

## Tutorial 7: Basic Relational Algebra

Jin, Ziyang  
# 34893140  
f4a0b

Kim, Joon Hyung  
# 35183128  
11m8

February 2018

Consider a database consisting of the relations, where the primary key of each relation is underlined.

**sailors**(sid, sname, rating, age)  
**boats**(bid, bname, color)  
**reserved**(sid, bid, date)

1. Find the names of sailors who have reserved at least two different boats with the same color.

- **RA**

$$\begin{aligned}rb &\leftarrow \pi_{sid, bid, color}(reserved \bowtie boats) \\ good &\leftarrow \pi_{sid}(rb \bowtie_{rb.sid=rb2.sid \wedge rb.bid \neq rb2.bid \wedge rb.color=rb2.color} \rho_{rb2}(rb)) \\ answer &\leftarrow \pi_{sname}(good \bowtie sailors)\end{aligned}$$

- **Datalog**

$$\begin{aligned}rb(S, B, C) &\leftarrow reserved(S, B, \_), boats(B, \_, C) \\ good(S) &\leftarrow rb(S, B, C), rb(S, B', C), B \neq B' \\ answer(N) &\leftarrow good(S), sailors(S, N, \_, \_)\end{aligned}$$

2. Find the names of sailors who have reserved all red boats.

- **RA**

$$\begin{aligned}allred &\leftarrow \pi_{bid}(\sigma_{color='red'} boats) \\ good &\leftarrow (\pi_{sid, bid} reserved) \div allred \\ answer &\leftarrow \pi_{sname}(good \bowtie sailors)\end{aligned}$$

- **Datalog**

$$\begin{aligned}allred(B) &\leftarrow boats(B, \_, 'red') \\ witness(S, B) &\leftarrow reserved(S, B, \_), allred(B) \\ bad(N) &\leftarrow sailors(S, N, \_, \_), reserved(S, B, \_), \neg witness(S, B) \\ answer(N) &\leftarrow sailors(\_, N, \_, \_), \neg bad(N)\end{aligned}$$

3. Find the name and color of boats which are reserved by all sailors rated above 7.

4. Find the name(s) of sailors with the lowest rating.
5. Find the name and rating of the oldest sailor(s).
6. Find the names of sailors who have reserved every boat reserved by those with a lower rating.