Ziyao Xu

Room B17, Hayes-Healy Hall Department of Applied and Computational Mathematics and Statistics (ACMS) University of Notre Dame

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EDUCATION

• Brown University
• Ph.D. in Applied Mathematics. Advisor: Chi-Wang Shu.

Providence, RI, USA
Sep. 2019 – May. 2023

Michigan Technological University

M.S. in Mathematical Sciences. Advisor: Yang Yang.

Jan. 2017 - May. 2019

Houghton, MI, USA

China University of Petroleum

B.E. in Petroleum Engineering.

Qingdao, Shandong, China Sep. 2012 - Jun. 2016

Professional Experience

University of Notre Dame
Postdoctoral Research Associate

Notre Dame, IN, USA Jul. 1, 2023 – Present

Research Interests

- Finite Element Methods
- Finite Difference Methods
- Computational Fluid Dynamics
- Flow and Transport in Porous Media

Preprints

- 1. Ziyao Xu, Guanyang Liu and Yong-Tao Zhang, A Conservative and Positivity-Preserving Discontinuous Galerkin Method for the Population Balance Equation, preprint.
- 2. Ziyao Xu and Yong-Tao Zhang, Exponential Time Differencing Runge-Kutta Discontinuous Galerkin (ETD-RKDG) Methods for Nonlinear Degenerate Parabolic Equations, preprint.
- 3. Ziyao Xu, Zheng Sun and Yong-Tao Zhang, Stability and Time-Step Constraints of Exponential Time Differencing Runge-Kutta Discontinuous Galerkin Methods for Advection-Diffusion Equations, submitted to Journal of Scientific Computing.
- 4. Yong Liu and Ziyao Xu, An interior penalty discontinuous Galerkin method for an interface model of flow in fractured porous media, preprint.

Publications

- 1. Xinyu Wu, Hui Guo, Ziyao Xu, Lulu Tian and Yang Yang, A reinterpreted discrete fracture model for wormhole propagation in fractured porous media, Journal of Computational Physics, accepted.
- 2. Ziyao Xu and Yong-Tao Zhang, High-order exponential time differencing multi-resolution alternative finite difference WENO methods for nonlinear degenerate parabolic equations, Journal of Computational Physics, v529 (2025), 113838.
- 3. Ziyao Xu and Chi-Wang Shu, A well-balanced conservative high-order alternative finite difference WENO (A-WENO) method for the shallow water equations, Advances in Water Resources, v196 (2025), 104898.
- 4. Ziyao Xu and Dennis Glaser, An extension of the box method discrete fracture model (Box-DFM) to include low-permeable barriers with minimal additional degrees of freedom, Advances in Water Resources, v195 (2025), 104869.

- 5. Ziyao Xu and Chi-Wang Shu, A high-order well-balanced discontinuous Galerkin method for hyperbolic balance laws based on the Gauss-Lobatto quadrature rules, Journal of Scientific Computing, v101 (2024), 39.
- 6. Ziyao Xu and Chi-Wang Shu, Local characteristic decomposition-free high order finite difference WENO schemes for hyperbolic systems endowed with a coordinate system of Riemann invariants, SIAM Journal on Scientific Computing, v46 (2024), pp.A1352-A1372.
- 7. Xinyu Wu, Hui Guo, Ziyao Xu and Yang Yang, A reinterpreted discrete fracture model for Darcy-Forchheimer flow in fractured porous media, Advances in Water Resources, v179 (2023), 104504.
- 8. Ziyao Xu and Chi-Wang Shu, On the conservation property of positivity-preserving discontinuous Galerkin methods for stationary hyperbolic equations, Journal of Computational Physics, v490 (2023), 112304.
- 9. Ziyao Xu, Zhaoqin Huang and Yang Yang, The hybrid-dimensional Darcy's law: A non-conforming reinterpreted discrete fracture model (RDFM) for single-phase flow in fractured media, Journal of Computational Physics, v473 (2022), 111749.
- 10. Ziyao Xu and Chi-Wang Shu, Third order maximum-principle-satisfying and positivity-preserving Lax-Wendroff discontinuous Galerkin methods for hyperbolic conservation laws, Journal of Computational Physics, v470 (2022), 111591.
- 11. Ziyao Xu and Chi-Wang Shu, High order conservative positivity-preserving discontinuous Galerkin method for stationary hyperbolic equations, Journal of Computational Physics, v466 (2022), 111410.
- 12. Hui Guo, Wenjing Feng, Ziyao Xu and Yang Yang, Conservative numerical methods for the reinterpreted discrete fracture model on non-conforming meshes and their applications in contaminant transportation in fractured porous media, Advances in Water Resources, v153 (2021), 103951.
- 13. Ziyao Xu and Yang Yang, The hybrid dimensional representation of permeability tensor: A reinterpretation of the discrete fracture model and its extension on nonconforming meshes, Journal of Computational Physics, v415 (2020), 109523.
- 14. Ziyao Xu, Yang Yang and Hui Guo, *High-order bound-preserving discontinuous Galerkin methods for wormhole propagation on triangular meshes*, Journal of Computational Physics, v390 (2019), pp.323-341.
- 15. Nattaporn Chuenjarern, Ziyao Xu and Yang Yang, High-order bound-preserving discontinuous Galerkin methods for compressible miscible displacements in porous media on triangular meshes, Journal of Computational Physics, v378 (2019), pp.110-128.
- 16. Hui Guo, Lulu Tian, Ziyao Xu, Yang Yang and Ning Qi, *High-order local discontinuous Galerkin method for simulating wormhole propagation*, Journal of Computational and Applied Mathematics, v350 (2019), pp.247-261.

Conference Proceedings

1. Ziyao Xu and Yang Yang, The hybrid-dimensional Darcy's law: A non-conforming reinterpreted discrete fracture model (RDFM) for the compressible miscible displacement and multicomponent gas flow in fractured media, SPE Reservoir Simulation Conference, (2023), SPE-212164-MS.

Presentations(Selected)

- SIAM Southeastern Atlantic Section (SEAS), The University of Tennessee, Knoxville, Mar 21-23, 2025. Presentation: Stability and Time-Step Constraints of Exponential Time Differencing Runge-Kutta Discontinuous Galerkin Methods for Advection-Diffusion Equations.
- The third North American High Order Methods Conference (NAHOMCon), Dartmouth College, Hanover, New Hampshire, June 17-19, 2024.

 Presentation: An Interior Penalty Discontinuous Galerkin (IPDG) Method for an Interface Model of Flow in

Fractured Porous Media.

- The 8th Annual Meeting of SIAM Central States Section, Lincoln, Nebraska, October 7-8, 2023. Presentation: A high-order well-balanced discontinuous Galerkin method for hyperbolic balance laws with non-hydrostatic equilibria.
- SPE Reservoir Simulation Conference, Galveston, Texas, March 28-30, 2023.

 Poster: The Hybrid-Dimensional Darcy's Law: A Non-Conforming Reinterpreted Discrete Fracture Model (RDFM) for the Compressible Miscible Displacement and Multicomponent Gas Flow in Fractured Media.
- CSCDR Seminar, Umass Dartmouth, North Dartmouth, MA, October 19, 2022.

 Presentation: On the Conservation and Lax-Wendroff Theorem of Positivity-preserving Discontinuous Galerkin Methods for Stationary Hyperbolic Equations.
- 2022 SIAM Annual Meeting, July 11-15, 2022. Co-organizer of MS8, MS23, MS49: Recent Advances in Computational Geosciences.
 - Presentation: A Reinterpreted Discrete Fracture Model for Fracture and Barrier Networks on Non-Conforming Meshes.
- Copper Country Workshop on Applied Mathematics, Statistics, and Data Sciences, Michigan Technologycal University, Houghton, MI, July 5-7, 2022.
 Presentation: High Order Conservative Positivity-Preserving Discontinuous Galerkin Method for Stationary
- Hyperbolic Equations.

 2021 SIAM Annual Meeting, July 19-24, 2021. Organizer of MS9: Models and Numerical Methods in
 - Computational Geosciences.

 Presentation: The Hybrid-Dimensional Darcy's Law: A Novel Discrete Fracture Model for Fracture and Barrier Networks on Non-Conforming Meshes.
- 2021 SIAM Conference on Mathematical & Computational Issues in the Geosciences, June 21-24, 2021.
 Presentation: The Hybrid-Dimensional Representation of Permeability Tensor: A Reinterpretation of the Discrete Fracture Model and its Extension on Nonconforming Meshes.
- 2019 SIAM Conference on Computational Science and Engineering, Spokane Convention Center, Spokane, WA, February 25 March 1, 2019. Organizer of MS329: Recent Advances in Discontinuous Galerkin Methods for Partial Differential Equations.
 - Presentation: High-Order Bound-Preserving Discontinuous Galerkin Method for Wormhole Propagation Model.

TEACHING EXPERIENCE

- ACMS 30530 Introduction to Probability, Lecturer, University of Notre Dame, Spring 2025
- ACMS 40630/60630 Nonlinear Dynamical Systems, Lecturer, University of Notre Dame, Fall 2023, Fall 2024
- ACMS 20620 Applied Linear Algebra, Lecturer, University of Notre Dame, Spring 2024
- APMA 0350 Applied Ordinary Differential Equations, TA, Brown University, Spring 2021
- APMA 1170 Introduction to Computational Linear Algebra, TA, Brown University, Fall 2020
- MA 2160 Calculus 2, Lecturer, Michigan Technological University, Spring 2018, Spring 2019
- MA 1135 Calculus for Life Sciences, Lecturer, Michigan Technological University, Fall 2018

Honors & Awards

- David Gottlieb Memorial Award, Division of Applied Mathematics, Brown University, 2023.
- Outstanding Research Award, Department of Mathematical Sciences, Michigan Technological University, 2019
- The First Prize Scholarship, China University of Petroleum, 2015
- National Scholarship, China, 2013, 2014

Skills

- Programming: Matlab, Julia, Python, C, LaTeX
- Languages: Mandarin (native), English (proficient)