

RacLab

Introduction to Drift Diffusion Model pt.2

Yang Ziyang

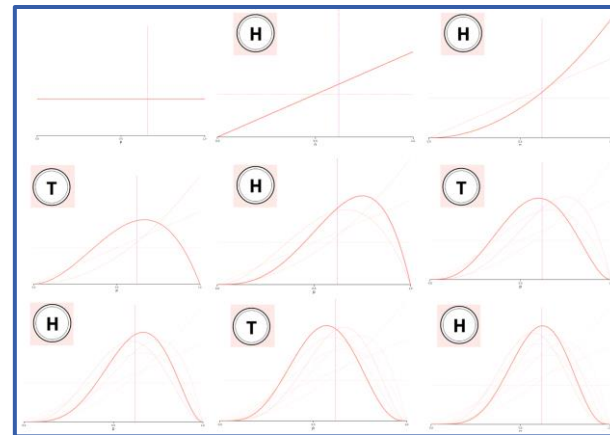
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Introduction

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Cognitive and Computational modeling Part.1

Yang Ziyang
2025.07.31



Hierarchical Bayesian parameter estimation of the Drift Diffusion Model

$$V_n = V_{n-1} + B_x = V_{n-1} + \mu + \varepsilon$$

选A的概率 P(A)
选B的概率 P(B)

漂移扩散过程(积累过程)等价于伯努利随机抽样过程

$$V_n = V_{n-1} + \log \frac{p_A(x_n)}{p_B(x_n)} = V_{n-1} + \frac{(\mu_A - \mu_B)^2}{\sigma_B^2} + \frac{\mu_A - \mu_B}{\sigma_B^2} \epsilon, \text{ where } \epsilon \sim \mathcal{N}(0, 1)$$

$$\frac{P(\{x_i\} | A)}{P(\{x_i\} | B)} = \prod_{i=1}^n \frac{P(x_i | A)}{P(x_i | B)}$$

x_n 为反应时，表达了在某一次决策时当反应时为 x_n 的情况下选择A的概率比选择B的概率大多少

$$\log \prod_{i=1}^n \frac{P(x_i | A)}{P(x_i | B)} = \sum_{i=1}^n \log \frac{P(x_i | A)}{P(x_i | B)}$$

在观测到反应时 t 之后，参数的条件概率密度——这就是我们真正想要估计的目标

已知参数 (v, a, z) ，观察到某个特定 t 的概率密度

Selfish behavior requires top-down control of prosocial motivation

$$f(v, a, z | t) = \frac{f(t | v, a, z) \cdot \text{先验} f(v, a, z)}{f(t)}$$

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Introduction to Drift Diffusion Model

Yang Ziyang
2025.05.28

Introduction

Environment

How to install HDDM (suitable for docker and linux)

https://huchuanpeng.com/post/hddm_installation_tutorial/

dockerHDDM:
从安装到入土

https://www.bilibili.com/video/BV17T421Y7MX/?spm_id_from=333.337.search-card.all.click&vd_source=30501c1c4b33ad073b7b7c3b06ab8a93

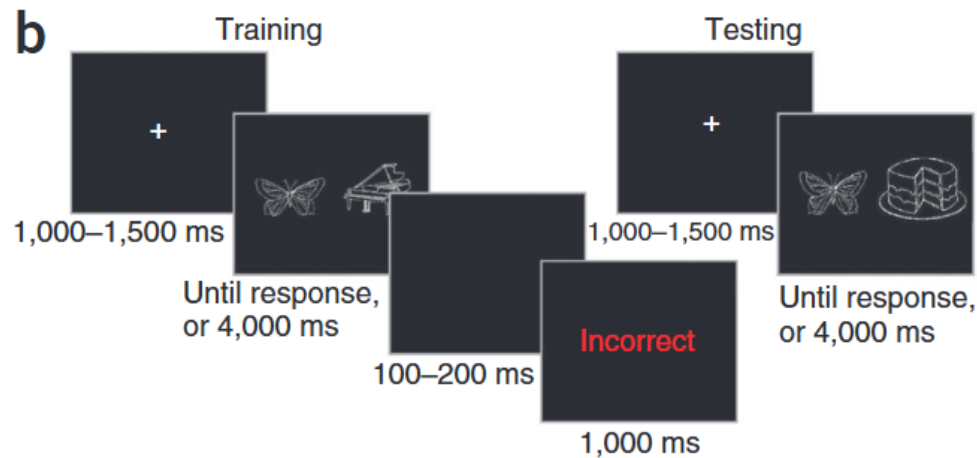
Introduction

Dataset

Article | Published: 25 September 2011

Subthalamic nucleus stimulation reverses mediofrontal influence over decision threshold

[James F Cavanagh](#) ✉, [Thomas V Wiecki](#), [Michael X Cohen](#), [Christina M Figueroa](#), [Johan Samanta](#), [Scott J Sherman](#) & [Michael J Frank](#) ✉



subject	stim	rt	choice	conf
	0 LL	1210	1 HC	
	0 WL	1630	1 LC	
	0 WW	1030	1 HC	
	0 WL	2770	1 LC	
	0 WW	1140	0 HC	
	0 WL	1150	1 LC	

		Stim	
		WW	LL
Conflict	High		
	Low		WL

Introduction

Dataset

subject	stim	rt	choice	conf
0	LL	1210	1	HC
0	WL	1630	1	LC
0	WW	1030	1	HC
0	WL	2770	1	LC
0	WW	1140	0	HC
0	WL	1150	1	LC



	subj_idx	stim	rt	response	conf
0	0	LL	1.210	1	HC
1	0	WL	1.630	1	LC
2	0	WW	1.030	1	HC
3	0	WL	2.770	1	LC
4	0	WW	1.140	0	HC

HDDM requires the inclusion of three columns of variables

“subj_idx” “rt” “response”

- ✓ “rt” must be *seconds*
- ✓ NaN values are not available.

- ✓ accuracy-coding
correct (1) and error (0)
- ✓ stimulus-coding
upper (1) and lower (0)

Introduction

Modelset

Model 0: base model: full model

```
mm0 = hddm.HDDM(df, include=['a', 'v', 't', 'z'])
```

Model 1: treat within-subj as between-subj: full model

```
mm1 = hddm.HDDM(df, include=['a', 'v', 't', 'z'],  
depends_on={'v': 'conf'})
```

Model 2: regression model (varying intercept and slope)

```
mm2 = hddm.HDDMRegressor(  
df, "v ~ 1 + C(conf, Treatment('LC'))",  
include=['a', 'v', 't', 'z'],  
group_only_regressors=False,  
keep_regressor_trace=True)
```

Introduction

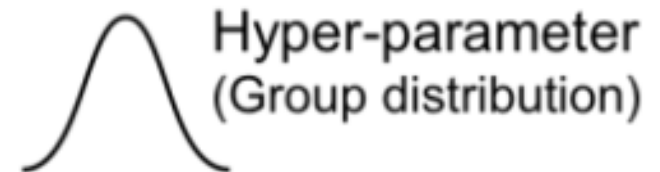
Model 1: treat within-subj as between-subj: full model

```
mm1 = hddm.HDDM(df, include=['a', 'v', 't', 'z'],  
depends_on={'v': 'conf'})
```

- **漂移率**依赖于一个**分类变量(HC/LC)**
- **漂移率的均值(Mean)和变异性(Std)**是基于群体水平共享的



漂移率是通过先验(统一的群体先验)来建模的



群体先验：
高冲突慢(v_HC 低)，低冲突快(v_LC 高)



所有被试的两个参数都强制受到群体先验的影响

Introduction

Model 2: regression model (varying intercept and slope)

```
mm2 = hddm.HDDMRegressor(  
    df, "v ~ 1 + C(conf, Treatment('LC'))",  
    include=['a', 'v', 't', 'z'],  
    group_only_regressors=False,  
    keep_regressor_trace=True)
```

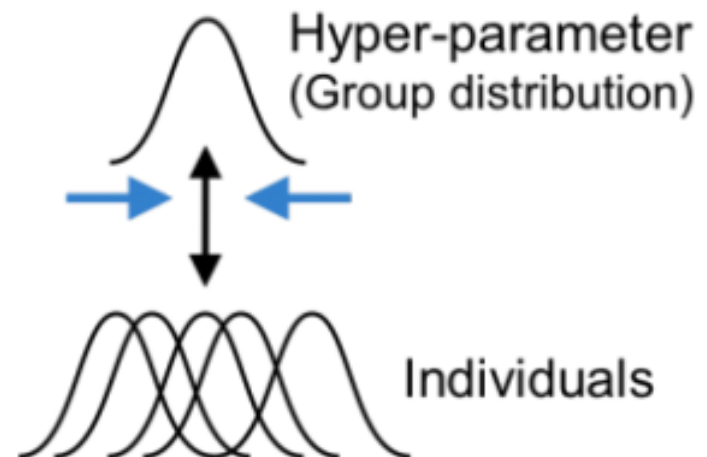
个体的参数会收缩到群体的先验上
但个体之间的差异会被保留下来



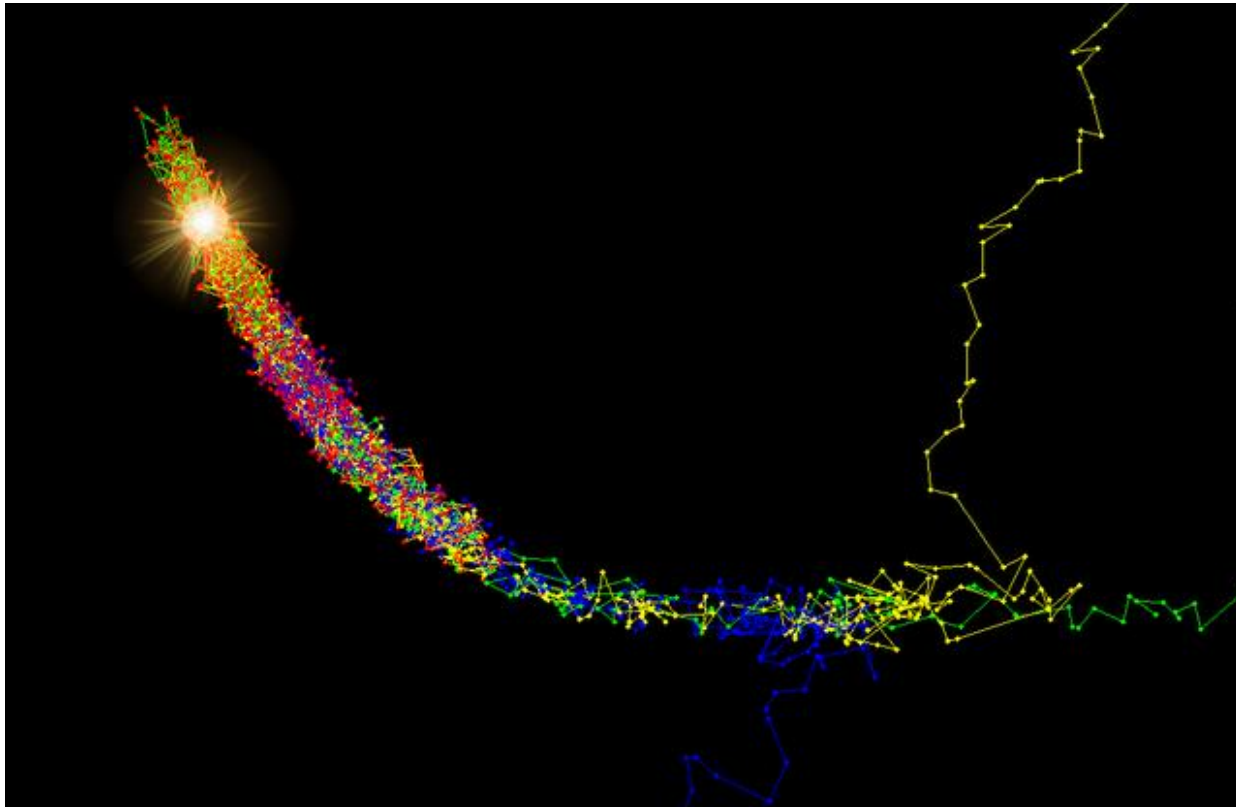
即同时考虑的群体差异和个体差异



允许为每个个体的参数设置独立的先验

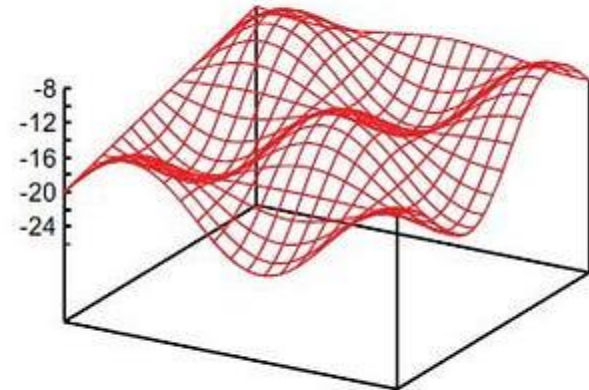
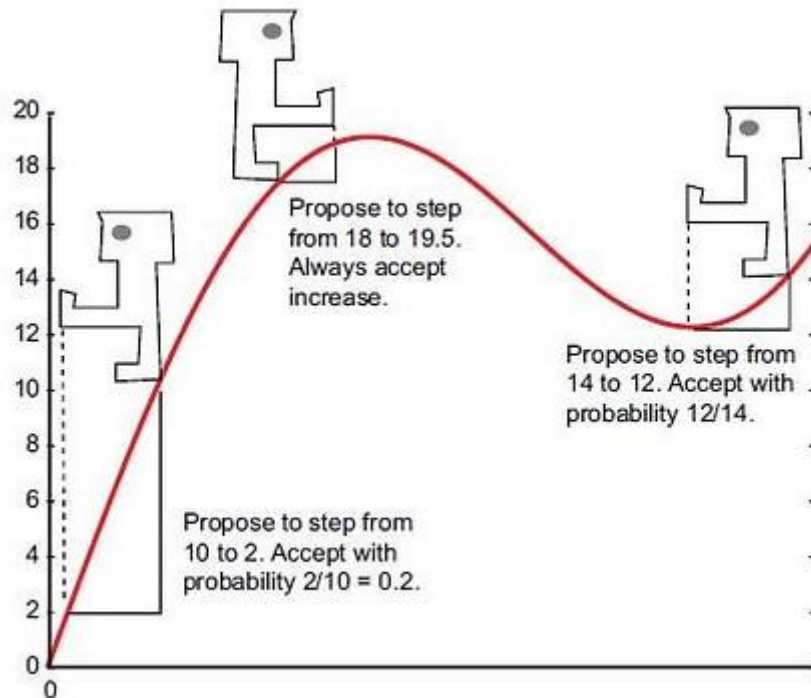


Markov chain Monte Carlo

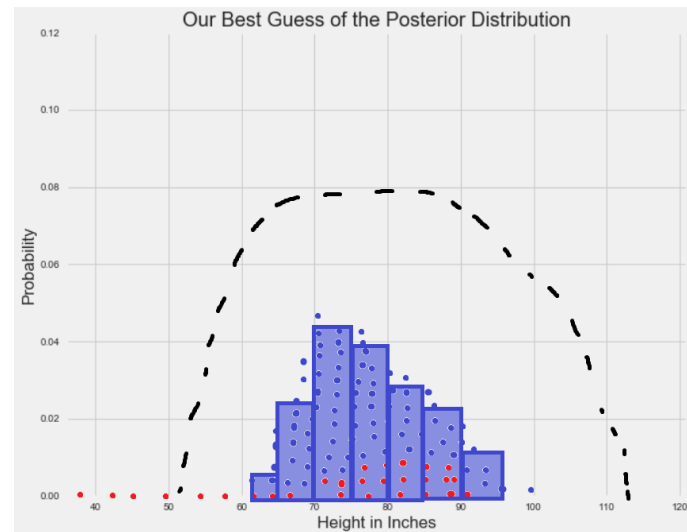
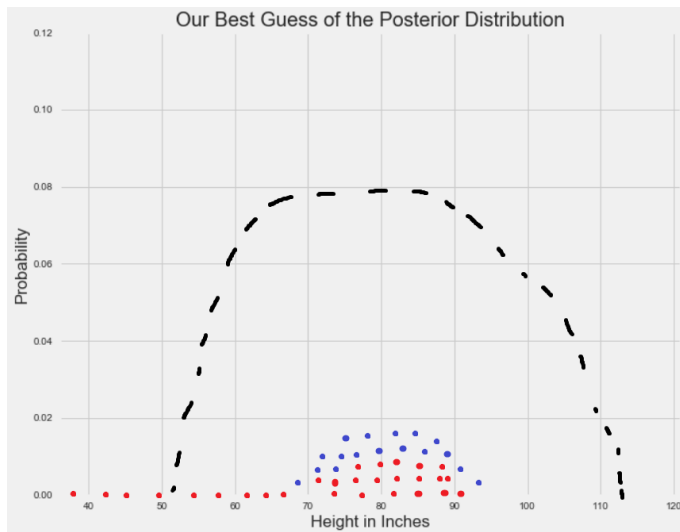
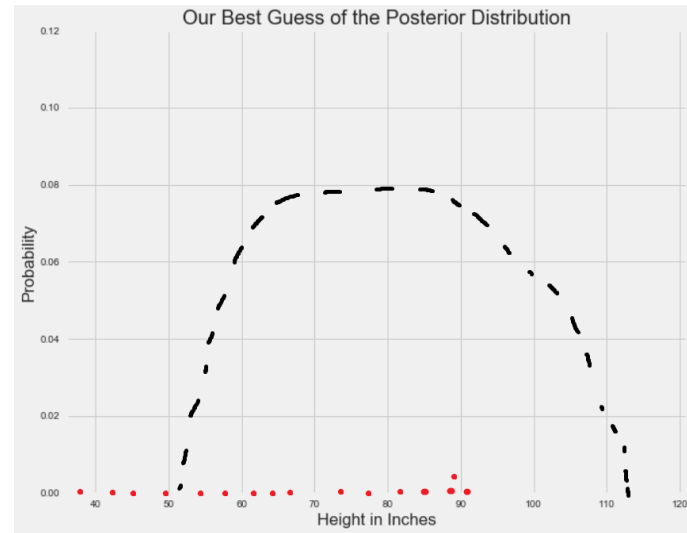
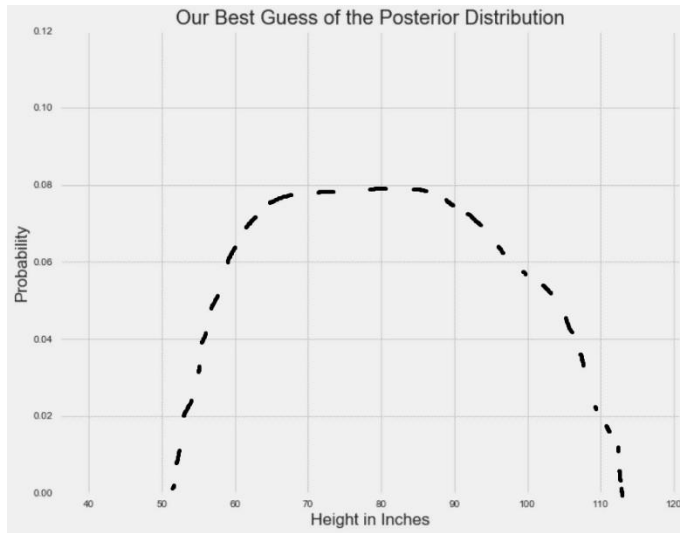


Introduction

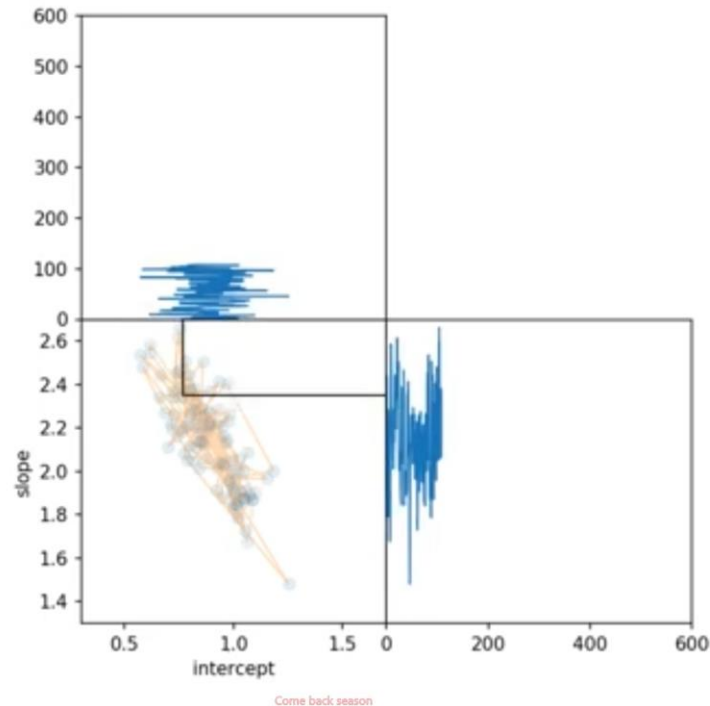
The MCMC sampler's objective is to generate more samples from high target distribution regions and fewer from low target distribution regions.



Introduction



Introduction



MCMC chains are **valid and reliable** when they fluctuate around a value and different chains are **indistinguishable** from each other, a scenario often referred to as a “**caterpillar**” shape.

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