

**Problem 1.** Find the inverse matrix of

$$A = \begin{pmatrix} 1 & 1 & 0 \\ 0 & 2 & -1 \\ 0 & 0 & 3 \end{pmatrix}.$$

**Problem 2.** Let  $A$  be an invertible matrix. Prove that  $A^{-1} = (\det A)^{-1}C^T$ , where  $C$  is the cofactor matrix.

**Problem 3.** Solve  $x + 2y = 0$ ,  $2x + y + z = 1$ ,  $y - z = 0$  by using the Cramer's rule.

**Problem 4.** Let us define the polynomials

$$P(x) = \begin{vmatrix} 1 & x & 3 & x^2 \\ 2 & 0 & 3 & -1 \\ x & x & 1 & 0 \\ x^3 & 0 & -x & 2 \end{vmatrix}, \quad Q(x) = \begin{vmatrix} 1 & x & x^2 \\ 4 & 0 & 1 \\ x & 2 & -1 \end{vmatrix}.$$

- (1) What are their orders and the coefficients of the highest order term.
- (2) Find  $Q'(0)$ .