

COMP261 Lecture 14

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Parsing 2 of 4: Grammars and Parsing



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*Te Whare Wānanga
o te Ūpoko o te Ika a Māui*



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Reading structured text – take two

- Now consider more complex forms of text:
 - *XML documents:*

```
<html><head><title>My Web Page</title></head>  
<body><p>Thank you for viewing my page!</p>  
</body></html>
```
 - *Java statement:*

```
while ( A[k] != x ) { k++; }
```
- More complex structures get cumbersome to describe with regular expressions.
- Some patterns, such as nested structures, can't be expressed with regular expressions.

Describing structured text: Grammars

- A **grammar** is a set of rules, describing the structure of strings in a formal language (set of strings).
- The rules describe how to form strings in the language, and names its structural components.
whileStmt ::= “while” “(“ condition “)” statement
- Can show alternative forms, and can be recursive:
statement ::= whileStmt | ifStmt | ...
- A grammar only describes the form of allowable strings, not their meaning.
- Official name is **context-free grammar** – look it up!

Example: Java statements (simplified!!)

Statement ::=

Variable “=” *Exp* “;” |

“if” “(“ *Exp* “)” *Statement* |

“if” “(“ *Exp* “)” *Statement* “else” *Statement* |

“while” “(“ *Exp* “)” *Statement* |

“do” *Statement* “while” “(“ *Exp* “)” |

“{“ *Statement-list* “}” |

...

Exp ::= Variable | Constant | ...

Ex: Look on-line for full Java grammar.

Example: A simple html grammar

HTMLFILE ::= "<html>" [HEAD] BODY "</html>"

HEAD ::= "<head>" TITLE "</head>"

TITLE ::= "<title>" TEXT "</title>"

BODY ::= "<body>" [BODYTAG]* "</body>"

BODYTAG ::= H1TAG | PTAG | OLTAG | ULTAG

H1TAG ::= "<h1>" TEXT "</h1>"

PTAG ::= "<p>" TEXT "</p>"

OLTAG ::= "" [LITAG]+ ""

ULTAG ::= "" [LITAG]+ ""

LITAG ::= "" TEXT ""

TEXT ::= [.[^]<>]]+ (*Sequence of characters other than < and >*)

Grammar structure: Terminals

- Literal strings or patterns of characters that can occur in texts
- Here they are enclosed in double quote marks
- Classes of terminals (like numbers, identifiers) defined by RE's.

HTMLFILE ::= "<html>" [HEAD] BODY "</html>"

HEAD ::= "<head>" TITLE "</head>"

TITLE ::= "<title>" TEXT "</title>"

BODY ::= "<body>" [BODYTAG]* "</body>"

BODYTAG ::= H1TAG | PTAG | OLTAG | ULTAG

H1TAG ::= "<h1>" TEXT "</h1>"

PTAG ::= "<p>" TEXT "</p>"

OLTAG ::= "" [LITAG]+ ""

ULTAG ::= "" [LITAG]+ ""

LITAG ::= "" TEXT ""

TEXT ::= [.[^]<>]⁺ (*Sequence of characters other than < and >*)

Grammar structure: Nonterminals

- Name structural components of strings (not part of the text)
- Defined by rules.

Top level nonterminal
(start symbol) usually first

HTMLFILE ::= "<html>" [HEAD] BODY "</html>"

HEAD ::= "<head>" TITLE "</head>"

TITLE ::= "<title>" TEXT "</title>"

BODY ::= "<body>" [BODYTAG]* "</body>"

BODYTAG ::= H1TAG | PTAG | OLTAG | ULTAG

H1TAG ::= "<h1>" TEXT "</h1>"

PTAG ::= "<p>" TEXT "</p>"

OLTAG ::= "" [LITAG]+ ""

ULTAG ::= "" [LITAG]+ ""

LITAG ::= "" TEXT ""

TEXT ::= [. [^ < >]]+ *(Sequence of characters other than < and >)*

Grammar structure: Meta-symbols

- Meta-symbols are fixed parts of the grammar notation.
- $::=$ = is defined as, $|$ = “or”
- $[...]$ = optional, $[...]^*$ = zero or more, $[...]^+$ = one or more

HTMLFILE $::=$ “<html>” [HEAD] BODY “</html>”

HEAD $::=$ “<head>” TITLE “</head>”

TITLE $::=$ “<title>” TEXT “</title>”

BODY $::=$ “<body>” [BODYTAG]^{*} “</body>”

BODYTAG $::=$ H1TAG | PTAG | OLTAG | ULTAG

H1TAG $::=$ “<h1>” TEXT “</h1>”

PTAG $::=$ “<p>” TEXT “</p>”

OLTAG $::=$ “” [LITAG]⁺ “”

ULTAG $::=$ “” [LITAG]⁺ “”

LITAG $::=$ “” TEXT “”

TEXT $::=$ $[.^{<>}]^+$ (*Sequence of characters other than < and >*)

Using the Grammar

Given some text:

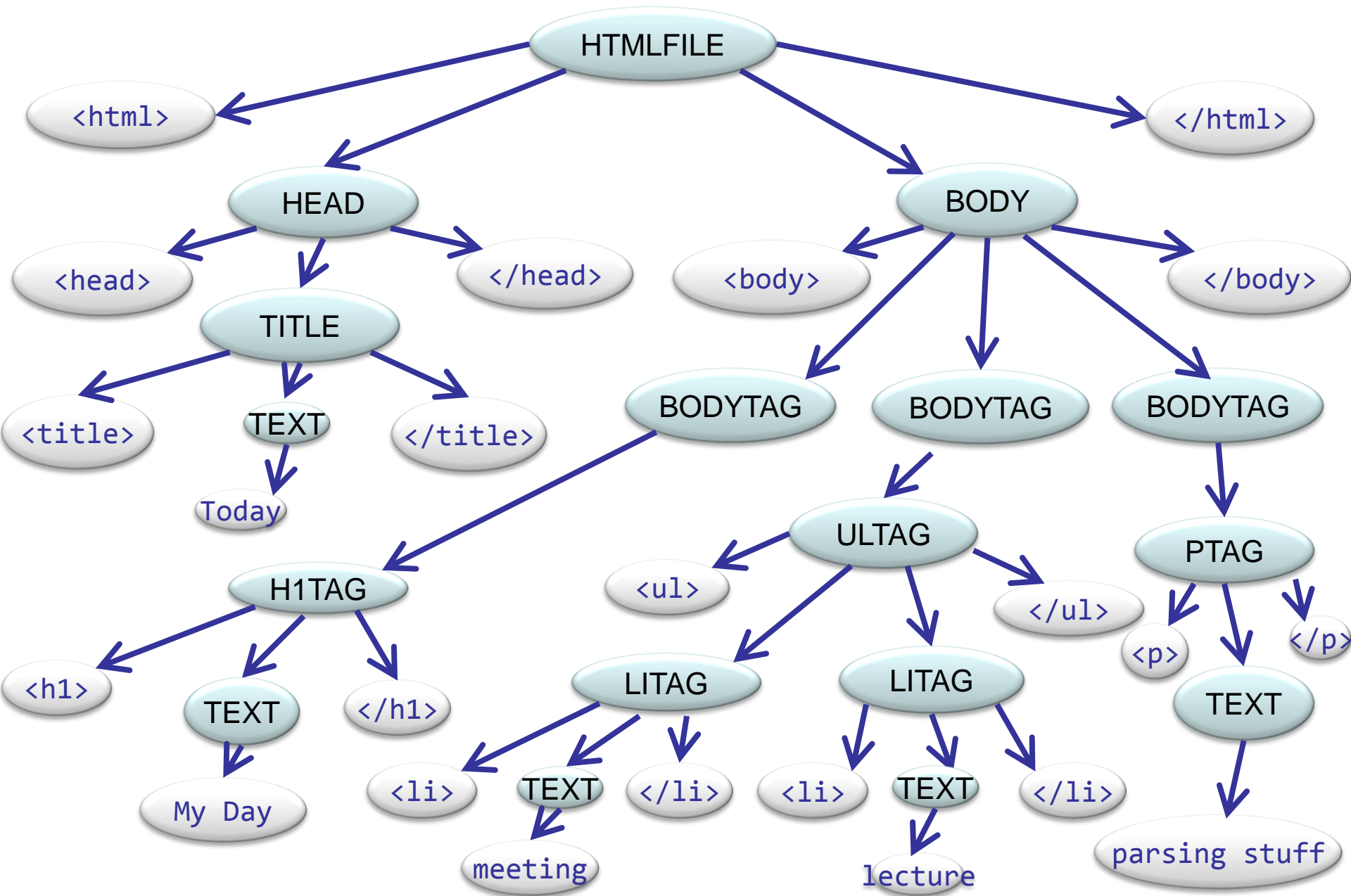
```
<html>  
<head><title> Today</title></head>  
<body><h1> My Day </h1>  
<ul><li>meeting</li><li> lecture </li></ul>  
<p> parsing stuff</p>  
</body>  
</html>
```

- Is it a valid piece of HTML?
 - Does it conform to the grammar rules?
- What is the structure? (Needed in order to process it)
 - what are the components?
 - what types are the components?
 - how are they related?

What kind of structure?

- Structure of a text is hierarchical
- Can be described by an **ordered tree**
 - Leaves correspond to terminals.
 - Internal nodes labelled with nonterminals.
 - Root is labelled with the start symbol.
 - Each internal node and its children correspond to a grammar rule (or an alternative in a grammar rule).
 - The text consists of all terminals on the **fringe** of the tree.
- A (**concrete**) **syntax tree** or **parse tree** represents the syntactic structure of a string according to the grammar, showing all the components of the rules.

Parse Tree



Grammars define possible parse trees

- Each grammar rule defines possible structures that may occur in a parse tree.

H1TAG ::= "<h1>" TEXT "</h1>"

BODYTAG ::= H1TAG | PTAG | OLTAG | ULTAG

HTMLFILE ::= "<html>" [HEAD] BODY "</html>"

- A text is in the language defined by a grammar iff you can construct a parse tree for it.

Parsing text

- Consider this example grammar:

Expr ::= Num | Add | Sub | Mul | Div

Add ::= "add" "(" Expr "," Expr ")"

Sub ::= "sub" "(" Expr "," Expr ")"

Mul ::= "mul" "(" Expr "," Expr ")"

Div ::= "div" "(" Expr "," Expr ")"

Num ::= [-+]?[0-9]+

(an optional sign followed by a sequence of digits)

- Check the following texts:

add(div(56 , 8), mul(sub(0, 10), mul (-1, 3)))

div(div(86, 5), 67) 50

add(-5, sub(50, 50), 4)

div(100, 0)

Parsing arithmetic expressions

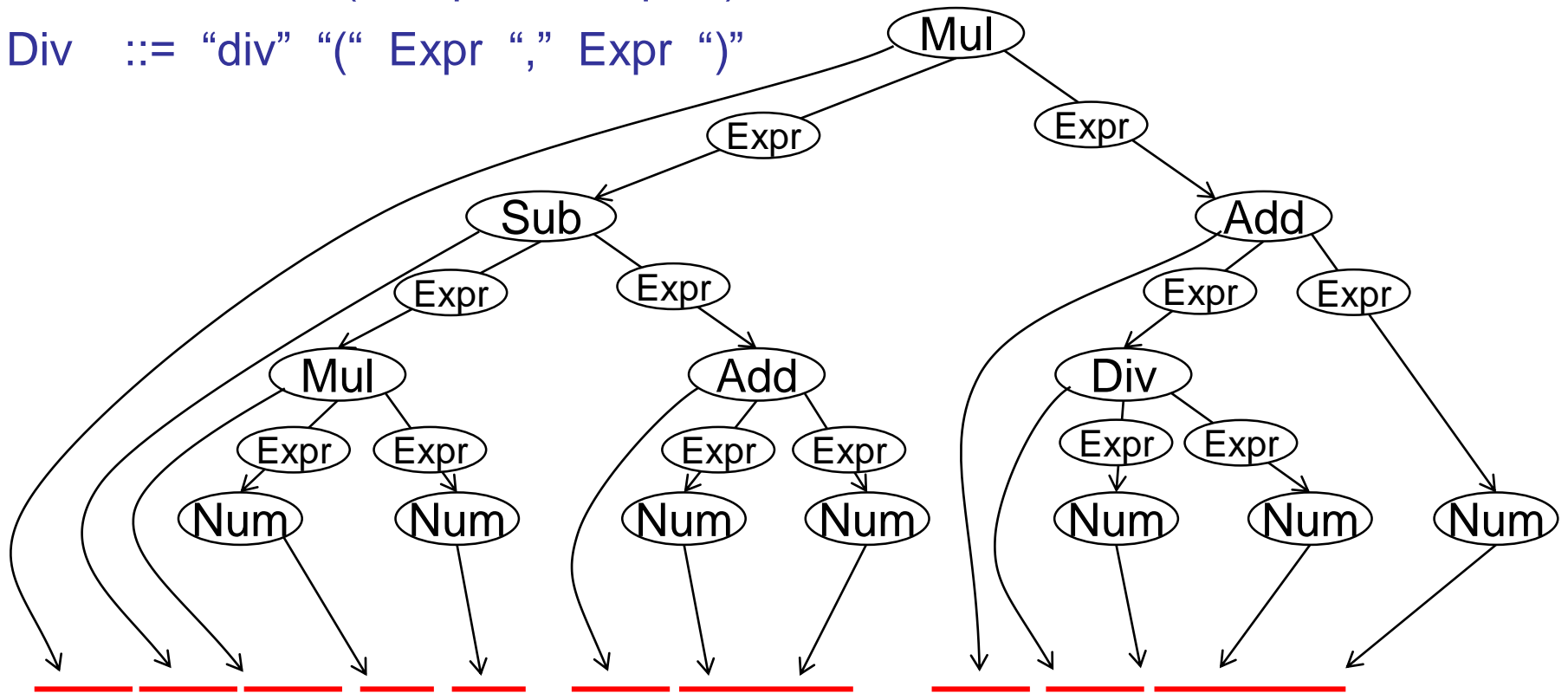
Expr ::= Num | Add | Sub | Mul | Div

Add ::= "add" "(" Expr "," Expr ")"

Sub ::= “sub” (“ Expr “,” Expr “)”

Mul ::= “mul” “(” Expr “,” Expr “)”

Div ::= “div” (“ Expr “,” Expr “)”



How do we write programs to do this?

Given: a grammar, and some text to be parsed:

1: Lexical analysis / Scanning / Tokenising

- Break up text into a sequence of tokens
- Remove white space (and comments)

2: Syntax analysis / Parsing

- Check if the text meets the grammar rules.
- Construct a parse tree for the text, according to the grammar.

- Separating scanning simplifies the parser.

Using a Scanner for Lexical Analysis

- We can use a scanner, as describe in lecture 13.
- Can read tokens one at a time as they are required by the parser,
- Or read the whole file/text and turn it into a list of tokens before parsing starts.

Idea: Write a Program to Mimic Rules!

- Write a parse method corresponding to each nonterminal that calls other methods for each nonterminal and calls the scanner for each terminal!
- E.g., given a grammar:
 FOO ::= “a” BAR | “b” BAZ
 BAR ::=

Parser would have a method:

```
public boolean parseFOO(Scanner s){  
    if (!s.hasNext())           { return false; }      // PARSE ERROR  
    String token = s.next();  
    if (token.equals("a"))       { return parseBAR(s); }  
    else if (token.equals("b")) { return parseBAZ(s); }  
    else                         { return false; }      // PARSE ERROR  
}
```

Top Down Recursive Descent Parser

A top down recursive descent parser:

- Built from a set of mutually-recursive procedures.
- Each procedure usually implements one rule of the grammar.
- Structure of the resulting program closely mirrors that of the grammar.
- Return Boolean if just checking, or parse tree.

Simple Parser:

- Look at next token
- Use token type to choose branch of the rule to follow
- Fail if token is missing or is of a non-matching type.

Requires the grammar rules to be highly constrained:

- Always able to choose next path given current state and next token.

Using the Scanner

Break input into tokens

- Use Scanner with delimiter:

```
public void parse(String input) {  
    Scanner s = new Scanner(input);  
    s.useDelimiter("\\s*(?=[(),])|(?<=[(),])\\s*");  
    if ( parseExpr(s) ) {  
        System.out.println("That is a valid expression");  
    }  
}
```

- Breaks the input into a sequence of tokens,
 - spaces are separator characters and not part of the tokens
 - tokens also delimited at round brackets and commas, which will be tokens in their own right.

Example: Simple expressions

- Consider the following grammar:

Expr ::= Num | Add | Sub | Mul | Div

Add ::= “add” “(” Expr “,” Expr “)”

Sub ::= “sub” “(” Expr “,” Expr “)”

Mul ::= “mul” “(” Expr “,” Expr “)”

Div ::= “div” “(” Expr “,” Expr “)”

Num ::= an optional sign followed by a sequence of digits:
[-+]?[0-9]+

- What does a parser based on this grammar look like?
 - There is a method for each non terminal.
 - They need to follow the structure of the grammar rules.

Parser for expressions - first attempt

```
public boolean parseExpr(Scanner s) {
    if ( !s.hasNext() ) { return false; }           // PARSE ERROR
    String token = s.next();
    if ( token is a number ) { return true; }
    if ( token = "add" ) { return parseAdd(s); }
    if ( token = "sub" ) { return parseSub(s); }
    if ( token = "mul" ) { return parseMul(s); }
    if ( token = "div" ) { return parseDiv(s); }
    else { return false; }           // PARSE ERROR
}
```

```
public boolean parseAdd(Scanner s) {
    if ( !s.hasNext() ) { return false; }           // PARSE ERROR
    String token = s.next();
    if ( token != "add" ) {return false; }           // PARSE ERROR
    token = s.next();
    if ( token != "(" ) {return false; }             // PARSE ERROR
    ...
```

What's wrong here??

Accessing the next token

- How does `parseAdd` access the next token, when `parseExpr` has already read it?
- If you read the next token to test it, it's no longer there for another method to inspect!
- One approach: Could implement an alternative scanner class with *current* and *advance* methods.

Accessing the next token

- A second approach: Save the next token (“lookahead”) in a field of a parser object, which contains the parser methods.
- Can keep the scanner in a field too, rather than pass it to every parser method.
- ```
public class Parser {
 Scanner s;
 Token t = null;
 public Parser(Scanner scanner) { s = scanner; }
 public parseExp() { ... }
 ...
}
```

# Looking at next token

- A third approach: Check for specific kinds of tokens. So lookahead token remains in the input.
- Scanner can test for a particular kind of token: `hasNextInt`, `hasNextFloat`, `hasNextBoolean`, ...
- Can also check for a particular string:
  - `s.hasNext("string to match")`:
    - is there another token, and does it match the string?
    - `if ( s.hasNext("add") ) { ... }`
- Or for a regular expression:
  - `if ( s.hasNext("[ -+]?[0-9]+") ) { ... }`
    - true if there is another token, which is an integer



# Parsing Expressions (checking only)

```
public boolean parseExpr(Scanner s) {
 if (s.hasNext("[-+]?[0-9]+")) { s.next(); return true; }
 if (s.hasNext("add")) { return parseAdd(s); }
 if (s.hasNext("sub")) { return parseSub(s); }
 if (s.hasNext("mul")) { return parseMul(s); }
 if (s.hasNext("div")) { return parseDiv(s); }
 return false;
}

public boolean parseAdd(Scanner s) {
 if (s.hasNext("add")) { s.next(); } else { return false; }
 if (s.hasNext("(")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(",")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(")") { s.next(); } else { return false; }
 return true;
}
```

# Parsing Expressions (checking only)

```
public boolean parseSub(Scanner s) {
 if (s.hasNext("sub")) { s.next(); } else { return false; }
 if (s.hasNext("(")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(",")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(")")) { s.next(); } else { return false; }
 return true;
}
```

same for parseMul and parseDiv

# Parsing Expressions (checking only)

Alternative, given similarity of Add, Sub, Mul, Div:

```
public boolean parseExpr(Scanner s) {
 if (s.hasNext("[-+]?[0-9]+")) { s.next(); return true; }
 if (s.hasNext("add|sub|mul|div")) {s.next();} else {return false;}
 if (s.hasNext("(")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(",")) { s.next(); } else { return false; }
 if (!parseExpr(s)) { return false; }
 if (s.hasNext(")")) { s.next(); } else { return false; }
 return true;
}
```

This amounts to changing the grammar to:

Expr ::= Num | Op "(" Expr "," Expr ")"

Op ::= "add" | "sub" | "mul" | "div"

Num ::= [ -+]?[0-9]+

And writing the code for parseOP and parseNum inline.

# Simplifying the parser

We can reduce the duplication in checking for terminals:

```
public boolean parseExpr(Scanner s) {
 if (s.hasNext("[-+]?[0-9]+")) { s.next(); return true; }
 require(s, "add|sub|mul|div");
 require(s, "(");
 if (!parseExpr(s)) { return false; }
 require(s, ",");
 if (!parseExpr(s)) { return false; }
 require(s, ")");
 return true;
}
```

// consume next token and return true if it matches pat, else false

```
public String require(Scanner s, String pat){
 if (s.hasNext(pat)) { s.next(); return true; }
 else { return null; } // Print error message?
}
```

# A Better parser: using patterns

- Give names to patterns to make program easier to understand and to modify
- Precompile the patterns for efficiency:

```
Pattern numPat = Pattern.compile(
 "[-+]?(\\d+([.]\\d*)?|[.]\\d+)");
Pattern addPat = Pattern.compile("add");
Pattern subPat = Pattern.compile("sub");
Pattern mulPat = Pattern.compile("mul");
Pattern divPat = Pattern.compile("div");
Pattern opPat =
 Pattern.compile("add|sub|mul|div");
Pattern openPat = Pattern.compile("\\(");
Pattern commaPat = Pattern.compile(",");
Pattern closePat = Pattern.compile("\\)");
// Should all be declared as private and final.
```

# A Better parser: using patterns

```
public Node parseExpr(Scanner s) {
 Node n;
 if (!s.hasNext()) { return false; }
 if (s.hasNext(numPat)) { return parseNumber(s); }
 if (s.hasNext(addPat)) { return parseAdd(s); }
 if (s.hasNext(subPat)) { return parseSub(s); }
 if (s.hasNext(mulPat)) { return parseMul(s); }
 if (s.hasNext(divPat)) { return parseDiv(s); }
 return false;
}
```