



Hacettepe University

Department of Electrical and Electronics Engineering

ELE 409 Digital Signal Processing Laboratory

EXPERIMENT 1 – THE DFT and ITS PROPERTIES
PRELIMINARY WORK

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7/11/2022

1)

Function :

```
function x=SinSamples(A,w,teta,d,ws)
fs=ws/(2*pi); % sampling frequency
ts=1/fs; % sampling period
n=0:1:ts-1; %number of sample
x=A*sin(w*n+teta);
end
```

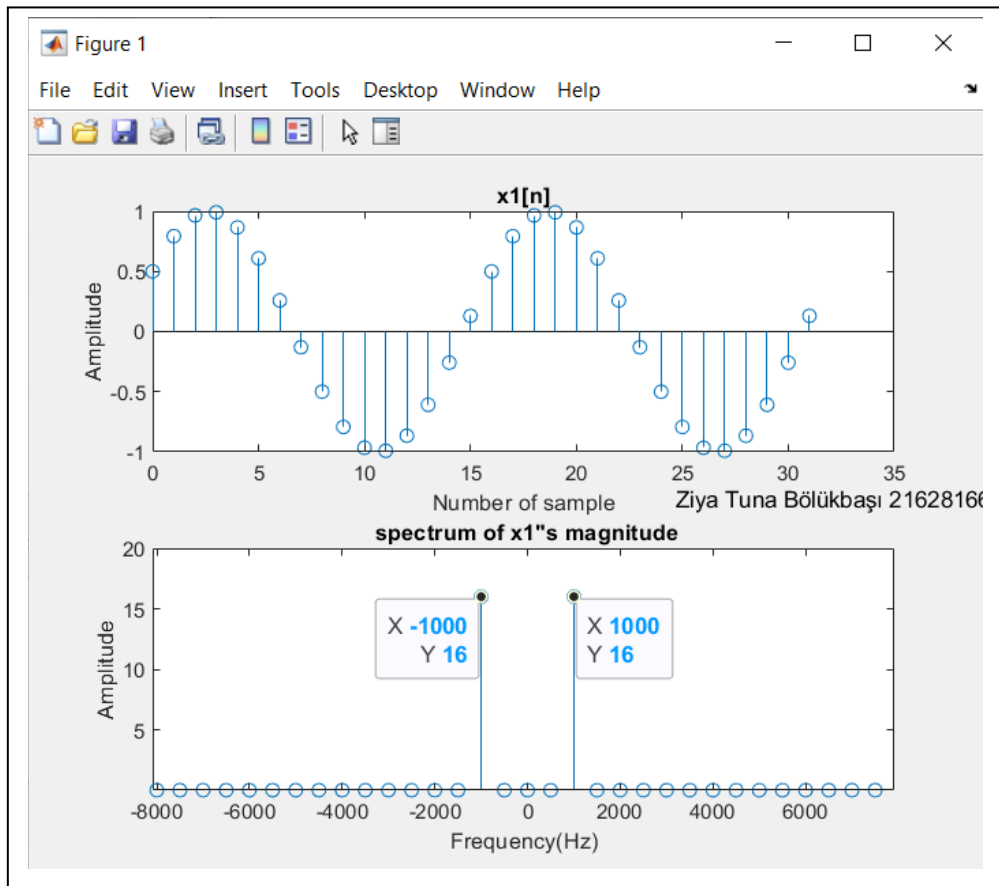
2)

Matlab Code :

a)

```
clc;
clear all;
close all;
fs=16000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,pi/6,0.002,2*pi*16000);
[ans2,n2]=sinsamplesfunction(1,2*pi*1000,0,0.002,2*pi*16000);
fft_ans1=fft(ans1);
fft_ans2=fft(ans2);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans2=fftshift(abs(fft_ans2));
length1=length(shift_fft_ans1);
length2=length(shift_fft_ans2);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency2=-fs/2:fs/length2:fs/2-fs/length2;
figure;

subplot(2,1,1);
stem(n1,ans1);
title('x1[n]');
xlabel('Number of sample');
ylabel('Amplitude');
subplot(2,1,2);
stem(range_of_frequency1,shift_fft_ans1);
title(' spectrum of x1"s magnitue');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')
```



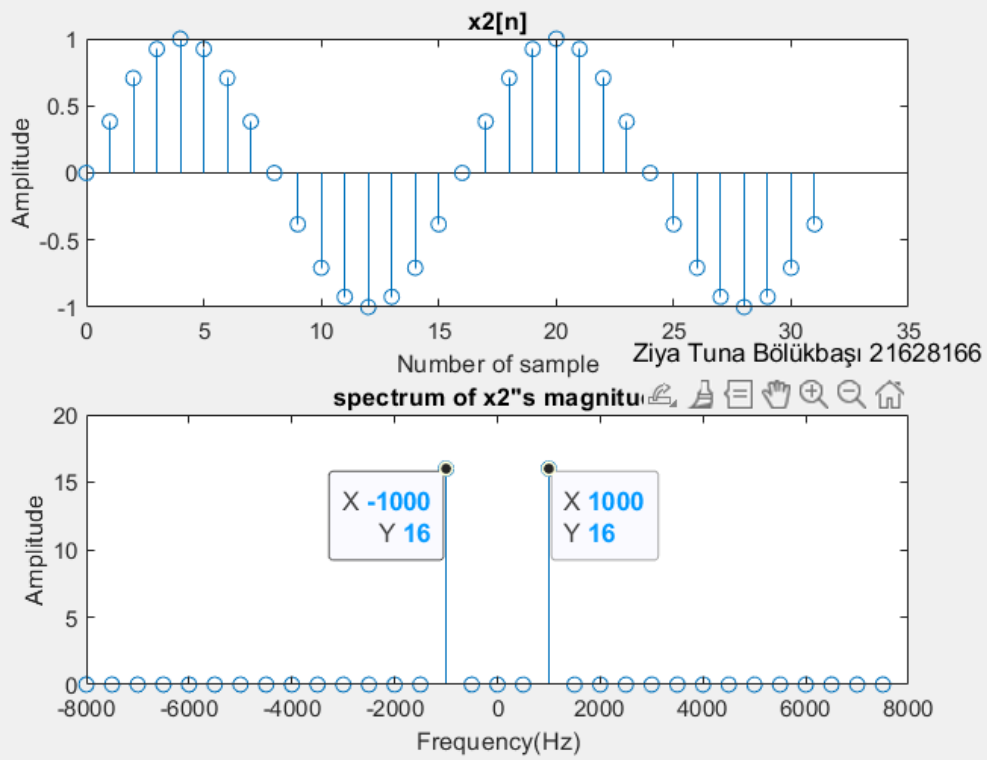
b)

```
clc;
clear all;
close all;
fs=16000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,pi/6,0.002,2*pi*16000);
[ans2,n2]=sinsamplesfunction(1,2*pi*1000,0,0.002,2*pi*16000);
fft_ans1=fft(ans1);
fft_ans2=fft(ans2);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans2=fftshift(abs(fft_ans2));
length1=length(shift_fft_ans1);
length2=length(shift_fft_ans2);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency2=-fs/2:fs/length2:fs/2-fs/length2;
figure;

subplot(2,1,1);
stem(n2,ans2);
title('x2[n]');
xlabel('Number of sample');
ylabel('Amplitude');
subplot(2,1,2);
stem(range_of_frequency2,shift_fft_ans2);
title(' spectrum of x2"s magnitude');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')
```

Figure 1

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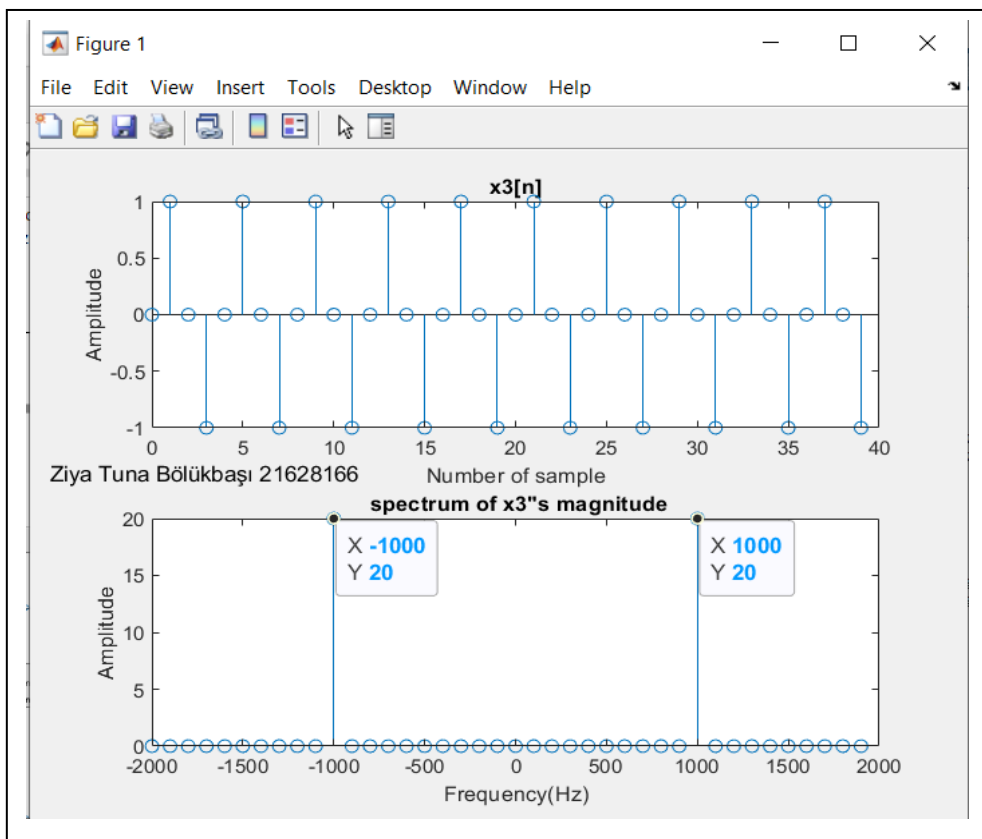


3)

Matlab code:

a)

```
clc;
clear all;
close all;
fs=4000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,0,0.01,2*pi*4000);
[ans2,n2]=sinsamplesfunction(1,2*pi*5000,0,0.01,2*pi*4000);
fft_ans1=fft(ans1);
fft_ans2=fft(ans2);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans2=fftshift(abs(fft_ans2));
length1=length(shift_fft_ans1);
length2=length(shift_fft_ans2);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency2=-fs/2:fs/length2:fs/2-fs/length2;
figure;
subplot(2,1,1);
stem(n1,ans1);
title('x3[n]');
xlabel('Number of sample');
ylabel('Amplitude');
subplot(2,1,2);
stem(range_of_frequency1,shift_fft_ans1);
title(' spectrum of x3"s magnitude');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')
```



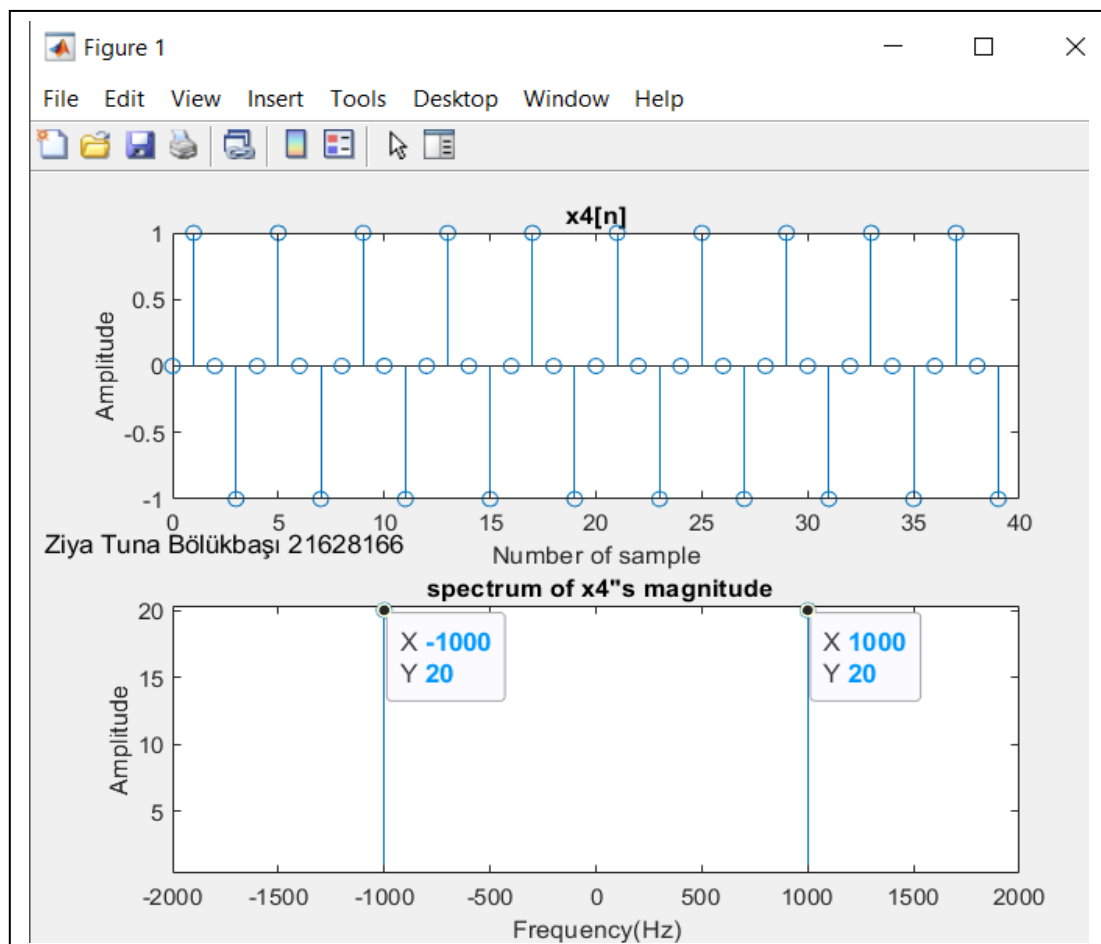
b)

```

clc;

clear all;
close all;
fs=4000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,0,0.01,2*pi*4000);
[ans2,n2]=sinsamplesfunction(1,2*pi*5000,0,0.01,2*pi*4000);
fft_ans1=fft(ans1);
fft_ans2=fft(ans2);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans2=fftshift(abs(fft_ans2));
length1=length(shift_fft_ans1);
length2=length(shift_fft_ans2);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency2=-fs/2:fs/length2:fs/2-fs/length2;
figure;
subplot(2,1,1);
stem(n2,ans2);
title('x4[n]');
xlabel('Number of sample');
ylabel('Amplitude');
subplot(2,1,2);
stem(range_of_frequency2,shift_fft_ans2);
title(' spectrum of x4"s magnitude');
xlabel('Frequency(Hz)')
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')

```



Sample frequency should be less than twice original frequency, according to Nyquist theorem. In first of these examples there is no issue but in second example, there is a contradiction in this theorem. Aliasing appears in second case because of this. In frequency domain, frequency of both cases is same.

4)

```

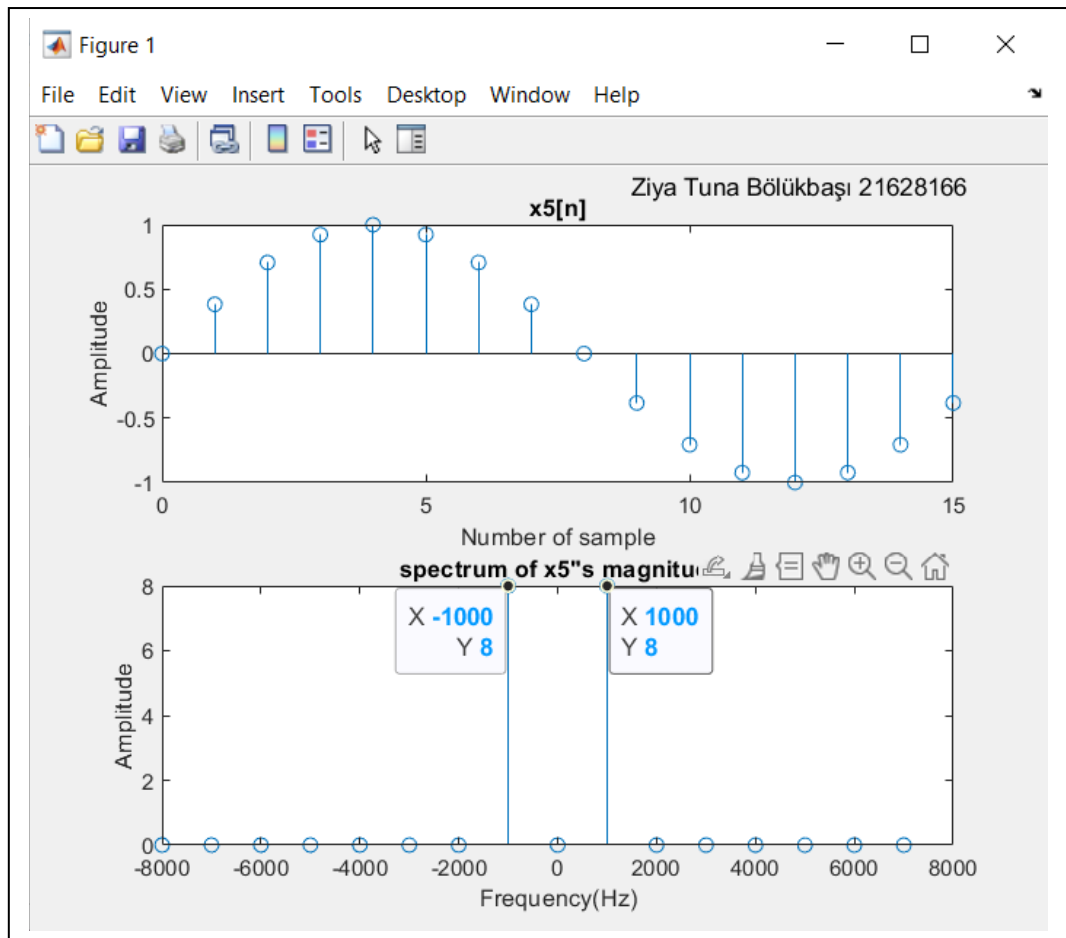
clc;
clear all;
close all;
fs=16000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,0,0.001,2*pi*16000);
[ans2,n2]=sinsamplesfunction(1,2*pi*1000,0,0.0015,2*pi*16000);
[ans3,n3]=sinsamplesfunction(1,2*pi*1000,0,0.002,2*pi*16000);
fft_ans1=fft(ans1);
fft_ans2=fft(ans2);
fft_ans3=fft(ans3);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans2=fftshift(abs(fft_ans2));
shift_fft_ans3=fftshift(abs(fft_ans3));
length1=length(shift_fft_ans1);
length2=length(shift_fft_ans2);
length3=length(shift_fft_ans3);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency2=-fs/2:fs/length2:fs/2-fs/length2;
range_of_frequency3=-fs/2:fs/length2:fs/2-fs/length3;
figure;
% a;
subplot(2,1,1);
stem(n1,ans1);
title('x5[n]');
xlabel('Number of sample');
ylabel('Amplitude');
subplot(2,1,2);
stem(range_of_frequency1,shift_fft_ans1);
title(' spectrum of x5"s magnitude');
xlabel('Frequency(Hz)')
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')

% b;
% subplot(2,1,1);
% stem(n2,ans2);
% title('x6[n]');
% xlabel('Number of sample');
% ylabel('Amplitude');
% subplot(2,1,2);
% stem(range_of_frequency2,shift_fft_ans2);
% title(' spectrum of x6"s magnitude');
% xlabel('Frequency(Hz)')
% ylabel('Amplitude')
% gtext('Ziya Tuna Bölükbaşı 21628166')

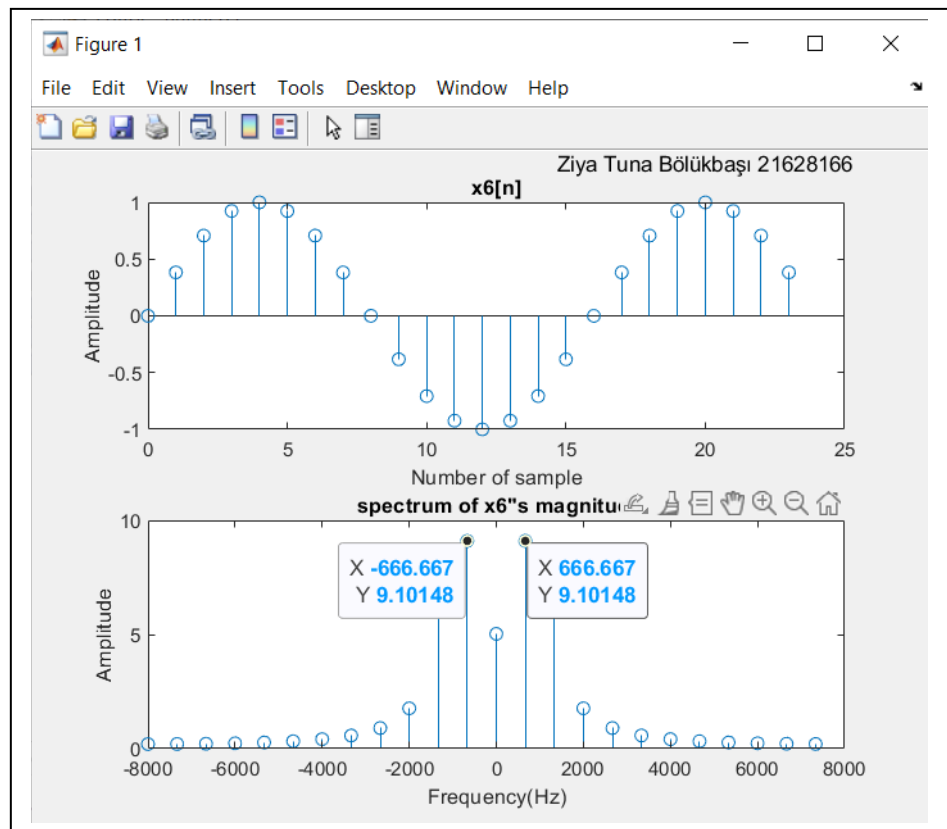
% c
% subplot(2,1,1);
% stem(n3,ans3);
% title('x7[n]');
% xlabel('Number of sample');
% ylabel('Amplitude');
% subplot(2,1,2);
% stem(range_of_frequency3,shift_fft_ans3);
% title(' spectrum of x7"s magnitude');
% xlabel('Frequency(Hz)')
% ylabel('Amplitude')
% gtext('Ziya Tuna Bölükbaşı 21628166')

```

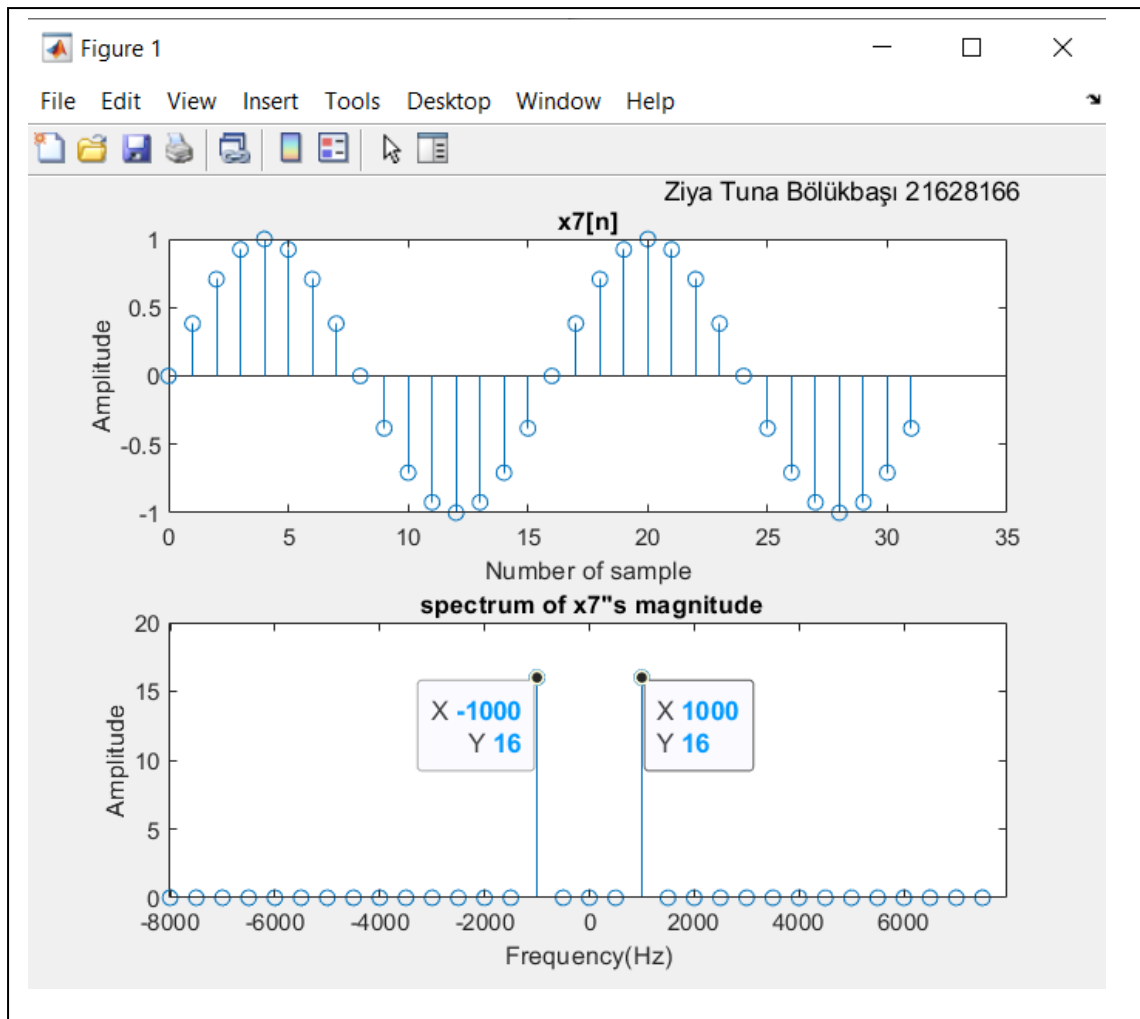
a)



b)



c)



In this problem we observe that vector needs to be an exact power of two in order to use fft. Magnitude spectrum are computed using fft. We could use ft because $x_5[n]$ and $x_7[n]$ signals provided in this question are exactly equivalent to Powers of two but $x_6[n]$. Because signal is not a power of two we were unable to determine spectrum using fft.

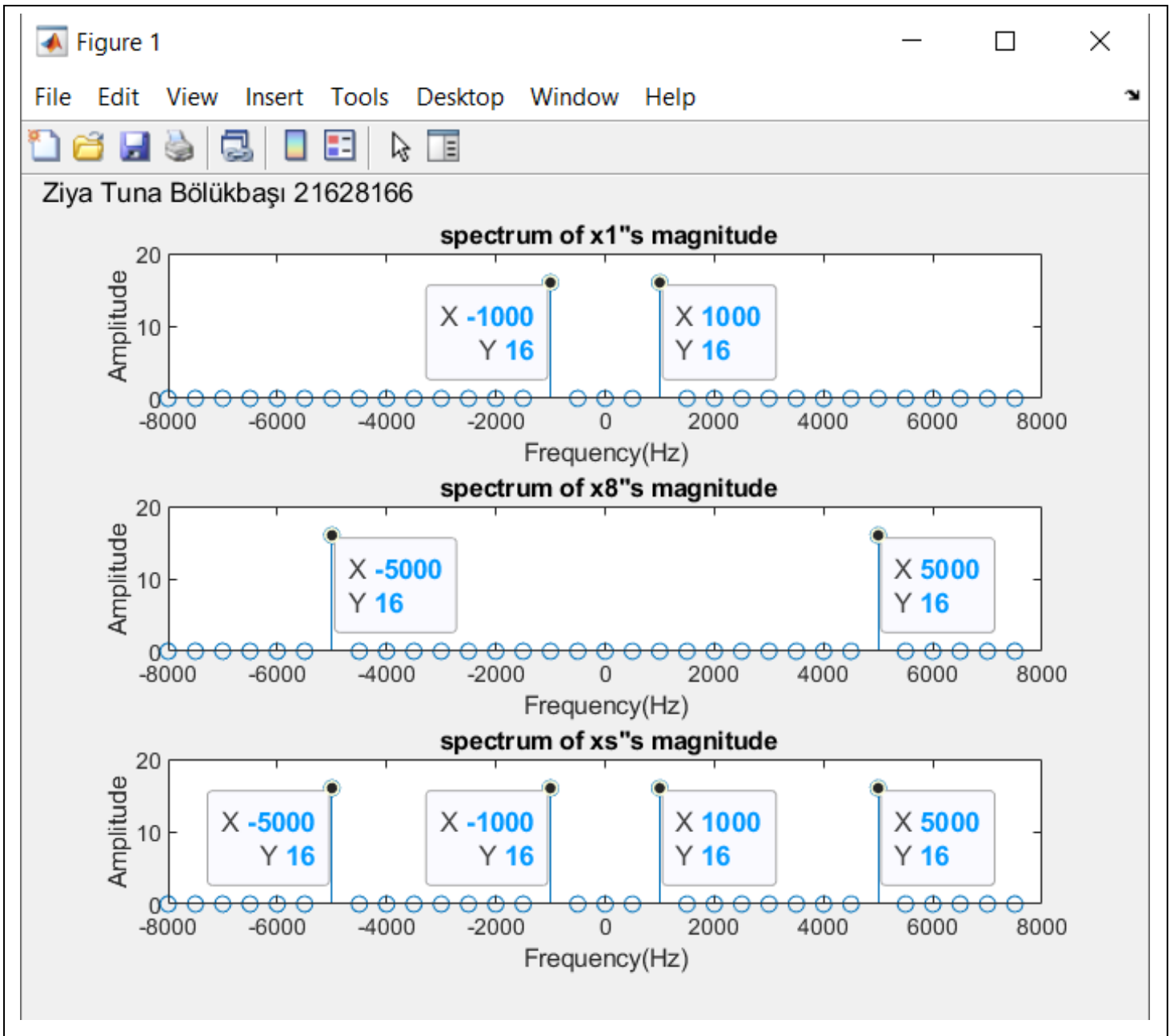
5)

Matlab code:

```
clc;
clear all;
close all;
fs=16000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,pi/6,0.002,2*pi*16000);
[ans8,n2]=sinsamplesfunction(1,2*pi*5000,pi/6,0.002,2*pi*16000);
x_s=ans1+ans8;
fft_ans1=fft(ans1);
fft_ans8=fft(ans8);
fft_ans_s=fft(x_s);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans8=fftshift(abs(fft_ans8));
shift_fft_ans_s=fftshift(abs(fft_ans_s));
length1=length(shift_fft_ans1);
length8=length(shift_fft_ans8);
length_s=length(shift_fft_ans_s);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency8=-fs/2:fs/length8:fs/2-fs/length8;
range_of_frequency_s=-fs/2:fs/length_s:fs/2-fs/length_s;
figure;
subplot(3,1,1);
stem(range_of_frequency1,shift_fft_ans1);
title(' spectrum of x1"s magnitude');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')

subplot(3,1,2);
stem(range_of_frequency8,shift_fft_ans8);
title(' spectrum of x8"s magnitude');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')

subplot(3,1,3);
stem(range_of_frequency_s,shift_fft_ans_s);
title(' spectrum of xs"s magnitude');
xlabel('Frequency(Hz) ');
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')
```



We can observe that dtft of sum of two waves is equal to sum of dtft of same two signals. As a result we prove dtft's linearity.

6)

Matlab Code:

```
clc;
clear all;
close all;
fs=16000;
[ans1,n1]=sinsamplesfunction(1,2*pi*1000,pi/6,0.002,2*pi*16000)
;
[ans8,n2]=sinsamplesfunction(1,2*pi*5000,pi/6,0.002,2*pi*16000)
;
x_s=ans1.*ans8;
fft_ans1=fft(ans1);
fft_ans8=fft(ans8);
fft_ans_s=fft(x_s);
shift_fft_ans1=fftshift(abs(fft_ans1));
shift_fft_ans8=fftshift(abs(fft_ans8));
shift_fft_ans_s=fftshift(abs(fft_ans_s));
length1=length(shift_fft_ans1);
length8=length(shift_fft_ans8);
length_s=length(shift_fft_ans_s);
range_of_frequency1=-fs/2:fs/length1:fs/2-fs/length1;
range_of_frequency8=-fs/2:fs/length8:fs/2-fs/length8;
range_of_frequency_s=-fs/2:fs/length_s:fs/2-fs/length_s;
figure;
subplot(3,1,1);
stem(range_of_frequency1,shift_fft_ans1);
title(' spectrum of x1"s magnitude');
xlabel('Frequency(Hz) ')
ylabel('Amplitude')

subplot(3,1,2);
stem(range_of_frequency8,shift_fft_ans8);
title(' spectrum of x8"s magnitude');
xlabel('Frequency(Hz) ')
ylabel('Amplitude')

subplot(3,1,3);
stem(range_of_frequency_s,shift_fft_ans_s);
title(' spectrum of xs"s magnitude');
xlabel('Frequency(Hz) ')
ylabel('Amplitude')
gtext('Ziya Tuna Bölükbaşı 21628166')
```



Multiplication in time domain corresponds to convolution in frequency domain.

$$5\text{kHz} + 1\text{kHz} = 6\text{kHz}$$

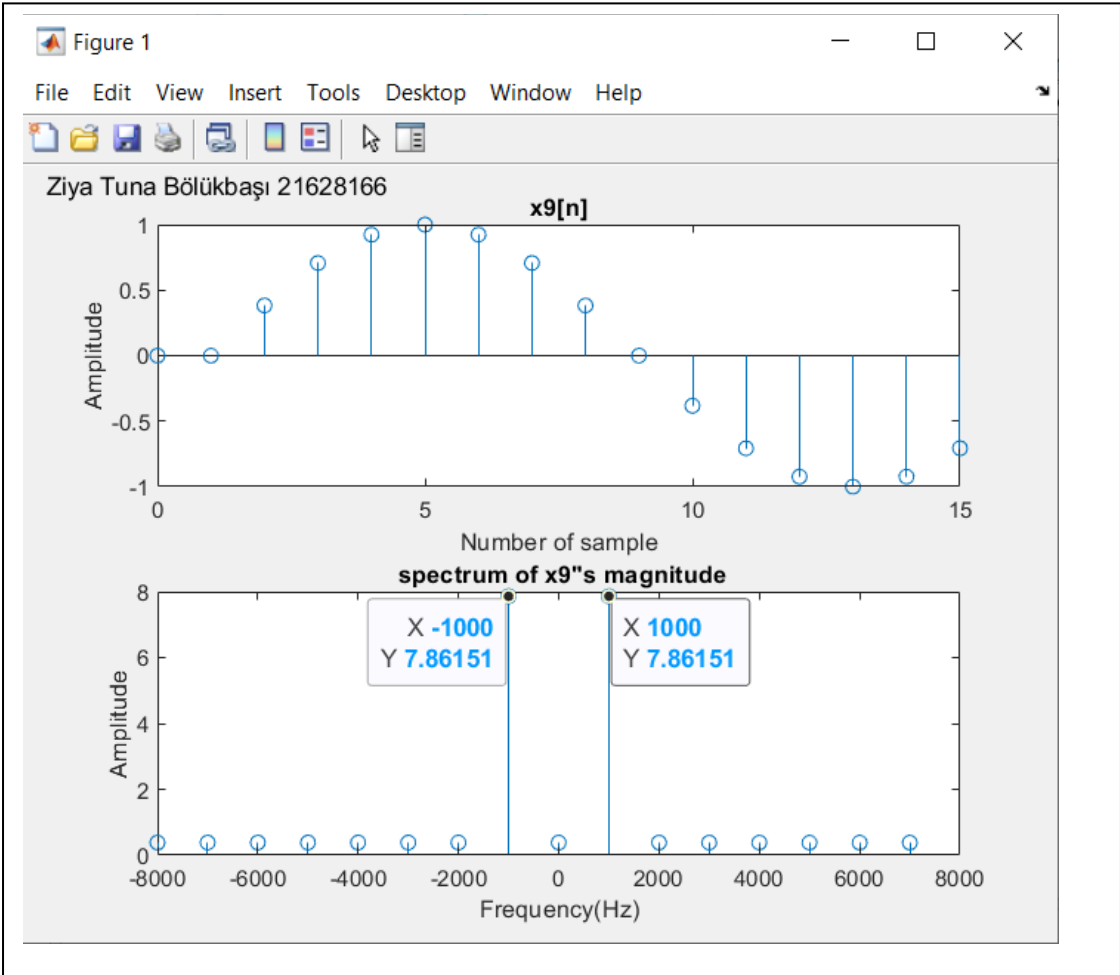
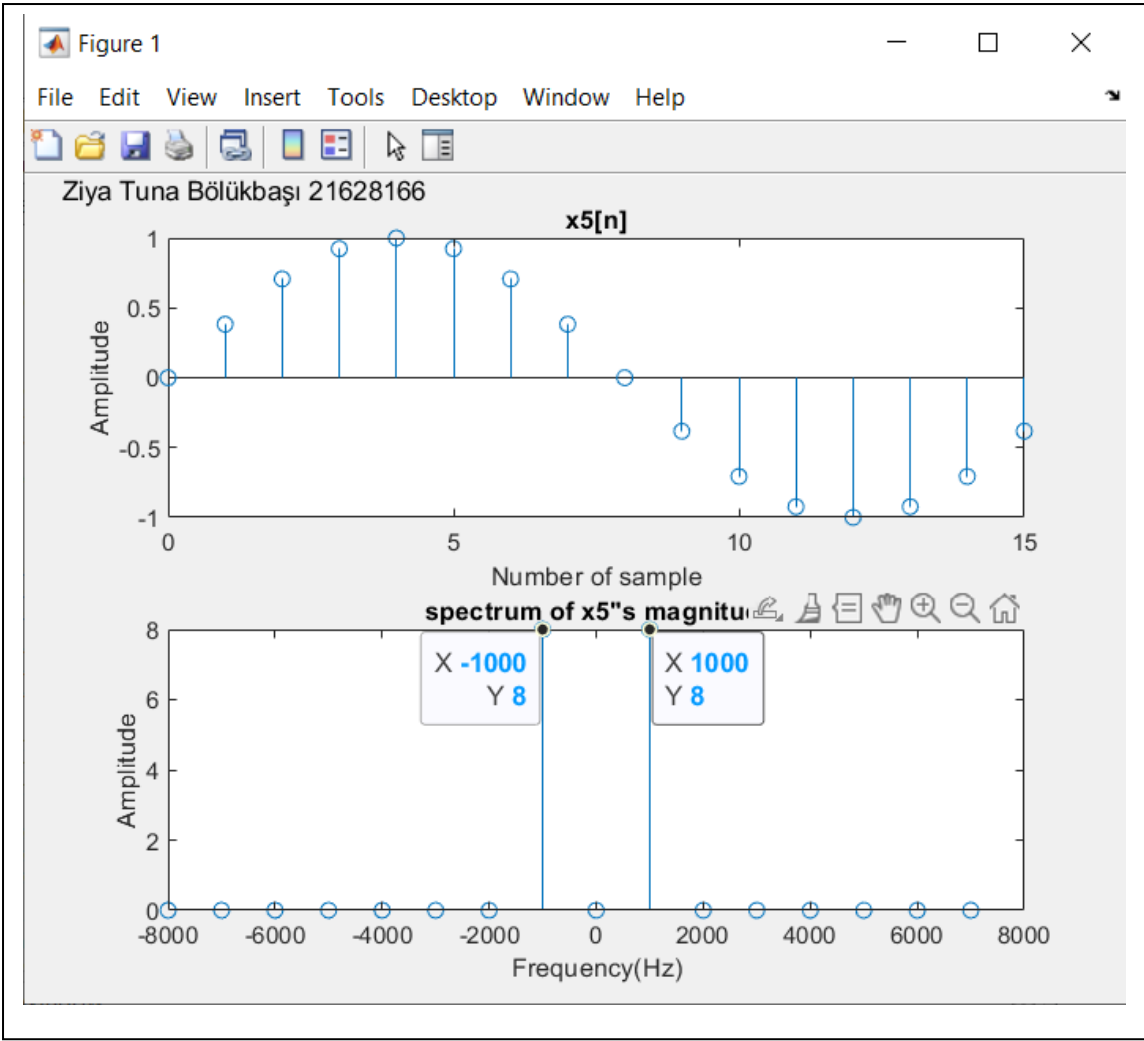
$$5\text{kHz} - 1\text{kHz} = 4\text{kHz}$$

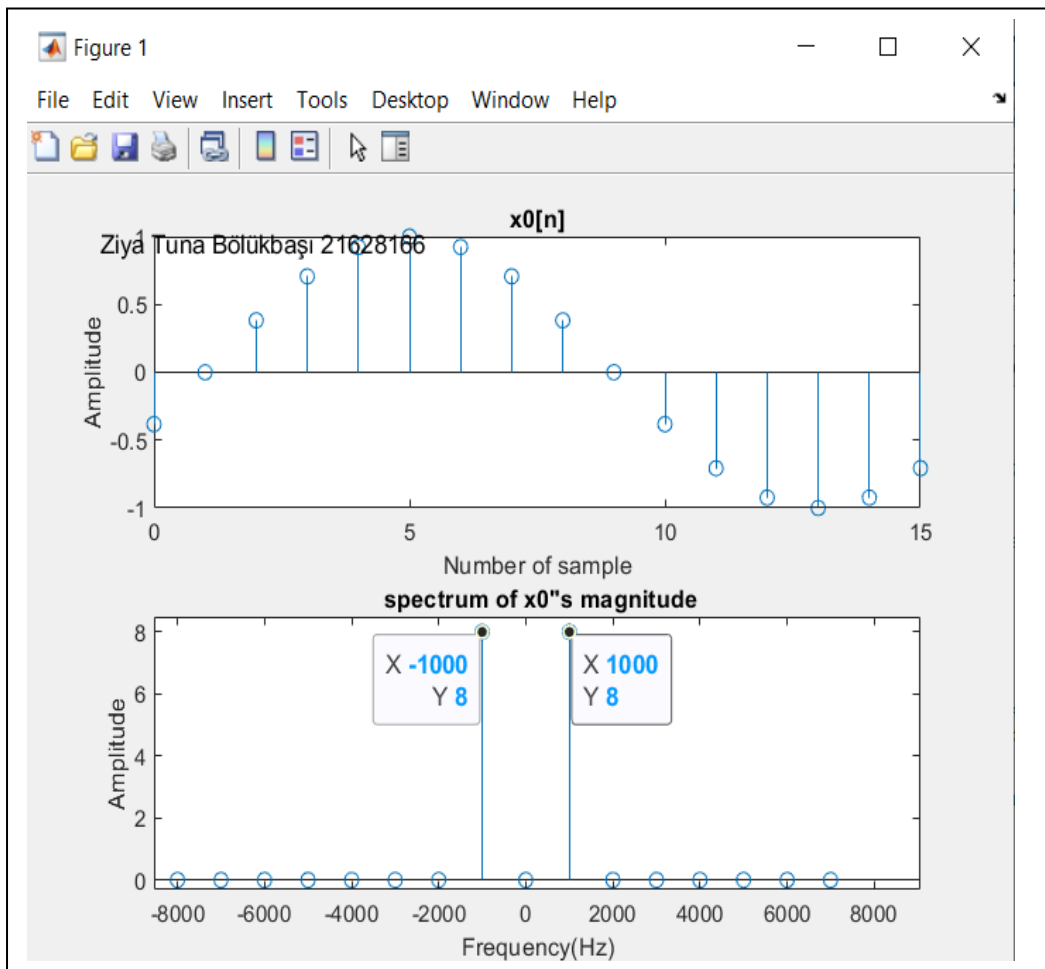
$$(-5\text{kHz}) + (-1\text{kHz}) = -6\text{kHz}$$

$$(-5\text{kHz}) - (-1\text{kHz}) = -4\text{kHz}$$

7)

```
clc;
clear all;
close all;
fs=16000;
[ans5,n5]=sinsamplesfunction(1,2*pi*1000,0,0.001,2*pi*16000);
l_ans5=length(ans5);
n9=zeros(1,l_ans5);
for x=2:l_ans5
    ans9(x)=ans5(x-1);
end
ans0=circshift(ans5,1);
fft_ans5=fft(ans5);
fft_ans9=fft(ans9);
fft_ans0=fft(ans0);
shift_fft_ans5=fftshift(abs(fft_ans5));
shift_fft_ans9=fftshift(abs(fft_ans9));
shift_fft_ans0=fftshift(abs(fft_ans0));
length5=length(shift_fft_ans5);
length9=length(shift_fft_ans9);
length0=length(shift_fft_ans0);
range_of_frequency5=-fs/2:fs/length5:fs/2-fs/length5;
range_of_frequency9=-fs/2:fs/length9:fs/2-fs/length9;
range_of_frequency0=-fs/2:fs/length0:fs/2-fs/length0;
%subplot(2,1,1);
%stem(n5,ans5);
%title('x5[n]');
%xlabel('Number of sample');
%ylabel('Amplitude');
%subplot(2,1,2);
%stem(range_of_frequency5,shift_fft_ans5);
%title(' spectrum of x5"s magnitude');
%xlabel('Frequency(Hz)');
%ylabel('Amplitude')
% gtext('Ziya Tuna Bölükbaşı 21628166')
% subplot(2,1,1);
% stem(n9,ans9);
% title('x9[n]');
% xlabel('Number of sample');
% ylabel('Amplitude');
% subplot(2,1,2);
% stem(range_of_frequency9,shift_fft_ans9);
% title(' spectrum of x9"s magnitude');
% xlabel('Frequency(Hz)');
% ylabel('Amplitude')
% gtext('Ziya Tuna Bölükbaşı 21628166')
% subplot(2,1,1);
% stem(n0,ans0);
% title('x0[n]');
% xlabel('Number of sample');
% ylabel('Amplitude');
% subplot(2,1,2);
% stem(range_of_frequency0,shift_fft_ans0);
% title(' spectrum of x0"s magnitude');
% xlabel('Frequency(Hz)');
% ylabel('Amplitude')
% gtext('Ziya Tuna Bölükbaşı 21628166')
```





The magnitude spectrum is not affected by phase shift.

8)

```
clc;
clear all;
close all;
[y1,fs]=audioread('C:\Users\Tuna\OneDrive -
hacettepe.edu.tr\Masaüstü\sound1.wav');
l_y1=length(y1);
sample1=0:1:l_y1-1;

for k=1:512
    y2(k)=y1(k);
end
l_y2=length(y2);
sample2=0:1:l_y2-1;
fft_y2=fft(y2);
shift_fft_y1=fftshift(abs(fft_y2));
lengthy2=length(fft_y2);
range_of_frequency_y2=-fs/2:fs/lengthy2:fs/2-fs/lengthy2;

figure;
plot(sample1,y1);
title('y(t) > Waveform of Sound1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166')

figure;
plot(sample2,y2);
title('New y(t) > Waveform of Sound1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166')

figure;
stem(sample2,y2);
title('New y[n] > WAveform of Sound1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166')

figure;
stem(range_of_frequency_y2,shift_fft_y1);
title('Spectrum of y1 magnitude > Magnitude Spectrum of
Sound1');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166')
```

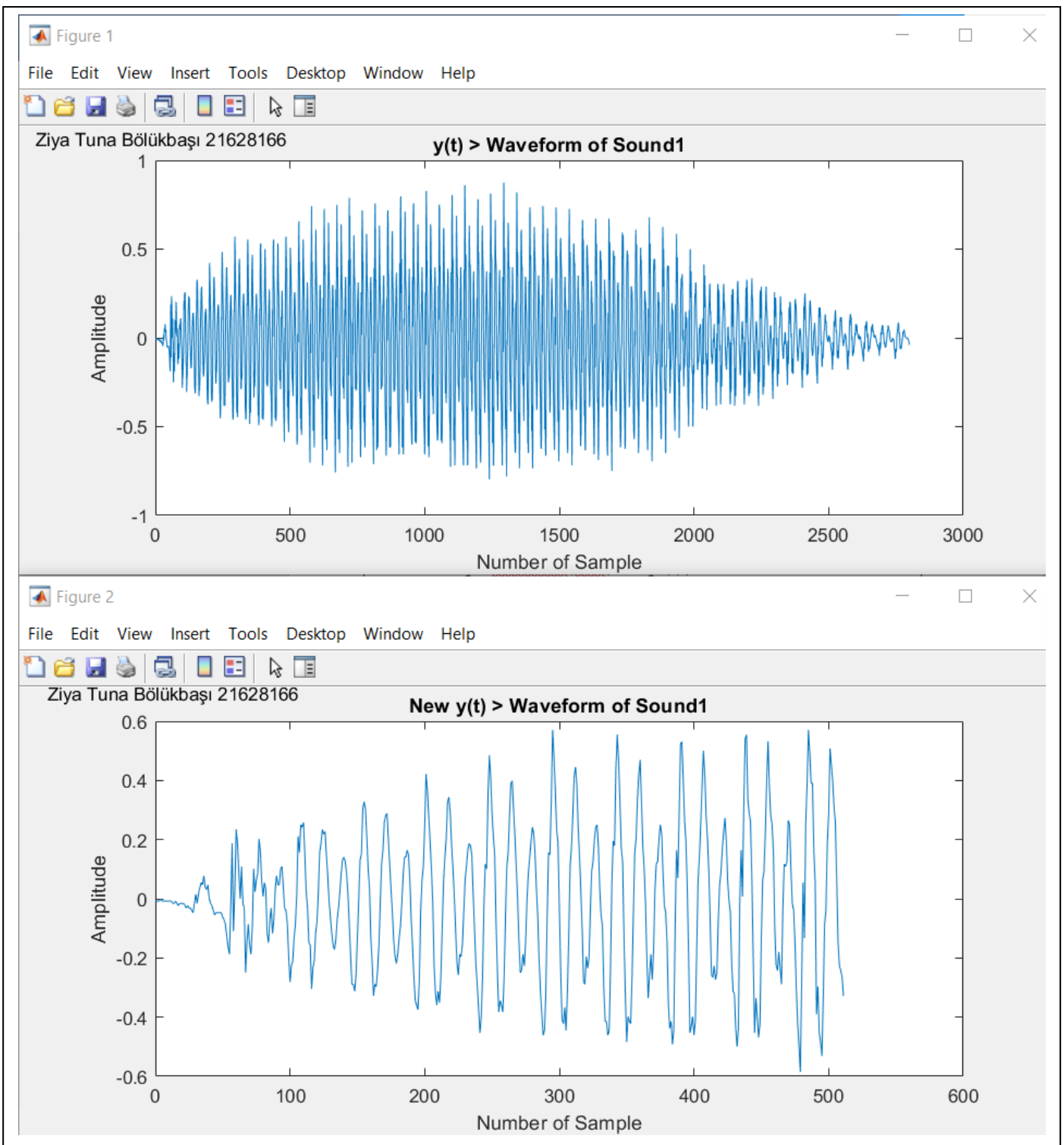


Figure 3

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Ziya Tuna Bölükbaşı 21628166

New y[n] > WAVEform of Sound1

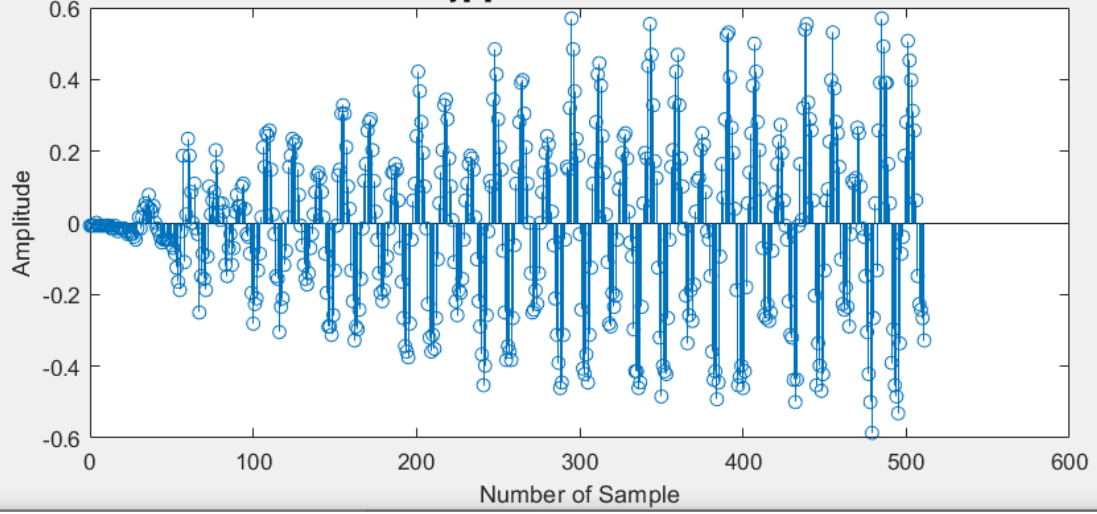
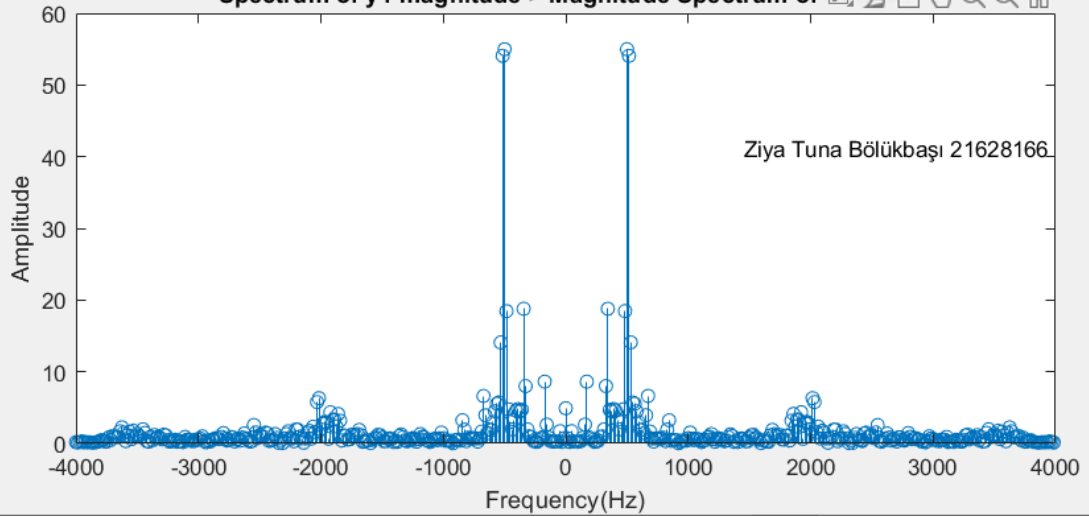


Figure 4

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Spectrum of y1 magnitude > Magnitude Spectrum of



9)

For x10[n] Matlab code

```
clc;
clear all;
close all;
n=0:1:255;
n10= sinc(0.2*(n-128));
length1=length(n10);
sample1=0:1:length1-1;
fs=1/length(n);
xdown1=downsample(n10,2);
length2=length(xdown1);
sample2=0:1:length2-1;
fft_n10=fft(n10);
shift_fft_n10=fftshift(abs(fft_n10));
lengthn10=length(fft_n10);
range_of_frequency_n10=-fs/2:fs/lengthn10:fs/2-fs/lengthn10;
fft_xdown1=fft(xdown1);
shift_fft_xdown1=fftshift(abs(fft_xdown1));
lengthxdown1=length(fft_xdown1);
range_of_frequency_xdown1=-fs/2:fs/lengthxdown1:fs/2-fs/lengthxdown1;
figure;
stem(sample1,n10);
title('x10');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(sample2,xdown1);
title('xdown1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(range_of_frequency_n10,shift_fft_n10);
title('x10 Magnitude Spectrum');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(range_of_frequency_xdown1,shift_fft_xdown1);
title('shift_fft_xdown1 Magnitude Spectrum');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

xinterp1=interp(xdown1,2);
length_xinterp1=length(xinterp1);
sample3=0:1:length_xinterp1-1;
fft_xinterp1=fft(xinterp1);
shift_fft_xinterp1=fftshift(abs(fft_xinterp1));
lengthxinterp1=length(fft_xinterp1);
range_of_frequency_xinterp1=-fs/2:fs/lengthxinterp1:fs/2-fs/lengthxinterp1;

figure;
stem(sample3,xinterp1);
title('xinterp1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');
```

Figure 1

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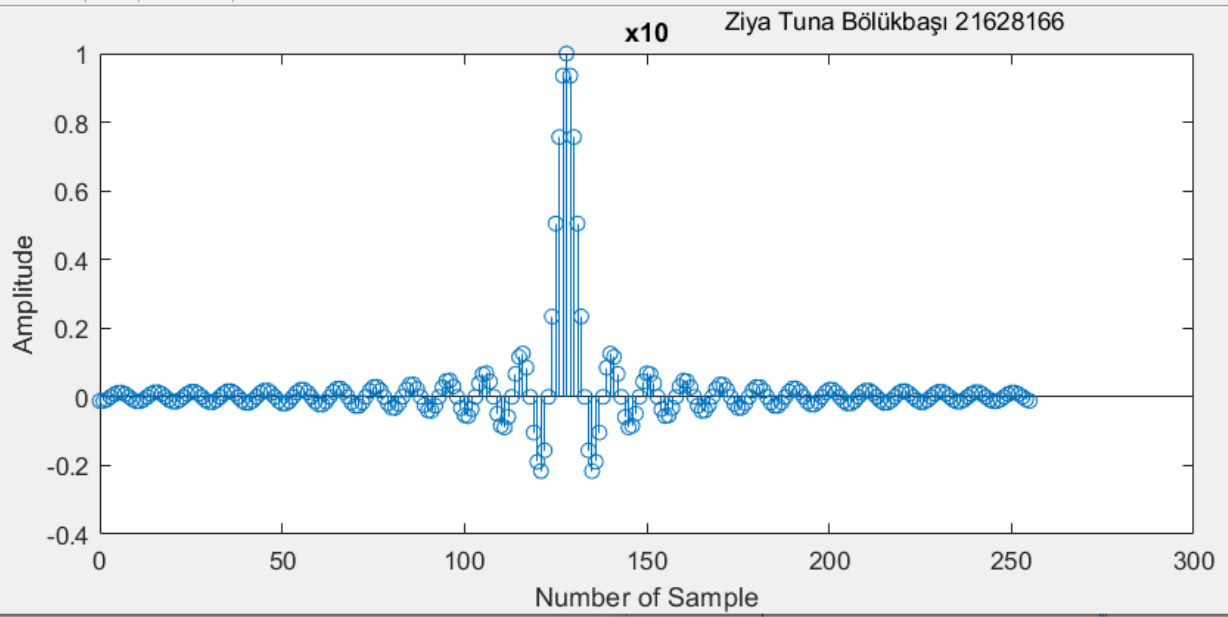


Figure 2

File Edit View Insert Tools Desktop Window Help

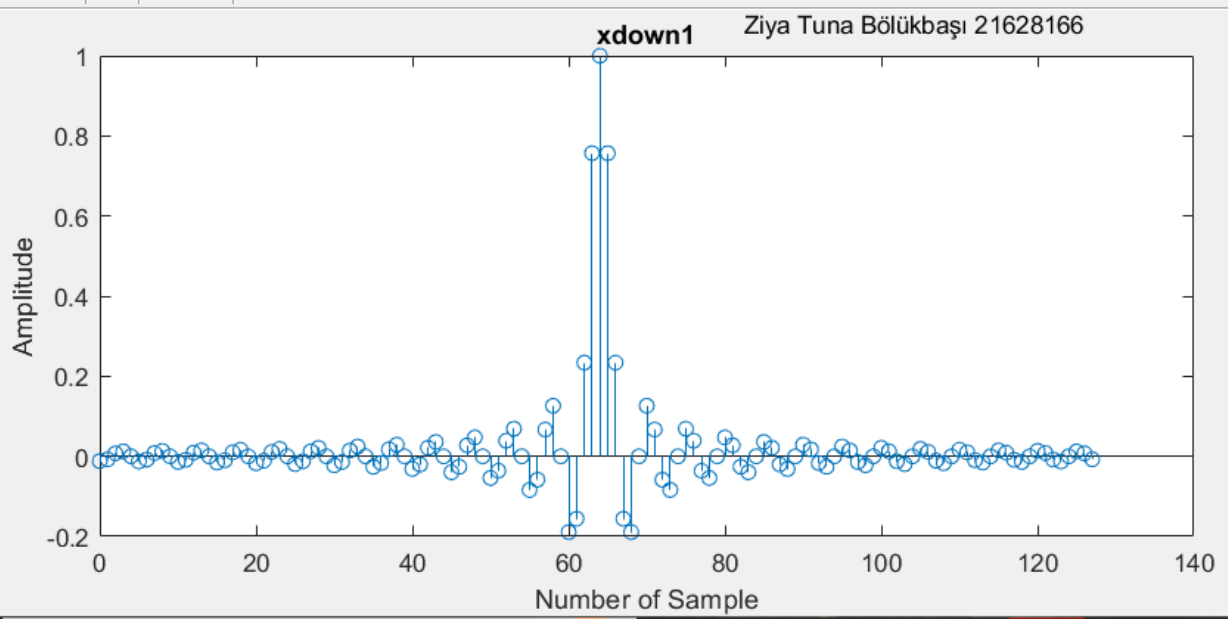


Figure 3

File Edit View Insert Tools Desktop Window Help

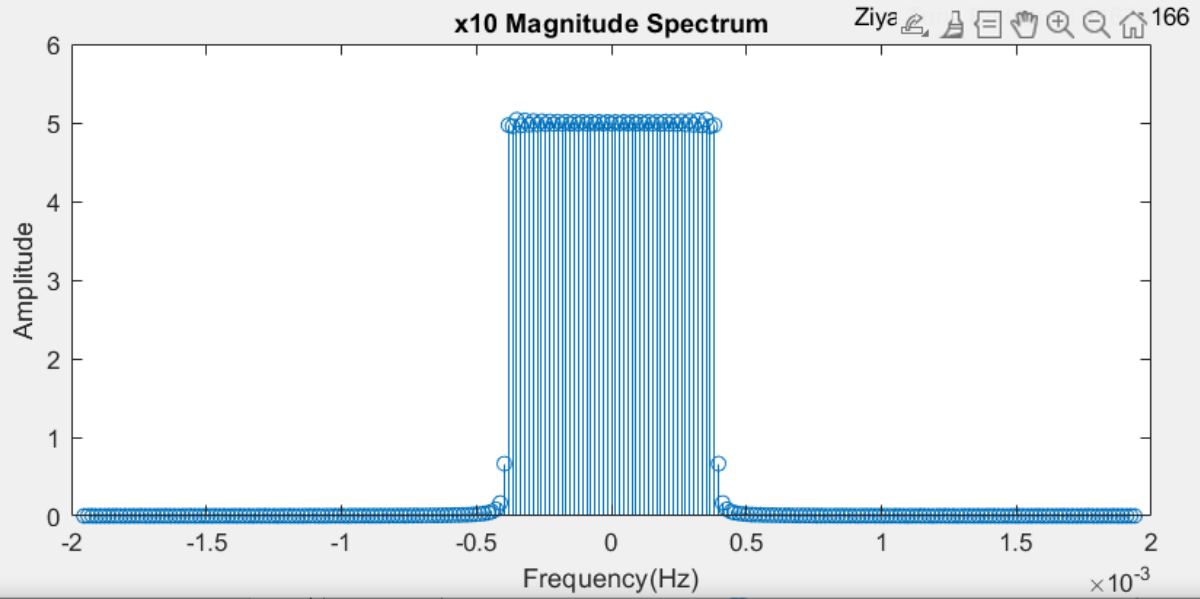


Figure 4

File Edit View Insert Tools Desktop Window Help

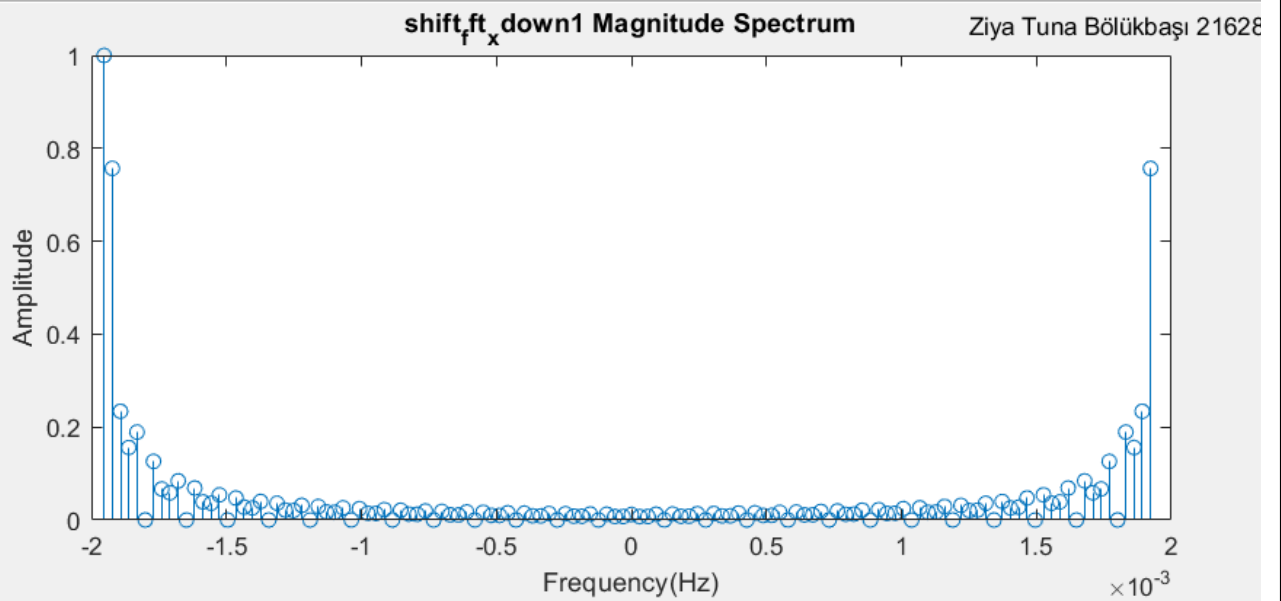


Figure 5

File Edit View Insert Tools Desktop Window Help

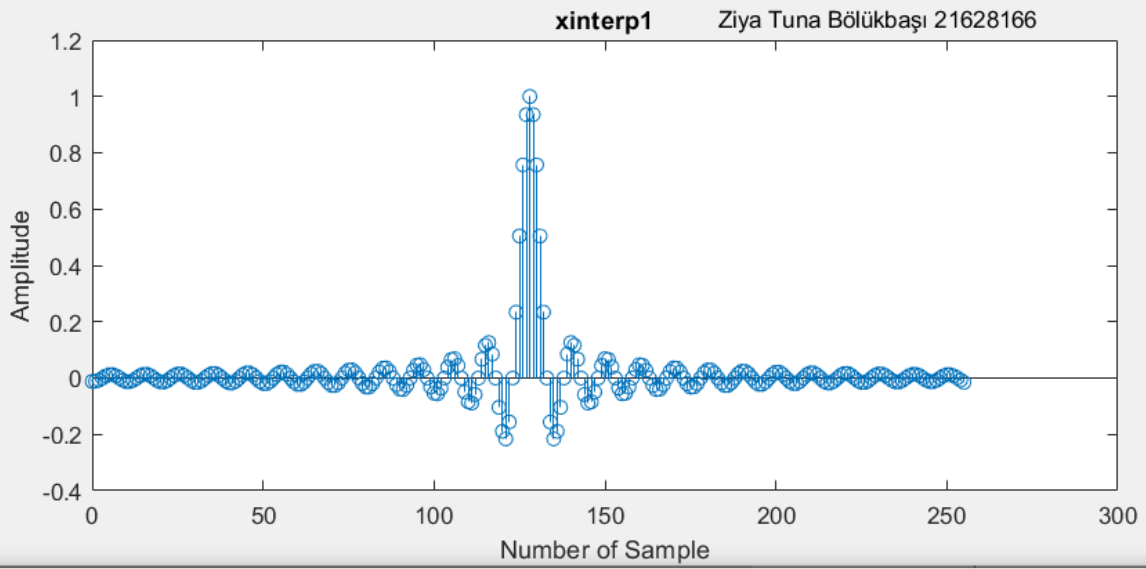
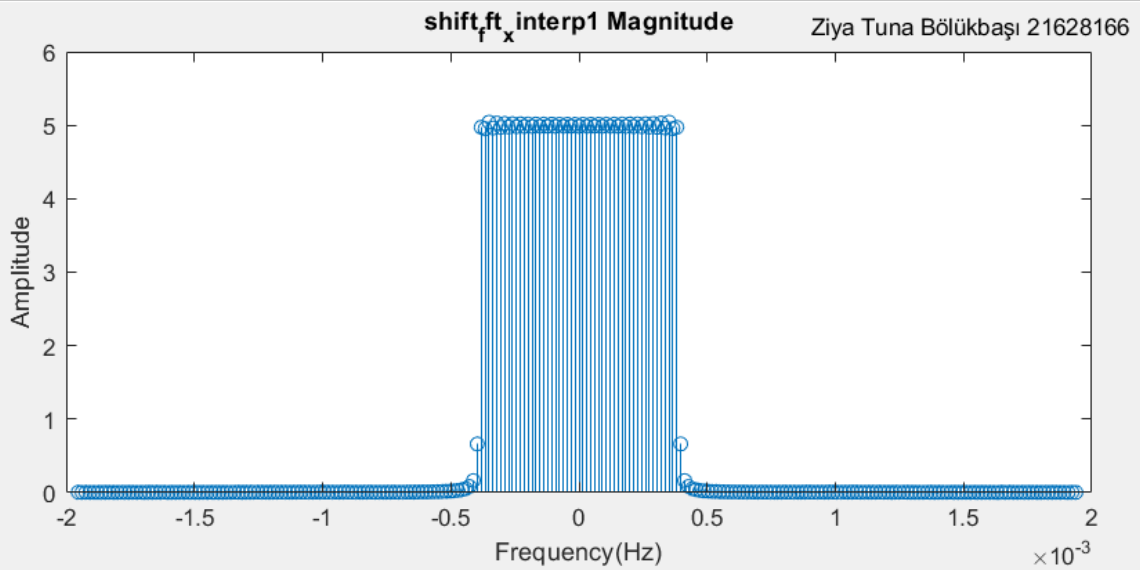


Figure 6

File Edit View Insert Tools Desktop Window Help



10)

For x11[n] Matlab Code

```
clc;
clear all;
close all;
n=0:1:255;
n10= sinc(0.8*(n-128));
length1=length(n10);
sample1=0:1:length1-1;
fs=1/length(n);
xdown1=downsample(n10,2);
length2=length(xdown1);
sample2=0:1:length2-1;
fft_n10=fft(n10);
shift_fft_n10=fftshift(abs(fft_n10));
lengthn10=length(fft_n10);
range_of_frequency_n10=-fs/2:fs/lengthn10:fs/2-fs/lengthn10;
fft_xdown1=fft(xdown1);
shift_fft_xdown1=fftshift(abs(fft_xdown1));
lengthxdown1=length(fft_xdown1);
range_of_frequency_xdown1=-fs/2:fs/lengthxdown1:fs/2-fs/lengthxdown1;
figure;
stem(sample1,n10);
title('x10');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(sample2,xdown1);
title('xdown1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(range_of_frequency_n10,shift_fft_n10);
title('x10 Magnitude Spectrum');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(range_of_frequency_xdown1,shift_fft_xdown1);
title('shift_fft_xdown1 Magnitude Spectrum');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

xinterp1=interp(xdown1,2);
length_xinterp1=length(xinterp1);
sample3=0:1:length_xinterp1-1;
fft_xinterp1=fft(xinterp1);
shift_fft_xinterp1=fftshift(abs(fft_xinterp1));
lengthxinterp1=length(fft_xinterp1);
range_of_frequency_xinterp1=-fs/2:fs/lengthxinterp1:fs/2-fs/lengthxinterp1;

figure;
stem(sample3,xinterp1);
title('xinterp1');
xlabel('Number of Sample');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');

figure;
stem(range_of_frequency_xinterp1,shift_fft_xinterp1);
title('shift_fft_xinterp1 Magnitude');
xlabel('Frequency(Hz)');
ylabel('Amplitude');
gtext('Ziya Tuna Bölükbaşı 21628166');
```


Figure 1

File Edit View Insert Tools Desktop Window Help

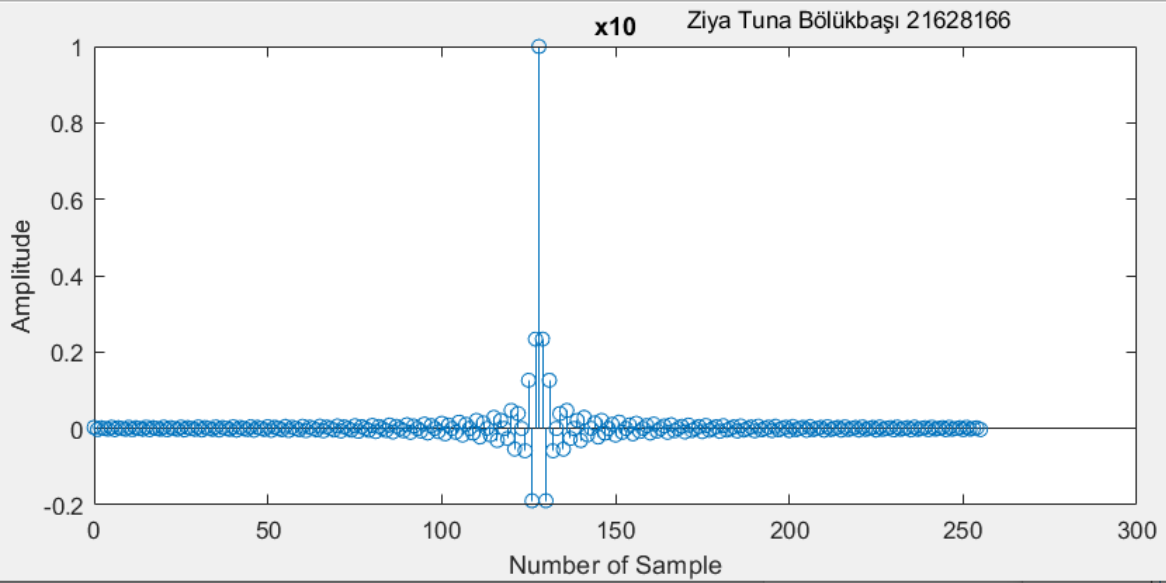


Figure 2

File Edit View Insert Tools Desktop Window Help

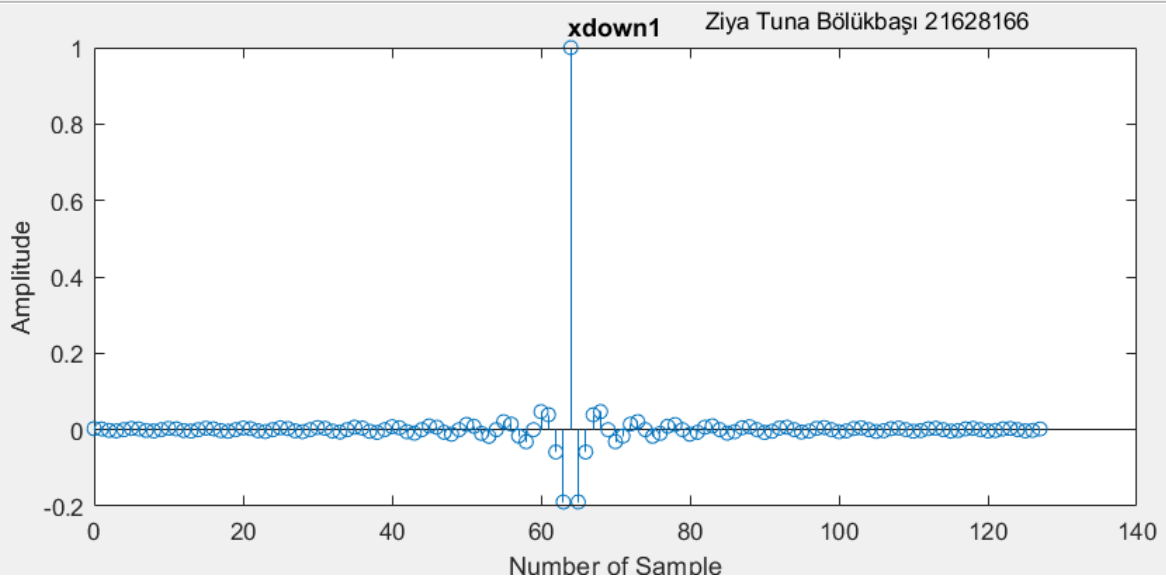


Figure 3

File Edit View Insert Tools Desktop Window Help

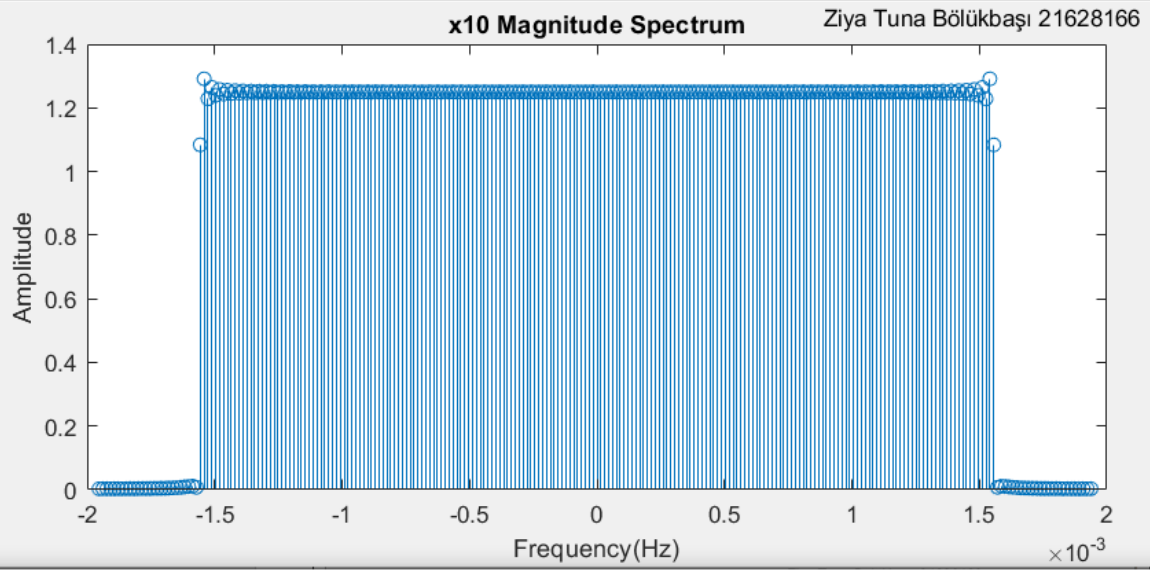


Figure 4

File Edit View Insert Tools Desktop Window Help

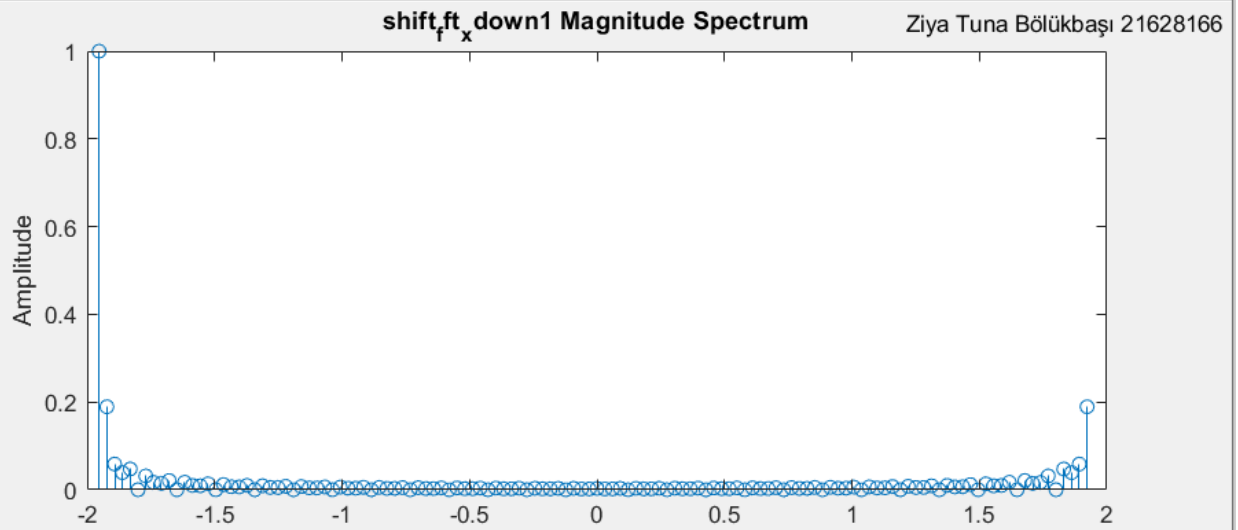


Figure 5

File Edit View Insert Tools Desktop Window Help

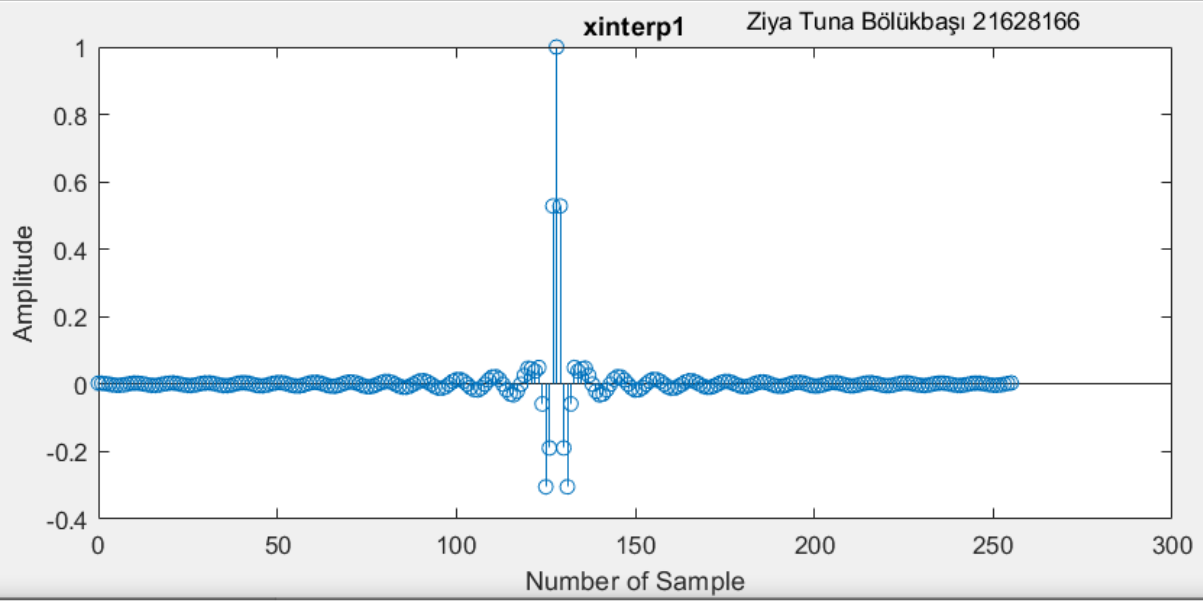


Figure 6

File Edit View Insert Tools Desktop Window Help

