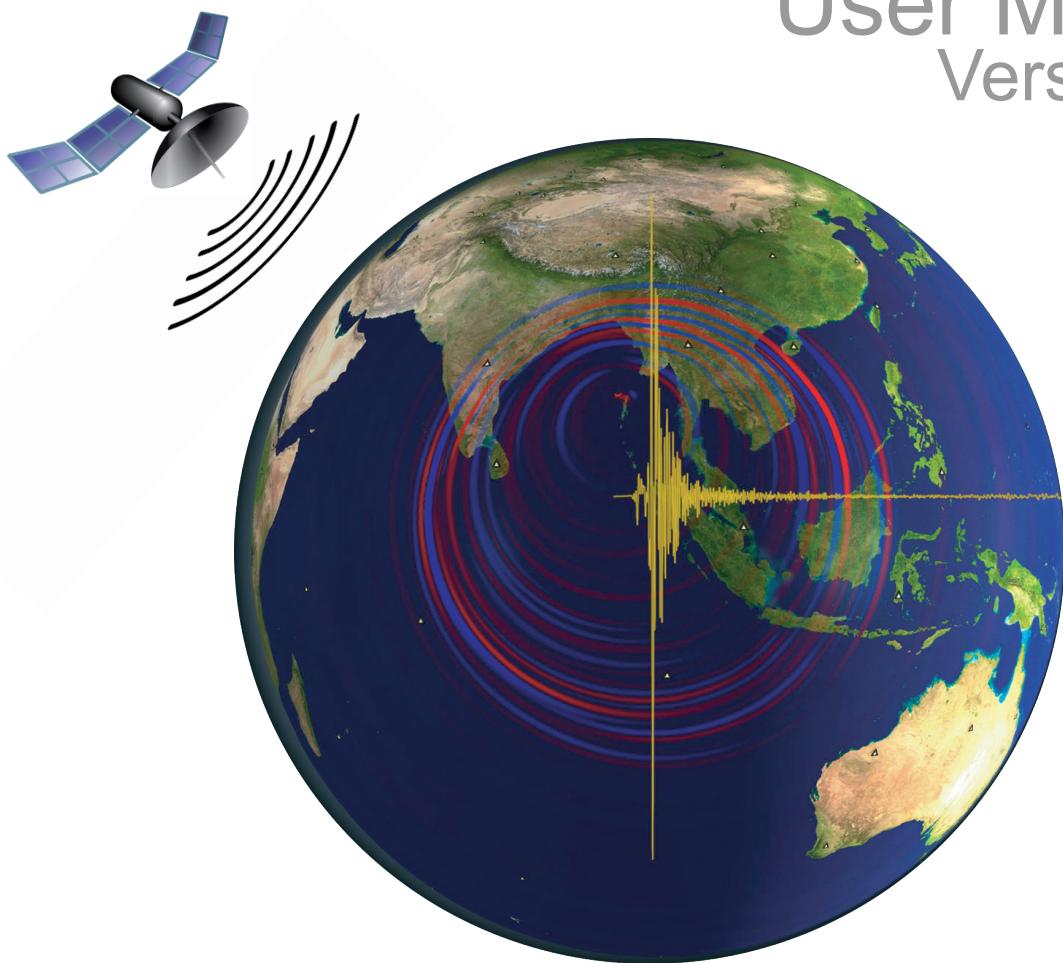


COMPUTATIONAL INFRASTRUCTURE FOR GEODYNAMICS (CIG)  
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# SPECFEM 3D Globe

User Manual  
Version 7.0



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# **SPECFEM3D\_GLOBE**

## **User Manual**

© Princeton University (USA) and CNRS / University of Marseille (France),  
ETH Zürich (Switzerland),  
Version 7.0

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## Authors

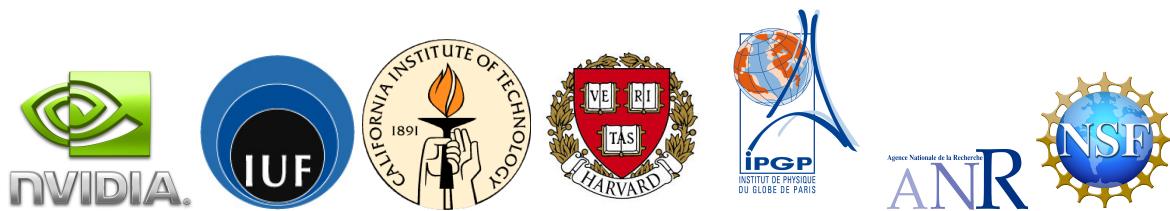
The SPECFEM3D package was first developed by Dimitri Komatitsch and Jean-Pierre Vilotte at Institut de Physique du Globe (IPGP) in Paris, France from 1995 to 1997 and then by Dimitri Komatitsch and Jeroen Tromp at Harvard University and Caltech, USA, starting in 1998. The story started on April 4, 1995, when Prof. Yvon Maday from CNRS and University of Paris, France, gave a lecture to Dimitri Komatitsch and Jean-Pierre Vilotte at IPG about the nice properties of the Legendre spectral-element method with diagonal mass matrix that he had used for other equations. We are deeply indebted and thankful to him for that. That followed a visit by Dimitri Komatitsch to OGS (Istituto Nazionale di Oceanografia e di Geofisica Sperimentale) in Trieste, Italy, in February 1995 to meet with Géza Seriani and Enrico Priolo, who introduced him to their 2D Chebyshev version of the spectral-element method with a non-diagonal mass matrix. We are deeply indebted and thankful to them for that.

Since then it has been developed and maintained by a development team: in alphabetical order, Michael Afanasiev, Jean-Paul (Pablo) Ampuero, Kazuto Ando, Kangchen Bai, Piero Basini, Céline Blitz, Alexis Bottero, Ebru Bozdağ, Emanuele Casarotti, Joseph Charles, Min Chen, Paul Cristini, Clément Durochat, Percy Galvez, Hom Nath Gharti, Dominik Göddeke, Vala Hjörleifsdóttir, Sue Kientz, Dimitri Komatitsch, Jesús Labarta, Piero Lanucara, Nicolas Le Goff, Piere Le Loher, Matthieu Lefebvre, Qinya Liu, Youshan Liu, David Luet, Yang Luo, Alessia Maggi, Federica Magnoni, Roland Martin, René Matzen, Dennis McRitchie, Jean-François Méhaut, Matthias Meschede, Peter Messmer, David Michéa, Takayuki Miyoshi, Vadim Monteiller, Surendra Nadh Somala, Tarje Nissen-Meyer, Daniel Peter, Kevin Pouget, Max Rietmann, Vittorio Ruggiero, Elliott Sales de Andrade, Brian Savage, Bernhard Schuberth, Anne Sieminski, James Smith, Leif Strand, Carl Tape, Jeroen Tromp, Seiji Tsuboi, Brice Videau, Jean-Pierre Vilotte, Zhinan Xie, Chang-Hua Zhang, Hejun Zhu.

The cover graphic of the manual was created by Santiago Lombeyda from Caltech's Center for Advanced Computing Research (CACR), USA, with free satellite clipart pictures from <http://www.4vector.com> and <http://www.clker.com> added to it.

The code is released open-source under the GNU version 3 license, see the license at the end of this manual.

## Current and past main participants or main sponsors of the SPECFEM project (in no particular order)



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# Chapter 1

## Introduction

**ANNOUNCEMENT:** SPECFEM3D\_GLOBE can now perform gravity field calculations in addition (or instead of) seismic wave propagation only. See flag GRAVITY\_INTEGRALS in file setup/constants.h.in. Please also refer to [http://komatitsch.free.fr/preprints/GJI\\_Martin\\_gravimetry\\_2017.pdf](http://komatitsch.free.fr/preprints/GJI_Martin_gravimetry_2017.pdf). And yes, that is the reason why I added a gravity observation satellite on the cover of the manual :-)

The software package SPECFEM3D\_GLOBE simulates three-dimensional global and regional seismic wave propagation and performs full waveform imaging (FWI) or adjoint tomography based upon the spectral-element method (SEM). The SEM is a continuous Galerkin technique [Tromp et al., 2008, Peter et al., 2011], which can easily be made discontinuous [Bernardi et al., 1994, Chaljub, 2000, Kopriva et al., 2002, Chaljub et al., 2003, Legay et al., 2005, Kopriva, 2006, Wilcox et al., 2010, Acosta Minolia and Kopriva, 2011]; it is then close to a particular case of the discontinuous Galerkin technique [Reed and Hill, 1973, Lesaint and Raviart, 1974, Arnold, 1982, Johnson and Pitkäranta, 1986, Bourdel et al., 1991, Falk and Richter, 1999, Hu et al., 1999, Cockburn et al., 2000, Giraldo et al., 2002, Rivière and Wheeler, 2003, Monk and Richter, 2005, Grote et al., 2006, Ainsworth et al., 2006, Bernacki et al., 2006, Dumbser and Käser, 2006, De Basabe et al., 2008, de la Puente et al., 2009, Wilcox et al., 2010, De Basabe and Sen, 2010, Étienne et al., 2010], with optimized efficiency because of its tensorized basis functions [Wilcox et al., 2010, Acosta Minolia and Kopriva, 2011]. In particular, it can accurately handle very distorted mesh elements [Oliveira and Seriani, 2011].

It has very good accuracy and convergence properties [Maday and Patera, 1989, Seriani and Priolo, 1994, Deville et al., 2002, Cohen, 2002, De Basabe and Sen, 2007, Seriani and Oliveira, 2008, Ainsworth and Wajid, 2009, 2010, Melvin et al., 2012]. The spectral element approach admits spectral rates of convergence and allows exploiting *hp*-convergence schemes. It is also very well suited to parallel implementation on very large supercomputers [Komatitsch et al., 2003, Tsuboi et al., 2003, Komatitsch et al., 2008, Carrington et al., 2008, Komatitsch et al., 2010b] as well as on clusters of GPU accelerating graphics cards [Komatitsch, 2011, Michéa and Komatitsch, 2010, Komatitsch et al., 2009, 2010a]. Tensor products inside each element can be optimized to reach very high efficiency [Deville et al., 2002], and mesh point and element numbering can be optimized to reduce processor cache misses and improve cache reuse [Komatitsch et al., 2008]. The SEM can also handle triangular (in 2D) or tetrahedral (in 3D) elements [Wingate and Boyd, 1996, Taylor and Wingate, 2000, Komatitsch et al., 2001, Cohen, 2002, Mercerat et al., 2006] as well as mixed meshes, although with increased cost and reduced accuracy in these elements, as in the discontinuous Galerkin method.

Note that in many geological models in the context of seismic wave propagation studies (except for instance for fault dynamic rupture studies, in which very high frequencies or supershear rupture need to be modeled near the fault, see e.g. Benjemaa et al. [2007, 2009], de la Puente et al. [2009], Tago et al. [2010]) a continuous formulation is sufficient because material property contrasts are not drastic and thus conforming mesh doubling bricks can efficiently handle mesh size variations [Komatitsch and Tromp, 2002a, Komatitsch et al., 2004, Lee et al., 2008, 2009a,b]. This is particularly true at the scale of the full Earth.

For a detailed introduction to the SEM as applied to global and regional seismic wave propagation, please consult Tromp et al. [2008], Peter et al. [2011], Komatitsch and Vilotte [1998], Komatitsch and Tromp [1999], Chaljub [2000], Komatitsch and Tromp [2002a,b], Komatitsch et al. [2002], Chaljub et al. [2003], Capdeville et al. [2003], Chaljub and Valette [2004], Chaljub et al. [2007]. A detailed theoretical analysis of the dispersion and stability properties of the SEM is available in Cohen [2002], De Basabe and Sen [2007], Seriani and Oliveira [2007], Seriani and Oliveira [2008] and Melvin et al. [2012].

Effects due to lateral variations in compressional-wave speed, shear-wave speed, density, a 3D crustal model, ellipticity, topography and bathymetry, the oceans, rotation, and self-gravitation are included. The package can accommodate full 21-parameter anisotropy [Chen and Tromp, 2007] as well as lateral variations in attenuation [Savage et al., 2010]. Adjoint capabilities and finite-frequency kernel simulations are also included [Tromp et al., 2008, Peter et al., 2011, Liu and Tromp, 2006, 2008, Fichtner et al., 2009, Virieux and Operto, 2009].

The SEM was originally developed in computational fluid dynamics [Patera, 1984, Maday and Patera, 1989] and has been successfully adapted to address problems in seismic wave propagation. Early seismic wave propagation applications of the SEM, utilizing Legendre basis functions and a perfectly diagonal mass matrix, include Cohen et al. [1993], Komatitsch [1997], Faccioli et al. [1997], Casadei and Gabellini [1997], Komatitsch and Vilotte [1998] and Komatitsch and Tromp [1999], whereas applications involving Chebyshev basis functions and a nondiagonal mass matrix include Seriani and Priolo [1994], Priolo et al. [1994] and Seriani et al. [1995]. In the Legendre version that we use in SPECFEM the mass matrix is purposely slightly inexact but diagonal (but can be made exact if needed, see Teukolsky [2015]), while in the Chebyshev version it is exact but non diagonal.

Beware that, in a spectral-element method, some spurious modes (that have some similarities with classical so-called "Hourglass modes" in finite-element techniques, although in the SEM they are not zero-energy modes) can appear in some (but not all) cases in the spectral element in which the source is located. Fortunately, they do not propagate away from the source element. However, this means that if you put a receiver in the same spectral element as a source, the recorded signals may in some cases be wrong, typically exhibiting some spurious oscillations, which are often even non causal. If that is the case, an easy option is to slightly change the mesh in the source region in order to get rid of these Hourglass-like spurious modes, as explained in Duczek et al. [2014], in which this phenomenon is described in details, and in which practical solutions to avoid it are suggested.

All SPECFEM3D\_GLOBE software is written in Fortran2003 with full portability in mind, and conforms strictly to the Fortran2003 standard. It uses no obsolete or obsolescent features of Fortran. The package uses parallel programming based upon the Message Passing Interface (MPI) [Gropp et al., 1994, Pacheco, 1997].

SPECFEM3D\_GLOBE won the Gordon Bell award for best performance at the SuperComputing 2003 conference in Phoenix, Arizona (USA) (see Komatitsch et al. [2003]). It was a finalist again in 2008 for a run at 0.16 petaflops (sustained) on 149,784 processors of the ‘Jaguar’ Cray XT5 system at Oak Ridge National Laboratories (USA) [Carrington et al., 2008]. It also won the BULL Joseph Fourier supercomputing award in 2010.

It reached the sustained one petaflop performance level for the first time in February 2013 on the Blue Waters Cray supercomputer at the National Center for Supercomputing Applications (NCSA), located at the University of Illinois at Urbana-Champaign (USA).

The package includes support for GPU graphics card acceleration [Komatitsch, 2011, Mich   and Komatitsch, 2010, Komatitsch et al., 2009, 2010a] and also supports OpenCL.

The next release of the code will include support for Convolutional or Auxiliary Differential Equation Perfectly Matched absorbing Layers (C-PML or ADE-PML) [Martin et al., 2008b,c, Martin and Komatitsch, 2009, Martin et al., 2010, Komatitsch and Martin, 2007] for the case of single-chunk simulations in regional models.

## 1.1 Citation

You can find all the references below in BibTeXformat in file doc/USER MANUAL/bibliography.bib.

If you use SPECFEM3D\_GLOBE for your own research, please cite at least one of the following articles: Komatitsch et al. [2016], Tromp et al. [2008], Peter et al. [2011], Vai et al. [1999], Lee et al. [2008, 2009a,b], Komatitsch et al. [2009, 2010a], van Wijk et al. [2004], Komatitsch et al. [2004], Chaljub et al. [2007], Madec et al. [2009], Komatitsch et al. [2010b], Carrington et al. [2008], Tromp et al. [2010a], Komatitsch et al. [2002], Komatitsch and Tromp [2002a,b, 1999] or Komatitsch and Vilotte [1998].

If you use the C-PML absorbing layer capabilities of the code, please cite at least one article written by the developers of the package, for instance:

- Xie et al. [2014],
- Xie et al. [2016].

If you use the UNDO\_ATTENUATION option of the code in order to produce full anelastic/viscoelastic sensitivity kernels, please cite at least one article written by the developers of the package, for instance (and in particular):

- Komatitsch et al. [2016].

More generally, if you use the attenuation (anelastic/viscoelastic) capabilities of the code, please cite at least one article written by the developers of the package, for instance:

- Komatitsch et al. [2016],
- Blanc et al. [2016].

If you use the kernel capabilities of the code, please cite at least one article written by the developers of the package, for instance:

- Tromp et al. [2008],
- Peter et al. [2011],
- Liu and Tromp [2006],
- Morency et al. [2009].

If you use this new version, which has non blocking MPI for much better performance for medium or large runs, please cite at least one of these five articles, in which results of 3D non blocking MPI runs are presented: Komatitsch et al. [2010a,b], Komatitsch [2011], Peter et al. [2011], Carrington et al. [2008].

If you use GPU graphics card acceleration please cite e.g. Komatitsch [2011], Mich  a and Komatitsch [2010], Komatitsch et al. [2009], and/or Komatitsch et al. [2010a].

If you work on geophysical applications, you may be interested in citing some of these application articles as well, among others: van Wijk et al. [2004], Ji et al. [2005], Krishnan et al. [2006a,b], Lee et al. [2008, 2009a,b], Chevrot et al. [2004], Favier et al. [2004], Ritsema et al. [2002], Godinho et al. [2009], Tromp and Komatitsch [2000], Savage et al. [2010]. If you use 3D mantle model S20RTS, please cite Ritsema et al. [1999].

Domain decomposition is explained in detail in Martin et al. [2008a], and excellent scaling up to 150,000 processor cores is shown for instance in Carrington et al. [2008], Komatitsch et al. [2008], Martin et al. [2008a], Komatitsch et al. [2010a], Komatitsch [2011].

The corresponding BibTeX entries may be found in file doc/USER MANUAL/bibliography.bib.

## 1.2 Support

This material is based upon work supported by the U.S. National Science Foundation under Grants No. EAR-0406751 and EAR-0711177, by the French CNRS, French INRIA Sud-Ouest MAGIQUE-3D, French ANR NUMASIS under Grant No. ANR-05-CIGC-002, and European FP6 Marie Curie International Reintegration Grant No. MIRG-CT-2005-017461. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the U.S. National Science Foundation, CNRS, INRIA, ANR or the European Marie Curie program.

# Chapter 2

## Getting Started

### 2.1 Configuring and compiling the source code

To get the SPECFEM3D\_GLOBE software package, type this:

```
git clone --recursive --branch devel https://github.com/geodynamics/specfem3d_globe.git
```

We recommend that you add ulimit -S -s unlimited to your .bash\_profile file and/or limit stacksize unlimited to your .cshrc file to suppress any potential limit to the size of the Unix stack.

Then, to configure the software for your system, run the `configure` shell script. This script will attempt to guess the appropriate configuration values for your system. However, at a minimum, it is recommended that you explicitly specify the appropriate command names for your Fortran compiler (another option is to define FC, CC and MPIF90 in your .bash\_profile or your .cshrc file):

```
./configure FC=gfortran CC=gcc MPIFC=mpif90
```

You can replace the GNU compilers above (gfortran and gcc) with other compilers if you want to; for instance for Intel ifort and icc use FC=ifort CC=icc instead.

Before running the `configure` script, you should probably edit file `flags.guess` to make sure that it contains the best compiler options for your system. Known issues or things to check are:

**GCC gfortran compiler** The code makes use of Fortran 2008 features, e.g., the contiguous array attribute. We thus recommend using a gfortran version 4.6.0 or higher.

**Intel ifort compiler** See if you need to add `-assume byterecl` for your machine. **In the case of that compiler, we have noticed that initial release versions sometimes have bugs or issues that can lead to wrong results when running the code, thus we strongly recommend using a version for which at least one service pack or update has been installed.** In particular, for version 17 of that compiler, users have reported problems (making the code crash at run time) with the `-assume buffered_io` option; if you notice problems, remove that option from file `flags.guess` or change it to `-assume nobuffered_io` and try again.

**IBM compiler** See if you need to add `-qsave` or `-qnosave` for your machine.

**Mac OS** You will probably need to install XCODE.

When compiling on an IBM machine with the `xlf` and `xlc` compilers, we suggest running the `configure` script with the following options:

```
./configure FC=xlf90_r MPIFC=mpif90 CC=xlc_r CFLAGS="-O3 -q64" FCFLAGS="-O3 -q64"
```

If you have problems configuring the code on a Cray machine, i.e. for instance if you get an error message from the `configure` script, try exporting these two variables: `MPI_INC=$CRAY_MPICH2_DIR/include` and

`FCLIBS=" "`, and for more details if needed you can refer to the `utils/Cray_compiler_information` directory. You can also have a look at the configure script called `utils/Cray_compiler_information/configure_SPECFEM`.

On SGI systems, `flags.guess` automatically informs `configure` to insert “`TRAP_FPE=OFF`” into the generated `Makefile` in order to turn underflow trapping off.

If you run very large meshes on a relatively small number of processors, the static memory size needed on each processor might become greater than 2 gigabytes, which is the upper limit for 32-bit addressing (dynamic memory allocation is always OK, even beyond the 2 GB limit; only static memory has a problem). In this case, on some compilers you may need to add “`-mcmodel=medium`” (if you do not use the Intel ifort / `icc` compiler) or “`-mcmodel=medium-shared-intel`” (if you use the Intel ifort / `icc` compiler) to the configure options of `CFLAGS`, `FCFLAGS` and `LDLDFLAGS` otherwise the compiler will display an error message (for instance “`relocation truncated to fit: R_X86_64_PC32 against .bss`” or something similar); on an IBM machine with the `xlf` and `xlc` compilers, using `-q64` is usually sufficient.

A summary of the most important configuration variables follows.

**FC** Fortran compiler command name. By default, `configure` will execute the command names of various well-known Fortran compilers in succession, picking the first one it finds that works.

**MPIFC** MPI Fortran command name. The default is `mpif90`. This must correspond to the same underlying compiler specified by `FC`; otherwise, you will encounter compilation or link errors when you attempt to build the code. If you are unsure about this, it is usually safe to set both `FC` and `MPIFC` to the MPI compiler command for your system:

```
./configure FC=mpif90 MPIFC=mpif90
```

**FLAGS\_CHECK** Compiler flags.

**LOCAL\_PATH\_IS\_ALSO\_GLOBAL** If you want the parallel mesher to write a parallel (i.e., split) database for the solver on the local disks of each of the compute nodes, set this flag to `.false.`. Some systems have no local disks (e.g., BlueGene) and other systems have a fast parallel file system (LUSTRE, GPFS) that is easy and reliable to use, in which case this variable should be set to `.true.`. Note that this flag is not used by the mesher nor the solver; it is only used for some of the (optional) post-processing. If you do not know what is best on your system, setting it to `.true.` is usually fine; or else, ask your system administrator.

In addition to reading configuration variables, `configure` accepts the following options:

**--enable-double-precision** The package can run either in single or in double precision mode. The default is single precision because for almost all calculations performed using the spectral-element method using single precision is sufficient and gives the same results (i.e. the same seismograms); and the single precision code is faster and requires exactly half as much memory. To specify double precision mode, simply provide `--enable-double-precision` as a command-line argument to `configure`. On many current processors (e.g., Intel, AMD, IBM Power), single precision calculations are significantly faster; the difference can typically be 10% to 25%. It is therefore better to use single precision. What you can do once for the physical problem you want to study is run the same calculation in single precision and in double precision on your system and compare the seismograms. If they are identical (and in most cases they will), you can select single precision for your future runs.

**--help** Directs `configure` to print a usage screen which provides a short description of all configuration variables and options. Note that the options relating to installation directories (e.g., `--prefix`) do not apply to `SPECFEM3D_GLOBE`.

The `configure` script runs a brief series of checks. Upon successful completion, it generates the files `Makefile`, `constants.h`, and `precision.h` in the working directory.

**Note:** If the `configure` script fails, and you don't know what went wrong, examine the log file `config.log`. This file contains a detailed transcript of all the checks `configure` performed. Most importantly, it includes the error output (if any) from your compiler.

The `configure` script automatically runs the script `flags.guess`. This helper script contains a number of suggested flags for various compilers; e.g., Portland, Intel, Absoft, NAG, Lahey, NEC, IBM and SGI. The software has run on a wide variety of compute platforms, e.g., various PC clusters and machines from Sun, SGI, IBM, Compaq, and NEC. The `flags.guess` script attempts to guess which compiler you are using (based upon the compiler command name) and choose the related optimization flags. The `configure` script then automatically inserts the suggested flags into `Makefile`. Note that `flags.guess` may fail to identify your compiler; and in any event, the default flags chosen by `flags.guess` are undoubtedly not optimal for your system. So, we encourage you to experiment with these flags (by editing the generated `Makefile` by hand) and to solicit advice from your system administrator. Selecting the right compiler and compiler flags can make a tremendous difference in terms of performance. We welcome feedback on your experience with various compilers and flags.

When using a slow or not too powerful shared disk system or when running extremely large simulations (on tens of thousands of processor cores), one can add `-DUSE_SERIAL CASCADE_FOR_IOS` to the compiler flags in file `flags.guess` before running `configure` to make the mesher output mesh data to the disk for one MPI slice after the other, and to make the solver do the same thing when reading the files back from disk. Do not use this option if you do not need it because it will slow down the mesher and the beginning of the solver if your shared file system is fast and reliable.

If you run scaling benchmarks of the code, for instance to measure its performance on a new machine, and are not interested in the physical results (the seismograms) for these runs, you can set `DO_BENCHMARK_RUN_ONLY` to `.true.` in file `setup/constants.h.in` before running the `configure` script.

If your compiler has problems with the `use mpi` statements that are used in the code, use the script called `replace_use_mpi_with_include_mpif_dot_h.pl` in the root directory to replace all of them with `include 'mpif.h'` automatically.

We recommend that you ask for exclusive use of the compute nodes when running on a cluster or a supercomputer, i.e., make sure that no other users are running on the same nodes at the same time. Otherwise your run could run out of memory if the memory of some nodes is used by other users, in particular when undoing attenuation using the `UNDO_ATTENUATION` option in `DATA/Par_file`. To do so, ask your system administrator for the option to add to your batch submission script; it is for instance `#BSUB -x` with SLURM and `#$ -l exclusive=TRUE` with Sun Grid Engine (SGE).

## 2.2 Using the GPU version of the code

SPECFEM3D\_GLOBE now supports OpenCL and NVIDIA CUDA GPU acceleration. OpenCL can be enabled with the `--with-opencl` flag, and the compilation can be controlled through three variables: `OCL_LIB=`, `OCL_INC=` and `OCL_GPU_FLAGS=`.

```
./configure --with-opencl OCL_LIB= OCL_INC= OCL_GPU_FLAGS=..
```

CUDA configuration can be enabled with `--with-cuda` flag and `CUDA_FLAGS=`, `CUDA_LIB=`, `CUDA_INC=` and `MPI_INC=` variables.

```
./configure --with-cuda=cuda5 CUDA_FLAGS= CUDA_LIB= CUDA_INC= MPI_INC= ..
```

Both environments can be compiled simultaneously by merging these two lines. For the runtime configuration, the `GPU_MODE` flag must be set to `.true.`. In addition, we use three parameters to select the environments and GPU:

```
GPU_RUNTIME = 0|1|2
GPU_PLATFORM = filter|*
GPU_DEVICE = filter|*
```

**GPU\_RUNTIME** sets the runtime environments: 2 for OpenCL, 1 for CUDA and 0 for compile-time decision (hence, SPECFEM should have been compiled with only one of `--with-opencl` or `--with-cuda`).

**GPU\_PLATFORM** and **GPU\_DEVICE** are both (case-insensitive) filters on the platform and device name in OpenCL, device name only in CUDA. In multiprocessor (MPI) runs, each process will pick a GPU in this filtered subset, in round-robin. The star filter (\*) will match the first platform and all its devices.

`GPU_RUNTIME`, `GPU_PLATFORM` and `GPU_DEVICE` are not read if `GPU_MODE` is not activated. Regarding the code, `--with-opencl` defines the macro-processor flag `USE_OPENCL` and `--with-cuda` defines `USE_CUDA`; and `GPU_RUNTIME` set the global variable `run_opencl` or `run_cuda`. Texture support has not been validated in OpenCL, but works as expected in CUDA.

Note about the OpenCL version: the OpenCL calculation kernels were created by Brice Videau and Kevin Pouget from Grenoble, France, using their software package called BOAST [Videau et al., 2013].

## 2.3 Compiling on an IBM BlueGene

More recent installation instruction for IBM BlueGene, from October 2012:

Edit file `flags.guess` and put this for `FLAGS_CHECK`:

```
-g -qfullpath -O2 -qsave -qstrict -qtune=qp -qarch=qp -qcache=auto -qhalt=w \
-qfree=f90 -qsuffix=f=f90 -qlanglvl=95pure -Q -Q+rank,swap_all -Wl,-relax
```

The most relevant are the `-qarch` and `-qtune` flags, otherwise if these flags are set to “auto” then they are wrongly assigned to the architecture of the front-end node, which is different from that on the compute nodes. You will need to set these flags to the right architecture for your BlueGene compute nodes, which is not necessarily “qp”; ask your system administrator. On some machines it is necessary to use `-O2` in these flags instead of `-O3` due to a compiler bug of the XLF version installed. We thus suggest to first try `-O3`, and then if the code does not compile or does not run fine then switch back to `-O2`. The debug flags (`-g`, `-qfullpath`) do not influence performance but are useful to get at least some insights in case of problems.

Before running `configure`, select the XL Fortran compiler by typing `module load bgq-xl/1.0` or `module load bgq-xl` (another, less efficient option is to load the GNU compilers using `module load bgq-gnu/4.4.6` or similar).

Then, to configure the code, type this:

```
./configure FC=bgxlf90_r MPIFC=mpixlf90_r CC=bgxlc_r LOCAL_PATH_IS ALSO_GLOBAL=true
```

Older installation instruction for IBM BlueGene, from 2011:

To compile the code on an IBM BlueGene, Laurent Léger from IDRIS, France, suggests the following: compile the code with

```
FLAGS\_CHECK="-O3 -qsave -qstrict -qtune=auto -qarch=450d -qcache=auto \
-qfree=f90 -qsuffix=f=f90 -g -qlanglvl=95pure -qhalt=w -Q -Q+rank,swap_all -Wl,-relax"
```

Option `-Wl,-relax` must be added on many (but not all) BlueGene systems to be able to link the binaries `xmeshfem3D` and `xspecfem3D` because the final link step is done by the GNU ld linker even if one uses `FC=bgxlf90_r`, `MP IFC=mpixlf90_r` and `CC=bgxlc_r` to create all the object files. On the contrary, on some BlueGene systems that use the native AIX linker option `-Wl,-relax` can lead to problems and must be suppressed from `flags.guess`. One then just needs to pass the right commands to the `configure` script:

```
./configure --prefix=/path/to/SPECFEM3DG_SP --host=Babel --build=BGP \
FC=bgxlf90_r MPIFC=mpixlf90_r CC=bgxlc_r \
LOCAL_PATH_IS ALSO_GLOBAL=false
```

This trick can be useful for all hosts on which one needs to cross-compile.

On BlueGene, one also needs to run the `xcreate_header_file` binary file manually rather than in the Makefile:

```
bgrun -np 1 -mode VN -exe ./bin/xcreate_header_file
```

## 2.4 Using a cross compiler

The “configure” script assumes that you will compile the code on the same kind of hardware as the machine on which you will run it. On some systems (for instance IBM BlueGene, see also the previous section) this might not be the case and you may compile the code using a cross compiler on a frontend computer that does not have the same architecture. In such a case, typing “make all” on the frontend will fail, but you can use one of these two solutions:

1/ create a script that runs “make all” on a node instead of on the frontend, if the compiler is also installed on the nodes

2/ after running the “configure” script, create two copies of the Makefiles:

**TODO: this has not been tested out yet, any feedback is welcome**

In `src/create_header_file/Makefile` put this instead of the current values:

```
FLAGS_CHECK = -O0
```

and replace

```
create_header_file: $O/create_header_file.o $(XCREATE_HEADER_OBJECTS)
 ${FCCOMPILER_CHECK} -o ${E}/xcreate_header_file $O/create_header_file.o $(XCREATE_HEADER_O
```

with

```
xcreate_header_file: $O/create_header_file.o $(XCREATE_HEADER_OBJECTS)
 ${MPIFCOMPILER_CHECK} -o ${E}/xcreate_header_file $O/create_header_file.o $(XCREATE_HEADER_O
```

In `src/specfem3D/Makefile` comment out these last two lines:

```
#${OUTPUT}/values_from_mesher.h: reqheader
#       (mkdir -p ${OUTPUT}; cd ${S_TOP}/; ./bin/xcreate_header_file)
```

Then:

```
make clean
make create_header_file
./bin/xcreate_header_file
make clean
make meshfem3D
make specfem3D
```

should work.

## 2.5 Adding OpenMP support in addition to MPI

OpenMP support can be enabled in addition to MPI. However, in many cases performance will not improve because our pure MPI implementation is already heavily optimized and thus the resulting code will in fact be slightly slower. A possible exception could be IBM BlueGene-type architectures.

To enable OpenMP, add the flag `--enable-openmp` to the configuration:

```
./configure --enable-openmp ..
```

This will add the corresponding OpenMP flag for the chosen Fortran compiler.

The DO-loop using OpenMP threads has a `SCHEDULE` property. The `OMP_SCHEDULE` environment variable can set the scheduling policy of that DO-loop. Tests performed by Marcin Zielinski at SARA (The Netherlands) showed that often the best scheduling policy is `DYNAMIC` with the size of the chunk equal to the number of OpenMP threads, but most preferably being twice as the number of OpenMP threads (thus chunk size = 8 for 4 OpenMP threads etc). If `OMP_SCHEDULE` is not set or is empty, the DO-loop will assume generic scheduling policy, which will slow down the job quite a bit.

## 2.6 Compiling on an Intel Xeon Phi (Knights Landing KNL)

In case you want to run simulations on a KNL chip, the compilation doesn't require much more effort than with any other CPU system. All you could add is the flag `-xMIC-AVX512` to your Fortran flags in the `Makefile` and use `--enable-openmp` for configuration.

Since there are different memory types available with a KNL, make sure to use fast memory allocations, i.e. MCDRAM, which has a higher memory bandwidth. Assuming you use a flat mode setup of the KNL chip, you could use the Linux tool `numactl` to specify which memory node to bind to. For example, check with

```
numactl --hardware
```

which node contains CPU cores and which one only binds to MCDRAM (~16GB). In flat mode setup, most likely node 1 does. For a small example on a single KNL with 4 MPI processes and 16 OpenMP threads each, you would run the solver with a command like

```
OMP_NUM_THREADS=16 mpirun -np 4 numactl --membind=1 ./bin/xspecfem3D
```

The ideal setup of MPI processes and OpenMP threads per KNL depends on your specific hardware and simulation setup. We see good results when using a combination of both, with a total number of threads slightly less than the total count of cores on the chip.

As a side remark for developers, another possibility would be to add following compiler directives in the source code (in file `src/specfem3D/specfem3D_par.F90`):

```
real(kind=CUSTOM_REAL), dimension(:, :, :), allocatable :: &
    displ_crust_mantle, veloc_crust_mantle, accel_crust_mantle
! FASTMEM attribute: note this attribute needs compiler flag -lmemkind to work...
!DEC$ ATTRIBUTES FASTMEM :: displ_crust_mantle, veloc_crust_mantle, accel_crust_mantle
```

These directives will work with Intel ifort compilers and will need the additional linker/compiler flag `-lmemkind` to work properly. We omitted these directives for now to avoid confusion with other possible simulation setups.

## 2.7 Visualizing the subroutine calling tree of the source code

Packages such as `doxywizard` can be used to visualize the subroutine calling tree of the source code. `Doxywizard` is a GUI front-end for configuring and running `doxygen`.

## 2.8 Becoming a developer of the code, or making small modifications in the source code

If you want to develop new features in the code, and/or if you want to make small changes, improvements, or bug fixes, you are very welcome to contribute. To do so, i.e. to access the development branch of the source code with read/write access (in a safe way, no need to worry too much about breaking the package, there is a robot called BuildBot that is in charge of checking and validating all new contributions and changes), please visit this Web page: <https://github.com/geodynamics/specfem3d/wiki>.

To visualize the call tree (calling tree) of the source code, you can see the Doxygen tool available in directory `doc/call_trees_of_the_source_code`.

# Chapter 3

## Running the Mesher `xmeshfem3D`

You are now ready to compile the mesher. In the directory with the source code, type ‘`make meshfem3D`’. If all paths and flags have been set correctly, the mesher should now compile and produce the executable `xmeshfem3D`. Note that all compiled executables are placed into the directory `bin/`. To run the executables, you must call them from the root directory, for example type ‘`mpirun -np 64 ./bin/meshfem3D`’ to run the mesher in parallel on 64 CPUs. This will allow the executables to find the parameter file `Par_file` in the relative directory location `./DATA`.

Input for the mesher (and the solver) is provided through the parameter file `Par_file`, which resides in the subdirectory `DATA`. Before running the mesher, a number of parameters need to be set in the `Par_file`. This requires a basic understanding of how the SEM is implemented, and we encourage you to read Komatitsch and Vilotte [1998], Komatitsch and Tromp [1999], Chaljub [2000], Komatitsch and Tromp [2002a,b], Komatitsch et al. [2002], Chaljub et al. [2003], Capdeville et al. [2003] and Chaljub and Valette [2004]. A detailed theoretical analysis of the dispersion and stability properties of the SEM is available in Cohen [2002], De Basabe and Sen [2007] and Seriani and Oliveira [2007].

In this chapter we will focus on simulations at the scale of the entire globe. Regional simulations will be addressed in Chapter 5. The spectral-element mesh for a `SPECFEM3D_GLOBE` simulation is based upon a mapping from the cube to the sphere called the *cubed sphere* [Sadourny, 1972, Ronchi et al., 1996]. This cubed-sphere mapping breaks the globe into 6 chunks, each of which is further subdivided in terms of  $n^2$  mesh slices, where  $n \geq 1$  is a positive integer, for a total of  $6 \times n^2$  slices (Figure 3.1). Thus the minimum number of processors required for a global simulation is 6 (although it is theoretically possible to run more than one slice per processor).

To run the mesher for a global simulation, the following parameters need to be set in the `Par_file` (the list below might be slightly obsolete or incomplete; for an up-to-date version, see comments in the default `Par_file` located in directory `DATA`):

**SIMULATION\_TYPE** is set to 1 for forward simulations, 2 for adjoint simulations for sources (see Section 6.1) and 3 for kernel simulations (see Section 10.3).

**SAVE\_FORWARD** is only set to `.true.` for a forward simulation with the last frame of the simulation saved, as part of the finite-frequency kernel calculations (see Section 10.3). For a regular forward simulation, leave `SIMULATION_TYPE` and `SAVE_FORWARD` at their default values.

**NCHUNKS** must be set to 6 for global simulations.

**ANGULAR\_WIDTH\_XI\_IN\_DEGREES** Not needed for a global simulation. (See Chapter 5 for regional simulations.)

**ANGULAR\_WIDTH\_ETA\_IN\_DEGREES** Not needed for a global simulation. (See Chapter 5 for regional simulations.)

**CENTER\_LATITUDE\_IN\_DEGREES** Not needed for a global simulation. (See Chapter 5 for regional simulations.)

**CENTER\_LONGITUDE\_IN\_DEGREES** Not needed for a global simulation. (See Chapter 5 for regional simulations.)

**GAMMA\_ROTATION\_AZIMUTH** Not needed for a global simulation. (See Chapter 5 for regional simulations.)

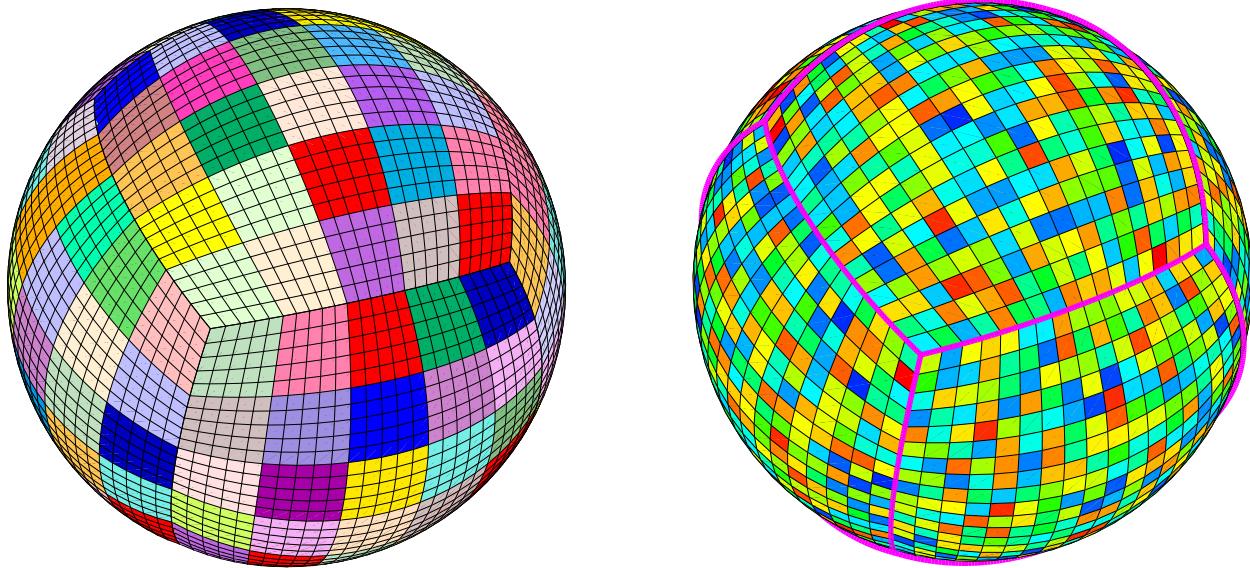


Figure 3.1: Each of the 6 chunks that constitutes the cubed sphere is subdivided in terms of  $n^2$  slices of elements, where  $n \geq 1$  is a positive integer, for a total of  $6 \times n^2$  slices (and therefore processors). The figure on the left shows a mesh that is divided in terms of  $6 \times 5^2 = 150$  slices as indicated by the various colors. In this cartoon, each slice contains  $5 \times 5 = 25$  spectral elements at the Earth’s surface. The figure on the right shows a mesh that is divided over  $6 \times 18^2 = 1944$  processors as indicated by the various colors. Regional simulations can be accommodated by using only 1, 2 or 3 chunks of the cubed sphere. One-chunk simulations may involve a mesh with lateral dimensions smaller than  $90^\circ$ , thereby accommodating smaller-scale simulations.

**NEX\_XI** The number of spectral elements along one side of a chunk in the cubed sphere (see Figure 3.1); this number *must* be a multiple of 16 and  $8 \times$  a multiple of NPROC\_XI defined below. We do not recommend using NEX\_XI less than 64 because the curvature of the Earth cannot be honored if one uses too few elements, and distorted elements can lead to inaccurate and unstable simulations, i.e., smaller values of NEX\_XI are likely to result in spectral elements with a negative Jacobian, in which case the mesher will exit with an error message. Table 3 summarizes various suitable choices for NEX\_XI and the related values of NPROC\_XI. Based upon benchmarks against semi-analytical normal-mode synthetic seismograms, Komatitsch and Tromp [2002a,b] determined that a NEX\_XI = 256 run is accurate to a shortest period of roughly 17 s. Therefore, since accuracy is determined by the number of grid points per shortest wavelength, for any particular value of NEX\_XI the simulation will be accurate to a shortest period determined approximately by

$$\text{shortest period (s)} \simeq (256/\text{NEX\_XI}) \times 17. \quad (3.1)$$

The number of grid points in each orthogonal direction of the reference element, i.e., the number of Gauss-Lobatto-Legendre points, is determined by NGLLX in the constants.h file. In the globe we use NGLLX = 5, for a total of  $5^3 = 125$  points per elements. We suggest not to change this value.

**NEX\_ETA** For global simulations NEX\_ETA must be set to the same value as NEX\_XI.

**NPROC\_XI** The number of processors or slices along one chunk of the cubed sphere (see Figure 3.1); we must have  $\text{NEX\_XI} = 8 \times c \times \text{NPROC\_XI}$ , where  $c \geq 1$  is a positive integer. See Table 3 for various suitable choices.

**NPROC\_ETA** For global simulations NPROC\_ETA must be set to the same value as NPROC\_XI.

**MODEL** Must be set to one of the following:

1D models with real structure:

**1D\_isotropic\_prem** Isotropic version of the spherically symmetric Preliminary Reference Earth Model (PREM) [Dziewoński and Anderson, 1981].

**1D\_transversely\_isotropic\_prem** Transversely isotropic version of PREM.

**1D\_iasp91** Spherically symmetric isotropic IASP91 model [Kennett and Engdahl, 1991].

**1D\_1066a** Spherically symmetric earth model 1066A [Gilbert and Dziewoński, 1975]. When ATTENUATION is on, it uses an unpublished 1D attenuation model from Scripps.

**1D\_ak135f\_no\_mud** Spherically symmetric isotropic AK135 model [Kennett et al., 1995] modified to use the density and Q attenuation models of Montagner and Kennett [1995]. That modified model is traditionally called AK135-F, see <http://rses.anu.edu.au/seismology/ak135/ak135f.html> for more details. As we do not want to use the 300 m-thick mud layer from that model nor the ocean layer, above the d120 discontinuity we switch back to the classical AK135 model of Kennett et al. [1995], i.e., we use AK135-F below and AK135 above.

**1D\_ref** A recent 1D Earth model developed by Kustowski et al. [2006]. This model is the 1D background model for the 3D models s362ani, s362wmani, s362ani\_prem, and s29ea.

For historical reasons and to provide benchmarks against normal-mode synthetics, the mesher accommodates versions of various 1D models with a single crustal layer with the properties of the original upper crust. These ‘one-crust’ models are:

```
1D_isotropic_prem_onecrust
1D_transversely_isotropic_prem_onecrust
1D_iasp91_onecrust
1D_1066a_onecrust
1D_ak135f_no_mud_onecrust
```

Fully 3D models:

**transversely\_isotropic\_prem\_plus\_3D\_crust\_2.0** This model has CRUST2.0 [Bassin et al., 2000] on top of a transversely isotropic PREM. We first extrapolate PREM mantle velocity up to the surface, then overwrite the model with CRUST2.0

**s20rts** By default, the code uses 3D mantle model S20RTS [Ritsema et al., 1999] and 3D crustal model Crust2.0 [Bassin et al., 2000]. Note that S20RTS uses transversely isotropic PREM as a background model, and that we use the PREM radial attenuation model when ATTENUATION is incorporated. See Chapter 12 for a discussion on how to change 3D models.

**s40rts** A global 3D mantle model [Ritsema et al., 2011] succeeding S20RTS with a higher resolution. S40RTS uses transversely isotropic PREM as a background model and the 3D crustal model Crust2.0 [Bassin et al., 2000]. We use the PREM radial attenuation model when ATTENUATION is incorporated.

**s362ani** A global shear-wave speed model developed by Kustowski et al. [2006]. In this model, radial anisotropy is confined to the uppermost mantle. The model (and the corresponding mesh) incorporate tomography on the 650~km and 410~km discontinuities in the 1D reference model REF.

**s362wmani** A version of S362ANI with anisotropy allowed throughout the mantle.

**s362ani\_prem** A version of S362ANI calculated using PREM as the 1D reference model.

**s29ea** A global model with higher resolution in the upper mantle beneath Eurasia calculated using REF as the 1D reference model.

**3D\_anisotropic** See Chapter 12 for a discussion on how to specify your own 3D anisotropic model.

**3D\_attenuation** See Chapter 12 for a discussion on how to specify your own 3D attenuation model.

**PPM** For a user-specified 3D model (Point-Profile-Model) given as ASCII-table, specifying Vs-perturbations with respect to PREM. See Chapter 12 for a discussion on how to specify your own 3D model.

**full\_sh** For a user-specified, transversely isotropic 3D model given in spherical harmonics. Coefficients for the crustal model (up to degree 40) are stored in files named C\*\*.dat and MOHO.dat, coefficients for the mantle model (up to degree 20) are stored in files named M\*\*.dat.

All model files reside in directory DATA/full\_sphericalharmonic\_model/. Note that to use the crustal model, one has to set the crustal type value ITYPE\_CRUSTAL\_MODEL = ICRUST\_CRUST\_SH in file setup/constants.h. This crustal model can be transversely isotropic as well.

**sglobberani\_iso** By default, the code uses 3D *isotropic* mantle model SGLOBE-rani [Chang et al., 2015] and the 3D crustal model includes perturbations from Crust2.0 [Bassin et al., 2000] as discussed in [Chang et al., 2015]. The model is parametrised horizontally in spherical harmonics up to lmax=35 and with 21 depth splines for the radial direction. Note that SGLOBE-rani uses transversely isotropic PREM as a background model, and that we use the PREM radial attenuation model when ATTENUATION is incorporated.

**sglobberani\_aniso** By default, the code uses 3D *anisotropic* mantle model SGLOBE-rani [Chang et al., 2015] and the 3D crustal model includes perturbations from Crust2.0 [Bassin et al., 2000] as discussed in [Chang et al., 2015]. Note that SGLOBE-rani uses transversely isotropic PREM as a background model, and that we use the PREM radial attenuation model when ATTENUATION is incorporated.

#### NOTE:

When a 3D mantle model is chosen in Par\_file, the simulations are performed together with the 3D crustal model Crust2.0. Alternatively, Crust2.0 can be combined with a higher resolution European crustal model EUCrust07 [Tesauro et al., 2008]. This can be done by setting the crustal type to ICRUST\_CRUSTMAPS in the constant.h file. It is also possible to run simulations using a 3D mantle model with a 1D crustal model on top. This can be done by setting the model in Par\_file to <3D mantle>\_1Dcrust, e.g., s20rts\_1Dcrust, s362ani\_1Dcrust, etc. In this case, the 1D crustal model will be the one that is used in the 3D mantle model as a reference model (e.g., transversely isotropic PREM for s20rts, REF for s362ani, etc.).

**OCEANS** Set to .true. if the effect of the oceans on seismic wave propagation should be incorporated based upon the approximate treatment discussed in Komatitsch and Tromp [2002b]. This feature is inexpensive from a numerical perspective, both in terms of memory requirements and CPU time. This approximation is accurate at periods of roughly 20 s and longer. At shorter periods the effect of water phases/reverberations is not taken into account, even when the flag is on.

**ELLIPTICITY** Set to .true. if the mesh should make the Earth model elliptical in shape according to Clairaut's equation [Dahlen and Tromp, 1998]. This feature adds no cost to the simulation. After adding ellipticity, the mesh becomes elliptical and thus geocentric and geodetic/geographic latitudes and colatitudes differ (longitudes are unchanged). From Dahlen and Tromp [1998]: "Spherically-symmetric Earth models all have the same hydrostatic surface ellipticity 1/299.8. This is 0.5 percent smaller than observed flattening of best-fitting ellipsoid 1/298.3. The discrepancy is referred to as the "excess equatorial bulge of the Earth", an early discovery of artificial satellite geodesy." From Paul Melchior, IUGG General Assembly, Vienna, Austria, August 1991 Union lecture, available at www.agu.org/books: "It turns out that the spheroidal models constructed on the basis of the spherically-symmetric models (PREM, 1066A) by using the Clairaut differential equation to calculate the flattening in function of the radius vector imply hydrostaticity. These have surface ellipticity 1/299.8 and a corresponding dynamical flattening of .0033 (PREM). The actual ellipticity of the Earth for a best-fitting ellipsoid is 1/298.3 with a corresponding dynamical flattening of .0034." Thus, flattening  $f = 1/299.8$  is what is used in SPECFEM3D\_GLOBE, as it should. And thus eccentricity squared  $e^2 = 1 - (1 - f)^2 = 1 - (1 - 1/299.8)^2 = 0.00665998813529$ , and the correction factor used in the code to convert geographic latitudes to geocentric is  $1 - e^2 = (1 - f)^2 = (1 - 1/299.8)^2 = 0.9933400118647$ . As a comparison, the classical World Geodetic System reference ellipsoid WGS 84 (see e.g. [http://en.wikipedia.org/wiki/World\\_Geodetic\\_System](http://en.wikipedia.org/wiki/World_Geodetic_System)) has  $f = 1/298.2572236$ .

**TOPOGRAPHY** Set to .true. if topography and bathymetry should be incorporated based upon model ETOPO4 [NOAA, 1988]. This feature adds no cost to the simulation. If you want to use other topographic models, use the script download\_the\_whole\_topography\_database\_if\_you\_want\_other\_topographic\_models.bash provided in the root directory of the code and change the name of the topographic model to use in file setup/constants.h.in before configuring the code with the configure script.

**GRAVITY** Set to `.true.` if self-gravitation should be incorporated in the Cowling approximation [Komatitsch and Tromp, 2002b, Dahlen and Tromp, 1998]. Turning this feature on is relatively inexpensive, both from the perspective of memory requirements as well as in terms of computational speed.

**ROTATION** Set to `.true.` if the Coriolis effect should be incorporated. Turning this feature on is relatively cheap numerically.

**ATTENUATION** Set to `.true.` if attenuation should be incorporated. Turning this feature on increases the memory requirements significantly (roughly by a factor of 2), and is numerically fairly expensive. Of course for realistic simulations this flag should be turned on. See Komatitsch and Tromp [1999, 2002a] for a discussion on the implementation of attenuation based upon standard linear solids.

**ABSORBING\_CONDITIONS** Set to `.false.` for global simulations. See Chapter 5 for regional simulations.

**RECORD\_LENGTH\_IN\_MINUTES** Choose the desired record length of the synthetic seismograms (in minutes). This controls the length of the numerical simulation, i.e., twice the record length requires twice as much CPU time. This feature is not used at the time of meshing but is required for the solver, i.e., you may change this parameter after running the mesher.

**PARTIAL\_PHYS\_DISPERSION\_ONLY or UNDO\_ATTENUATION** To undo attenuation for sensitivity kernel calculations or forward runs with `SAVE_FORWARD` use one (and only one) of the two flags below. `UNDO_ATTENUATION` is much better (it is exact) and is simpler to use but it requires a significant amount of disk space for temporary storage. It has the advantage of requiring only two simulations for adjoint tomography instead of three in the case of `PARTIAL_PHYS_DISPERSION_ONLY`, i.e. for adjoint tomography it is globally significantly less expensive (each run is slightly more expensive, but only two runs are needed instead of three).

When using `PARTIAL_PHYS_DISPERSION_ONLY`, to make the approximation reasonably OK you need to take the following steps:

1/ To calculate synthetic seismograms, do a forward simulation with full attenuation for the model of interest. The goal is to get synthetics that match the data as closely as possible.

2a/ Make measurements and produce adjoint sources by comparing the resulting synthetics with the data. In the simplest case of a cross-correlation traveltimes measurement, use the time-reversed synthetic in the window of interest as the adjoint source.

2b/ Do a second forward calculation with `PARTIAL_PHYS_DISPERSION_ONLY = .true.` and save the last snapshot.

3/ Do an adjoint calculation using the adjoint source calculated in 1/, the forward wavefield reconstructed based on 2b/, use `PARTIAL_PHYS_DISPERSION_ONLY = .true.` for the adjoint wavefield, and save the kernel.

Thus the kernel calculation uses `PARTIAL_PHYS_DISPERSION_ONLY = .true.` for both the forward and the adjoint wavefields. This is in the spirit of the banana-donut kernels. But the data that are assimilated are based on the full 3D synthetic with attenuation.

Another, equivalent way of explaining it is:

1/ Calculate synthetics with full attenuation for the current model. Compare these to the data and measure frequency-dependent traveltimes  $\Delta\tau(\omega)$ , e.g.. based upon multi-tapering.

2/ Calculate synthetics with `PARTIAL_PHYS_DISPERSION_ONLY = .true.` and construct adjoint sources by combining the seismograms from this run with the measurements from 1/. So in the expressions for the multi-taper adjoint source you use the measurements from 1/, but synthetics calculated with `PARTIAL_PHYS_DISPERSION_ONLY = .true..`

3/ Construct a kernel by calculating an adjoint wavefield based on the sources constructed in 2/ and convolving it with a forward wavefield with `PARTIAL_PHYS_DISPERSION_ONLY = .true..` Again, both the forward and adjoint calculations use `PARTIAL_PHYS_DISPERSION_ONLY = .true..`

Note that if you replace multi-taper measurements with cross-correlation measurements you will measure a cross-correlation traveltimes anomaly in 1/, i.e., some delay time  $\Delta T$ . Then you would calculate an adjoint wavefield with `PARTIAL_PHYS_DISPERSION_ONLY = .true.` and use the resulting time-reversed seismograms weighted by  $\Delta T$  as the adjoint source. This wavefield interacts with a forward wavefield calculated with `PARTIAL_PHYS_DISPERSION_ONLY = .true..` If  $\Delta T = 1$  one gets a banana-donut kernel, i.e., a

kernel for the case in which there are no observed seismograms (no data), as explained for instance on page 5 of Zhou et al. [2011].

**MOVIE\_SURFACE** Set to `.false.`, unless you want to create a movie of seismic wave propagation on the Earth's surface. Turning this option on generates large output files. See Section 10.2 for a discussion on the generation of movies. This feature is not used at the time of meshing but is relevant for the solver.

**MOVIE\_VOLUME** Set to `.false.`, unless you want to create a movie of seismic wave propagation in the Earth's interior. Turning this option on generates huge output files. See Section 10.2 for a discussion on the generation of movies. This feature is not used at the time of meshing but is relevant for the solver.

**NTSTEP\_BETWEEN\_FRAMES** Determines the number of timesteps between movie frames. Typically you want to save a snapshot every 100 timesteps. The smaller you make this number the more output will be generated! See Section 10.2 for a discussion on the generation of movies. This feature is not used at the time of meshing but is relevant for the solver.

**HDUR\_MOVIE** determines the half duration of the source time function for the movie simulations. When this parameter is set to be 0, a default half duration that corresponds to the accuracy of the simulation is provided.

**SAVE\_MESH\_FILES** Set this flag to `.true.` to save AVS (<http://www.avs.com>), OpenDX (<http://www.opendx.org>), or ParaView (<http://www.paraview.org>) mesh files for subsequent viewing. Turning the flag on generates large (distributed) files in the `LOCAL_PATH` directory. See Section 10.1 for a discussion of mesh viewing features.

**NUMBER\_OF\_RUNS** On machines with a run-time limit, for instance for a batch/queue system, a simulation may need to be completed in stages. This option allows you to select the number of stages in which the simulation will be completed (1, 2 or 3). Choose 1 for a run without restart files. This feature is not used at the time of meshing but is required for the solver. At the end of the first or second stage of a multi-stage simulation, large files are written to the file system to save the current state of the simulation. This state is read back from the file system at the beginning of the next stage of the multi-stage run. Reading and writing the states can be very time consuming depending on the nature of the network and the file system (in this case writing to the local file system, i.e., the disk on a node, is preferable).

**NUMBER\_OF\_THIS\_RUN** If you choose to perform the run in stages, you need to tell the solver what stage run to perform. This feature is not used at the time of meshing but is required for the solver.

**LOCAL\_PATH** Directory in which the databases generated by the mesher will be written. Generally one uses a directory on the local disk of the compute nodes, although on some machines these databases are written on a parallel (global) file system (see also the earlier discussion of the `LOCAL_PATH_IS ALSO_GLOBAL` flag in Chapter 2). The mesher generates the necessary databases in parallel, one set for each of the  $6 \times \text{NPROC}_X I^2$  slices that constitutes the mesh (see Figure 3.1). After the mesher finishes, you can log in to one of the compute nodes and view the contents of the `LOCAL_PATH` directory to see the (many) files generated by the mesher.

**NTSTEP\_BETWEEN\_OUTPUT\_INFO** This parameter specifies the interval at which basic information about a run is written to the file system (`timestamp*` files in the `OUTPUT_FILES` directory). If you have access to a fast machine, set `NTSTEP_BETWEEN_OUTPUT_INFO` to a relatively high value (e.g., at least 100, or even 1000 or more) to avoid writing output text files too often. This feature is not used at the time of meshing. One can set this parameter to a larger value than the number of time steps to avoid writing output during the run.

**NTSTEP\_BETWEEN\_OUTPUT\_SEISMOS** This parameter specifies the interval at which synthetic seismograms are written in the `LOCAL_PATH` directory. The seismograms can be created in three different formats by setting the parameters `OUTPUT_SEISMOS_ASCII_TEXT`, `OUTPUT_SEISMOS_SAC_ALPHANUM` and `OUTPUT_SEISMOS_SAC_BINARY`. One can choose any combination of these parameters (details on the formats follow in the description of each parameter). SAC (<http://www.iris.edu/software/sac/>) is a signal-processing software package. If a run crashes, you may still find usable (but shorter than requested) seismograms in this directory. On a fast machine set `NTSTEP_BETWEEN_OUTPUT_SEISMOS` to a relatively high value to avoid writing to the seismograms too often. This feature is not used at the time of meshing.

**NTSTEP\_BETWEEN\_READ\_ADJSRC** The number of adjoint sources read in each time for an adjoint simulation.

**USE\_FORCE\_POINT\_SOURCE** Turn this flag on to use a (tilted) FORCESOLUTION force point source instead of a CMTSOLUTION moment-tensor source. When the force source does not fall exactly at a grid point, the solver interpolates the force between grid points using Lagrange interpolants. This option can be useful for vertical force, normal force, tilted force, impact force, etc. Note that in the FORCESOLUTION file, you will need to edit the East, North and vertical components of an arbitrary (not necessarily unitary, the code will normalize it automatically) direction vector of the force vector; thus refer to Appendix A for the orientation of the reference frame. This vector is made unitary internally in the solver and thus only its direction matters here; its norm is ignored and the norm of the force used is the factor force source times the source time function.

**OUTPUT\_SEISMOS\_ASCII\_TEXT** Set this flag to `.true.` if you want to have the synthetic seismograms written in two-column ASCII format (the first column contains time in seconds and the second column the displacement in meters of the recorded signal, no header information). Files will be named with extension `.ascii`, e.g., `NT.STA.?X?.sem.ascii` where NT and STA are the network and station codes given in STATIONS file, and ?X? is the channel code (see Appendix E).

**OUTPUT\_SEISMOS\_SAC\_ALPHANUM** Set this flag to `.true.` if you want to have the synthetic seismograms written in alphanumeric (human readable) SAC format, which includes header information on the source and receiver parameters (e.g., source/receiver coordinates, station name, etc., see Appendix D). For details on the format, please check the SAC webpage (<http://www.iris.edu/software/sac/>). Files will be named with extension `.sacan`.

**OUTPUT\_SEISMOS\_SAC\_BINARY** Set this flag to `.true.` if you want to have the synthetic seismograms written in binary SAC format. The header information included is the same as for the alphanumeric SAC format (see Appendix D). Using this format requires the least disk space, which may be particularly important if you have a large number of stations. For details on the binary format please also check the SAC webpage (<http://www.iris.edu/software/sac/>) and Appendix D. Files will be named with extension `.sac`.

**ROTATE\_SEISMOGRAMS\_RT** Set this flag to `.true.` if you want to have radial (R) and transverse (T) horizontal components of the synthetic seismograms (default is `.false.` → East (E) and North (N) components).

**WRITE\_SEISMOGRAMS\_BY\_MAIN** Set this flag to `.true.` if you want to have all the seismograms written by the main process (no need to collect them on the nodes after the run).

**SAVE\_ALL\_SEISMOS\_IN\_ONE\_FILE** Set this flag to `.true.` if you want to have all the seismograms saved in one large combined file instead of one file per seismogram to avoid overloading shared non-local file systems such as GPFS for instance.

**USE\_BINARY\_FOR\_LARGE\_FILE** Set this flag to `.true.` if you want to use binary instead of ASCII for that large file (not used if `SAVE_ALL_SEISMOS_IN_ONE_FILE = .false.`)

**RECEIVERS\_CAN\_BE\_BURIED** This flag accommodates stations with instruments that are buried, i.e., the solver will calculate seismograms at the burial depth specified in the STATIONS file. This feature is not used at the time of meshing.

**PRINT\_SOURCE\_TIME\_FUNCTION** Turn this flag on to print information about the source time function in the file `OUTPUT_FILES/plot_source_time_function.txt`. This feature is not used at the time of meshing.

**NUMBER\_OF\_SIMULTANEOUS\_RUNS** adds the ability to run several calculations (several earthquakes) in an embarrassingly-parallel fashion from within the same run; this can be useful when using a very large supercomputer to compute many earthquakes in a catalog, in which case it can be better from a batch job submission point of view to start fewer and much larger jobs, each of them computing several earthquakes in parallel. To turn that option on, set parameter `NUMBER_OF_SIMULTANEOUS_RUNS` to a value greater than 1. To implement that, we create `NUMBER_OF_SIMULTANEOUS_RUNS` MPI sub-communicators, each of them being labeled "my\_local\_mpi\_comm\_world", and we use them in all the routines in "src/shared/parallel.f90", except in `MPI_ABORT()` because in that case we need to kill the entire run. When that option is on, of

course the number of processor cores used to start the code in the batch system must be a multiple of NUMBER\_OF\_SIMULTANEOUS\_RUNS, all the individual runs must use the same number of processor cores, which as usual is NPROC in the Par\_file, and thus the total number of processor cores to request from the batch system should be NUMBER\_OF\_SIMULTANEOUS\_RUNS \* NPROC. All the runs to perform must be placed in directories called run0001, run0002, run0003 and so on (with exactly four digits).

Imagine you have 10 independent calculations to do, each of them on 100 cores; you have three options:

1/ submit 10 jobs to the batch system

2/ submit a single job on 1000 cores to the batch, and in that script create a sub-array of jobs to start 10 jobs, each running on 100 cores (see e.g. [http://www.schedmd.com/slurmdocs/job\\_array.html](http://www.schedmd.com/slurmdocs/job_array.html))

3/ submit a single job on 1000 cores to the batch, start SPECFEM3D on 1000 cores, create 10 sub-communicators, cd into one of 10 subdirectories (called e.g. run0001, run0002,... run0010) depending on the sub-communicator your MPI rank belongs to, and run normally on 100 cores using that sub-communicator.

The option NUMBER\_OF\_SIMULTANEOUS\_RUNS implements 3/.

**BROADCAST\_SAME\_MESH\_AND\_MODEL** : if we perform simultaneous runs in parallel, if only the source and receivers vary between these runs but not the mesh nor the model (velocity and density) then we can also read the mesh and model files from a single run in the beginning and broadcast them to all the others; for a large number of simultaneous runs for instance when solving inverse problems iteratively this can DRASTICALLY reduce I/Os to disk in the solver (by a factor equal to NUMBER\_OF\_SIMULTANEOUS\_RUNS), and reducing I/Os is crucial in the case of huge runs. Thus, always set this option to .true. if the mesh and the model are the same for all simultaneous runs. In that case there is no need to duplicate the mesh and model file database (the content of the DATABASES\_MPI directories) in each of the run0001, run0002,... directories, it is sufficient to have one in run0001 and the code will broadcast it to the others).

**USE\_FAILSAFE\_MECHANISM** : if one or a few of these simultaneous runs fail, kill all the runs or let the others finish using a fail-safe mechanism (in most cases, should be set to true).

TODO / future work to do: currently the BROADCAST\_SAME\_MESH\_AND\_MODEL option assumes to have the (main) mesh files in run0001/DATABASES\_MPI or run0001/OUTPUT\_FILES/DATABASES\_MPI. However, for adjoint runs you still need a DATABASES\_MPI folder in each of the sub-runs directories, e.g. run0002/DATABASES\_MPI, etc. to store the forward wavefields, kernels etc. of each sub-run. This would not be needed for forward simulations.

TODO / future work to do: the sensitivity kernel summing and smoothing tools in directory src/tomography are currently not ported to this new option to do many runs simultaneously, only the solver (src/specfem3d) is. Thus these tools should work, but in their current version will need to be run for each simulation result independently. More precisely, the current kernel summing and smoothing routines work fine, with the exception that you need to move out the mesh files (and also the parameters). This works because these routines consider multiple runs by design. You simply have to provide them the directories where the kernels are.

NPROC_XI	processors	NEX_XI									
1	6	64	80	96	112	128	144	160	176	192	208
2	24	64	80	96	112	128	144	160	176	192	208
3	54	96	144	192	240	288	336	384	432	480	528
4	96	64	96	128	160	192	224	256	288	320	352
5	150	80	160	240	320	400	480	560	640	720	800
6	216	96	144	192	240	288	336	384	432	480	528
7	294	112	224	336	448	560	672	784	896	1008	1120
8	384	64	128	192	256	320	384	448	512	576	640
9	486	144	288	432	576	720	864	1008	1152	1296	1440
10	600	80	160	240	320	400	480	560	640	720	800
11	726	176	352	528	704	880	1056	1232	1408	1584	1760
12	864	96	192	288	384	480	576	672	768	864	960
13	1014	208	416	624	832	1040	1248	1456	1664	1872	2080
14	1176	112	224	336	448	560	672	784	896	1008	1120
15	1350	240	480	720	960	1200	1440	1680	1920	2160	2400
16	1536	128	256	384	512	640	768	896	1024	1152	1280
17	1734	272	544	816	1088	1360	1632	1904	2176	2448	2720
18	1944	144	288	432	576	720	864	1008	1152	1296	1440
19	2166	304	608	912	1216	1520	1824	2128	2432	2736	3040
20	2400	160	320	480	640	800	960	1120	1280	1440	1600
21	2646	336	672	1008	1344	1680	2016	2352	2688	3024	3360
22	2904	176	352	528	704	880	1056	1232	1408	1584	1760
23	3174	368	736	1104	1472	1840	2208	2576	2944	3312	3680
24	3456	192	384	576	768	960	1152	1344	1536	1728	1920
25	3750	400	800	1200	1600	2000	2400	2800	3200	3600	4000
26	4056	208	416	624	832	1040	1248	1456	1664	1872	2080
27	4374	432	864	1296	1728	2160	2592	3024	3456	3888	4320
28	4704	224	448	672	896	1120	1344	1568	1792	2016	2240
29	5046	464	928	1392	1856	2320	2784	3248	3712	4176	4640
30	5400	240	480	720	960	1200	1440	1680	1920	2160	2400
31	5766	496	992	1488	1984	2480	2976	3472	3968	4464	4960
32	6144	256	512	768	1024	1280	1536	1792	2048	2304	2560
33	6534	528	1056	1584	2112	2640	3168	3696	4224	4752	5280
34	6936	272	544	816	1088	1360	1632	1904	2176	2448	2720
35	7350	560	1120	1680	2240	2800	3360	3920	4480	5040	5600
36	7776	288	576	864	1152	1440	1728	2016	2304	2592	2880
37	8214	592	1184	1776	2368	2960	3552	4144	4736	5328	5920
38	8664	304	608	912	1216	1520	1824	2128	2432	2736	3040
39	9126	624	1248	1872	2496	3120	3744	4368	4992	5616	6240
40	9600	320	640	960	1280	1600	1920	2240	2560	2880	3200
41	10086	656	1312	1968	2624	3280	3936	4592	5248	5904	6560
42	10584	336	672	1008	1344	1680	2016	2352	2688	3024	3360
43	11094	688	1376	2064	2752	3440	4128	4816	5504	6192	6880
44	11616	352	704	1056	1408	1760	2112	2464	2816	3168	3520
45	12150	720	1440	2160	2880	3600	4320	5040	5760	6480	7200
46	12696	368	736	1104	1472	1840	2208	2576	2944	3312	3680
47	13254	752	1504	2256	3008	3760	4512	5264	6016	6768	7520
48	13824	384	768	1152	1536	1920	2304	2688	3072	3456	3840
49	14406	784	1568	2352	3136	3920	4704	5488	6272	7056	7840
50	15000	400	800	1200	1600	2000	2400	2800	3200	3600	4000
51	15606	816	1632	2448	3264	4080	4896	5712	6528	7344	8160

NPROC_XI	processors	NEX_XI									
52	16224	416	832	1248	1664	2080	2496	2912	3328	3744	4160
53	16854	848	1696	2544	3392	4240	5088	5936	6784	7632	8480
54	17496	432	864	1296	1728	2160	2592	3024	3456	3888	4320
55	18150	880	1760	2640	3520	4400	5280	6160	7040	7920	8800
56	18816	448	896	1344	1792	2240	2688	3136	3584	4032	4480
57	19494	912	1824	2736	3648	4560	5472	6384	7296	8208	9120
58	20184	464	928	1392	1856	2320	2784	3248	3712	4176	4640
59	20886	944	1888	2832	3776	4720	5664	6608	7552	8496	9440
60	21600	480	960	1440	1920	2400	2880	3360	3840	4320	4800
61	22326	976	1952	2928	3904	4880	5856	6832	7808	8784	9760
62	23064	496	992	1488	1984	2480	2976	3472	3968	4464	4960
63	23814	1008	2016	3024	4032	5040	6048	7056	8064	9072	10080
64	24576	512	1024	1536	2048	2560	3072	3584	4096	4608	5120
65	25350	1040	2080	3120	4160	5200	6240	7280	8320	9360	10400
66	26136	528	1056	1584	2112	2640	3168	3696	4224	4752	5280
67	26934	1072	2144	3216	4288	5360	6432	7504	8576	9648	10720
68	27744	544	1088	1632	2176	2720	3264	3808	4352	4896	5440
69	28566	1104	2208	3312	4416	5520	6624	7728	8832	9936	11040
70	29400	560	1120	1680	2240	2800	3360	3920	4480	5040	5600
71	30246	1136	2272	3408	4544	5680	6816	7952	9088	10224	11360
72	31104	576	1152	1728	2304	2880	3456	4032	4608	5184	5760
73	31974	1168	2336	3504	4672	5840	7008	8176	9344	10512	11680
74	32856	592	1184	1776	2368	2960	3552	4144	4736	5328	5920
75	33750	1200	2400	3600	4800	6000	7200	8400	9600	10800	12000
76	34656	608	1216	1824	2432	3040	3648	4256	4864	5472	6080
77	35574	1232	2464	3696	4928	6160	7392	8624	9856	11088	12320
78	36504	624	1248	1872	2496	3120	3744	4368	4992	5616	6240
79	37446	1264	2528	3792	5056	6320	7584	8848	10112	11376	12640
80	38400	640	1280	1920	2560	3200	3840	4480	5120	5760	6400
81	39366	1296	2592	3888	5184	6480	7776	9072	10368	11664	12960
82	40344	656	1312	1968	2624	3280	3936	4592	5248	5904	6560
83	41334	1328	2656	3984	5312	6640	7968	9296	10624	11952	13280
84	42336	672	1344	2016	2688	3360	4032	4704	5376	6048	6720
85	43350	1360	2720	4080	5440	6800	8160	9520	10880	12240	13600
86	44376	688	1376	2064	2752	3440	4128	4816	5504	6192	6880
87	45414	1392	2784	4176	5568	6960	8352	9744	11136	12528	13920
88	46464	704	1408	2112	2816	3520	4224	4928	5632	6336	7040
89	47526	1424	2848	4272	5696	7120	8544	9968	11392	12816	14240
90	48600	720	1440	2160	2880	3600	4320	5040	5760	6480	7200
91	49686	1456	2912	4368	5824	7280	8736	10192	11648	13104	14560
92	50784	736	1472	2208	2944	3680	4416	5152	5888	6624	7360
93	51894	1488	2976	4464	5952	7440	8928	10416	11904	13392	14880
94	53016	752	1504	2256	3008	3760	4512	5264	6016	6768	7520
95	54150	1520	3040	4560	6080	7600	9120	10640	12160	13680	15200
96	55296	768	1536	2304	3072	3840	4608	5376	6144	6912	7680
97	56454	1552	3104	4656	6208	7760	9312	10864	12416	13968	15520
98	57624	784	1568	2352	3136	3920	4704	5488	6272	7056	7840
99	58806	1584	3168	4752	6336	7920	9504	11088	12672	14256	15840
100	60000	800	1600	2400	3200	4000	4800	5600	6400	7200	8000
101	61206	1616	3232	4848	6464	8080	9696	11312	12928	14544	16160
102	62424	816	1632	2448	3264	4080	4896	5712	6528	7344	8160

NPROC_XI	processors	NEX_XI									
103	63654	1648	3296	4944	6592	8240	9888	11536	13184	14832	16480
104	64896	832	1664	2496	3328	4160	4992	5824	6656	7488	8320
105	66150	1680	3360	5040	6720	8400	10080	11760	13440	15120	16800
106	67416	848	1696	2544	3392	4240	5088	5936	6784	7632	8480
107	68694	1712	3424	5136	6848	8560	10272	11984	13696	15408	17120
108	69984	864	1728	2592	3456	4320	5184	6048	6912	7776	8640
109	71286	1744	3488	5232	6976	8720	10464	12208	13952	15696	17440
110	72600	880	1760	2640	3520	4400	5280	6160	7040	7920	8800
111	73926	1776	3552	5328	7104	8880	10656	12432	14208	15984	17760
112	75264	896	1792	2688	3584	4480	5376	6272	7168	8064	8960
113	76614	1808	3616	5424	7232	9040	10848	12656	14464	16272	18080
114	77976	912	1824	2736	3648	4560	5472	6384	7296	8208	9120
115	79350	1840	3680	5520	7360	9200	11040	12880	14720	16560	18400
116	80736	928	1856	2784	3712	4640	5568	6496	7424	8352	9280
117	82134	1872	3744	5616	7488	9360	11232	13104	14976	16848	18720
118	83544	944	1888	2832	3776	4720	5664	6608	7552	8496	9440
119	84966	1904	3808	5712	7616	9520	11424	13328	15232	17136	19040
120	86400	960	1920	2880	3840	4800	5760	6720	7680	8640	9600
121	87846	1936	3872	5808	7744	9680	11616	13552	15488	17424	19360
122	89304	976	1952	2928	3904	4880	5856	6832	7808	8784	9760
123	90774	1968	3936	5904	7872	9840	11808	13776	15744	17712	19680
124	92256	992	1984	2976	3968	4960	5952	6944	7936	8928	9920
125	93750	2000	4000	6000	8000	10000	12000	14000	16000	18000	20000
126	95256	1008	2016	3024	4032	5040	6048	7056	8064	9072	10080
127	96774	2032	4064	6096	8128	10160	12192	14224	16256	18288	20320
128	98304	1024	2048	3072	4096	5120	6144	7168	8192	9216	10240
129	99846	2064	4128	6192	8256	10320	12384	14448	16512	18576	20640

Table 3.2: Sample choices for NEX\_XI given NPROC\_XI based upon the relationship  $\text{NEX\_XI} = 8 \times c \times \text{NPROC\_XI}$ , where the integer  $c \geq 1$ . The number of MPI slices, i.e., the total number of required processors, is  $6 \times \text{NPROC\_XI}^2$ , as illustrated in Figure 3.1. The approximate shortest period at which the global simulation is accurate for a given value of NEX\_XI can be estimated by running the small serial program `xcreate_header_file`.

Finally, you need to provide a file that tells MPI what compute nodes to use for the simulations. The file must have a number of entries (one entry per line) at least equal to the number of processors needed for the run. A sample file is provided in the file `mymachines`. This file is not used by the mesher or solver, but is required by the `go_mesher` and `go_solver` default job submission scripts. See Chapter 11 for information about running the code on a system with a scheduler, e.g., LSF.

Now that you have set the appropriate parameters in the `Par_file` and have compiled the mesher, you are ready to launch it! This is most easily accomplished based upon the `go_mesher` script. When you run on a PC cluster, the script assumes that the nodes are named `n001`, `n002`, etc. If this is not the case, change the `tr -d 'n'` line in the script. You may also need to edit the last command at the end of the script that invokes the `mpirun` command.

Mesher output is provided in the `OUTPUT_FILES` directory in `output_mesher.txt`; this file provides lots of details about the mesh that was generated. Alternatively, output can be directed to the screen instead by uncommenting a line in `constants.h`:

```
! uncomment this to write messages to the screen
! integer, parameter :: IMAIN = ISTANDARD_OUTPUT
```

Note that on very fast machines, writing to the screen may slow down the code.

Another file generated by the mesher is the header file `OUTPUT_FILES/values_from_mesher.h`. This file specifies a number of constants and flags needed by the solver. These values are passed statically to the solver for reasons of speed. Some useful statistics about the mesh are also provided in this file.

For a given model, set of nodes, and set of parameters in `Par_file`, one only needs to run the mesher once and for all, even if one wants to run several simulations with different sources and/or receivers (the source and receiver information is used in the solver only).

Please note that it is difficult to correctly sample S waves in the inner core of the Earth because S-wave velocity is very small there. Therefore, correctly sampling S waves in the inner core would require a very dense mesh, which in turn would drastically reduce the time step of the explicit time scheme because the P wave velocity is very high in the inner core (Poisson's ratio is roughly equal to 0.44). Because shear wave attenuation is very high in the inner core ( $Q_\mu$  is approximately equal to 85), we have therefore decided to design the inner core mesh such that P waves are very well sampled but S waves are right at the sampling limit or even slightly below. This works fine because spurious numerical oscillations due to S-wave subsampling are almost completely suppressed by attenuation. However, this implies that one should not use SPECFEM3D\_GLOBE with the regular mesh and period estimates of Table 3 to study the PKJKP phase very precisely. If one is interested in that phase, one should use typically 1.5 times to twice the number of elements NEX indicated in the table.

Regarding fluid/solid coupling at the CMB and ICB, in SPECFEM3D\_GLOBE we do not use the fluid-solid formulation of Komatitsch and Tromp [2002a] and Komatitsch and Tromp [2002b] anymore, we now use a displacement potential in the fluid (rather than a velocity potential as in Komatitsch and Tromp [2002a] and Komatitsch and Tromp [2002b]). This leads to the simpler fluid-solid matching condition introduced by Chaljub and Valette [2004] with no numerical iterations at the CMB and ICB.

For accuracy reasons, in the mesher the coordinates of the mesh points (arrays `xstore`, `ystore` and `zstore`) are always created in double precision. If the solver is compiled in single precision mode, the mesh coordinates are converted to single precision before being saved in the local mesh files.

## 3.1 Memory requirements

The SPECFEM3D\_GLOBE memory requirements can be estimated before or after running the mesher using the small serial program `./bin/xcreate_header_file`, which reads the input file `DATA/Par_file` and displays the total amount of memory that will be needed by the mesher and the solver to run it. This way, users can easily modify the parameters and check that their simulation will fit in memory on their machine. The file created by `xcreate_header_file` is called `OUTPUT_FILES/values_from_mesher.h` and contains even more details about the future simulation.

Please note that running these codes is optional because no information needed by the solver is generated.

## Chapter 4

# Running the Solver **xspecfem3D**

Now that you have successfully run the mesher, you are ready to compile the solver. For reasons of speed, the solver uses static memory allocation. Therefore it needs to be recompiled (type ‘make clean’ and ‘make specfem3D’) every time one reruns the mesher with different parameters. To compile the solver one needs a file generated by the mesher in the directory `OUTPUT_FILES` called `values_from_mesher.h`, which contains parameters describing the static size of the arrays as well as the setting of certain flags.

The solver needs three input files in the `DATA` directory to run: the `Par_file` that was discussed in detail in Chapter 3, the earthquake source parameter file `CMTSOLUTION` or the force source parameter file `FORCESOLUTION`, and the stations file `STATIONS`. Most parameters in the `Par_file` should be set prior to running the mesher. Only the following parameters may be changed after running the mesher:

- the simulation type control parameters: `SIMULATION_TYPE` and `SAVE_FORWARD`
- the record length `RECORD_LENGTH_IN_MINUTES`
- the movie control parameters `MOVIE_SURFACE`, `MOVIE_VOLUME`, and `NTSTEPS_BETWEEN_FRAMES`
- the multi-stage simulation parameters `NUMBER_OF_RUNS` and `NUMBER_OF_THIS_RUN`
- the output information parameters `NTSTEP_BETWEEN_OUTPUT_INFO`, `NTSTEP_BETWEEN_OUTPUT_SEISMOS`, `OUTPUT_SEISMOS_ASCII_TEXT`, `OUTPUT_SEISMOS_SAC_ALPHANUM`, `OUTPUT_SEISMOS_SAC_BINARY` and `ROTATE_SEISMOGRAMS_RT`
- the `RECEIVERS_CAN_BE_BURIED` and `PRINT_SOURCE_TIME_FUNCTION` flags

Any other change to the `Par_file` implies rerunning both the mesher and the solver.

For any particular earthquake, the `CMTSOLUTION` file that represents the point source may be obtained directly from the Harvard Centroid-Moment Tensor (CMT) web page (<http://www.globalcmt.org>). It looks like this:

Preliminary Determination of Epicenter										body-wave magnitude mb	surface-wave magnitude Ms	PDE event name
year	day	min	sec	latitude	longitude	depth						
month	hour											
PDE	2002	11	3	22	12	41.00	63.5200	-147.4400	4.9	7.0	8.5	CENTRAL ALASKA
event name:	110302J											
time shift:	47.0000											
half duration:	23.5000											
latitude:	63.2300											
longitude:	-144.8900											
depth:	15.0000											
Mrr:	5.130000e+26											
Mtt:	-6.038000e+27											
Mpp:	5.525000e+27											
Mrt:	1.830000e+26											
Mrp:	2.615000e+27											
Mtp:	-3.937000e+27											

Harvard CMT solution

$$\mathbf{M} = \begin{bmatrix} M_{rr} & M_{r\theta} & M_{r\phi} \\ M_{r\theta} & M_{\theta\theta} & M_{\theta\phi} \\ M_{r\phi} & M_{\theta\phi} & M_{\phi\phi} \end{bmatrix}$$

$$M_0 = \frac{1}{\sqrt{2}} (\mathbf{M} : \mathbf{M})^{1/2} \approx 7.48 \times 10^{27} \text{ dyne cm}$$

$$M_w = \frac{2}{3} (\log_{10} M_0 - 16.1) \approx 7.85$$

Figure 4.1: CMTSOLUTION file obtained from the Harvard CMT catalog. The top line is the initial estimate of the source, which is used as a starting point for the CMT solution.  $\mathbf{M}$  is the moment tensor,  $M_0$  is the seismic moment, and  $M_w$  is the moment magnitude.

The CMTSOLUTION should be edited in the following way:

- For point-source simulations (see finite sources, page 29) we recommend setting the source half-duration parameter `half duration` equal to zero, which corresponds to simulating a step source-time function, i.e., a moment-rate function that is a delta function. If `half duration` is not set to zero, the code will use a Gaussian (i.e., a signal with a shape similar to a ‘smoothed triangle’, as explained in Komatitsch and Tromp [2002a] and shown in Fig 4.2) source-time function with half-width `half duration`. We prefer to run the solver with `half duration` set to zero and convolve the resulting synthetic seismograms in post-processing after the run, because this way it is easy to use a variety of source-time functions (see Section 13.2). Komatitsch and Tromp [2002a] determined that the noise generated in the simulation by using a step source time function may be safely filtered out afterward based upon a convolution with the desired source time function and/or low-pass filtering. Use the postprocessing script `process_syn.p1` (see Section 13.2.2) with the `-h` flag, or the serial code `convolve_source_timefunction.f90` and the script `utils/convolve_source_timefunction.csh` for this purpose, or alternatively use signal-processing software packages such as SAC (<http://www.iris.edu/software/sac/>). Type

```
make convolve_source_timefunction
```

to compile the code and then set the parameter `hdur` in `utils/convolve_source_timefunction.csh` to the desired half-duration.

- The zero time of the simulation corresponds to the center of the triangle/Gaussian, or the centroid time of the earthquake. The start time of the simulation is  $t = -1.5 * \text{half duration}$  (the 1.5 is to make sure the moment rate function is very close to zero when starting the simulation). To convert to absolute time  $t_{\text{abs}}$ , set

$$t_{\text{abs}} = t_{\text{pde}} + \text{time shift} + t_{\text{synthetic}}$$

where  $t_{\text{pde}}$  is the time given in the first line of the CMTSOLUTION, `time shift` is the corresponding value from the original CMTSOLUTION file and  $t_{\text{synthetic}}$  is the time in the first column of the output seismogram.

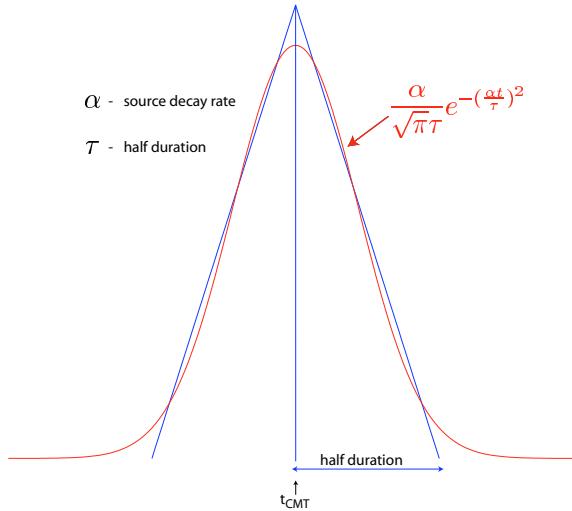


Figure 4.2: Comparison of the shape of a triangle and the Gaussian function actually used.

If you know the earthquake source in strike/dip/rake format rather than in CMTSOLUTION format, use the C code `utils/strike_dip_rake_to_CMTSOLUTION.c` to convert it. The conversion formulas are given for instance in Aki and Richards [1980]. Note that the Aki and Richards [1980] convention is slightly different from the Harvard CMTSOLUTION convention (the sign of some components is different). The C code outputs both.

Centroid latitude and longitude should be provided in geographical coordinates. The code converts these coordinates to geocentric coordinates [Dahlen and Tromp, 1998]. Of course you may provide your own source representations by designing your own CMTSOLUTION file. Just make sure that the resulting file adheres to the Harvard CMT conventions (see Appendix A). Note that the first line in the CMTSOLUTION file is the Preliminary Determination of Earthquakes (PDE) solution performed by the USGS NEIC, which is used as a seed for the Harvard CMT inversion. The PDE solution is based upon P waves and often gives the hypocenter of the earthquake, i.e., the rupture initiation point, whereas the CMT solution gives the ‘centroid location’, which is the location with dominant moment release. The PDE solution is not used by our software package but must be present anyway in the first line of the file.

In the current version of the code, the solver can run with a non-zero time shift in the CMTSOLUTION file. Thus one does not need to set time shift to zero as it was the case for previous versions of the code. time shift is only used for writing centroid time in the SAC headers (see Appendix D). CMT time is obtained by adding time shift to the PDE time given in the first line in the CMTSOLUTION file. Therefore it is recommended not to modify time shift to have the correct timing information in the SAC headers without any post-processing of seismograms.

To simulate a kinematic rupture, i.e., a finite-source event, represented in terms of  $N_{\text{sources}}$  point sources, provide a CMTSOLUTION file that has  $N_{\text{sources}}$  entries, one for each subevent (i.e., concatenate  $N_{\text{sources}}$  CMTSOLUTION files to a single CMTSOLUTION file). At least one entry (not necessarily the first) must have a zero time shift, and all the other entries must have non-negative time shift. If none of the entries has a zero time shift in the CMTSOLUTION file, the smallest time shift is subtracted from all sources to initiate the simulation. Each subevent can have its own half duration, latitude, longitude, depth, and moment tensor (effectively, the local moment-density tensor).

Note that the zero in the synthetics does NOT represent the hypocentral time or centroid time in general, but the timing of the *center* of the source triangle with zero time shift (Fig 4.3).

Although it is convenient to think of each source as a triangle, in the simulation they are actually Gaussians (as they have better frequency characteristics). The relationship between the triangle and the Gaussian used is shown in Fig 4.2. For finite fault simulations it is usually not advisable to use a zero half duration and convolve afterwards, since the half duration is generally fixed by the finite fault model.

The FORCESOLUTION file should be edited in the following way:

- The first line is only the header for the force solution, which can be used as the identifier for the force source.
- `time shift`: For a single force source, set this parameter equal to 0.0 (The solver will not run otherwise!); the time shift parameter would simply apply an overall time shift to the synthetics, something that can be done in the post-processing (see Section 13.2).
- `half duration`: Set the half duration value (s) for Step source time function. In case that the solver uses a (pseudo) Dirac delta source time function to represent a force point source, a very short duration of five time steps is automatically set by default. For a Ricker source time function, set the dominant frequency value (Hz). See the parameter `source time function`: below for source time functions.
- `latitude`: Set the latitude of the force source.
- `longitude`: Set the longitude of the force source.
- `depth`: Set the depth of the force source (km).
- `source time function`: Set the type of source time function. 0 = Step function, 1= Ricker function.
- `factor force source`: Set the magnitude of the force source.
- `component dir vect source E`: Set the East component of a direction vector for the force source. Direction vector is not necessarily a unit vector.
- `component dir vect source N`: Set the North component of a direction vector for the force source.
- `component dir vect source Z_up`: Set the vertical component of a direction vector for the force source. Sign convention follows the positive upward direction.

Where necessary, set a FORCESOLUTION file in the same way you configure a CMTSOLUTION file with  $N_{\text{sources}}$  entries, one for each subevent (i.e., concatenate  $N_{\text{sources}}$  FORCESOLUTION files to a single FORCESOLUTION file). At least one entry (not necessarily the first) must have a zero `time shift`, and all the other entries must have non-negative `time shift`. Each subevent can have its own set of parameters `latitude`, `longitude`, `depth`, `half duration`, etc.

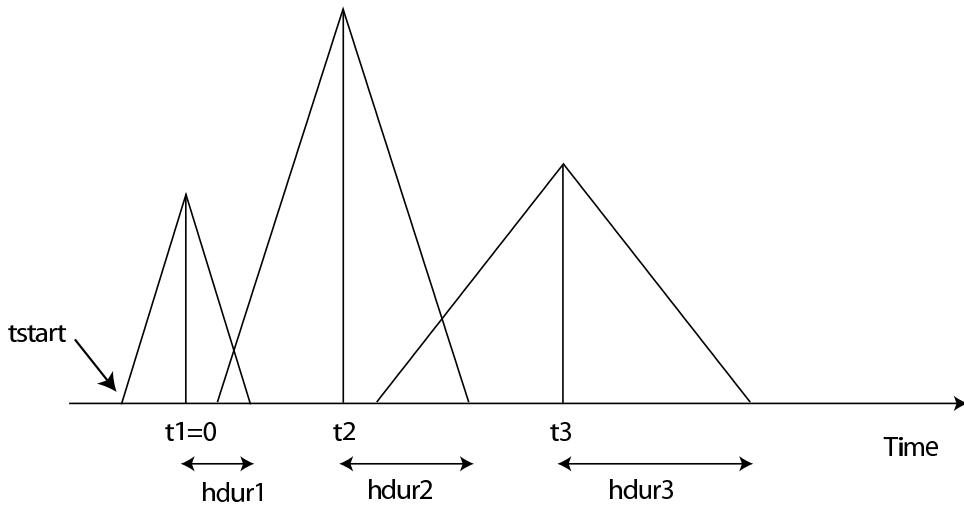


Figure 4.3: Example of timing for three sources. The center of the first source triangle is defined to be time zero. Note that this is NOT in general the hypocentral time, or the start time of the source (marked as `tstart`). The parameter `time shift` in the CMTSOLUTION file would be `t1(=0)`, `t2`, `t3` in this case, and the parameter `half duration` would be `hdur1`, `hdur2`, `hdur3` for the sources 1, 2, 3 respectively.

Network		Longitude (deg)		Burial (m)	
Station	Latitude (deg)		Elevation (m)		
SFJD	IU	66.9960	-50.6215	328.0	0.0
SAML	IU	-8.9488	-63.1832	130.0	0.0
BBSR	IU	32.3712	-64.6962	6.0	0.0
RAO	IU	-29.2517	-177.9183	110.0	0.0
LAST	GE	35.1610	25.4790	870.0	0.0
MCK	AK	63.7323	-148.9349	618.0	0.0
CTAO	AS	-20.0882	146.2545	357.0	0.0
KONO	AS	59.6491	9.5982	216.0	0.0
MAJO	AS	36.5409	138.2083	431.0	0.0
:	:	:	:	:	:

Figure 4.4: Sample STATIONS file. Station latitude and longitude should be provided in geographical coordinates. The width of the station label should be no more than 32 characters (see MAX\_LENGTH\_STATION\_NAME in the constants.h file), and the network label should be no more than 8 characters (see MAX\_LENGTH\_NETWORK\_NAME in the constants.h file).

The solver can calculate seismograms at any number of stations for basically the same numerical cost, so the user is encouraged to include as many stations as conceivably useful in the STATIONS file, which looks like this:

Each line represents one station in the following format:

```
Station Network Latitude(degrees) Longitude(degrees) Elevation(m) burial(m)
```

If you want to put a station on the ocean floor, just set elevation and burial depth in the STATIONS file to 0. Equivalently you can also set elevation to a negative value equal to the ocean depth, and burial depth to 0.

Solver output is provided in the OUTPUT\_FILES directory in the output\_solver.txt file. Output can be directed to the screen instead by uncommenting a line in constants.h:

```
! uncomment this to write messages to the screen
! integer, parameter :: IMAIN = ISTANDARD_OUTPUT
```

Note that on very fast machines, writing to the screen may slow down the code.

While the solver is running, its progress may be tracked by monitoring the ‘timestamp\*’ files in the OUTPUT\_FILES directory. These tiny files look something like this:

```
Time step #          200
Time:   0.6956667    minutes
Elapsed time in seconds =      252.6748970000000
Elapsed time in hh:mm:ss =      0 h 04 m 12 s
Mean elapsed time per time step in seconds =      1.263374485000000
Max norm displacement vector U in solid in all slices (m) =      1.9325
Max non-dimensional potential Ufluid in fluid in all slices = 1.1058885E-22
```

The timestamp\* files provide the Mean elapsed time per time step in seconds, which may be used to assess performance on various machines (assuming you are the only user on a node), as well as the Max norm displacement vector U in solid in all slices (m) and Max non-dimensional potential Ufluid in fluid in all slices. If something is wrong with the model, the mesh, or the source, you will see the code become unstable through exponentially growing values of the displacement and/or fluid potential with time, and ultimately the run will be terminated by the program when either of these values becomes greater than STABILITY\_THRESHOLD defined in constants.h. You can control the rate at which the timestamp files are written based upon the parameter NTSTEP\_BETWEEN\_OUTPUT\_INFO in the Par\_file.

Having set the `Par_file` parameters, and having provided the `CMTSOLUTION` and `STATIONS` files, you are now ready to launch the solver! This is most easily accomplished based upon the `go_solver` script (see Chapter 11 for information about running the code through a scheduler, e.g., LSF). You may need to edit the last command at the end of the script that invokes the `mpirun` command. Another option is to use the `runall` script, which compiles and runs both mesher and solver in sequence. This is a safe approach that ensures using the correct combination of mesher output and solver input.

It is important to realize that the CPU and memory requirements of the solver are closely tied to choices about attenuation (`ATTENUATION`) and the nature of the model (i.e., isotropic models are cheaper than anisotropic models). We encourage you to run a variety of simulations with various flags turned on or off to develop a sense for what is involved.

For the same model, one can rerun the solver for different events by simply changing the `CMTSOLUTION` file, and/or for different stations by changing the `STATIONS` file. There is no need to rerun the mesher. Of course it is best to include as many stations as possible, since this does not add significantly to the cost of the simulation.

## 4.1 Note on the simultaneous simulation of several earthquakes

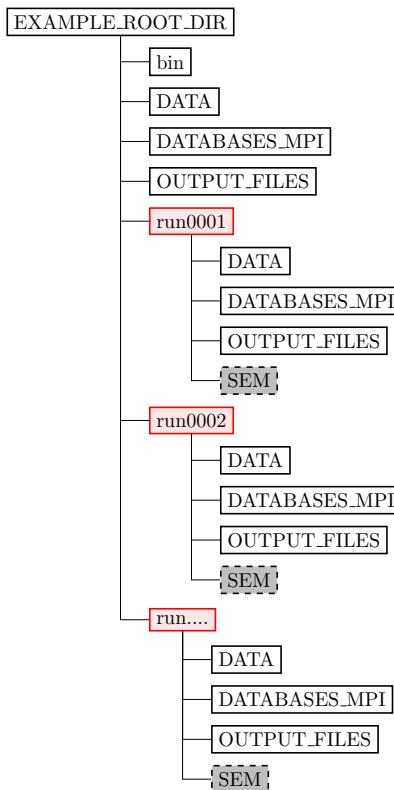


Figure 4.5: Directory structure when simulating several earthquakes at once. To improve readability, only directories have been drawn.

Figure 4.5 shows what the directory structure should look like when simulating multiple earthquakes at ones.

- The simulation is launched within the root directory `EXAMPLE_ROOT_DIR` (usually `mpirun -np N ./bin/xspecfem3D`).
- `DATA` should contain the `Par_file` parameter file with `NUMBER_OF_SIMULTANEOUS_RUNS` as explained in Chapter 3.

- DATABASES\_MPI and OUTPUT\_FILES directory may contain the mesher output but they are not required as they are superseded by the ones in the runXXX directories.
- runXXXX directories must be created beforehand. There should be as many as NUMBER\_OF\_SIMULTANEOUS\_RUNS and the numbering should be contiguous, starting from 0001. They all should have DATA, DATABASES\_MPI and OUTPUT\_FILES directories. Additionally a SEM directory containing adjoint sources have to be created to perform adjoint simulations.
- runXXXX/DATA directories must all contain a CMTSOLUTION file, a STATIONS file along with an eventual STATIONS\_ADJOINT file.
- If BROADCAST\_SAME\_MESH\_AND\_MODEL is set to `true`. in DATA/Par\_file, only run0001/OUTPUT\_FILES and run0001/DATABASES\_MPI directories need to contain the files outputted by the mesher.
- If BROADCAST\_SAME\_MESH\_AND\_MODEL is set to `false`. in DATA/Par\_file, every runXXXX/OUTPUT\_FILES and runXXXX/DATABASES\_MPI directories need to contain the files outputted by the mesher. Note that while the meshes might have been created from different models and parameter sets, they should have been created using the same number of MPI processes.

# Chapter 5

## Regional Simulations

The code has the option of running in one-chunk or six-chunk mode. The one-chunk options may be used for higher resolution regional simulations. A one-chunk mesh may have lateral dimensions other than the customary  $90^\circ$  per chunk, which can further increase the resolution of the mesh, and thus reduce the shortest period in the synthetic seismograms (but of course then also reducing the time step in order for the simulation to remain stable).

A disadvantage of regional simulations is that one needs to use approximate absorbing boundary conditions on the side and bottom edges of the model (e.g., see Komatitsch and Tromp [1999] for a description of the paraxial boundary conditions used). Figure 5.1 on the following page and Figure 5.2 on page 36 show an example of a one-chunk mesh centered on the Japan subduction zone, applied in the Japan regional waveform simulation [Chen et al., 2007].

### 5.1 One-Chunk Simulations

For a one-chunk regional simulation the following parameters need to be set in the `Par_file`:

**NCHUNKS** Must be set to 1.

**ANGULAR\_WIDTH\_XI\_IN\_DEGREES** Denotes the width of one side of the chunk ( $90^\circ$  is a classical value, but you can make it more or less if you want).

**ANGULAR\_WIDTH\_ETA\_IN\_DEGREES** Denotes the width of the second side of the chunk ( $90^\circ$  is a classical value, but you can make it more or less if you want). Note that this value may be different from **ANGULAR\_WIDTH\_XI\_IN\_DEGREES**.

**CENTER\_LATITUDE\_IN\_DEGREES** Defines the latitude of the center of the chunk (degrees).

**CENTER\_LONGITUDE\_IN\_DEGREES** Defines the longitude of the center of the chunk (degrees).

**GAMMA\_ROTATION\_AZIMUTH** Defines the rotation angle of the chunk about its center measured counter clockwise from due North (degrees). The corners of the mesh are output in `OUTPUT_FILES/values_from_mesher.h`. The output corner progression in `OUTPUT_FILES/values_from_mesher.h` is bottom left, bottom right, top left, top right. The rotation azimuth can be changed in the `Par_file` and the corners output (`OUTPUT_FILES/values_from_mesher.h`) by using `xcreate_header_file`. It is important to note that the mesher or the solver does not need to be run to determine the limits of a 1-chunk simulation.

**NEX\_XI** The number of spectral elements along the  $\xi$  side of the chunk. This number *must* be  $8 \times$  a multiple of `NPROC_XI` defined below. For a  $90^\circ$  chunk, we do not recommend using `NEX_XI` less than 64 because the curvature of the Earth cannot be honored if one uses too few elements, which results in inaccurate and unstable simulations.

**NEX\_ETA** The number of spectral elements along the  $\eta$  side of the chunk. This number *must* be  $8 \times$  a multiple of `NPROC_ETA` defined below. Note that in order to get elements that are close to square on the Earth's surface, the following ratios should be similar:

```
ANGULAR_WIDTH_XI_IN_DEGREES / NEX_XI
ANGULAR_WIDTH_ETA_IN_DEGREES / NEX_ETA
```

Because of the geometry of the cubed sphere, the option of having different values for NEX\_XI and NEX\_ETA is available only for regional simulations when NCHUNKS = 1 (1/6th of the sphere).

**NPROC\_XI** The number of processors or mesh slices along the  $\xi$  side of the chunk. To accommodate the mesh doubling layers, we must have  $NEX_XI = 8 \times c \times NPROC_XI$ , where  $c \geq 1$  is a positive integer. See Table 3 for various suitable choices.

**NPROC\_ETA** The number of processors or slices along the  $\eta$  side of the chunk; we must have  $NEX_ETA = 8 \times c \times NPROC_ETA$ , where  $c \geq 1$  is a positive integer. NPROC\_XI and NPROC\_ETA must be equal when NCHUNKS = 6.

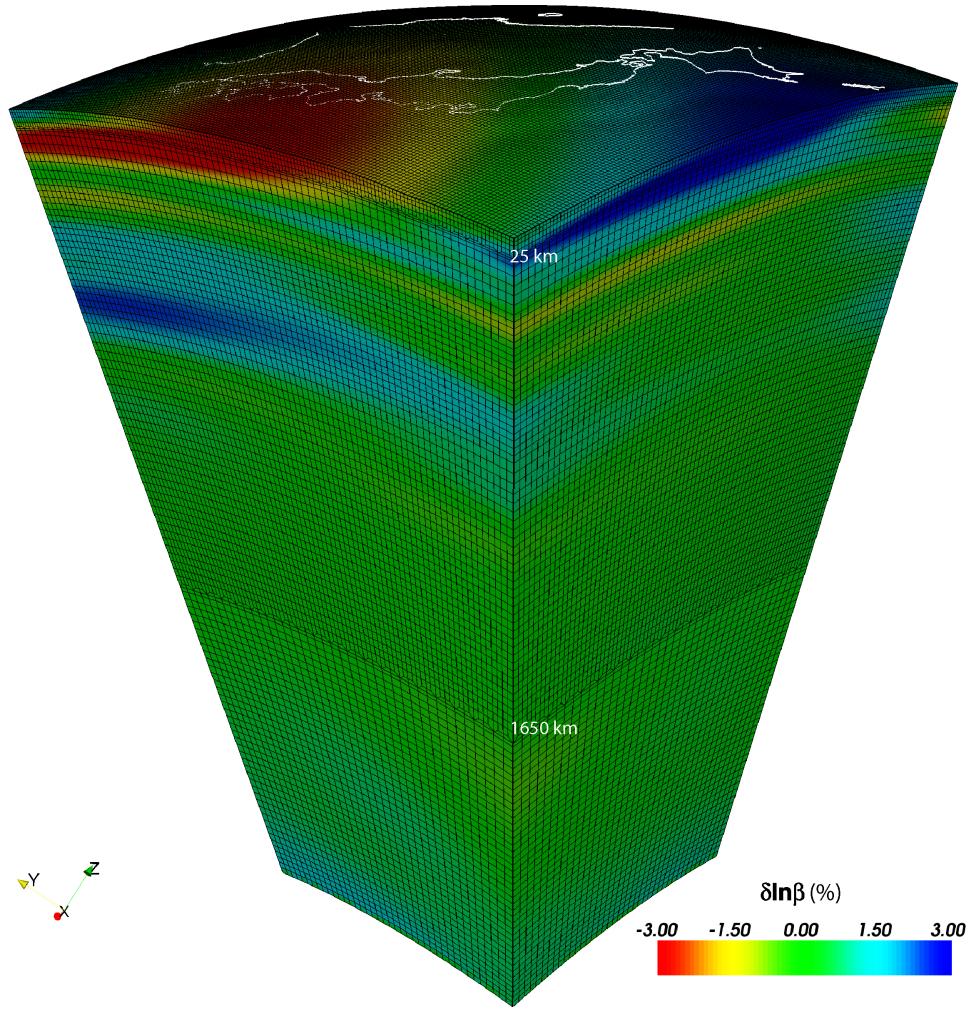


Figure 5.1: S-wave velocity anomalies from the global tomographic model s20rts [Ritsema and Van Heijst, 2000] are superimposed on the mesh. For parallel computing purposes, the one-chunk SEM simulation is subdivided in terms of 64 slices. The center of the chunk is at  $(38.5^\circ \text{N}, 137.5^\circ \text{E})$ , and the lateral dimensions are  $30^\circ \times 30^\circ$ . Two doubling layers are indicated at a depth of 25 km (PREM Moho depth) and a depth of about 1650 km. Shows full view of 25 neighboring slices; see Figure 5.2 for close-up of upper mantle mesh.

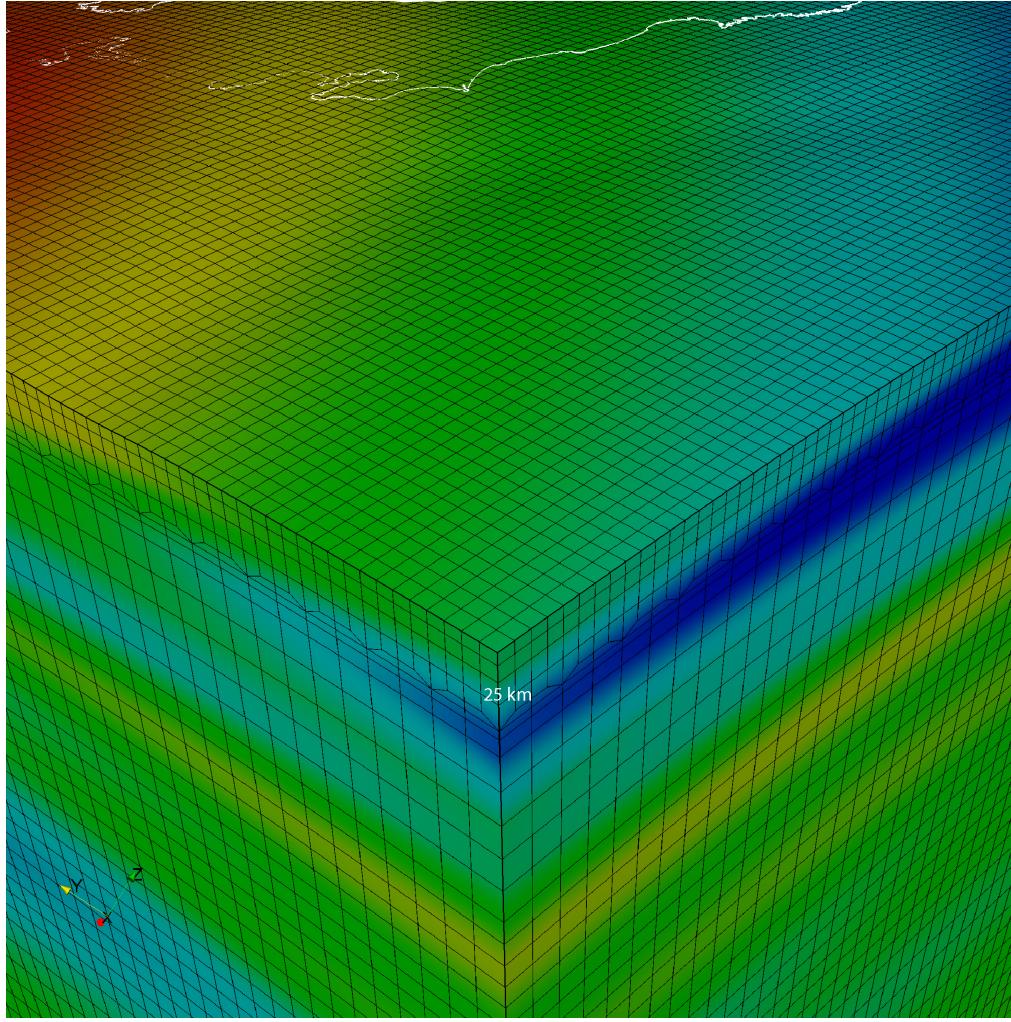


Figure 5.2: Close-up view of the upper mantle mesh shown in Figure 5.1. Note that the element size in the crust (top layer) is  $13 \text{ km} \times 13 \text{ km}$ , and that the size of the spectral elements is doubled in the upper mantle. The velocity variation is captured by  $\text{NGLL} = 5$  grid points in each direction of the elements [Komatitsch and Tromp, 2002a,b].

**ABSORBING\_CONDITIONS** Set to `.true.` for regional simulations. For instance, see Komatitsch and Tromp [1999] for a description of the paraxial boundary conditions used. Note that these conditions are never perfect, and in particular surface waves may partially reflect off the artificial boundaries. Note also that certain arrivals, e.g., PKIKPPKIKP, will be missing from the synthetics.

When the width of the chunk is different from  $90^\circ$  (or the number of elements is greater than 1248), the radial distribution of elements needs to be adjusted as well to maintain spectral elements that are as cube-like as possible. The code attempts to do this, but be sure to view the mesh with your favorite graphics package to make sure that the elements are well behaved. Remember: a high-quality mesh is paramount for accurate simulations. In addition to a reorganization of the radial distribution of elements, the time stepping and period range in which the attenuation is applied is automatically determined. The minimum and maximum periods for attenuation are:

$$\omega_{\max} = \omega_{\min} \times 10^{W_3}$$

where  $W_3$  is the optimal width in frequency for 3 Standard Linear Solids, about 1.75. See `read_compute_parameters.f90` for more details.

The time stepping is determined in a similar fashion as Equation (48) in Komatitsch and Tromp [2002a]:

$$\text{dt} = S_c \text{ Element Width in km } (r = \text{ICB}) / \text{Velocity } (r = \text{ICB})$$

where  $S_c$  is the stability condition (about 0.4). We use the radius at the inner core boundary because this is where the maximum velocity/element width occurs. Again, see `read_compute_parameters.f90` for all the details.

The approximate shortest period at which a regional simulation is accurate may be determined based upon the relation

$$\text{shortest period (s)} \simeq (256/\text{NEX\_XI}) \times (\text{ANGULAR\_WIDTH\_XI\_IN\_DEGREES}/90) \times 17. \quad (5.1)$$

# Chapter 6

## Adjoint Simulations

Adjoint simulations are generally performed for two distinct applications. First, they can be used for earthquake source inversions, especially earthquakes with large ruptures such as the Sumatra-Andaman event [Lay et al., 2005, Ammon et al., 2005, Park et al., 2005]. Second, they can be used to generate finite-frequency sensitivity kernels that are a critical part of tomographic inversions based upon 3D reference models [Tromp et al., 2005, Liu and Tromp, 2006, Tromp et al., 2008, Liu and Tromp, 2008]. In either case, source parameter or velocity structure updates are sought to minimize a specific misfit function (e.g., waveform or traveltimes differences), and the adjoint simulation provides a means of computing the gradient of the misfit function and further reducing it in successive iterations. Applications and procedures pertaining to source studies and finite-frequency kernels are discussed in Sections 6.1 and 6.2, respectively. The two related parameters in the `Par_file` are `SIMULATION_TYPE` (1, 2 or 3) and `SAVE_FORWARD` (boolean).

### 6.1 Adjoint Simulations for Sources Only (not for the Model)

In the case where a specific misfit function is minimized to invert for the earthquake source parameters, the gradient of the misfit function with respect to these source parameters can be computed by placing time-reversed seismograms at the receivers and using them as sources in an adjoint simulation, and then the value of the gradient is obtained from the adjoint seismograms recorded at the original earthquake location.

#### 1. Prepare the adjoint sources

- (a) First, run a regular forward simulation (`SIMULATION_TYPE = 1` and `SAVE_FORWARD = .false.`). You can automatically set these two variables using the `utils/change_simulation_type.pl` script:  
`utils/change_simulation_type.pl -f`  
and then collect the recorded seismograms at all the stations given in `DATA/STATIONS`.
- (b) Then select the stations for which you want to compute the time-reversed adjoint sources and run the adjoint simulation, and compile them into the `DATA/STATIONS_ADJOINT` file, which has the same format as the regular `DATA/STATIONS` file.
  - Depending on what type of misfit function is used for the source inversion, adjoint sources need to be computed from the original recorded seismograms for the selected stations and saved in the `SEM/` directory with the format `NT.STA.?X?.adj`, where `STA`, `NT` are the station name and network code given in the `DATA/STATIONS_ADJOINT` file, and `?X?` represents the channel name of a particular adjoint seismogram where the first letter corresponds to the band code governed by the resolution of simulations, for example, generally `MX?` for the current resolution of global simulations (see Appendix E for details). The last letter of channel names is the component name `E/N/Z`.
  - The adjoint seismograms are in the same format as the original seismogram (`NT.STA.?X?.sem?`), with the same start time, time interval and record length.
- (c) Notice that even if you choose to time reverse only one component from one specific station, you still need to supply all three components because the code is expecting them (you can set the other two components to be zero).

- (d) Also note that since time-reversal is done in the code itself, no explicit time-reversing is needed for the preparation of the adjoint sources, i.e., the adjoint sources are in the same forward time sense as the original recorded seismograms.

## 2. Set the related parameters and run the adjoint simulation

In the DATA/Par\_file, set the two related parameters to be `SIMULATION_TYPE = 2` and `SAVE_FORWARD = .false.`. More conveniently, use the scripts `utils/change_simulation_type.pl` to modify the Par\_file automatically (`change_simulation_type.pl -a`). Then run the solver to launch the adjoint simulation.

## 3. Collect the seismograms at the original source location

After the adjoint simulation has completed successfully, get the seismograms from directory `OUTPUT_FILES`.

- These adjoint seismograms are recorded at the locations of the original earthquake sources given by the DATA/CMTSOLUTION file, and have names of the form `NT.S?????.S???.sem` for the six-component strain tensor (SNN, SEE, SZZ, SNE, SNZ, SEZ) at these locations, and `NT.S?????.?X?.sem` for the three-component displacements (i.e., MXN, MXE, MXZ) recorded at these locations.
- `?????` denotes the source number; for example, if the original CMTSOLUTION provides only a point source, then the seismograms collected will start with `S00001`.
- These adjoint seismograms provide critical information for the computation of the gradient of the misfit function.

## 6.2 Adjoint Simulations for Finite-Frequency Kernels (Kernel Simulation)

Finite-frequency sensitivity kernels are computed in two successive simulations (please refer to Liu and Tromp [2006] and Tromp et al. [2008] for details).

### 1. Run a forward simulation with the state variables saved at the end of the simulation

Prepare the CMTSOLUTION and STATIONS files, set the parameters `SIMULATION_TYPE = 1` and `SAVE_FORWARD = .true.` in the Par\_file (`change_simulation_type -F`), and run the solver.

- Notice that attenuation is not fully implemented yet for the computation of finite-frequency kernels; if `ATTENUATION = .true.` is set in the Par\_file, only effects on phase shift are accounted for but not on amplitude of the signals. However, we suggest you use the same setting for ATTENUATION as for your forward simulations.
- We also suggest you modify the half duration of the CMTSOLUTION to be similar to the accuracy of the simulation (see Equation 3.1 or 5.1) to avoid too much high-frequency noise in the forward wavefield, although theoretically the high-frequency noise should be eliminated when convolved with an adjoint wavefield with the proper frequency content.
- This forward simulation differs from the regular simulations (`SIMULATION_TYPE = 1` and `SAVE_FORWARD = .false.`) described in the previous chapters in that the state variables for the last time step of the simulation, including wavefields of the displacement, velocity, acceleration, etc., are saved to the LOCAL\_PATH to be used for the subsequent simulation.
- For regional simulations, the files recording the absorbing boundary contribution are also written to the LOCAL\_PATH when `SAVE_FORWARD = .true..`

### 2. Prepare the adjoint sources

The adjoint sources need to be prepared the same way as described in Section 6.1, item 1.

- In the case of traveltime finite-frequency kernel for one source-receiver pair, i.e., point source from the CMTSOLUTION, and one station in the STATIONS\_ADJOINT list, we supply a sample program in `utils/adjoint_sources/travelttime` to cut a certain portion of the original displacement seismograms and convert them into the proper adjoint source to compute the finite-frequency kernel.

```
xcreate_adjsrc_travelttime t1 t2 ifile[0-5] E/N/Z-ascii-files [baz]
```

where  $t_1$  and  $t_2$  are the start and end time of the portion you are interested in,  $ifile$  denotes the component of the seismograms to be used (0 for all three components, 1 for east, 2 for north, and 3 for vertical, 4 for transverse, and 5 for radial component),  $E/N/Z$ -ascii-files indicate the three-component displacement seismograms in the right order, and  $baz$  is the back-azimuth of the station from the event location. Note that  $baz$  is only supplied when  $ifile = 4$  or  $5$ .

- Similarly, a sample program to compute adjoint sources for amplitude finite-frequency kernels may be found in `utils/adjoint_sources/amplitude` and used in the same way as described for travelttime measurements

```
xcreate_adjsrc_amplitude t1 t2 ifile[0-5] E/N/Z-ascii-files [baz].
```

For adjoint runs (`SIMULATION_TYPE = 3`), the adjoint sources need to be put in the "SEM" sub-directory in the root directory of the code.

If your adjoint source have names of the following form for instance:

`NET.STA00.MXZ.sem.ascii.adj` `NET.STA00.MXZ.sem.ascii.adj`

you will need to rename them to:

`NET.STA00.MXZ.adj` `NET.STA00.MXZ.adj`

i.e. suppress ".sem.ascii".

You will also need to create a file called `STATIONS_ADJOINT` in the "DATA" directory in the root directory of the code. That file can be identical to the `DATA/STATIONS` file if you had a single station in `STATIONS`.

### 3. Run the kernel simulation

With the successful forward simulation and the adjoint source ready in `SEM/`, set `SIMULATION_TYPE = 3` and `SAVE_FORWARD = .false.` in the `Par_file(change_simulation_type.pl -b)`, and rerun the solver.

- The adjoint simulation is launched together with the back reconstruction of the original forward wavefield from the state variables saved from the previous forward simulation, and the finite-frequency kernels are computed by the interaction of the reconstructed forward wavefield and the adjoint wavefield.
- The back-reconstructed seismograms at the original station locations are saved to the `OUTPUT_FILES` directory at the end of the kernel simulations.
- These back-constructed seismograms can be compared with the time-reversed original seismograms to assess the accuracy of the backward reconstruction, and they should match very well (in the time-reversed sense).
- The files containing the density, P-wave speed and S-wave speed kernels are saved in the `LOCAL_PATH` with the names of `proc??????_reg_?_rho(alpha,beta)_kernel.bin`, where `proc???????` represents the processor number, and `reg_?` denotes the region these kernels are for, including mantle (`reg_1`), outer core (`reg_2`), and inner core (`reg_3`). The output kernels are in the unit of  $s/km^3$ .
- Note that if you set the flag `APPROXIMATE_HESS_KL = .true.` in the `constants.h` file and recompile the solver, the adjoint simulation also saves files `proc??????_reg_1_hess_kernel.bin` which can be used as preconditioners in the crust-mantle region for iterative inverse optimization schemes.

### 4. Run the boundary kernel simulation

If you set the `SAVE_BOUNDARY_MESH = .true.` in the `constants.h` file before the simulations, i.e., at the beginning of step 1, you will get not only the volumetric kernels as described in step 3, but also boundary kernels for the Earth's internal discontinuities, such as Moho, 410-km discontinuity, 670-km discontinuity, CMB and ICB. These kernel files are also saved in the local scratch directory defined by `LOCAL_PATH` and have names such as `proc??????_reg_1(2)_Moho(d400,d670,CMB,ICB)_kernel.bin`. For a theoretical derivation of the boundary kernels, refer to Tromp et al. [2005], and for the visualization of the boundary kernels, refer to Section 10.3.

### 5. Run the anisotropic kernel simulation

Instead of the kernels for the isotropic wave speeds, you can also compute the kernels for the 21 independent components  $C_{IJ}$ ,  $I, J = 1, \dots, 6$  (using Voigt's notation) of the elastic tensor in the (spherical) geographical coordinate system. This is done by setting `ANISOTROPIC_KL = .true.` in `constants.h` before step 3. The definition of the parameters  $C_{IJ}$  in terms of the corresponding components  $c_{ijkl}, i, j, k, l = 1, 2, 3$  of the elastic tensor in spherical coordinates follows Chen and Tromp [2007]. The computation of the anisotropic kernels is only implemented in the crust and mantle regions. The 21 anisotropic kernels are saved in the `LOCAL_PATH` in one file with the name of `proc?????_reg1_cijkl_kernel.bin` (with `proc?????` the processor number). The output kernels correspond to perturbation  $\delta C_{IJ}$  of the elastic parameters and their unit is in  $s/GPa/km^3$ . For consistency, the output density kernels with this option turned on are for a perturbation  $\delta\rho$  (and not  $\frac{\delta\rho}{\rho}$ ) and their unit is in  $s / (kg/m^3) / km^3$ . These ‘primary’ anisotropic kernels can then be combined to obtain the kernels related to other descriptions of anisotropy. This can be done, for example, when combining the kernel files from slices into one mesh file (see Section 10.3).

In general, the first three steps need to be run sequentially to ensure proper access to the necessary files at different stages. If the simulations are run through some cluster scheduling system (e.g., LSF), and the forward simulation and the subsequent kernel simulations cannot be assigned to the same set of computer nodes, the kernel simulation will not be able to access the database files saved by the forward simulation. Solutions for this problem are provided in Chapter 11. Visualization of the finite-frequency kernels is discussed in Section 10.3.

## **Chapter 7**

# **Doing tomography, i.e., updating the model based on the sensitivity kernels obtained**

The process is described in the same chapter of the manual of SPECFEM3D. Please refer to it.

# Chapter 8

## Noise Cross-correlation Simulations

The new version of SPECFEM3D\_GLOBE includes functionality for seismic noise tomography. Users are recommended to familiarize themselves first with the procedures for running regular earthquake simulations (Chapters 3–5) and adjoint simulations (Chapter 6). Also, make sure you read the paper ‘Noise cross-correlation sensitivity kernels’ [Tromp et al., 2010b] in order to understand noise simulations from a theoretical perspective.

### 8.1 New Requirements on ‘Old’ Input Parameter Files

As usual, the three main input files are crucial: DATA/Par\_file, DATA/CMTSOLUTION and DATA/STATIONS.

DATA/CMTSOLUTION is required for all simulations. However, it may seem unexpected to have it listed here, since the noise simulations should have nothing to do with the earthquake – hence the DATA/CMTSOLUTION. For noise simulations, it is critical to have no earthquakes. In other words, the moment tensor specified in DATA/CMTSOLUTION must be set to ZERO!

DATA/STATIONS remains the same as in previous earthquake simulations, except that the order of stations listed in DATA/STATIONS is now important. The order will be used later to identify the ‘main’ receiver, i.e., the one that simultaneously cross correlates with the others. Please be noted that the actual station file used in the simulation is OUTPUT\_FILES/STATIONS\_FILTERED, which is generated when you run your simulations. (e.g., in regional simulations we may have included stations out of the region of our interests in DATA/STATIONS, so we have to get rid of them.)

DATA/Par\_file also requires careful attention. New to this version of SPECFEM3D\_GLOBE, a parameter called NOISE\_TOMOGRAPHY has been added that specifies the type of simulation to be run. NOISE\_TOMOGRAPHY is an integer with possible values 0, 1, 2 and 3. For example, when NOISE\_TOMOGRAPHY equals 0, a regular earthquake simulation will be run. When NOISE\_TOMOGRAPHY is equal to 1/2/3, you are about to run step 1/2/3 of the noise simulations respectively. Should you be confused by the three steps, refer to Tromp et al. [2010b] for details.

Another change to DATA/Par\_file involves the parameter RECORD\_LENGTH\_IN\_MINUTES. While for regular earthquake simulations this parameter specifies the length of synthetic seismograms generated, for noise simulations it specifies the length of the seismograms used to compute cross correlations. The actual cross correlations are thus twice this length. The code automatically makes modification accordingly, if NOISE\_TOMOGRAPHY is not zero.

There are other parameters in DATA/Par\_file which should be given specific values. For instance, NUMBER\_OF\_RUNS and NUMBER\_OF\_THIS\_RUN must be 1; ROTATE\_SEISMOGRAMS\_RT, SAVE\_ALL\_SEISMOGRAMS\_IN\_ONE\_FILES, USE\_BINARY\_FOR\_LARGE\_FILE and MOVIE\_COARSE should be .false.. Moreover, since the first two steps for calculating noise cross-correlation kernels correspond to forward simulations, SIMULATION\_TYPE must be 1 when NOISE\_TOMOGRAPHY equals 1 or 2. Also, we have to reconstruct the ensemble forward wavefields in adjoint simulations, therefore we need to set SAVE\_FORWARD to .true. for the second step, i.e., when NOISE\_TOMOGRAPHY

equals 2. The third step is for kernel constructions. Hence `SIMULATION_TYPE` should be 3, whereas `SAVE_FORWARD` must be `.false..`

## 8.2 Noise Simulations: Step by Step

Proper parameters in those ‘old’ input files are not enough for noise simulations to run. We have a lot more ‘new’ input parameter files to specify: for example, the ensemble-averaged noise spectrum, the noise distribution etc. However, since there are a few ‘new’ files, it is better to introduce them sequentially. Read through this section even if you don’t understand some parts temporarily, since some examples you can go through are provided in this package.

### 8.2.1 Pre-simulation

- As usual, we first configure the software package using:

```
./configure FC=ifort MPIFC=mpif90
```

- Next, we need to compile the source code using:

```
make xmshfem3D
make xspecfem3D
```

Before compilation, the `DATA/Par_file` must be specified correctly, e.g., `NOISE_TOMOGRAPHY` shouldn’t be zero; `RECORD_LENGTH_IN_MINUTES`, `NEX_XI` and `NEX_ETA` must be what you want in your real simulations. Otherwise you may get wrong informations which will cause problems later. (it is good to always re-compile the code before you run simulations)

- After compiling, you will find two important numbers besides the needed executables:

```
number of time steps = 31599
time_stepping of the solver will be: 0.19000
```

The first number will be denoted as `NSTEP` from now on, and the second one as `dt`. The two numbers are essential to calculate the ensemble-averaged noise spectrum from either Peterson’s noise model or just a simple flat power spectrum (corresponding to 1-bit preprocessing). Should you miss the two numbers, you can run `./xcreate_header_file` to bring them up again (with correct `DATA/Par_file`!). FYI, `NSTEP` is determined by `RECORD_LENGTH_IN_MINUTES` in `DATA/Par_file`, which is automatically doubled in noise simulations; whereas `dt` is derived from `NEX_XI` and `NEX_ETA`, or in other words your element sizes.

- A Matlab script is provided to generate the ensemble-averaged noise spectrum.

```
EXAMPLES/noise_examples/NOISE_TOMOGRAPHY.m (main program)
EXAMPLES/noise_examples/PetersonNoiseModel.m
```

In Matlab, simply run:

```
NOISE_TOMOGRAPHY(NSTEP, dt, Tmin, Tmax, NOISE_MODEL)
```

`NSTEP` and `dt` have been given when compiling the `specfem3D` source code; `Tmin` and `Tmax` correspond to the period range you are interested in; `NOISE_MODEL` denotes the noise model you will be using. Details can be found in the Matlab script.

After running the Matlab script, you will be given the following information (plus a figure in Matlab):

```
*****
the source time function has been saved in:
/data2/yangl/3D_NOISE/S_squared          (note this path must be different)
S_squared should be put into directory:
./NOISE_TOMOGRAPHY/ in the SPECFEM3D_GLOBE package
```

In other words, the Matlab script creates a file called `S_squared`, which is the first ‘new’ input file we encounter for noise simulations.

One may choose a flat noise spectrum rather than Peterson’s noise model. This can be done easily by modifying the Matlab script a little bit.

- Create a new directory in the SPECFEM3D\_GLOBE package, name it as `NOISE_TOMOGRAPHY`. In fact, this new directory should have been created already when checking out the package. We will add/replace some information needed in this folder.
- Put the Matlab-generated-file `S_squared` in `NOISE_TOMOGRAPHY`.

That’s to say, you will have a file `NOISE_TOMOGRAPHY/S_squared` in the SPECFEM3D\_GLOBE package.

- Create a file called `NOISE_TOMOGRAPHY/irec_main_noise`. Note that this file should be put in directory `NOISE_TOMOGRAPHY` as well. This file contains only one integer, which is the ID of the ‘main’ receiver. For example, if in this file shows 5, it means that the fifth receiver listed in `DATA/STATIONS` becomes the ‘main’. That’s why we mentioned previously that the order of receivers in `DATA/STATIONS` is important.

Note that in regional (1- or 2-chunk) simulations, the `DATA/STATIONS` may contain receivers not within the selected chunk(s). Therefore, the integer in `NOISE_TOMOGRAPHY/irec_main_noise` is actually the ID in `DATA/STATIONS_FILTERED` (which is generated by `xspecfem3D`).

- Create a file called `NOISE_TOMOGRAPHY/nu_main`. This file holds three numbers, forming a (unit) vector. It describes which component we are cross-correlating at the ‘main’ receiver, i.e.,  $\hat{v}^\alpha$  in Tromp et al. [2010b]. The three numbers correspond to N/E/Z components respectively.
- Describe the noise direction and distributions in `src/specfem3d/noise_tomography.f90`. Search for a subroutine called `noise_distribution_direction` in `noise_tomography.f90`. It is actually located at the very beginning of `noise_tomography.f90`. The default assumes vertical noises and a uniform distribution across the whole physical domain. It should be quite self-explanatory for modifications. Should you modify this part, you have to re-compile the source code. (again, that’s why we recommend that you always re-compile the code before you run simulations)

## 8.2.2 Simulations

As discussed in Tromp et al. [2010b], it takes three simulations to obtain one contribution of the ensemble sensitivity kernels:

- Step 1: simulation for generating wavefield

```
SIMULATION_TYPE = 1
NOISE_TOMOGRAPHY = 1
SAVE_FORWARD not used, can be either .true. or .false.
```

- Step 2: simulation for ensemble forward wavefield

```
SIMULATION_TYPE = 1
NOISE_TOMOGRAPHY = 2
SAVE_FORWARD = .true.
```

- Step 3: simulation for ensemble adjoint wavefield and sensitivity kernels

```
SIMULATION_TYPE = 3
NOISE_TOMOGRAPHY = 3
SAVE_FORWARD = .false.
```

Note Step 3 is an adjoint simulation, please refer to previous chapters on how to prepare adjoint sources and other necessary files, as well as how adjoint simulations work.

It's better to run the three steps continuously within the same job, otherwise you have to collect the saved surface movies from the old nodes to the new nodes.

### 8.2.3 Post-simulation

After those simulations, you have all stuff you need, either in the `OUTPUT_FILES` or in the directory specified by `LOCAL_PATH` in `DATA/Par_file` (most probably on local nodes). Collect whatever you want from the local nodes to your workstation, and then visualize them. This process is the same as what you may have done for regular earthquake simulations. Refer Chapter 10 if you have problems.

Simply speaking, two outputs are the most interesting: the simulated ensemble cross correlations and one contribution of the ensemble sensitivity kernels.

The simulated ensemble cross correlations are obtained after the second simulation (Step 2). Seismograms in `OUTPUT_FILES` are actually the simulated ensemble cross correlations. Collect them immediately after Step 2, or the Step 3 will overwrite them. Note that we have a ‘main’ receiver specified by `NOISE_TOMOGRAPHY/irec_main_noise`, the seismogram at one station corresponds to the cross correlation between that station and the ‘main’. Since the seismograms have three components, we may obtain cross correlations for different components as well, not necessarily the cross correlations between vertical components.

One contribution of the ensemble cross-correlation sensitivity kernels are obtained after Step 3, stored in the `LOCAL_PATH` on local nodes. The ensemble kernel files are named the same as regular earthquake kernels.

You need to run another three simulations to get the other contribution of the ensemble kernels, using different forward and adjoint sources given in Tromp et al. [2010b].

## 8.3 Examples

In order to illustrate noise simulations in an easy way, three examples are provided in `EXAMPLES/noise_examples/`. Note however that they are created for a specific cluster (SESAME@PRINCETON). You have to modify them to fit your own cluster.

The three examples can be executed using (in directory `EXAMPLES/noise_examples/`):

```
./run_this_example.sh regional
./run_this_example.sh global_short
./run_this_example.sh global_long
```

Each corresponds to one example, but they are pretty similar.

Although the job submission only works on SESAME@PRINCETON, the procedure itself is universal. You may review the whole process described in the last section by following commands in those examples.

Finally, note again that those examples show only one contribution of the ensemble kernels!

## Chapter 9

# Gravity integral calculations for the gravity field of the Earth

SPECFEM can now compute the gravity field as well as its derivatives (i.e., gravity gradiometry) generated by any given 3D Earth model at the height of an observation satellite, for instance GOCE (see e.g. [en.wikipedia.org/wiki/Gravity\\_Field\\_and\\_Steady-State\\_Ocean\\_Circulation\\_Explorer](https://en.wikipedia.org/wiki/Gravity_Field_and_Steady-State_Ocean_Circulation_Explorer)). That feature is still experimental but should work just fine.

To see how it is implemented and to use it, type this in the root directory of the code:

```
grep -i GRAVITY_INTEGRALS src/*/*
```

All main gravity field computations can be found in file `src/meshfem3d/gravity_integrals.F90`. Please make sure you compile the code with double-precision, i.e., use flag `--enable-double-precision` for the configuration of the package.

# Chapter 10

## Graphics

### 10.1 Meshes

Use the serial code `combine_AVSDX.f90` (type ‘`make combine_AVSDX`’ and then ‘`xcombine_AVSDX`’) to generate AVS (<http://www.avs.com>) output files (in AVS UCD format) or OpenDX (<http://www.opendx.org>) output files showing the mesh, the MPI partition (slices), the NCHUNKS chunks, the source and receiver location, etc. Use the AVS UCD files `AVS_continent_boundaries.inp` and `AVS_plate_boundaries.inp` or the OpenDX files `DX_continent_boundaries.dx` and `DX_plate_boundaries.dx` (that can be created using Perl scripts located in `utils/Visualization/opendx_AVs`) for reference.

### 10.2 Movies

To make a surface or volume movie of the simulation, set parameters `MOVIE_SURFACE`, `MOVIE_VOLUME`, and `NTSTEP_BETWEEN_FRAMES` in the `Par_file`. Turning on the movie flags, in particular `MOVIE_VOLUME`, produces large output files. `MOVIE_VOLUME` files are saved in the `LOCAL_PATH` directory, whereas `MOVIE_SURFACE` output files are saved in the `OUTPUT_FILES` directory. We save the velocity field. The look of a movie is determined by the half-duration of the source. The half-duration should be large enough so that the movie does not contain frequencies that are not resolved by the mesh, i.e., it should not contain numerical noise. This can be accomplished by selecting a CMT `HALF_DURATION > 1.1 × smallest period` (see figure 4.1). When `MOVIE_SURFACE = .true.` or `MOVIE_VOLUME = .true.`, the half duration of each source in the `CMTSOLUTION` file is replaced by

$$\sqrt{(\text{HALF_DURATION}^2 + \text{HDUR_MOVIE}^2)}$$

**NOTE:** If `HDUR_MOVIE` is set to 0.0, the code will select the appropriate value of  $1.1 \times \text{smallest period}$ . As usual, for a point source one can set `HALF_DURATION` in the `Par_file` to be 0.0 and `HDUR_MOVIE = 0.0` to get the highest frequencies resolved by the simulation, but for a finite source one would keep all the `HALF_DURATIONS` as prescribed by the finite source model and set `HDUR_MOVIE = 0.0`.

#### 10.2.1 Movie Surface

When running `xspecfem3D` with the `MOVIE_SURFACE` flag turned on the code outputs `moviedata??????` files in the `OUTPUT_FILES` directory. The files are in a fairly complicated binary format, but there are two programs provided to convert the output into more user friendly formats. The first one, `create_movie_AVSDX.f90` outputs data in ASCII, OpenDX, AVS, or ParaView format. Run the code from the source directory (type ‘`make create_movie_AVSDX`’ first) to create an input file in your format of choice. The code will prompt the user for input parameters. The second program `create_movie_GMT_global.f90` outputs ASCII xyz files, convenient for use with GMT. This codes uses significantly less memory than `create_movie_AVSDX.f90` and is therefore useful for high resolution runs. A README file and sample Perl scripts to create movies using GMT are provided in directory `utils/Visualization/GMT`.

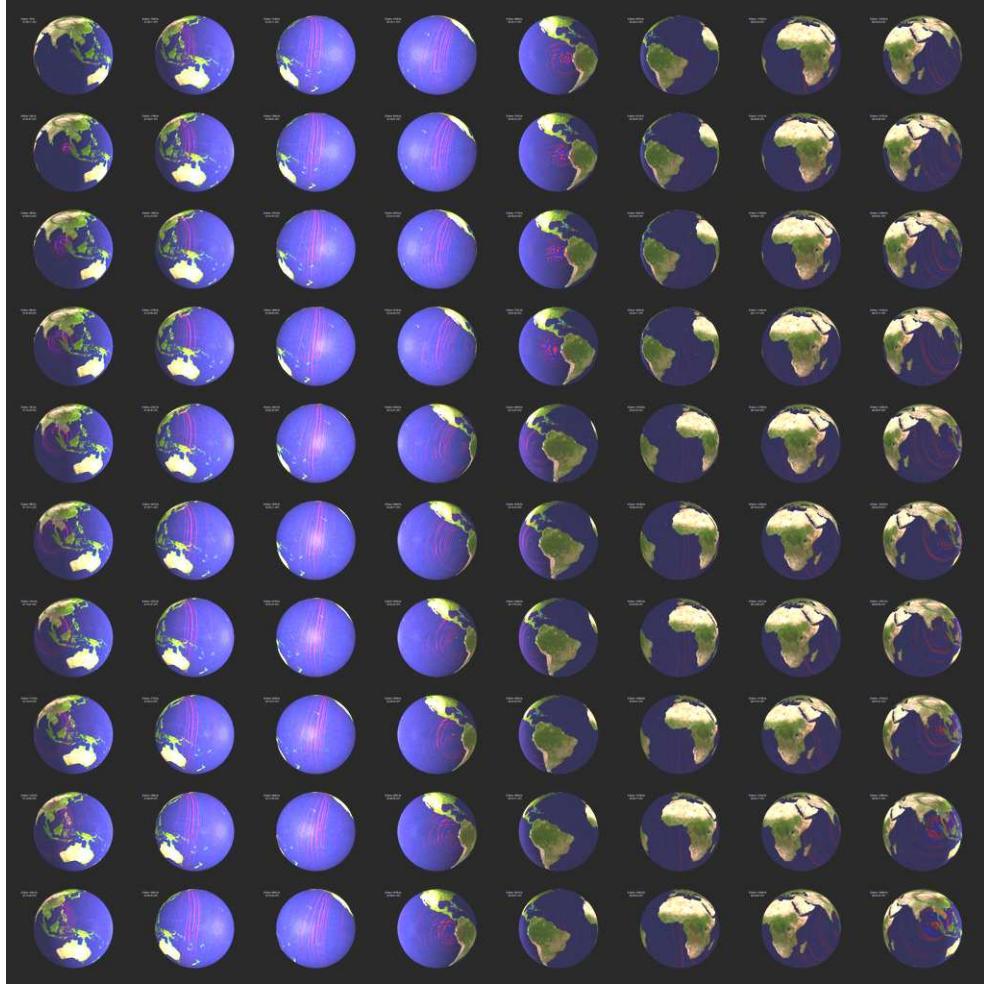


Figure 10.1: Snapshots from a global movie for the December 26, 2004, M=9.2 Sumatra-Andaman earthquake. Time runs down successive columns.

### 10.2.2 Movie Volume

When running xspecfem3D with the `MOVIE_VOLUME` flag turned on, the code outputs several files in `LOCAL_DIR`. As the files can be very large, there are several flags in the `Par_file` that control the region in space and time that is saved. These are: `MOVIE_TOP_KM`, `MOVIE_BOTTOM_KM`, `MOVIE_WEST_DEG`, `MOVIE_EAST_DEG`, `MOVIE_NORTH_DEG`, `MOVIE_SOUTH_DEG`, `MOVIE_START` and `MOVIE_STOP`. The code will save a given element if the center of the element is in the prescribed volume.

**The Top/Bottom:** Depth below the surface in kilometers, use `MOVIE_TOP = -100.0` to make sure the surface is stored.

**West/East:** Longitude, degrees East [-180.0/180.0]

**North/South:** Latitute, degrees North [-90.0/90.0]

**Start/Stop:** Frames will be stored at `MOVIE_START + i*NSTEP_BETWEEN_FRAMES`, where `i=(0,1,2...)` while `i*NSTEP_BETWEEN_FRAMES <= MOVIE_STOP`

The code saves several files, and the output is saved by each processor. The first is `proc??????_movie3D_info.txt` which contains two numbers, first the number of points within the prescribed volume within this particular slice, and

second the number of elements. The next files are `proc??????_movie3D_x.bin`, `proc??????_movie3D_y.bin`, `proc??????_movie3D_z.bin` which store the locations of the points in the 3D mesh.

Finally the code stores the “value” at each of the points. Which value is determined by `MOVIE_VOLUME_TYPE` in the `Par_file`. Choose 1 to save the strain, 2 to save the time integral of strain, and 3 to save  $\mu$ \*time integral of strain in the subvolume. Choosing 4 causes the code to save the trace of the stress and the deviatoric stress in the whole volume (not the subvolume in space), at the time steps specified. The name of the output file will depend on the `MOVIE_VOLUME_TYPE` chosen.

Setting `MOVIE_VOLUME_COARSE = .true.` will make the code save only the corners of the elements, not all the points within each element for `MOVIE_VOLUME_TYPE = 1, 2, 3`.

To make the code output your favorite “value” simply add a new `MOVIE_VOLUME_TYPE`, a new subroutine to `write_movie_volume.f90` and a subroutine call to `specfem3D.F90`.

A utility program to combine the files produced by `MOVIE_VOLUME_TYPE = 1, 2, 3` is provided in `combine_paraview_strain_data.f90`. Type `xcombine_paraview_strain_data` to get the usage statement. The program `combine_vol_data.f90` can be used for `MOVIE_VOLUME_TYPE = 4`.

## 10.3 Finite-Frequency Kernels

The finite-frequency kernels computed as explained in Section 6.2 are saved in the `LOCAL_PATH` at the end of the simulation. Therefore, we first need to collect these files on the front end, combine them into one mesh file, and visualize them with some auxilliary programs. Examples of kernel simulations may be found in the `EXAMPLES` directory.

### 1. Create slice files

We will only discuss the case of one source-receiver pair, i.e., the so-called banana-doughnut kernels. Although it is possible to collect the kernel files from all slices onto the front end, it usually takes up too much storage space (at least tens of gigabytes). Since the sensitivity kernels are the strongest along the source-receiver great circle path, it is sufficient to collect only the slices that are along or close to the great circle path.

A Perl script `utils/Visualization/VTK_Paraview/global_slice_number.pl` can help to figure out the slice numbers that lie along the great circle path (both the minor and major arcs), as well as the slice numbers required to produce a full picture of the inner core if your kernel also illuminates the inner core.

- (a) You need to first compile the utility programs provided in the `utils/Visualization/VTK_Paraview/global_slice_util` directory. Then copy the `CMTSOLUTION` file, `STATIONS_ADJOINT`, and `Par_file`, and run:

```
global_slice_number.pl CMTSOLUTION STATIONS_ADJOINT Par_file
```

In the case of visualization boundary kernels or spherical cross-sections of the volumetric kernels, it is necessary to obtain the slice numbers that cover a belt along the source and receiver great circle path, and you can use the hybrid version:

```
globe_slice_number2.pl CMTSOLUTION STATIONS _ADJOINT \
    Par_file belt_width_in_degrees
```

A typical value for `belt_width_in_degrees` can be 20.

- (b) For a full 6-chunk simulation, this script will generate the `slice_minor`, `slice_major`, `slice_ic` files, but for a one-chunk simulation, this script only generates the `slice_minor` file.
- (c) For cases with multiple sources and multiple receivers, you need to provide a slice file before proceeding to the next step.

### 2. Collect the kernel files

After obtaining the slice files, you can collect the corresponding kernel files from the given slices.

- (a) To accomplish this, you can use or modify the scripts in `utils/collect_database` directory:

```
copy_m(oc,ic)_globe_database.pl slice_file lsf_machine_file filename [jobid]
```

for volumetric kernels, where `lsf_machine_file` is the machine file generated by the LSF scheduler, `filename` is the kernel name (e.g., `rho_kernel`, `alpha_kernel` and `beta_kernel`), and the optional `jobid` is the name of the subdirectory under `LOCAL_PATH` where all the kernel files are stored. For boundary kernels, you need to use

```
copy_surf_globe_database.pl slice_file lsf_machine_file filename [jobid]
```

where the `filename` can be `Moho_kernel`, `d400_kernel`, `d670_kernel`, `CMB_kernel` and `ICB_kernel`.

- (b) After executing this script, all the necessary mesh topology files as well as the kernel array files are collected to the local directory on the front end.

### 3. Combine kernel files into one mesh file

We use an auxiliary program `combine_vol_data.f90` to combine the volumetric kernel files from all slices into one mesh file, and `combine_surf_data.f90` to combine the surface kernel files.

- (a) Compile it in the global code directory:

```
make combine_vol_data
./bin/xcombine_vol_data slice_list kernel_filename input_topo_dir \
    input_file_dir output_dir low/high-resolution-flag-0-or-1 [region]
```

where `input_dir` is the directory where all the individual kernel files are stored, and `output_dir` is where the mesh file will be written. Give 0 for low resolution and 1 for high resolution. If `region` is not specified, all three regions (crust and mantle, outer core, inner core) will be collected, otherwise, only the specified region will be.

Here is an example:

```
./xcombine_vol_data slices_major alpha_kernel input_topo_dir input_file_dir output_dir 1
```

For surface sensitivity kernels, use

```
./bin/xcombine_surf_data slice_list filename surfname input_dir output_dir low/high-resolution 2D/3D
```

where `surfname` should correspond to the specific kernel file name, and can be chosen from `Moho`, `400`, `670`, `CMB` and `ICB`.

- (b) Use 1 for a high-resolution mesh, outputting all the GLL points to the mesh file, or use 0 for low resolution, outputting only the corner points of the elements to the mesh file. Use 0 for 2D surface kernel files and 1 for 3D volumetric kernel files.
- (c) Use `region = 1` for the mantle, `region = 2` for the outer core, `region = 3` for the inner core, and `region = 0` for all regions.
- (d) The output mesh file will have the name `reg_?_rho(alpha,beta)_kernel.mesh`, or `reg_?_Moho(d400,d670,CMB,ICB)_kernel.surf`.

### 4. Convert mesh files into .vtu files

- (a) We next convert the `.mesh` file into the VTU (Unstructured grid file) format which can be viewed in ParaView, for example:

```
mesh2vtu -i file.mesh -o file.vtu
```

- (b) Notice that this program `mesh2vtu`, in the `utils/Visualization/VTK_Paraview/mesh2vtu` directory, uses the VTK (<http://www.vtk.org>) run-time library for its execution. Therefore, make sure you have it properly installed.

### 5. Copy over the source and receiver .vtk file

In the case of a single source and a single receiver, the simulation also generates the `OUTPUT_FILES/sr.vtk` file to describe the source and receiver locations, which can be viewed in Paraview in the next step.

### 6. View the mesh in ParaView

Finally, we can view the mesh in ParaView (<http://www.paraview.org>).

- (a) Open ParaView.
- (b) From the top menu, File → Open data, select `file.vtu`, and click the Accept button.
  - If the mesh file is of moderate size, it shows up on the screen; otherwise, only the outline is shown.
- (c) Click Display Tab → Display Style → Representation and select wireframe of surface to display it.
- (d) To create a cross-section of the volumetric mesh, choose Filter → cut, and under Parameters Tab, choose Cut Function → plane.
- (e) Fill in center and normal information given by the standard output from `global_slice_number.pl` script.
- (f) To change the color scale, go to Display Tab → Color → Edit Color Map and reselect lower and upper limits, or change the color scheme.
- (g) Now load in the source and receiver location file by File → Open data, select `sr.vtk`, and click the Accept button. Choose Filter → Glyph, and represent the points by ‘spheres’.
- (h) For more information about ParaView, see the ParaView Users Guide (<http://www.paraview.org/files/v1.6/ParaViewUsersGuide.PDF>).

For illustration purposes, Figure 10.2 shows P-wave speed finite-frequency kernels from cross-correlation travelttime and amplitude measurements for a P arrival recorded at an epicentral distance of  $60^\circ$  for a deep event.

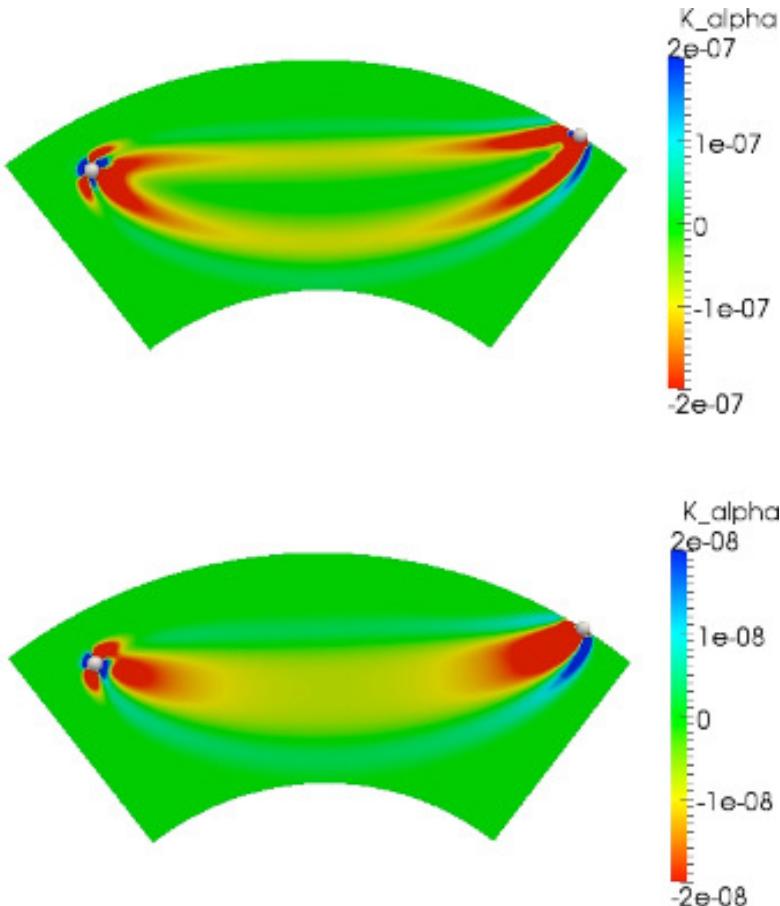


Figure 10.2: P-wave speed finite-frequency kernels from cross-correlation travelttime (top) and amplitude (bottom) measurements for a P arrival recorded at an epicentral distance of  $60^\circ$ . The kernels together with the associated files and routines to reproduce them may be found in `EXAMPLES/global_PREM_kernels/`.

# Chapter 11

## Running through a Scheduler

The code is usually run on large parallel machines, often PC clusters, most of which use schedulers, i.e., queuing or batch management systems to manage the running of jobs from a large number of users. The following considerations need to be taken into account when running on a system that uses a scheduler:

- The processors/nodes to be used for each run are assigned dynamically by the scheduler, based on availability. Therefore, in order for the mesher and the solver (or between successive runs of the solver) to have access to the same database files (if they are stored on hard drives local to the nodes on which the code is run), they must be launched in sequence as a single job.
- On some systems, the nodes to which running jobs are assigned are not configured for compilation. It may therefore be necessary to pre-compile both the mesher and the solver. A small program provided in the distribution called `create_header_file.f90` can be used to directly create `OUTPUT_FILES/values_from_mesher.h` using the information in the `DATA/Par_file` without having to run the mesher (type ‘`make create_header_file`’ to compile it and ‘`./bin/xcreate_header_file`’ to run it; refer to the sample scripts below). The solver can now be compiled as explained above.
- One feature of schedulers/queuing systems is that they allow submission of multiple jobs in a “launch and forget” mode. In order to take advantage of this property, care needs to be taken that output and intermediate files from separate jobs do not overwrite each other, or otherwise interfere with other running jobs.

We describe here in some detail a job submission procedure for the Caltech 1024-node cluster, CITerra, under the LSF scheduling system. We consider the submission of a regular forward simulation. The two main scripts are `run_lsf.bash`, which compiles the Fortran code and submits the job to the scheduler, and `go_mesher_solver_lsf.bash`, which contains the instructions that make up the job itself. These scripts can be found in `utils/Cluster/lstf` directory and can straightforwardly be modified and adapted to meet more specific running needs.

### 11.1 `run_lsf.bash`

This script first sets the job queue to be ‘normal’. It then compiles the mesher and solver together, figures out the number of processors required for this simulation from `DATA/Par_file`, and submits the LSF job.

```
#!/bin/bash
# use the normal queue unless otherwise directed queue="-q normal"
if [ $# -eq 1 ]; then
    echo"Setting the queue to $1"
    queue="-q $1"
fi
# compile the mesher and the solver
d='date'
echo"Starting compilation $d"
```

```

make clean
make meshfem3D
make create_header_file

./bin/xcreate_header_file

make specfem3D

d=`date`
echo"Finished compilation $d"

# compute total number of nodes needed
NPROC_XI='grep ^NPROC_XI DATA/Par_file | cut -c 34- '
NPROC_ETA='grep ^NPROC_ETA DATA/Par_file | cut -c 34- '
NCHUNKS='grep ^NCHUNKS DATA/Par_file | cut -c 34- '

# total number of nodes is the product of the values read
numnodes=$(( $NCHUNKS * $NPROC_XI * $NPROC_ETA ))

echo "Submitting job"
bsub $queue -n $numnodes -W 60 -K <go_mesher_solver_lsf_globe.bash

```

## 11.2 go\_mesher\_solver\_lsf\_globe.bash

This script describes the job itself, including setup steps that can only be done once the scheduler has assigned a job-ID and a set of compute nodes to the job, the `run_lsf.bash` commands used to run the mesher and the solver, and calls to scripts that collect the output seismograms from the compute nodes and perform clean-up operations.

1. First the script directs the scheduler to save its own output and output from `stdout` into `OUTPUT_FILES/%J.o`, where `%J` is short-hand for the job-ID; it also tells the scheduler what version of `mpich` to use (`mpich_gm`) and how to name this job (`go_mesher_solver_lsf`).
2. The script then creates a list of the nodes allocated to this job by echoing the value of a dynamically set environment variable `LSB_MCPU_HOSTS` and parsing the output into a one-column list using the Perl script `utils/Cluster/lsf/remap_lsf_machines.pl`. It then creates a set of scratch directories on these nodes (`/scratch/$USER/DATABASES_MPI`) to be used as the `LOCAL_PATH` for temporary storage of the database files. The scratch directories are created using `shmux`, a shell multiplexor that can execute the same commands on many hosts in parallel. `shmux` is available from `Shmux` (<http://web.taranis.org/shmux/>). Make sure that the `LOCAL_PATH` parameter in `DATA/Par_file` is also set properly.
3. The next portion of the script launches the mesher and then the solver using `run_lsf.bash`.
4. The final portion of the script performs clean up on the nodes using the Perl script `cleanmulti.pl`

```

#!/bin/bash -v
#BSUB -o OUTPUT_FILES/%J.o
#BSUB -a mpich_gm
#BSUB -J go_mesher_solver_lsf

BASEMPIDIR=/scratch/$USER/DATABASES_MPI
echo "$LSB_MCPU_HOSTS" > OUTPUT_FILES/lsf_machines
echo "$LSB_JOBID" > OUTPUT_FILES/jobid

./remap_lsf_machines.pl OUTPUT_FILES/lsf_machines > OUTPUT_FILES/machines

# Modif : create a directory for this job
shmux -M50 -Sall \

```

```
-c "mkdir -p /scratch/$USER;mkdir -p $BASEMPIDIR.$LSB_JOBID" - < OUTPUT_FILES/machines >/dev/null  
  
# Set the local path in Par_file  
sed -e "s:^LOCAL_PATH .*:LOCAL_PATH = $BASEMPIDIR.$LSB_JOBID:" < DATA/Par_file > DATA/Par_file.tmp  
mv DATA/Par_file.tmp DATA/Par_file  
  
current_pwd=$PWD  
  
mpirun.lsf --gm-no-shmem --gm-copy-env $current_pwd/bin/xmeshfem3D  
mpirun.lsf --gm-no-shmem --gm-copy-env $current_pwd/bin/xspecfem3D  
  
# clean up  
cleanbase_jobid.pl OUTPUT_FILES/machines DATA/Par_file
```

### 11.3 `run_lsf.kernel` and `go_mesher_solver_globe.kernel`

For kernel simulations, you can use the sample run scripts `run_lsf.kernel` and `go_mesher_solver_globe.kernel` provided in `utils/Cluster` directory, and modify the command-line arguments of `xcreate_adjsrc_travelttime` in `go_mesher_solver_globe.kernel` according to the start and end time of the specific portion of the forward seismograms you are interested in.

# Chapter 12

## Changing the Model

In this section we explain how to change the crustal, mantle, or inner core models. These changes involve contributing specific subroutines that replace existing subroutines in the `SPECFEM3D_GLOBE` package.

### 12.1 Changing the Crustal Model

The 3D crustal model Crust2.0 [Bassin et al., 2000] is superimposed onto the mesh by the subroutine `model_crust.f90`. To accomplish this, the flag `CRUSTAL`, set in the subroutine `get_model_parameters.f90`, is used to indicate a 3D crustal model. When this flag is set to `.true.`, the crust on top of the 1D reference model (PREM, IASP91, or AK135F\_NO\_MUD) is removed and replaced by extending the mantle. The 3D crustal model is subsequently overprinted onto the crust-less 1D reference model. The call to the 3D crustal routine is of the form

```
call model_crust(lat,lon,r,vp,vs,rho,moho,foundcrust,CM_V,elem_in_crust)
```

Input to this routine consists of:

**lat** Latitude in degrees.

**lon** Longitude in degrees.

**r** Non-dimensionalized radius ( $0 < r < 1$ ).

Output from the routine consists of:

**vp** Non-dimensionalized compressional wave speed at location (`lat,lon,r`).

**vs** Non-dimensionalized shear wave speed.

**rho** Non-dimensionalized density.

**moho** Non-dimensionalized Moho depth.

**found\_crust** Logical that is set to `.true.` only if crust exists at location (`lat,lon,r`), i.e., `.false.` for radii `r` in the mantle. This flag determines whether or not a particular location is in the crust and, if so, what parameters to assign to the mesh at this location.

**CM\_V** Fortran structure that contains the parameters, variables and arrays that describe the model.

**elem\_in\_crust** Logical that is used to force the routine to return crustal values, even if the location would be below the crust.

All output needs to be non-dimensionalized according to the convention summarized in Appendix B. You can replace this subroutine by your own routine *provided you do not change the call structure of the routine*, i.e., the new routine should take exactly the same input and produce the required, properly non-dimensionalized output.

Part of the file `model_crust.f90` is the subroutine `model_crust_broadcast`. The call to this routine takes argument `CM_V` and is used to once-and-for-all read in the databases related to Crust2.0 and broadcast the model to all parallel processes. If you replace the file `model_crust.f90` with your own implementation, you *must* provide a `model_crust_broadcast` routine, even if it does nothing. Model constants and variables read by the routine `model_crust_broadcast` are passed to the subroutine `read_crust_model` through the structure `CM_V`. An alternative crustal model could use the same construct. Please feel free to contribute subroutines for new models and send them to us so that they can be included in future releases of the software.

**NOTE:** If you decide to create your own version of file `model_crust.f90`, you must add calls to `MPI_BCAST` in the subroutine `model_crust_broadcast` after the call to the `read_crust_model` subroutine that reads the isotropic mantle model once and for all in the mesher. This is done in order to read the (potentially large) model data files on the main node (which is the processor of rank 0 in our code) only and then send a copy to all the other nodes using an MPI broadcast, rather than using an implementation in which all the nodes would read the same model data files from a remotely-mounted home file system, which could create a bottleneck on the network in the case of a large number of nodes. For example, in the current call to that routine from `model_crust.f90`, we write:

```

! the variables read are declared and stored in structure CM_V
if(myrank == 0) call read_crust_model(CM_V)

! broadcast the information read on the main node to all the nodes
call MPI_BCAST(CM_V%thlr,NKEYS_CRUST*NLAYERS_CRUST,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(CM_V%velocp,NKEYS_CRUST*NLAYERS_CRUST,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(CM_V%velocp,NKEYS_CRUST*NLAYERS_CRUST,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(CM_V%dens,NKEYS_CRUST*NLAYERS_CRUST,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(CM_V%abbreviation,NCAP_CRUST*NCAP_CRUST,MPI_CHARACTER,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(CM_V%code,2*NKEYS_CRUST,MPI_CHARACTER,0,MPI_COMM_WORLD,ier)

```

## 12.2 Changing the Mantle Model

This section discusses how to change isotropic and anisotropic 3D mantle models. Usually such changes go hand-in-hand with changing the 3D crustal model.

### 12.2.1 Isotropic Models

The 3D mantle model S20RTS [Ritsema et al., 1999] is superimposed onto the mantle mesh by the subroutine `model_s20rts.f90`. The call to this subroutine is of the form

```
call model_s20rts(radius,theta,phi,dvs,dvp,drho,D3MM_V)
```

Input to this routine consists of:

**radius** Non-dimensionalized radius ( $\text{RCMB}/\text{R}_\text{EARTH} < r < \text{RMOHO}/\text{R}_\text{EARTH}$ ; for a given 1D reference model, the constants `RCMB` and `RMOHO` are set in the `get_model_parameters.f90` file). The code expects the isotropic mantle model to be defined between the Moho (with radius `RMOHO` in m) and the core-mantle boundary (CMB; radius `RCMB` in m) of a 1D reference model. When a 3D crustal model is superimposed, as will usually be the case, the 3D mantle model is stretched to fill any potential gap between the radius of the Moho in the 1D reference model and the Moho in the 3D crustal model. Thus, when the Moho in the 3D crustal model is shallower than the Moho in the reference model, e.g., typically below the oceans, the mantle model is extended to fill this gap.

**theta** Colatitude in radians.

**phi** Longitude in radians.

Output from the routine are the following non-dimensional perturbations:

**dvs** Relative shear-wave speed perturbations  $\delta\beta/\beta$  at location (`radius,theta,phi`).

**dvp** Relative compressional-wave speed perturbations  $\delta\alpha/\alpha$ .

**drho** Relative density perturbations  $\delta\rho/\rho$ .

**D3MM\_V** Fortran structure that contains the parameters, variables and arrays that describe the model.

You can replace the `model_s20rts.f90` file with your own version *provided you do not change the call structure of the routine*, i.e., the new routine should take exactly the same input and produce the required relative output.

Part of the file `model_s20rts.f90` is the subroutine `model_s20rts_broadcast`. The call to this routine takes argument `D3MM_V` and is used to once-and-for-all read in the databases related to S20RTS. If you replace the file `model_s20rts.f90` with your own implementation, you *must* provide a `model_s20rts_broadcast` routine, even if it does nothing. Model constants and variables read by the routine `model_s20rts_broadcast` are passed to the subroutine `read_model_s20rts` through the structure `D3MM_V`. An alternative mantle model should use the same construct.

**NOTE:** If you decide to create your own version of file `model_s20rts.f90`, you must add calls to `MPI_BCAST` in the subroutine `model_s20rts_broadcast` after the call to the `read_model_s20rts` subroutine that reads the isotropic mantle model once and for all in the mesher. This is done in order to read the (potentially large) model data files on the main node (which is the processor of rank 0 in our code) only and then send a copy to all the other nodes using an MPI broadcast, rather than using an implementation in which all the nodes would read the same model data files from a remotely-mounted home file system, which could create a bottleneck on the network in the case of a large number of nodes. For example, in the current call to that routine from `model_s20rts.f90`, we write:

```

! the variables read are declared and stored in structure D3MM_V
if(myrank == 0) call read_model_s20rts(D3MM_V)

! broadcast the information read on the main node to all the nodes
call MPI_BCAST(D3MM_V%dvs_a, (NK+1)*(NS+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%dvs_b, (NK+1)*(NS+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%dvp_a, (NK+1)*(NS+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%dvp_b, (NK+1)*(NS+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%spknt, NK+1,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%qq0, (NK+1)*(NK+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(D3MM_V%qq, 3*(NK+1)*(NK+1),MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)

```

## 12.2.2 Anisotropic Models

Three-dimensional anisotropic mantle models may be superimposed on the mesh based upon the subroutine `model_aniso_mantle.f90`

The call to this subroutine is of the form

```

call model_aniso_mantle(r,theta,phi,rho, &
c11,c12,c13,c14,c15,c16,c22,c23,c24,c25,c26, &
c33,c34,c35,c36,c44,c45,c46,c55,c56,c66,AMM_V)

```

Input to this routine consists of:

- r** Non-dimensionalized radius ( $RCMB/R_{\text{EARTH}} < r < RMOHO/R_{\text{EARTH}}$ ; for a given 1D reference model, the constants `RCMB` and `RMOHO` are set in the `get_model_parameters.f90` file). The code expects the anisotropic mantle model to be defined between the Moho and the core-mantle boundary (CMB). When a 3D crustal model is superimposed, as will usually be the case, the 3D mantle model is stretched to fill any potential gap between the radius of the Moho in the 1D reference model and the Moho in the 3D crustal model. Thus, when the Moho in the 3D crustal model is shallower than the Moho in the reference model, e.g., typically below the oceans, the mantle model is extended to fill this gap.

**theta** Colatitude in radians.

**phi** Longitude in radians.

Output from the routine consists of the following non-dimensional model parameters:

**rho** Non-dimensionalized density  $\rho$ .

**c11, ..., c66** 21 non-dimensionalized anisotropic elastic parameters.

**AMM\_V** Fortran structure that contains the parameters, variables and arrays that describe the model.

You can replace the `model_aniso_mantle.f90` file by your own version *provided you do not change the call structure of the routine*, i.e., the new routine should take exactly the same input and produce the required relative output. Part of the file `model_aniso_mantle.f90` is the subroutine `model_aniso_mantle_broadcast`. The call to this routine takes argument `AMM_V` and is used to once-and-for-all read in the static databases related to the anisotropic model. When you choose to replace the file `model_aniso_mantle.f90` with your own implementation you *must* provide a `model_aniso_mantle_broadcast` routine, even if it does nothing. Model constants and variables read by the routine `model_aniso_mantle_broadcast` are passed through the structure `AMM_V`. An alternative anisotropic mantle model should use the same construct.

**NOTE:** If you decide to create your own version of file `model_aniso_mantle.f90`, you must add calls to `MPI_BCAST` in file `model_aniso_mantle.f90` after the call to the `read_aniso_mantle_model` subroutine that reads the anisotropic mantle model once and for all in the mesher. This is done in order to read the (potentially large) model data files on the main node (which is the processor of rank 0 in our code) only and then send a copy to all the other nodes using an MPI broadcast, rather than using an implementation in which all the nodes would read the same model data files from a remotely-mounted home file system, which could create a bottleneck on the network in the case of a large number of nodes. For example, in the current call to that routine from `model_aniso_mantle.f90`, we write:

```

! the variables read are declared and stored in structure AMM_V
if(myrank == 0) call read_aniso_mantle_model(AMM_V)

! broadcast the information read on the main node to all the nodes
call MPI_BCAST(AMM_V%par1,1,MPI_INTEGER,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(AMM_V%beta,14*34*37*73,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)
call MPI_BCAST(AMM_V%pro,47,MPI_DOUBLE_PRECISION,0,MPI_COMM_WORLD,ier)

```

Rotation of the anisotropic tensor elements from one coordinate system to another coordinate system may be accomplished based upon the subroutine `rotate_aniso_tensor`. Use of this routine requires understanding the coordinate system used in `SPECFEM3D_GLOBE`, as discussed in Appendix A.

### 12.2.3 Point-Profile Models

In order to facilitate the use of your own specific mantle model, you can choose `PPM` as model in the `DATA/Par_file` file and supply your own model as an ASCII-table file. These generic models are given as depth profiles at a specified lon/lat location and a perturbation (in percentage) with respect to the shear-wave speed values from PREM. The ASCII-file should have a format like:

```

#lon(deg), lat(deg), depth(km), Vs-perturbation wrt PREM(%), Vs-PREM (km/s)
-10.00000    31.00000    40.00000     -1.775005    4.400000
-10.00000    32.00000    40.00000     -1.056823    4.400000
...

```

where the first line is a comment line and all following ones are specifying the Vs-perturbation at a lon/lat location and a given depth. The last entry on each line is specifying the absolute value of Vs (however this value is only given as a supplementary information and not used any further). The background model is PREM with a transverse isotropic layer between Moho and 220 km depth. The specified Vs-perturbations are added as isotropic perturbations. Please see the file `DATA/PPM/README` for more informations how to setup the directory `DATA/PPM` to use your own ASCII-file.

To change the code behavior of these `PPM`-routines, please have a look at the implementation in the source code file `model_ppm.f90` and set the flags and scaling factors as needed for your purposes. Perturbations in density and  $V_p$  may be scaled to the given Vs-perturbations with constant scaling factors by setting the appropriate values in this source code file. In case you want to change the format of the input ASCII-file, see more details in the Appendix F.

## 12.3 Anelastic Models

Three-dimensional anelastic (attenuation) models may be superimposed onto the mesh based upon your subroutine `model_atten3D.f90`. The call to this routine would be as follows

```
call model_atten3D(radius, colatitude, longitude, Qmu, QRFSI12_Q, idoubling)
```

Input to this routine consists of:

**radius** scaled radius of the earth: 0 (center)  $\leq r \leq$  1(surface)

**latitude** Colatitude in degrees:  $0^\circ \leq \theta \leq 180^\circ$

**longitude** Longitude in degrees:  $-180^\circ \leq \phi \leq 180^\circ$

**QRFSI12\_Q** Fortran structure that contains the parameters, variables and arrays that describe the model

**idoubling** value of the doubling index flag in each radial region of the mesh

Output to this routine consists of:

**Qmu** Shear wave quality factor:  $0 < Q_\mu < 5000$

A 3-D attenuation model QRFSI12 [Dalton et al., 2008] is provided, as well as 1-D models with a PREM and a 1DREF attenuation structure. By default the PREM attenuation model is taken, using the routine `model_attenuation_1D_PREM`, found in `model_attenuation.f90`.

To create your own three-dimensional attenuation model, you add your model using a routine like the `model_atten3D_QRFSI12` subroutine and the example routine above as a guide and replace the call in file `meshfem3D_models.f90` to your own subroutine.

Note that the resolution and maximum value of anelastic models are truncated. This speeds the construction of the standard linear solids during the meshing stage. To change the resolution, currently at one significant figure following the decimal, or the maximum value (5000), consult `constants.h`. In order to prevent unexpected results, quality factors  $Q_\mu$  should never be equal to 0 outside of the inner core.

# Chapter 13

## Post-Processing Scripts

Several post-processing scripts/programs are provided in the `utils/seis_process` directory, most of which need to be adjusted for different systems, for example, the path of the executable programs. Here we only list the available scripts and provide a brief description, and you can either refer to the related sections for detailed usage or, in many cases, type the script/program name without arguments to see its usage.

### 13.1 Clean Local Database

After all the simulations are done, you may need to clean the local scratch disks for the next simulation. This is especially important in the case of 1- or 2-chunk kernel simulations, where very large files are generated for the absorbing boundaries to help with the reconstruction of the regular forward wavefield. A sample script is provided in `utils/Cluster/lsf`:

```
cleanbase.pl machines
```

### 13.2 Process Data and Synthetics

In many cases, the SEM synthetics are calculated and compared to observed seismograms recorded at seismic stations. Since the SEM synthetics are accurate for a certain frequency range, both the original data and the synthetics need to be processed before a comparison can be made. For such comparisons, the following steps are recommended:

1. Make sure that both synthetic and observed seismograms have the correct station/event and timing information.
2. Convolve synthetic seismograms with a source time function with the half duration specified in the `CMTSOLUTION` file, provided, as recommended, you used a zero half duration in the SEM simulations.
3. Resample both observed and synthetic seismograms to a common sampling rate.
4. Cut the records using the same window.
5. Remove the trend and mean from the records and taper them.
6. Remove the instrument response from the observed seismograms (recommended) or convolve the synthetic seismograms with the instrument response.
7. Make sure that you apply the same filters to both observed and synthetic seismograms. Preferably, avoid filtering your records more than once.
8. Now, you are ready to compare your synthetic and observed seismograms.

We generally use the following scripts for processing:

### 13.2.1 process\_data.pl

This script cuts a given portion of the original data, filters it, transfers the data into a displacement record, and picks the first P and S arrivals. For more functionality, type ‘process\_data.pl’ without any argument. An example of the usage of the script:

```
process_data.pl -m CMTSOLUTION -s 1.0 -l 0/4000 -i -f -t 40/500 -p -x bp DATA/1999.330*.LH?.SAC
```

which has resampled the SAC files to a sampling rate of 1 seconds, cut them between 0 and 4000 seconds, transferred them into displacement records and filtered them between 40 and 500 seconds, picked the first P and S arrivals, and added suffix ‘bp’ to the file names.

Note that all of the scripts in this section actually use SAC, saclst and/or IASP91 to do the core operations; therefore make sure that the SAC, saclst and IASP91 packages are installed on your system, and that all the environment variables are set properly before running these scripts.

### 13.2.2 process\_syn.pl

This script converts the synthetic output from the SEM code from ASCII to SAC format, and performs similar operations as ‘process\_data.pl’. An example of the usage of the script:

```
process_syn.pl -m CMTSOLUTION -h -a STATIONS -s 1.0 -l 0/4000 -f -t 40/500 -p -x bp SEM/*.MX?.sem
```

which will convolve the synthetics with a triangular source-time function from the CMTSOLUTION file, convert the synthetics into SAC format, add event and station information into the SAC headers, resample the SAC files with a sampling rate of 1 seconds, cut them between 0 and 4000 seconds, filter them between 40 and 500 seconds with the same filter used for the observed data, pick the first P and S arrivals, and add the suffix ‘bp’ to the file names.

More options are available for this script, such as adding a time shift to the origin time of the synthetics, convolving the synthetics with a triangular source time function with a given half duration, etc. Type process\_syn.pl without any argument for detailed usage.

### 13.2.3 rotate.pl

To rotate the horizontal components of both the data and the synthetics (i.e., MXN and MXE) to the transverse and radial directions (i.e., MXT and MXR), use rotate.pl:

data example:

```
rotate.pl -l 0 -L 4000 -d DATA/*.LHE.SAC.bp
```

synthetics example:

```
rotate.pl -l 0 -L 4000 SEM/*.MXE.sem.sac.bp
```

where the first command performs rotation on the SAC data obtained through IRIS (which may have timing information written in the filename), while the second command rotates the processed synthetics.

For synthetics, another (simpler) option is to set flag ROTATE\_SEISMOGRAMS\_RT to .true. in the parameter file DATA/Par\_file.

### 13.2.4 clean\_sac\_headers\_after\_crash.sh

Note: You need to have the sismoutil-0.9b package installed on your computer if you want to run this script on binary SAC files. The software is available via the ORFEUS web site (<http://www.orfeus-eu.org>).

In case the simulation crashes during run-time without computing and writing all time steps, the SAC files (if flags OUTPUT\_SEISMOS\_SAC\_ALPHANUM or OUTPUT\_SEISMOS\_SAC\_BINARY have been set to .true.) are corrupted and cannot be used in SAC. If the simulation ran long enough so that the synthetic data may still be of use, you can run the script called clean\_sac\_headers\_after\_crash.sh (located in the utils/ directory) on the SAC files to correct the header variable NPTS to the actually written number of time steps. The script must be called from the SPECFEM3D main directory, and the input argument to this script is simply a list of SAC seismogram files.

### 13.3 Map Local Database

A sample program `remap_database` is provided to map the local database from a set of machines to another set of machines. This is especially useful when you want to run mesher and solver, or different types of solvers separately through a scheduler (refer to Chapter 11).

```
run_lsf.bash --gm-no-shmem --gm-copy-env remap_database \
old_machines 150 [old_jobid new_jobid]
```

where `old_machines` is the LSF machine file used in the previous simulation, and 150 is the number of processors in total. Note that you need to supply `old_jobid` and `new_jobid(%J)` which are the LSF job-IDs for the old and new run if your databases are stored in a sub-directory named after the jobid on the scratch disk.

## Chapter 14

# Information for developers of the code, and for people who want to learn how the technique works

You can get a very simple 1D version of a demo code (there is one in Fortran and one in Python):

```
git clone --recursive https://github.com/geodynamics/specfem1d.git
```

We also have simple 3D demo source codes that implement the SEM in a single, small program, in directory `utils/small_SEM_solvers_in_Fortran_and_C_without_MPI_to_learn` of the `specfem3d` package. They are useful to learn how the spectral-element method works, and how to write or modify a code to implement it. Also useful to test new ideas by modifying these simple codes to run some tests. We also have a similar, even simpler, demo source code for the 2D case in directory

`utils/small_SEM_solver_in_Fortran_without_MPI_to_learn` of the `specfem2d` package.

For information on how to contribute to the code, i.e., for how to make your modifications, additions or improvements part of the official package, see <https://github.com/geodynamics/specfem3d/wiki>.

# Simulation features supported in SPECFEM3D\_GLOBE

The following lists all available features for a SPECFEM3D\_GLOBE simulation, where *CPU*, *CUDA* and *OpenCL* denote the code versions for CPU-only simulations, CUDA and OpenCL hardware support, respectively.

Feature		<i>CPU</i>	<i>CUDA</i>	<i>OpenCL</i>
<b>Physics</b>	Ocean load	X	X	X
	Ellipticity	X	X	X
	Topography	X	X	X
	Gravity	X	X	X
	Rotation	X	X	X
	Attenuation	X	X	X
<b>Simulation Setup</b>	Global (6-chunks)	X	X	X
	Regional (1,2-chunk)	X	X	X
	Restart/Checkpointing	X	X	X
	Simultaneous runs	X	X	X
	ADIOS file I/O	X	X	X
<b>Sensitivity kernels</b>	Partial physical dispersion	X	X	X
	Undoing of attenuation	X	X	X
	Anisotropic kernels	X	X	X
	Transversely isotropic kernels	X	X	X
	Isotropic kernels	X	X	X
	Approximate Hessian	X	X	X
<b>Time schemes</b>	Newmark	X	X	X
	LDDRK	X	-	-
<b>Visualization</b>	Surface movie	X	X	X
	Volumetric movie	X	X	X
<b>Seismogram formats</b>	Ascii	X	X	X
	SAC	X	X	X
	ASDF	X	X	X
	Binary	X	X	X

# Bug Reports and Suggestions for Improvements

To report bugs or suggest improvements to the code, please send an e-mail to the CIG Computational Seismology Mailing List ([cig-seismo@geodynamics.org](mailto:cig-seismo@geodynamics.org)).

# Notes and Acknowledgements

In order to keep the software package thread-safe in case a multithreaded implementation of MPI is used, developers should not add modules or common blocks to the source code but rather use regular subroutine arguments (which can be grouped in “derived types” if needed for clarity).

The Gauss-Lobatto-Legendre subroutines in `gll_library.f90` are based in part on software libraries from the Massachusetts Institute of Technology, Department of Mechanical Engineering (Cambridge, Massachusetts, USA). The non-structured global numbering software was provided by Paul F. Fischer (Brown University, Providence, Rhode Island, USA, now at Argonne National Laboratory, USA).

OpenDX (<http://www.opendx.org>) is open-source based on IBM Data Explorer, AVS (<http://www.avs.com>) is a trademark of Advanced Visualization Systems, and ParaView (<http://www.paraview.org>) is an open-source visualization platform.

Please e-mail your feedback, questions, comments, and suggestions to the CIG Computational Seismology Mailing List ([cig-seismo@geodynamics.org](mailto:cig-seismo@geodynamics.org)).

# Copyright

Main ‘historical’ authors: Dimitri Komatitsch and Jeroen Tromp (there are now many more!).

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This program is free software; you can redistribute it and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation (see Appendix G).

Please note that by contributing to this code, the developer understands and agrees that this project and contribution are public and fall under the open source license mentioned above.

## Evolution of the code:

v. 7.0, many developers, January 2015: simultaneous MPI runs, ADIOS file I/O support, ASDF seismograms, new seismogram names, tomography tools, CUDA and OpenCL GPU support, CEM model support, updates AK135 model, binary topography files, fixes geocentric/geographic conversions, updates ellipticity and gravity factors, git versioning system.

v. 6.0, Daniel Peter (ETH Zürich, Switzerland), Dimitri Komatitsch and Zhinan Xie (CNRS / University of Marseille, France), Elliott Sales de Andrade (University of Toronto, Canada), and many others, in particular from Princeton University, USA, April 2014: more flexible MPI implementation, GPU support, exact undoing of attenuation, LDDRK4-6 higher-order time scheme, etc...

v. 5.1, Dimitri Komatitsch, University of Toulouse, France and Ebru Bozdag, Princeton University, USA, February 2011: non blocking MPI for much better scaling on large clusters; new convention for the name of seismograms, to conform to the IRIS standard; new directory structure.

v. 5.0, many developers, February 2010: new Moho mesh stretching honoring crust2.0 Moho depths, new attenuation assignment, new SAC headers, new general crustal models, faster performance due to Deville routines and enhanced loop unrolling, slight changes in code structure (see also trivia at program start).

v. 4.0 David Michéa and Dimitri Komatitsch, University of Pau, France, February 2008: first port to GPUs using CUDA, new doubling brick in the mesh, new perfectly load-balanced mesh, more flexible routines for mesh design, new inflated central cube with optimized shape, far fewer mesh files saved by the mesher, global arrays sorted to speed up the simulation, seismograms can be written by the main process, one more doubling level at the bottom of the outer core if needed (off by default).

v. 3.6 Many people, many affiliations, September 2006: adjoint and kernel calculations, fixed IASP91 model, added AK135F\_NO\_MUD and 1066a, fixed topography/bathymetry routine, new attenuation routines, faster and better I/Os on very large systems, many small improvements and bug fixes, new ‘configure’ script, new Pyre version, new user’s manual etc..

v. 3.5 Dimitri Komatitsch, Brian Savage and Jeroen Tromp, Caltech, July 2004: any size of chunk, 3D attenuation, case of two chunks, more precise topography/bathymetry model, new Par\_file structure.

v. 3.4 Dimitri Komatitsch and Jeroen Tromp, Caltech, August 2003: merged global and regional codes, no iterations in fluid, better movies.

v. 3.3 Dimitri Komatitsch, Caltech, September 2002: flexible mesh doubling in outer core, inlined code, OpenDX support.

v. 3.2 Jeroen Tromp, Caltech, July 2002: multiple sources and flexible PREM reading.

v. 3.1 Dimitri Komatitsch, Caltech, June 2002: vectorized loops in solver and merged central cube.

v. 3.0 Dimitri Komatitsch and Jeroen Tromp, Caltech, May 2002: ported to SGI and Compaq, double precision solver, more general anisotropy.

v. 2.3 Dimitri Komatitsch and Jeroen Tromp, Caltech, August 2001: gravity, rotation, oceans and 3-D models.

v. 2.2 Dimitri Komatitsch and Jeroen Tromp, Caltech, USA, March 2001: final MPI package.

v. 2.0 Dimitri Komatitsch, Harvard, USA, January 2000: MPI code for the globe.

v. 1.0 Dimitri Komatitsch, UNAM, Mexico, June 1999: first MPI code for a chunk.

Jeroen Tromp and Dimitri Komatitsch, Harvard, USA, July 1998: first chunk solver using OpenMP on a Sun machine.

Dimitri Komatitsch, IPG Paris, France, December 1996: first 3-D solver for the CM-5 Connection Machine, parallelized on 128 processors using Connection Machine Fortran.

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## Appendix A

# Reference Frame Convention

The code uses the following convention for the Cartesian reference frame:

- the  $x$  axis points East
- the  $y$  axis points North
- the  $z$  axis points up

Note that this convention is different from both the Aki and Richards [1980] convention and the Harvard Centroid-Moment Tensor (CMT) convention. The Aki & Richards convention is

- the  $x$  axis points North
- the  $y$  axis points East
- the  $z$  axis points down

and the Harvard CMT convention is

- the  $x$  axis points South
- the  $y$  axis points East
- the  $z$  axis points up

## Appendix B

# Non-Dimensionalization Conventions

All physical parameters used are non-dimensionalized internally in the code in order to work in a reference Earth of radius 1. In Table B.1 in the right column are the values by which we divide the parameters of the left column internally to perform the calculations. The values output and saved by the code (seismograms, sensitivity kernels...) are then scaled back to the right physical dimensions before being saved.

quantity (units)	divided internally by
distance (m)	R_EARTH
time (s)	$1/\sqrt{\text{PI} \times \text{GRAV} \times \text{RHOAV}}$
density (kg/m <sup>3</sup> )	RHOAV

Table B.1: Non-dimensionalization convention employed internally by the code. The constants R\_EARTH (the radius of the Earth), PI (the number  $\pi$ ), GRAV (the universal gravitational constant), and RHOAV (the Earth's average density) are defined in the `constants.h` file.

## Appendix C

# Benchmarks

Komatitsch and Tromp [2002a,b] carefully benchmarked the spectral-element simulations of global seismic waves against normal-mode seismograms. Version 4.0 of SPECFEM3D\_GLOBE has been benchmarked again following the same procedure.

In this appendix we present two tests: a ‘long-period’ (periods longer than 17 s) simulation of a shallow event in isotropic PREM [Dziewoński and Anderson, 1981] without the ocean layer, without attenuation but including the effects of self-gravitation (in the Cowling approximation) (Figures C.1 and C.2), and a ‘short-period’ (periods longer than 9 s) simulation of a deep event in transversely isotropic PREM without the ocean layer and including the effects of self-gravitation and attenuation (Figures C.3, C.4 and C.5).

The normal-mode synthetics are calculated with the code `QmXD` using mode catalogs with a shortest period of 8 s generated by the code `OBANI`. No free-air, tilt, or gravitational potential corrections were applied [Dahlen and Tromp, 1998]. We also turned off the effect of the oceans in `QmXD`.

The normal-mode and SEM displacement seismograms are first calculated for a step source-time function, i.e., setting the parameter `half duration` in the `CMTSOLUTION` file to zero for the SEM simulations. Both sets of seismograms are subsequently convolved with a triangular source-time function using the processing script `utils/seis_process/process_syn.pl`. They are also band-pass filtered and the horizontal components are rotated to the radial and transverse directions (with the script `utils/seis_process/rotate.pl`).

The match between the normal-mode and SEM seismograms is quite remarkable for the experiment with attenuation, considering the very different implementations of attenuation in the two computations (e.g., frequency domain versus time domain, constant Q versus absorption bands).

Further tests can be found in the `EXAMPLES` directory. It contains the normal-mode and SEM seismograms, and the parameters (`STATIONS`, `CMTSOLUTION` and `Par_file`) for the SEM simulations.

Important remark: when comparing SEM results to normal mode results, one needs to convert source and receiver coordinates from geographic to geocentric coordinates, because on the equator the geographic and geocentric latitude are identical but not elsewhere. Even for spherically-symmetric simulations one must perform this conversion because the source and receiver locations provided by `globalCMT.org` and `IRIS` involve geographic coordinates.

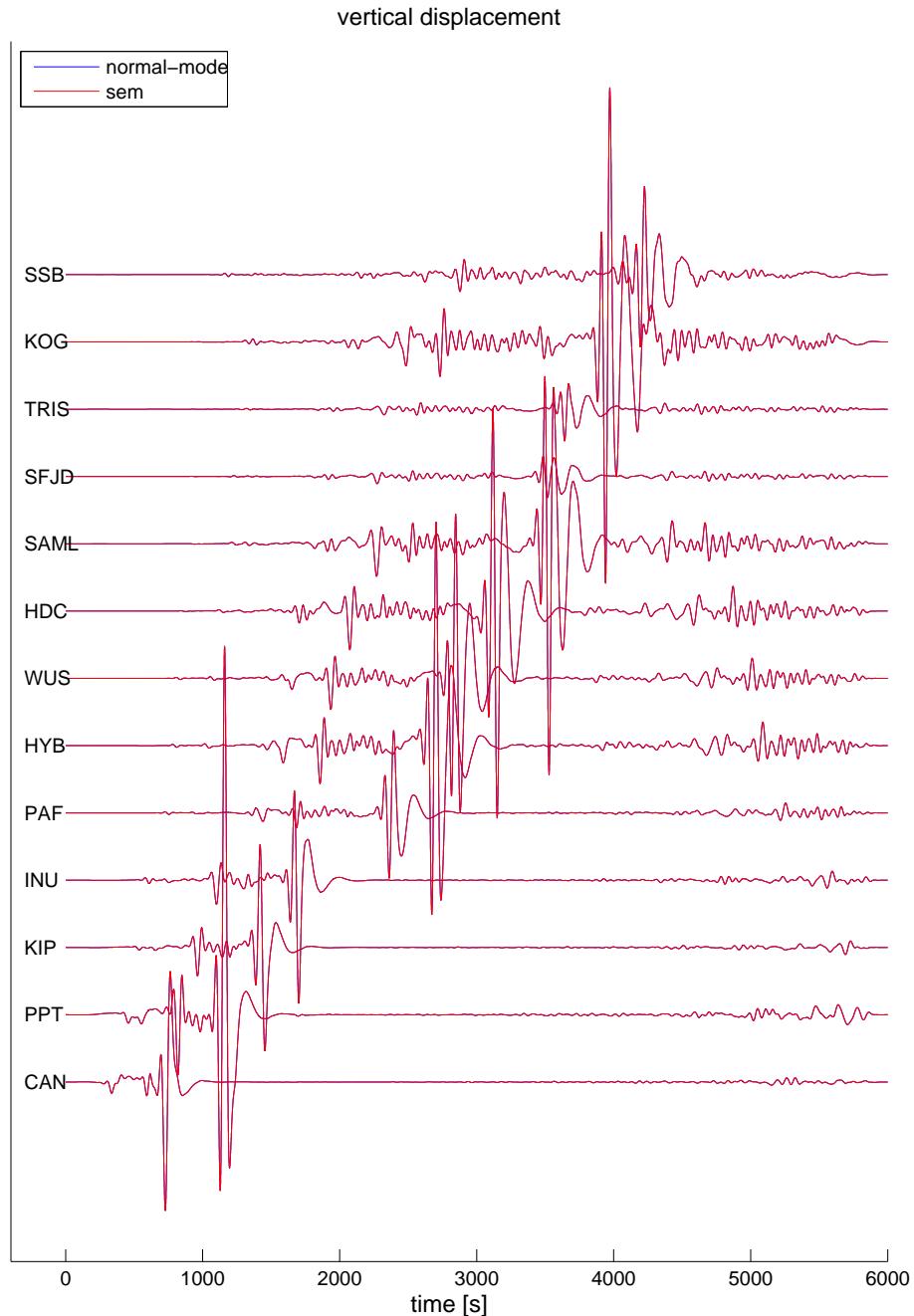


Figure C.1: Normal-mode (blue) and SEM (red) vertical displacements in isotropic PREM considering the effects of self-gravitation but not attenuation for 13 stations at increasing distance from the 1999 November 26th Vanuatu event located at 15 km depth. The SEM computation is accurate for periods longer than 17 s. The seismograms have been filtered between 50 s and 500 s. The station names are indicated on the left.

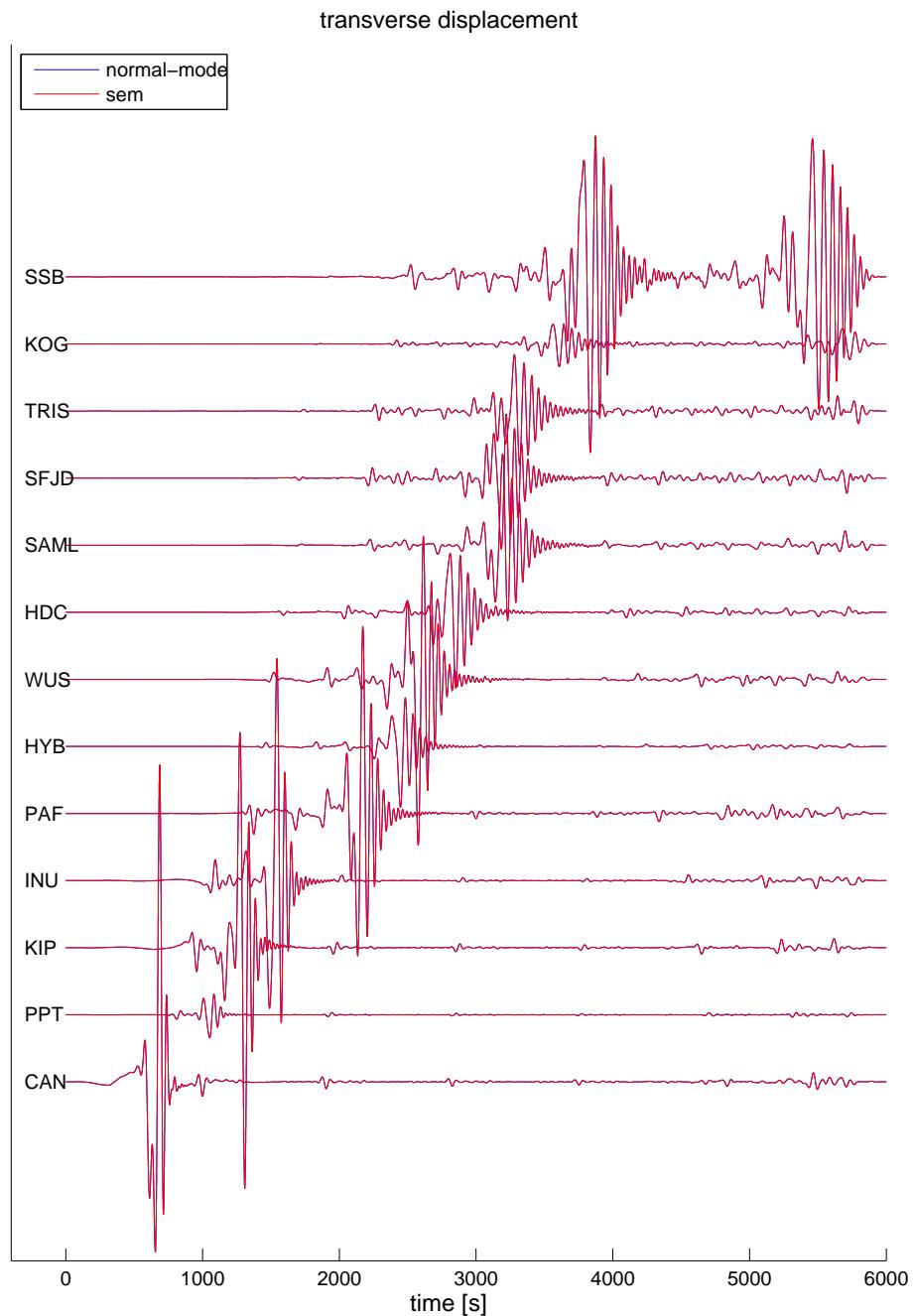


Figure C.2: Same as in Figure C.1 for the transverse displacements.

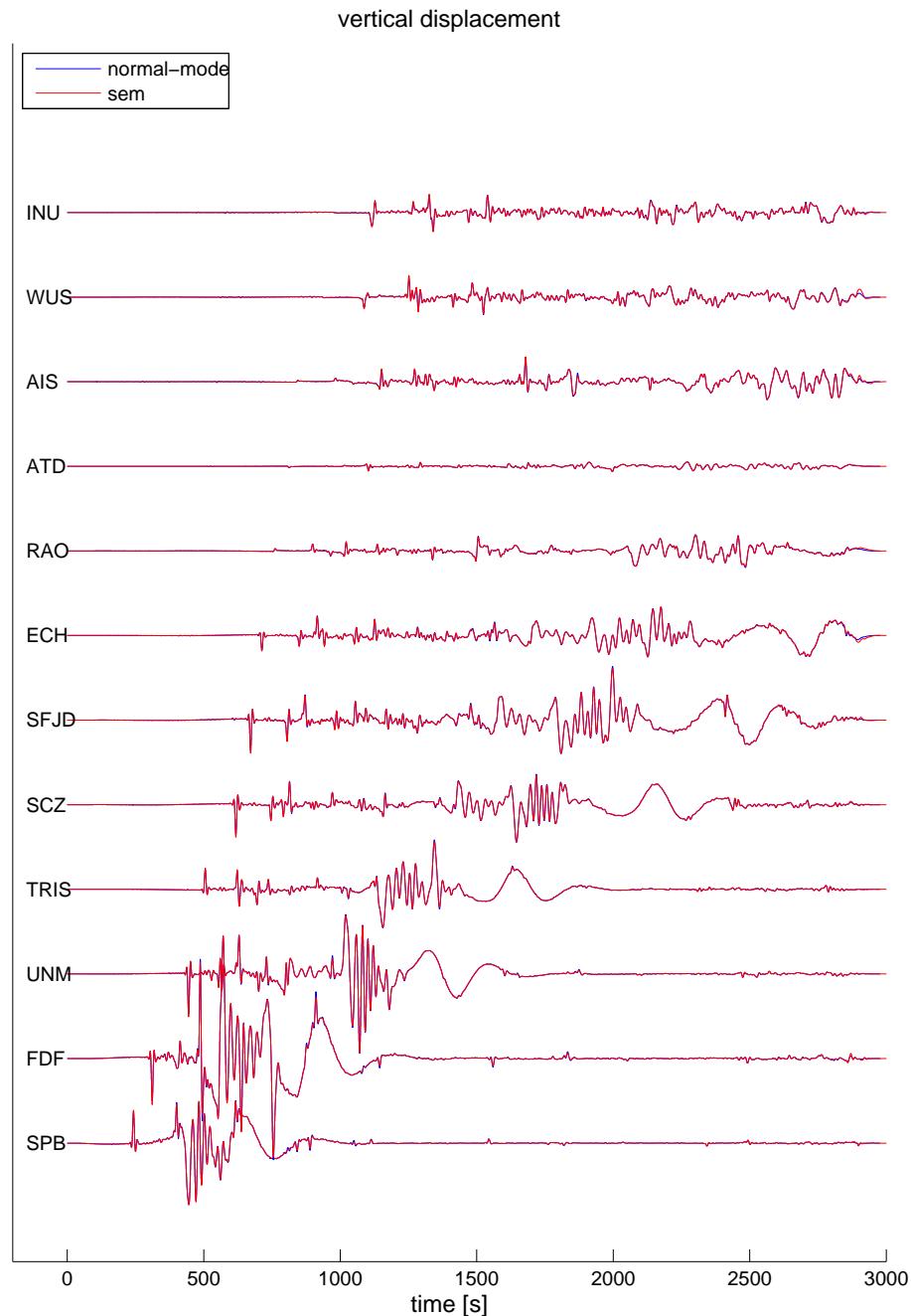


Figure C.3: Normal-mode (blue) and SEM (red) vertical displacements in transversely isotropic PREM considering the effects of self-gravitation and attenuation for 12 stations at increasing distance from the 1994 June 9th Bolivia event located at 647 km depth. The SEM computation is accurate for periods longer than 9 s. The seismograms have been filtered between 10 s and 500 s. The station names are indicated on the left.

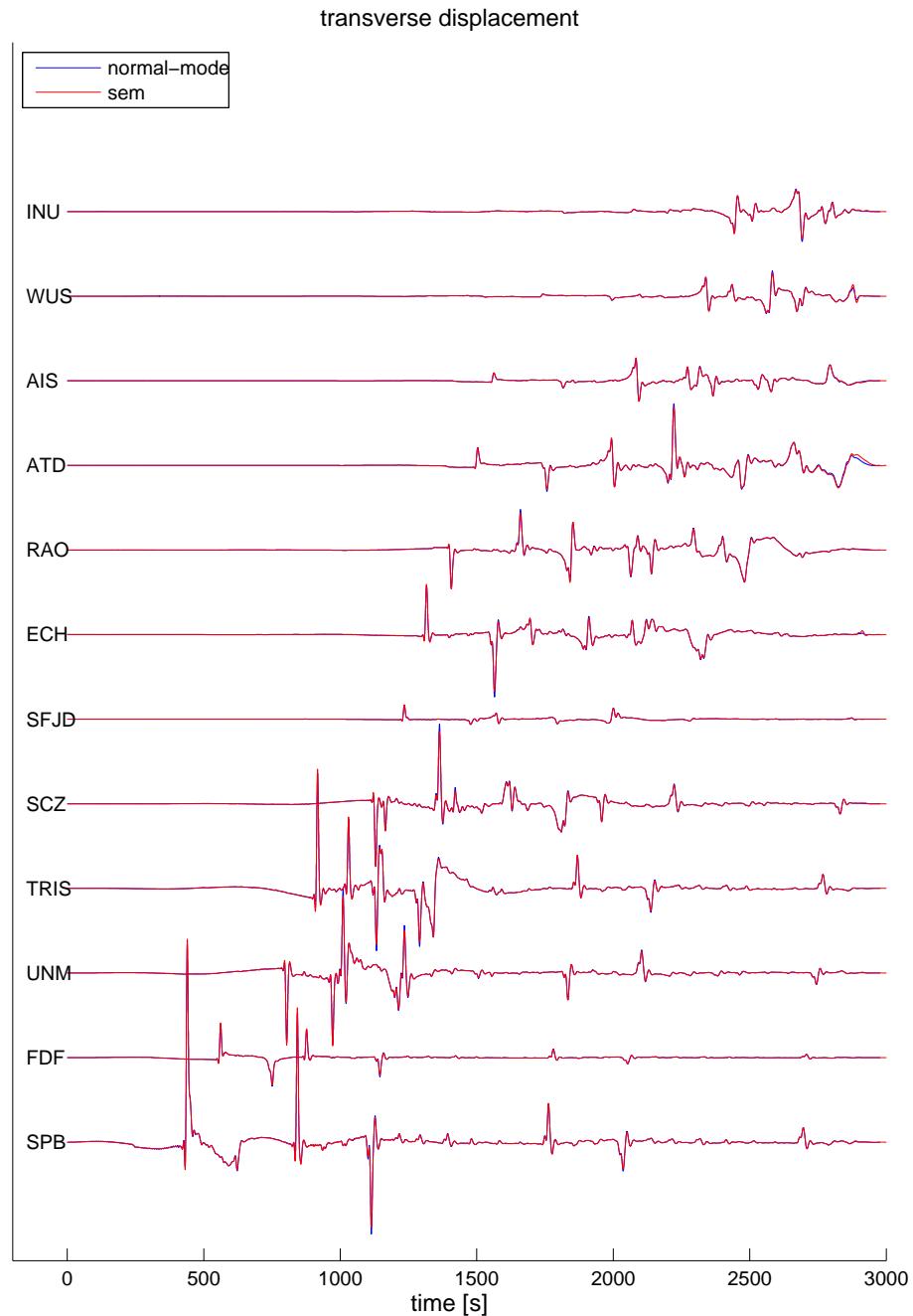


Figure C.4: Same as in Figure C.3 for the transverse displacements.

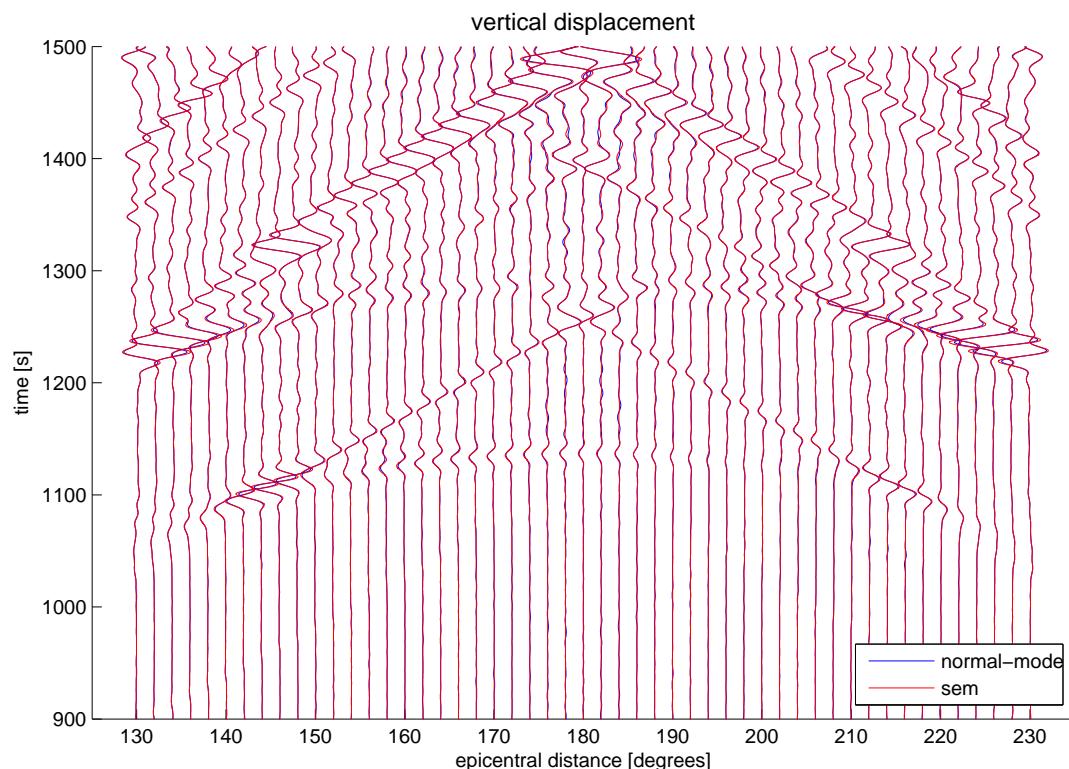


Figure C.5: Seismograms recorded between 130 degrees and 230 degrees, showing in particular the good agreement for core phases such as PKP. This figure is similar to Figure 24 of Komatitsch and Tromp [2002a]. The results have been filtered between 15 s and 500 s.

## Appendix D

# SAC Headers

Information about the simulation (i.e., event/station information, sampling rate, etc.) is written in the header of the seismograms in SAC format. The list of values and related explanation are given in Figure D.1. Please check the SAC webpages (<http://www.iris.edu/software/sac/>) for further information. Please note that the reference time KZTIME is the centroid time ( $t_{\text{CMT}} = t_{\text{PDE}} + \text{time shift}$ ) which corresponds to zero time in the synthetics. For kinematic rupture simulations, KZTIME is equal to the CMT time of the source having the minimum time-shift in the CMTSOLUTION file, and coordinates, depth and half-duration of the event are not provided in the headers.

<b>FILE: AAK.II.MXZ.sem.sac</b>	
NPTS = 37200	number of points per data component
B = -2.250000e+00	beginning value of time array
E = 6.005389e+03	end value of time array
IFTYPE = TIME SERIES FILE	type of file
LEVEN = TRUE	TRUE if data is evenly spaced
DELTA = 1.615000e-01	sampling rate (s)
IDEP = DISPLACEMENT (NM)	type of seismograms*
DEPMIN = -5.038710e-07	minimum displacement value
DEPMAX = 5.296865e-07	maximum displacement value
DEPMEN = -6.698920e-10	mean displacement value
OMARKER = 0	reference time in synthetics
KZDATE = FEB 04 (035), 2010	event date
KZTIME = 17:48:15.599	event origin time (centroid time)
IZTYPE = EVENT ORIGIN TIME	reference time
KSTNM = AAK	station name
CMPAZ = 0.000000e+00	component azimuth (degrees clockwise from north)
CMPINC = 0.000000e+00	component incident angle (degrees from vertical)
STLA = 4.263900e+01	station latitude (degrees, north positive)
STLO = 7.449400e+01	station longitude (degrees, east positive)
STEL = 1.645000e+03	station elevation (meters)
STDP = 3.000000e+01	station depth below surface (meters)
KEVNM = 201002041748A	event name
EVLA = -1.950000e+01	event CMT latitude (degrees, north positive)
EVLO = -1.732400e+02	event CMT longitude (degrees, east positive)
EVDP = 2.500000e+01	event CMT depth (km)
IEVTYP = EARTHQUAKE	event type
DIST = 1.326017e+04	great circle distance between event and station (km)
AZ = 3.085366e+02	event to station azimuth (degrees)
BAZ = 9.023685e+01	station to event azimuth (backazimuth, degrees)
GCARC = 1.191897e+02	great circle distance between event and station (degrees)
LOVROK = TRUE	TRUE if it is ok to write the file on disk
USER0 = 1.500000e+00	source half-duration (s)
USER1 = 1.700000e+01	shortest period at which simulations are accurate (s)
USER2 = 5.000000e+02	longest period at which simulations are accurate (s)
KUSER0 = SEM	method used to compute synthetic seismograms
KUSER1 = v5.1.0	version of the SEM code
KUSER2 = Tiger	
NNVHDR = 6	header version number
SCALE = 1.000000e+09	scale factor to convert the unit of the synthetics from meters to nanometers
LPSPOL = TRUE	TRUE if station components have positive polarity
LCALDA = TRUE	TRUE if DIST, AZ, BAZ and GCARC are calculated from station and event coordinates
KCMPNM = MXZ	station component name
KNETWK = II	station network name

\* the unit of synthetic seismograms is "meters". Seismograms should be scaled by the header SCALE to obtain units of nanometers.

Figure D.1: List of SAC headers and their explanations for a sample seismogram.

## Appendix E

# Channel Codes of Seismograms

Seismic networks, such as the Global Seismographic Network (GSN), generally involve various types of instruments with different bandwidths, sampling properties and component configurations. There are standards to name channel codes depending on instrument properties. IRIS (<http://www.iris.edu>) uses SEED/FDSN format for channel codes, which are represented by three letters, such as LHN, BHZ, etc. In older versions of the SPECFEM package, a common format was used for the channel codes of all seismograms, which was LHE/LHN/LHZ for three components. To avoid confusion when comparisons are made to observed data, we are now using the FDSN convention for SEM seismograms. In the following, we give a brief explanation of the FDSN convention and how it is adopted in SEM seismograms. Please visit [http://www.iris.edu/manuals/SEED\\_appA.htm](http://www.iris.edu/manuals/SEED_appA.htm) for further information.

**Band code:** The first letter in the channel code denotes the band code of seismograms, which depends on the response band and the sampling rate of instruments. The list of band codes used by IRIS is shown in Figure E.1. The sampling rate of SEM synthetics is controlled by the resolution of simulations rather than instrument properties. However, for consistency, we follow the FDSN convention for SEM seismograms governed by their sampling rate. For SEM synthetics, we consider band codes for which  $dt \leq 1$  s. The FDSN convention also considers the response band of instruments. For instance, short-period and broad-band seismograms with the same sampling rate correspond to different band codes, such as S and B, respectively. In such cases, we consider SEM seismograms as broad band, ignoring the corner period ( $\geq 10$  s) of the response band of instruments (note that at these resolutions, the minimum period in the SEM synthetics will be less than 10 s). Accordingly, when you run a simulation the band code will be chosen depending on the resolution of the synthetics, and channel codes of SEM seismograms will start with either L, M, B, H, C or F, shown by red color in the figure.

**Instrument code:** The second letter in the channel code corresponds to instrument codes, which specify the family to which the sensor belongs. For instance, H and L are used for high-gain and low-gain seismometers, respectively. The instrument code of SEM seismograms will always be X, as assigned by FDSN for synthetic seismograms.

**Orientation code:** The third letter in channel codes is an orientation code, which generally describes the physical configuration of the components of instrument packages. SPECFEM uses the traditional orientation code E/N/Z (East-West, North-South, Vertical) for three components.

**EXAMPLE:** Depending on the resolution of your simulations, if the sampling rate is greater than 0.1 s and less than 1 s, a seismogram recorded on the vertical component of station AAK will be named IU.AAK.MXZ.sem.sac, whereas it will be IU.AAK.BXZ.sem.sac, if the sampling rate is greater than 0.0125 and less equal to 0.1 s.

Band code	Band type	Sampling rate (sec)	Corner period (sec)
F	...	> 0.0002 to <= 0.001	$\geq 10 \text{ sec}$
G	...	> 0.0002 to <= 0.001	< 10 sec
D	...	> 0.001 to <= 0.004	< 10 sec
C	...	> 0.001 to <= 0.004	$\geq 10 \text{ sec}$
E	Extremely Short Period	$\leq 0.0125$	< 10 sec
S	Short Period	$\leq 0.1$ to $> 0.0125$	< 10 sec
H	High Broad Band	$\leq 0.0125$	$\geq 10 \text{ sec}$
B	Broad Band	$\leq 0.1$ to $> 0.0125$	$\geq 10 \text{ sec}$
M	Mid Period	$< 1$ to $> 0.1$	
L	Long Period	1	
V	Very Long Period	10	
U	Ultra Long Period	100	
R	Extremely Long Period	1000	
P	On the order of 0.1 to 1 day	$\leq 100000$ to $> 10000$	
T	On the order of 1 to 10 days	$\leq 1000000$ to $> 100000$	
Q	Greater than 10 days	$> 1000000$	
A	Administrative Instrument Channel	variable	NA
O	Opaque Instrument Channel	variable	NA

Figure E.1: The FDSN band code convention is based on the sampling rate and the response band of instruments. Please visit [http://www.iris.edu/manuals/SEED\\_appA.htm](http://www.iris.edu/manuals/SEED_appA.htm) for further information. Grey rows show the relative band-code range in SPECFEM, and the band codes used to name SEM seismograms are denoted in red.

# Appendix F

## Troubleshooting

### FAQ

**configuration fails:** Examine the log file 'config.log'. It contains detailed informations. In many cases, the path's to these specific compiler commands F90, CC and MPIF90 won't be correct if './configure' fails.

Please make sure that you have a working installation of a Fortran compiler, a C compiler and an MPI implementation. You should be able to compile this little program code:

```
program main
  include 'mpif.h'
  integer, parameter :: CUSTOM_MPI_TYPE = MPI_REAL
  integer ier
  call MPI_INIT(ier)
  call MPI_BARRIER(MPI_COMM_WORLD,ier)
  call MPI_FINALIZE(ier)
end
```

**compilation fails:** In case a compilation error like the following occurs, stating

```
...
obj/meshfem3D.o: In function `MAIN__':
meshfem3D.f90:(.text+0x14): undefined reference to `_gfortran_set_std'
...

```

make sure you're pointing to the right 'mpif90' wrapper command.

Normally, this message will appear when you are mixing two different Fortran compilers. That is, using e.g. gfortran to compile non-MPI files and mpif90, wrapper provided for e.g. ifort, to compile MPI-files.

fix: e.g. specify

```
./configure FC=gfortran MPIF90=/usr/local/openmpi-gfortran/bin/mpif90
```

**changing PPM model routines fails:** In case you want to modify the PPM-routines in file model\_ppm.f90, please consider the following points:

1. Please check in file get\_model\_parameter.f90 that the entry for PPM models looks like:

```
...
else if(MODEL_ROOT == 'PPM') then
  ! overimposed based on isotropic-prem
CASE_3D = .true.
CRUSTAL = .true.
MODEL_3D_MANTLE_PERTUBATIONS = .true.
ONE_CRUST = .true.
THREE_D_MODEL = THREE_D_MODEL_PPM
TRANSVERSE_ISOTROPY = .true. ! to use transverse-isotropic prem
...

```

You can set `TRANSVERSE_ISOTROPY` to `.false.` in case you want to use the isotropic PREM as 1D background model.

2. Transverse isotropy would mean different values for horizontal and vertically polarized wave speeds, i.e. different for `vph` and `vpv`, `vsh` and `vsv`, and it includes an additional parameter `eta`. By default, we take these wave speeds from PREM and add your model perturbations to them. For the moment, your model perturbations are added as isotropic perturbations, using the same `dvp` for `vph` and `vpv`, and `dvs` for `vsh` and `vsv`, see in `meshfem3D_models.f90`:

```
...
case(THREE_D_MODEL_PPM )
  ! point profile model
  call model_PPM(r_used,theta,phi,dvs,dvp,drho)
  vpv=vpv*(1.0d0+dvp)
  vph=vph*(1.0d0+dvp)
  vsv=vsv*(1.0d0+dvs)
  vsh=vsh*(1.0d0+dvs)
  rho=rho*(1.0d0+drho)
...

```

You could modify this to add different perturbations for `vph` and `vpv`, resp. `vsh` and `vsv`. This would basically mean that you add transverse isotropic perturbations. You can see how this is done with e.g. the model `s362ani`, following the flag `THREE_D_MODEL_S362ANI` on how to modify accordingly the file `meshfem3D_models.f90`.

In case you want to add more specific model routines, follow the code sections starting with:

```
! ---
!
! ADD YOUR MODEL HERE
!
! ---


```

to see code sections sensitive to model updates.

# Appendix G

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**Version 3, 29 June 2007**

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