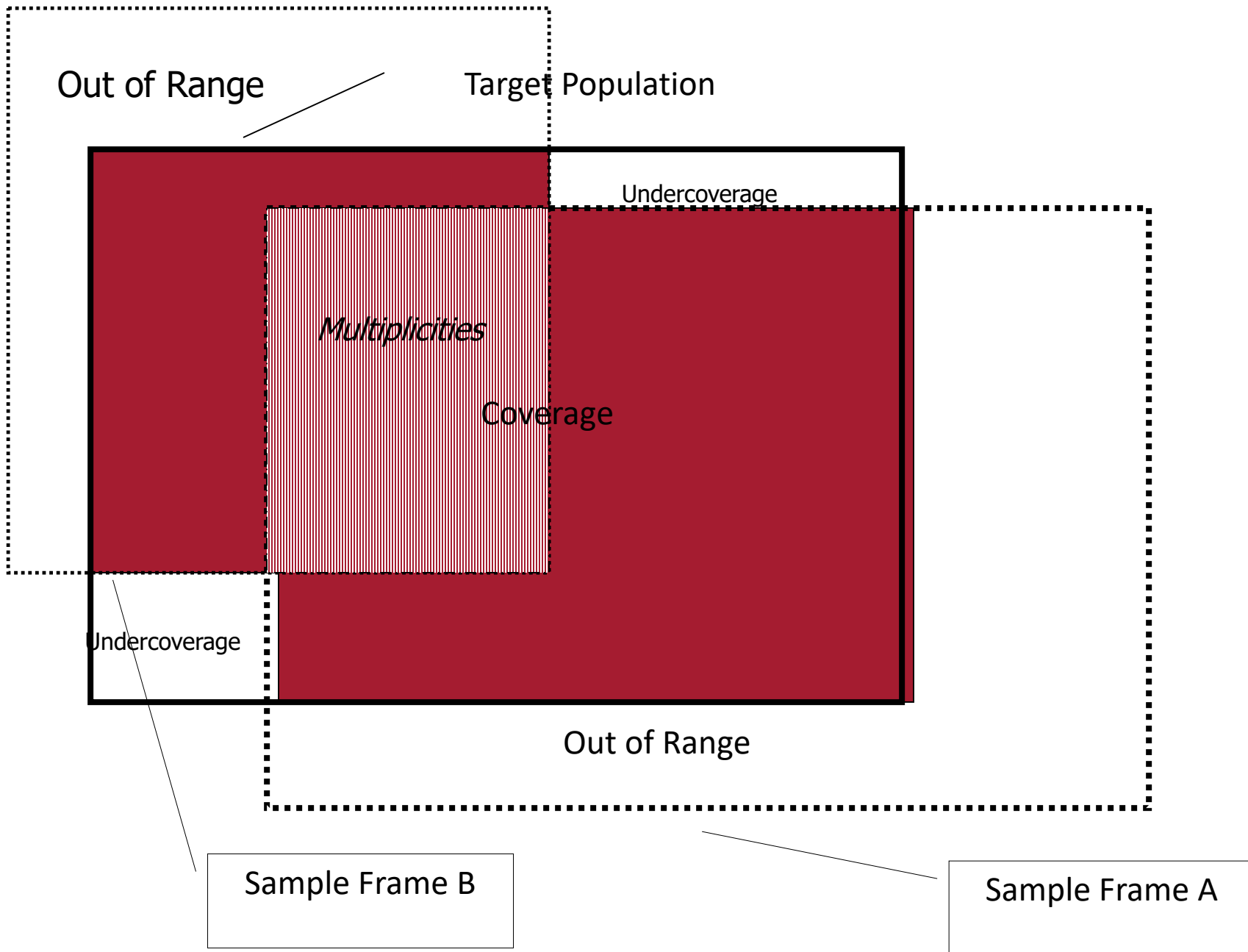
Relationship Between Target Population and Sample Frame

<i>Relationship</i>	<i>Name</i>	<i>Problems</i>
One-to-one	Perfect	None
One-to-None	Undercoverage	Bias
None-to-One	Low Incidence	Cost-Effectiveness
One to Many	Multiplicity	Probabilities
Many to One	Clustering	Probabilities

Example of Sample Frame

Population	Sample	
<i>Ed Ash</i>	→ 617-555-1234	
<i>Peggy Bolton</i>	→ 617-555-1235	<i>Clustering</i>
<i>Tony Bolton</i>	↗ 617-555-1235	
<i>David Chandler</i>	→ 617-555-1236	<i>Multiplicity</i>
	↘ 617-555-1237	
<i>Philip Elm</i>		
<i>(Not Assigned)</i>	617-555-1238	<i>Empty Record</i>





Measuring the Effect of Coverage Error on Population Estimates:

$$Y = \frac{N_c}{N} Y_c + \frac{N_{nc}}{N} Y_{nc}$$

Y = The value of the statistic in the target population

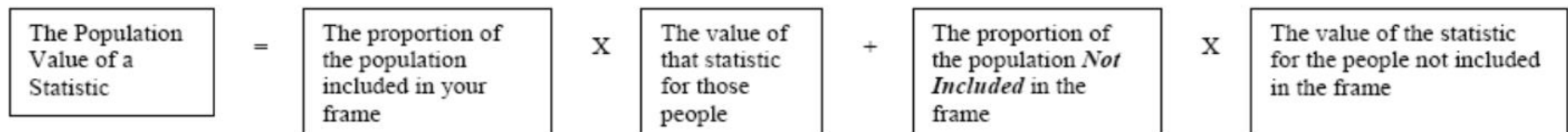
N_c = Number in the target population covered by the frame population

N = Total number in the target population

Y_c = Value of the statistic for those covered by the frame population

Y_{nc} = Value of the statistic for those not covered by the frame population

In Words:



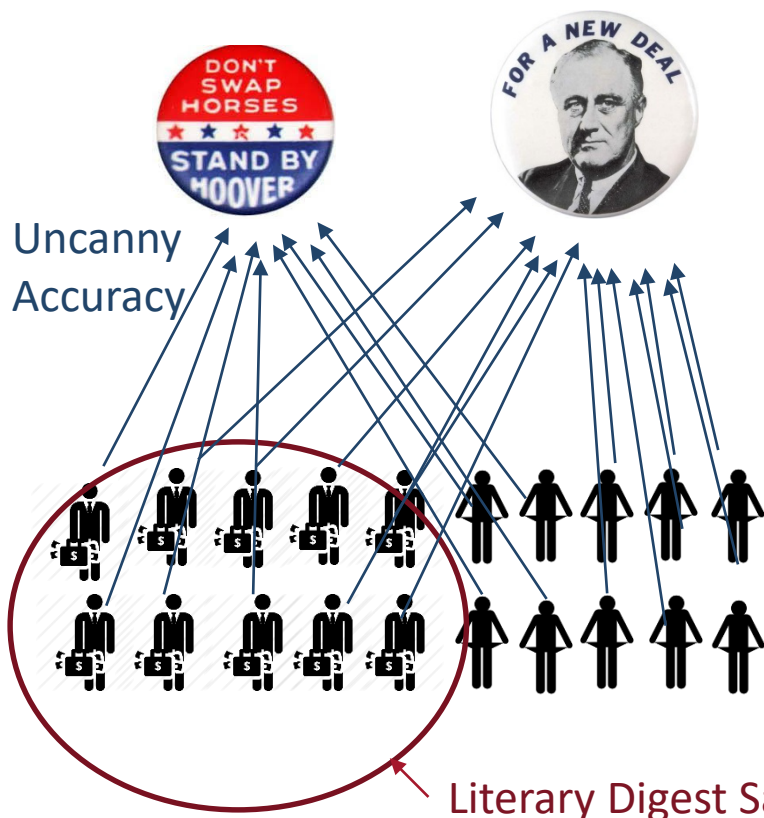
Thus the impact of coverage error is based on two things:

- The percent of the total population excluded from the sample frame
- The difference on the statistic of interest between those included in the frame and those excluded

Differences Between 1932 and 1936

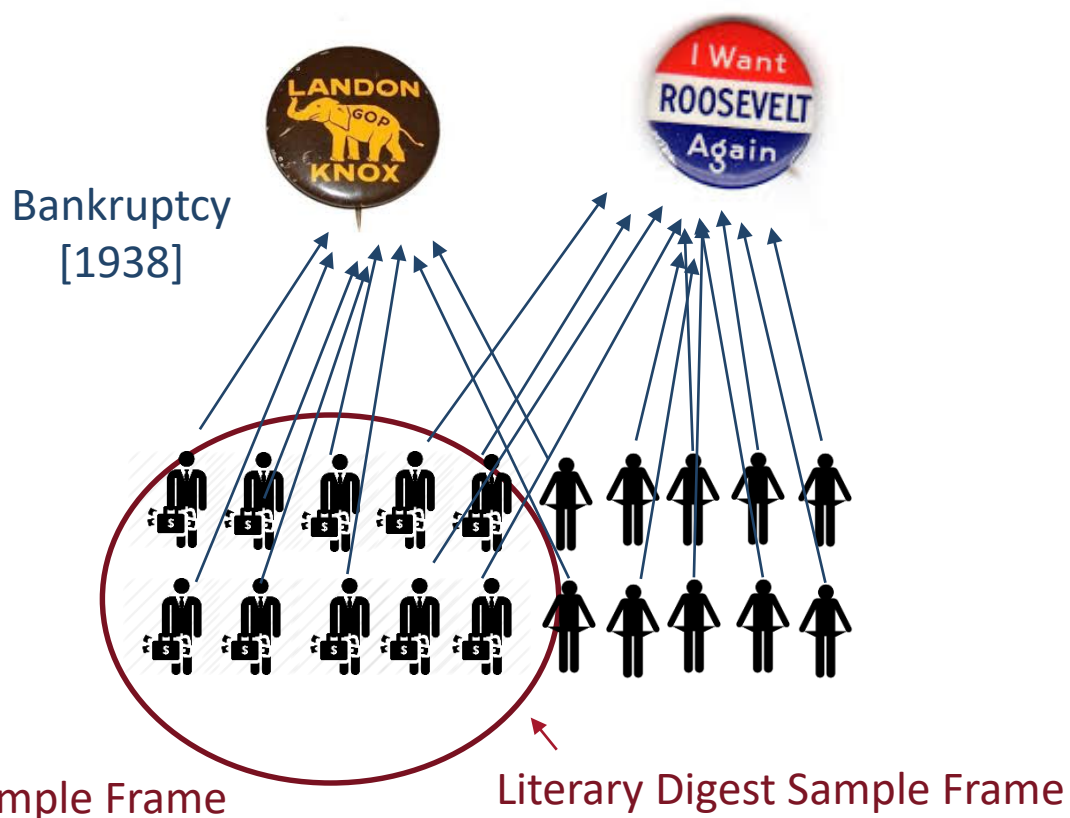
High Noncoverage

Low Differences Between Covered and Non-covered



High Noncoverage

High Differences Between Covered and Non-Covered



Considerations in Design

- What frames might be available for population?
 - Lists
 - Sets of procedures
- What is relationship of unit of frame to population?
- What is coverage of population in potential sample frames?
- What is incidence of respondents in potential sample frames?

General Populations

- Broad populations of residents
- No list available
- No easy way to target

Special Populations

- Narrow definition
- Lists may be available
- Targeted frames may be feasible

General versus Special Populations

➤ **Levels of analysis**

Sometimes the conceptual population to which we infer our data doesn't match the survey population from which we collect information.

Contents:

One survey may gather information about different things

Example: A survey of fast-food customers may yield information about different visits to fast food restaurants, people who eat fast food, households who eat fast food

Units

One survey may gather information about a different conceptual unit than the person

Example: A survey of households may interview a head of household or other household member

Example: A survey of land use may interview landowners to infer to acreage.

Example: A survey to estimate the number of job applicants who receive pre-employment drug tests might interview human resource officers at businesses.

Time-Frames

A survey may gather information about more than one time period

Example: A survey of investors might look at current and past ownership of investment instruments

Examples of Special Populations

- Usage – customers, visitors, participants, etc.
- Occupations
 - Journalists
 - Firefighters
 - People who work three jobs
 - Jazz Musicians
 - People who barter at flea markets
- Employees
- Companies

Chocolate Activity

- Stick hand in bag and mix
- Select **ten** chocolates randomly
- Count number of Green Wrapper chocolates (out of ten)
- Put chocolates back in bag
- Enter Data in Qualtrics Survey



Scientific and Non- Scientific Samples

Scientific Samples

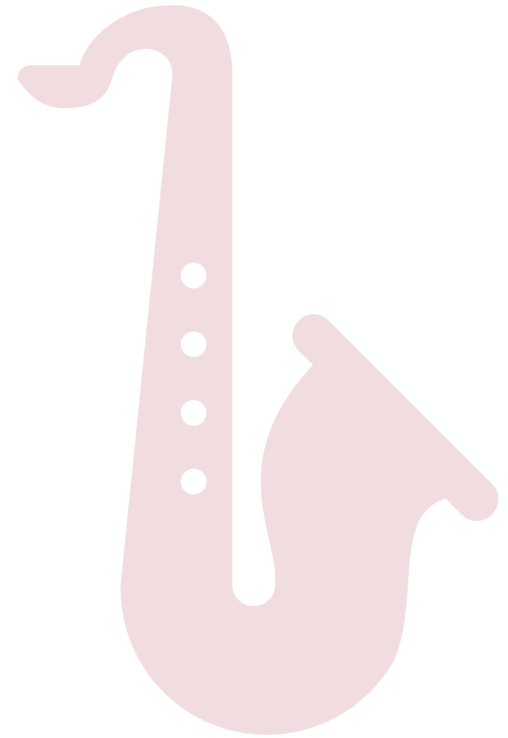
- *Based on Probability Theory*
- *Allow Inference to Sample Frame*
- *Sample Variance and Error Can Be Calculated*
 - Sample Records Are Drawn From a Well-Specified Frame
 - Sample Records Are Drawn According to Well-Specified Procedures With Known Properties
 - Each Sample Record Has a Known Non-Zero Probability of Selection
 - Data are Adjusted (Weighted) As Required To Reflect Sample Design

Non-Probability Samples

- Availability Samples
 - Convenience Samples
 - Volunteer Cases
- Purposive Cases
 - Typical Cases
 - Critical Cases
- Respondent Driven Samples
- Quota Samples



How Could We Sample Jazz Musicians?



Respondent Driven Sampling (RDS)

- Useful when population definition may be rich or complex
- Useful when population may be rare
- Most useful if rare populations are part of networks
- Select set of seeds
- Give coupons to respondents to recruit other members of population
- Continue process multiple times
- Examples: Prostitutes, IV Drug Users, Illegal immigrants, Jazz Musicians,

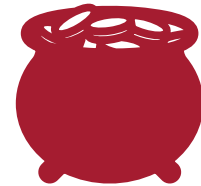


Scientific Samples

- *Based on Probability Theory*
- *Allow Inference to Sample Frame*
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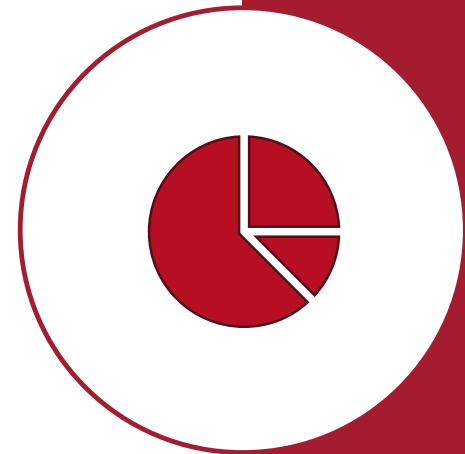
Green Chocolate Example

- Population is Chocolates in Bag
- Statistic is whether chocolate has **Green** or **Orange** wrapper
- Chocolates are randomly mixed in bag
- Each chocolate has an equal probability of being selected
- In samples of ten, number of **green** chocolates is estimate of percentage of population that is green



Green Chocolate Example

- Population: 142 total chocolates
 - 52 **Green** wrapped chocolates (36.62%)
 - 90 **Orange** wrapped chocolates (63.38%)
- Probability of selection:
- In samples of ten:
 - $10/142 \approx .07$
- Each chocolate had an equal probability of being selected



Two Key Statistical Elements Found in Any Population

**Central Tendency
(Mean)**

**Dispersion
(Variance or Standard Deviation)**

Why Randomize?

- Statistical Theory is based on randomization
- If a sample is randomized, errors are randomly distributed
- In the long run, errors or biases cancel each other out
- If these biases cancel each other out in the long run, then in the long run, the sample mean equals the population mean, and the sample variance equals the population variance
- Randomization works across all biases and errors, including those that we don't think about or know about.

Simple Random Samples (SRS)

- All population members have an equal chance of being selected
- Statistics are easy to calculate
- An **Equal Probability Selection Method (EPSEM)** sample
- Most statistics assume Sampling with Replacement
- In practice **Sampling Without Replacement (SWOR)** is most practical

How to Pull a Simple Random Sample From a Complete Frame:

Determine the size of your sample frame (N)

Determine the desired number of sample records you need (n)

Calculate your sampling fraction (k): $\left(\frac{n}{N}\right)$

Generate a Random Number for each frame element

It's easiest to calculate a random number between 0 and 1, and carry it out to many decimal places

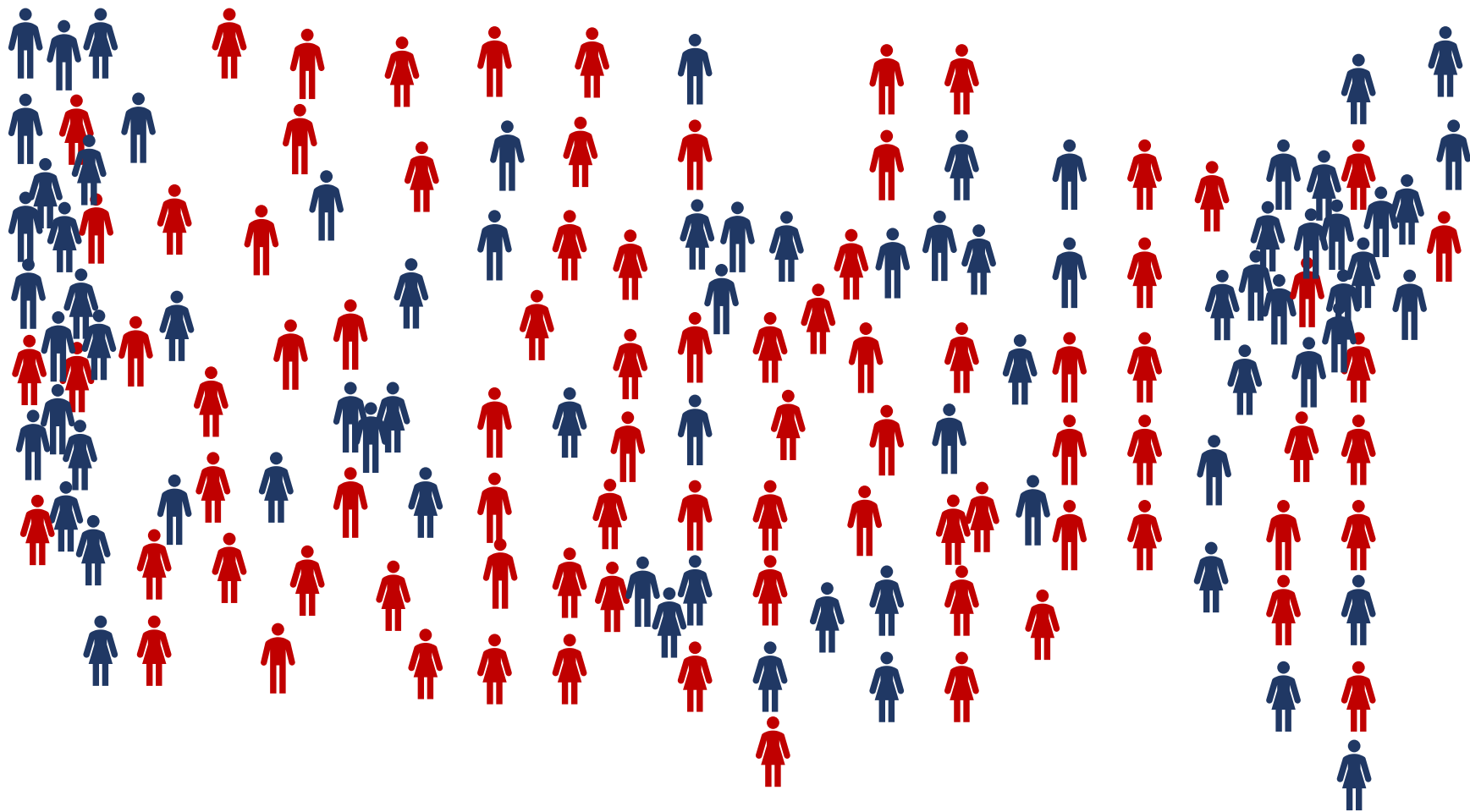
If the random number is Less Than or Equal to the Sampling Fraction, Include the element in your sample. Otherwise, exclude it.

How to Pull a Systematic Random Sample From a Complete Frame:

- Determine the total number of records in your frame (List) (N)
- Determine the desired number of sample records you need (n)
- Calculate your sampling fraction (k): $\left(\frac{n}{N}\right)$
- Generate a Random Number between 1 and k
- Count until you reach this random number and select this record
- Count from this randomly selected record and select every k th record until you reach the end of the list

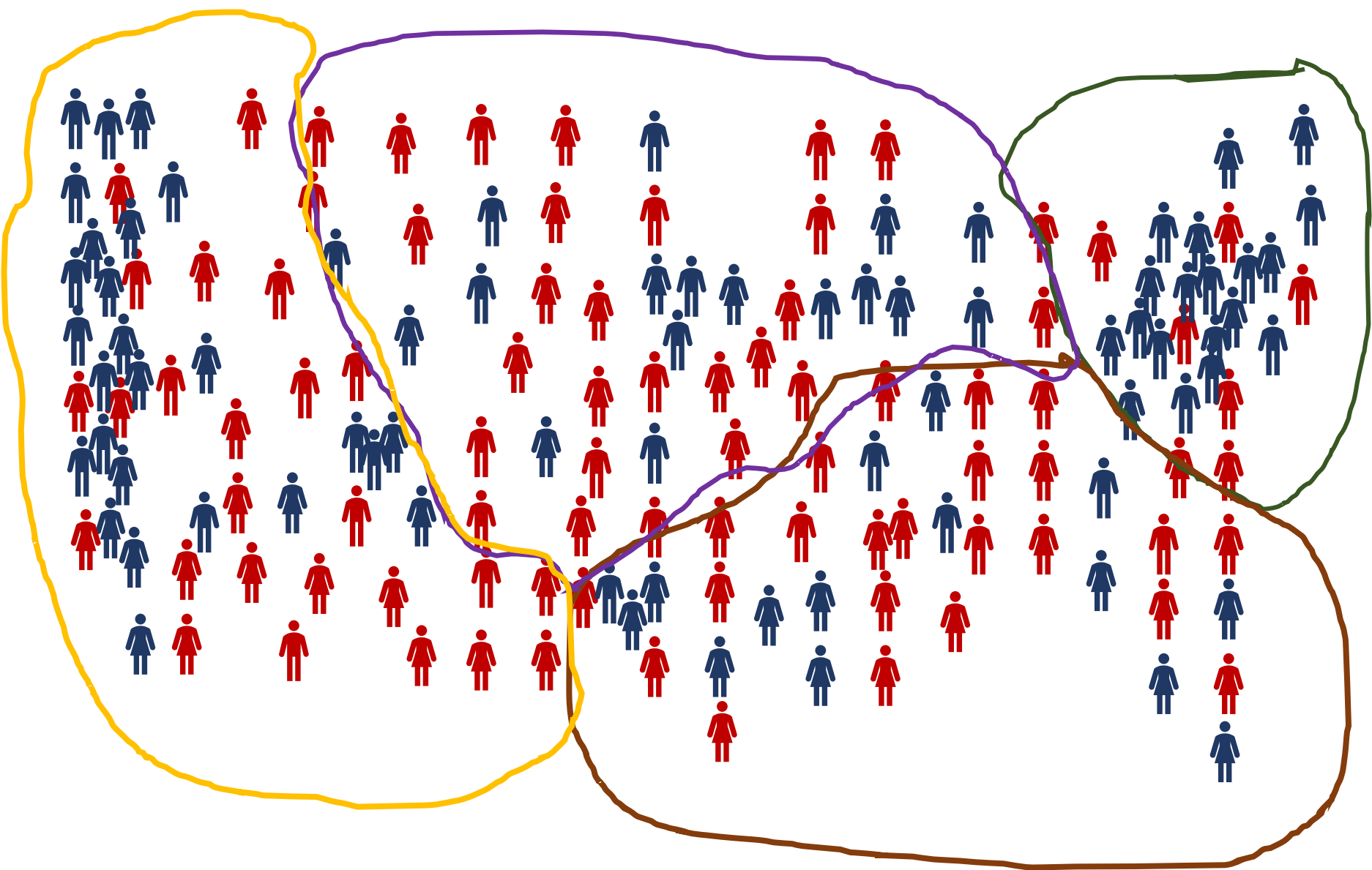
Stratification:

- Sample is divided into pre-designated units or partitions
- Strata should be homogeneous (heterogeneity between strata)
- Sample is drawn separately from each stratum



Benefits of Stratification:

- Insures that stratification elements are represented proportionally in overall survey data
 - Protects against error or bias *in the short run*
- Reduces overall sample variance
 - Increases precision of estimates
- Can allow more precise estimates of sub-groups if disproportionate stratification is used



Example of Proportionate Stratification:

Research Objective: Conduct a survey to assess attitudes toward the electoral college

Research Method: Telephone survey of 1,000 telephone households in United States during November 2000

Sample Frame: List of all possible residential telephone numbers in US

Effective Sampling Fraction: You need to draw 6 telephone numbers to reach 1,000 households

Option 1: Draw a Simple Random Sample of 6,000 telephone numbers from your frame

Option 2:

- Divide the US into four (4) regions
- Determine the proportion of all households that are located in each region
- Draw a separate simple random sample within each of these four regions with an n that is proportionate to that regions size

Regional Sample Stratification For US National Survey

Stratum (Census Region)	Population	Percent	Sample Records	Estimated Interviews
Northeast	39,418,789	19.97%	1,198	200
North Central	46,076,032	23.35%	1,401	233
South	69,894,352	35.42%	2,125	354
West	41,954,834	21.26%	1,276	213
Total	197,344,007	100%	6,000	1,000

**Sample Design For Connecticut Child Care Facilities
Proportional to Region and Type of Facility
(n=1,200)**

Facility Type	Region	N	Percent	Sample if Proportional
Child Care Center	Southwest	351	5.14%	62
	South Central	308	4.51%	54
	Eastern	290	4.25%	51
	North Central	530	7.77%	93
	Northwest	288	4.22%	51
Family Home	Southwest	647	9.48%	114
	South Central	951	13.94%	167
	Eastern	1,019	14.93%	179
	North Central	1,744	25.56%	307
	Northwest	695	10.19%	122
Total:		6,823	100.00%	1200

Sample Design And Weights For Connecticut Child Care Facilities
Disproportionate Sample Design
(n=1,200)

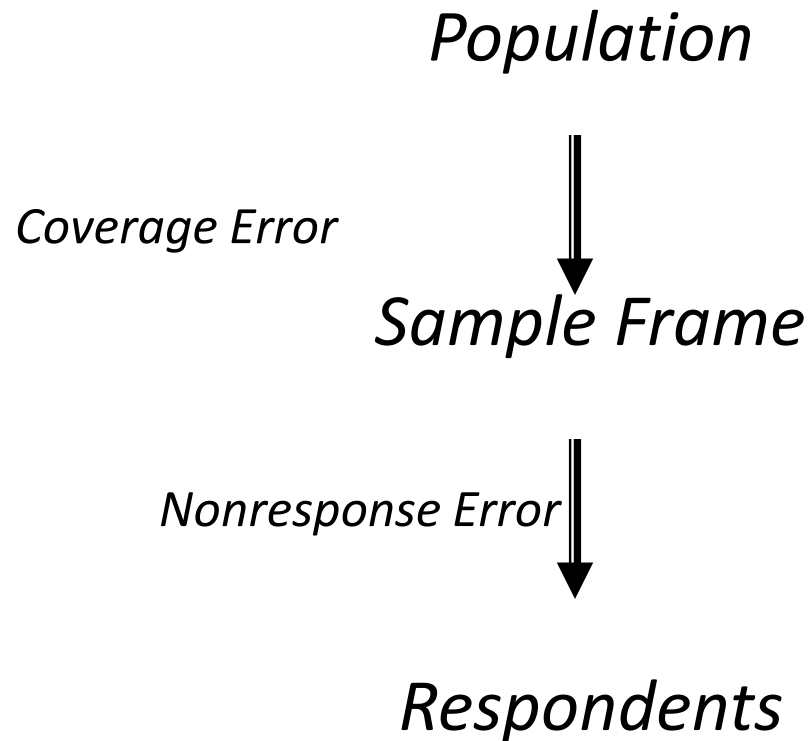
Facility Type	Region	N	Population Percent	Expected	Observed	Sample Weight
Child Care Center	Southwest	351	5.14%	62	120	0.52
	South Central	308	4.51%	54	120	0.45
	Eastern	290	4.25%	51	120	0.43
	North Central	530	7.77%	93	120	0.78
	Northwest	288	4.22%	51	120	0.43
Family Home	Southwest	647	9.48%	114	120	0.95
	South Central	951	13.94%	167	120	1.39
	Eastern	1,019	14.93%	179	120	1.49
	North Central	1,744	25.56%	307	120	2.56
	Northwest	695	10.19%	122	120	1.02
Total:		6,823	100.00%	1,200	1,200	

The background of the slide features several thin, curved lines in shades of gray, some solid and some dashed, creating a sense of motion or flow. A large, dark red rectangular box is positioned on the left side, containing the title text.

Considerations in Design

- What frames might be available for population?
 - Lists
 - Sets of procedures
- What is relationship of unit of frame to population?
- What is coverage of population in potential sample frames?
- What is incidence of respondents in potential sample frames?

Survey Sampling -- Summary



Population Specification

Conceptualize Inferential Population

- Begin by considering overall analytic goals of survey
- Determine extent and type of inference
- Fully elaborate and consider the nature of the inferential population, including different types of unusual cases and variants

Operationalize Inferential Population in Target Population

- Develop specific definition
- Specify selection criteria and rules in detail

Specify Frame Population in Relation to Target Population

- Specifically list details of frame population that meet and do not meet criteria of target population
- Be very specific about details, including sources and dates of databases or lists
- Specify procedures for dealing with potential incongruities between frame and target population

Systematic Sampling:

- Useful if full population list is only available electronically
 - Data entry (or scanning) of “hard-copy” list represent alternatives
- Sample records are systematically taken from a list so that every “kth” record is taken, and the list is sampled from beginning to end (*sometimes called “nth-ing”*)
- Random start point should be used
- If list is ordered in a periodic manner serious bias can occur
- If list is ordered (or electronic list is sorted appropriately) systematic sampling represents a method of implicitly stratifying a sample

How to Pull a Systematic Random Sample From a Complete Frame:

- Determine the total number of records in your frame (List) (N)
- Determine the desired number of sample records you need (n)
- Calculate your sampling fraction (k): $\left(\frac{n}{N}\right)$
- Generate a Random Number between 1 and k
- Count until you reach this random number and select this record
- Count from this randomly selected record and select every k th record until you reach the end of the list

Implicit Stratification:

- Utilizes Relevant Information About Frame to Order Frame
- Provides Many Benefits of Explicit Stratification
- Can Incorporate More Information Than Explicit Stratification
- Typically Used in Conjunction with Explicit Stratification

How to Implicitly Stratify a Sample:

- Sort Frame On Key Variables
- Take Systematic Sample or Systematic Random Sample From Sorted Frame

Cluster Sampling:

- Use when full population enumeration is not possible
- Use for cost efficiencies
- Use when physically required by research design
- Use when clustering of population is of analytic interest

Overview of Clustered Sample:

- Enumerate initial or Primary Sampling Units (PSU's)
- Select Sample (may be stratified) of PSU's
- If necessary, select further clusters below PSU stage
- If necessary, enumerate further clusters or elements in sufficient detail to calculate probabilities of selection
- Select n sample records from final or ultimate cluster

How Many Clusters? How many units?

- The fewer clusters, the more economical the sample
- The more clusters, the more precise the overall sample
- The more units within each cluster, the more precise the estimates within that cluster
- In general population surveys, five units within each cluster is the norm

Probability Proportionate to Size Sampling:

- Method of multistage cluster sampling
- Results in an EPSEM sample
- Often called a “self-weighting sample”
- Typically results in better population coverage than cluster sampling with PSU's selected with equal probability

Method:

- Select PSU's with a probability proportionate to their overall size
- Select equal number of elements from each PSU

Probability of Selection:

$$\boxed{\text{Element Probability}} = \boxed{\text{Number of Clusters Selected}} \times \boxed{\frac{\text{Cluster Size}}{\text{Population Size}}} \times \boxed{\frac{\text{Elements Selected Per Cluster}}{\text{Cluster Size}}}$$

PPS Example:

EPSEM Exit Poll With PPS Design

	N	Prob.	n	f	Total Prob.
Precinct 1	500	.13	100	1/5	.03
Precinct 2	1,000	.25	100	1/10	.03
Precinct 3	200	.05	100	1/2	.03
Precinct 4	800	.20	100	1/8	.03
Precinct 5	500	.13	100	1/5	.03
Precinct 6	<u>1,000</u>	<u>.25</u>	100	<u>1/10</u>	<u>.03</u>
Total:	4,000				

Example:

EPSEM Exit Poll With PSU's Selected With Equal Probability

	N	Prob.	f	n	Total Prob.
Precinct 1	500	.17	1/7	75	.03
Precinct 2	1,000	.17	1/7	150	.03
Precinct 3	200	.17	1/7	30	.03
Precinct 4	800	.17	1/7	120	.03
Precinct 5	500	.17	1/7	75	.03
Precinct 6	<u>1,000</u>	<u>.17</u>	<u>1/7</u>	150	<u>.03</u>
Total:	4,000				



Sampling People who Go to Baseball Games at Fenway Park

A Taxonomy of Probability Selection Methods

I.	Equal Probabilities of Selection (EPSEM): (a) Equal Probabilities at all stages of sample design (b) Equal overall probabilities obtained through compensating unequal probabilities at several stages	Unequal Probabilities for different stages; ordinarily compensated with inverse weights (a) Caused by irregularities in selection frames and procedures (b) disproportionate allocation designed for optimum allocation
II.	Element Sampling: Single stage, sampling unit contains only one element	Cluster Sampling: Sampling units are clusters of elements (a) One-stage cluster sampling (b) Subsampling or multistage sampling (c) Equal clusters (d) unequal clusters
III.	Unstratified Selection: Sampling units selected from entire population	Stratified Sampling: separated selections from partitions, or strata, of population
IV.	Random Selection of individual sampling units from entire stratum or population	Systematic Selection or sampling units with selection interval applied to list
V.	One-Phase sampling: Final sample selected directly from entire population	Two-Phase (or double) sampling: final sample selected from first-phase sample, which obtains information for stratification or estimation

Source: Leslie Kish; *Survey Sampling*, New York: John Wiley & Sons, 1965