

#### COMP261 Lecture 19

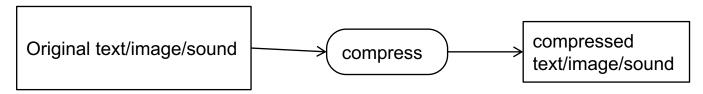
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**Data Compression 1** 



#### **Data/Text Compression**

- Files containing text, sound, video etc. can be huge!
   E.g. a blu ray movie is about 25gb.
- Can we reduce the amount of time/space required to transmit/store them?
- E.g. text files are hugely redundant we use 8 bits (or more) to store each character, but there is far less information than that.
- Compression is about reducing the memory required to store some information.



#### Lossless v. Lossy Data Compression

#### Data compression may be:

#### Lossless:

- No information is lost just gets stored more compactly
- Can retrieve the original data exactly (decompress)
- Important for text and some numerical data
  - compress to store/transmit, decompress to use

#### Lossy:

- Information may be lost
- Can't retrieve the original data exactly
- Acceptable in some contexts
  - data is stored and used in compressed form
- E.g. mp3 compresses sound files

## Lossless v. Lossy Data Compression

- Lossless compression only possible if there is redundancy in the original.
- Compression identifies and removes some of the redundant elements.
- Eg:
  - Identify repeated patterns
  - If lots of repeated characters, replace by count and character
  - Construct a dictionary and replace words by indexes to it

## Coding – one symbol at a time compression

#### Problem:

- Given a set of symbols (characters, numbers, ...)
- Encode them as bit strings
  - Use a separate code for each symbol
- Try to minimising the total number of bits.
- Solution: Huffman coding
  - Very clever solution, very widely used
  - Combining several great ideas!
- Note: When coding data to store/transmit, we often add extra bits (i.e. redundancy) so we can detect errors:
  - See parity bits, error-correcting codes.
  - This can still be done with compressed data.

#### **Equal Length Codes**

Obvious approach:
 Use the same number of bits for every symbol to be encoded.

• E.g. digits:

```
symbol: 0 1 2 3 4 5 6 7 8 9 code: 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001
```

E.g. letters:

```
symbol: a b c d e f g ... z code: 00001 00010 00011 00100 00101 00110 00111 ... 11010
```

## **Equal Length Codes**

How many bits are needed?

```
Digits:
symbol: 0 1 2 3 4 5 6 7 8 9
code: 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001
```

10 symbols, 4 bits

Letters:

```
symbol: a b c d e f g ... z code: 00001 00010 00011 00100 00101 00110 00111 ... 11010
```

26 symbols, 5 bits Already better than 8 bits per symbol!

Ex: How many bits for upper and lower case letters?

## **Equal Length Codes**

- With N bits, we can have up to 2<sup>N</sup> different codes.
- For N different symbols, need log₂N bits per symbol
   10 numbers, message length = 4
   26 letters, message length = 5
- If there are many repeated symbols, can we do better?

#### Variable Length Codes

- Great idea #1:
  - More efficient to have variable length codes
  - Use fewer bits for more common symbols
- Eg for letters, suppose:

   a occurs 50% of the time,
   b occurs 25% of time,
   d-e each occur 5% of time,
   f-j each occur 2% of time.

```
Encode:
a by '0'
b by '1'
c by '10'
d by '100'
e by '101'
g by '110'
...
i by '1001'
```

#### Variable Length Codes

```
sym: a b c d e f g h i j code: 0 1 10 11 100 101 110 111 1000 1001
```

String: aabajabaab

Fixed: 0000 0000 0001 0000 1001 0000 0010 0000 0000 0001

(using 4 bits each as only 10 letters used)

Variable: 0 0 1 0 1001 0 10 0 0 1

Takes 14 bits, rather than 40.

#### Variable length encoding

- Problem: where are the boundaries?
- How can we tell if 1010 is code for j, cab or baba?
- A possible approach:
  - Use 0 as a "sentinel bit" to mark the end of a code
  - But then can only use 1's for the code itself
- That's not so good can we do better?

#### Prefix-free codes

Great idea #2:

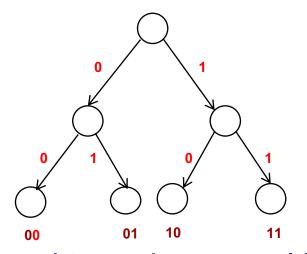
 Design codes so that no code is the prefix of another code!

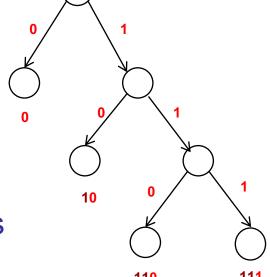
• Eg:

How do we design prefix-free code?

#### Prefix-free codes

 We can think of prefix-free codes as path labels to leaves in a binary tree (similar to a Trie).





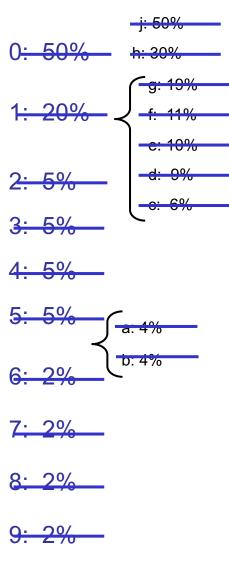
- Balanced tree gives equal length codes
- Linear tree is like using a sentinel bit
- What tree shape will give best codes?
- Want more frequent symbols at the top, less frequent at the bottom – but not too far away!

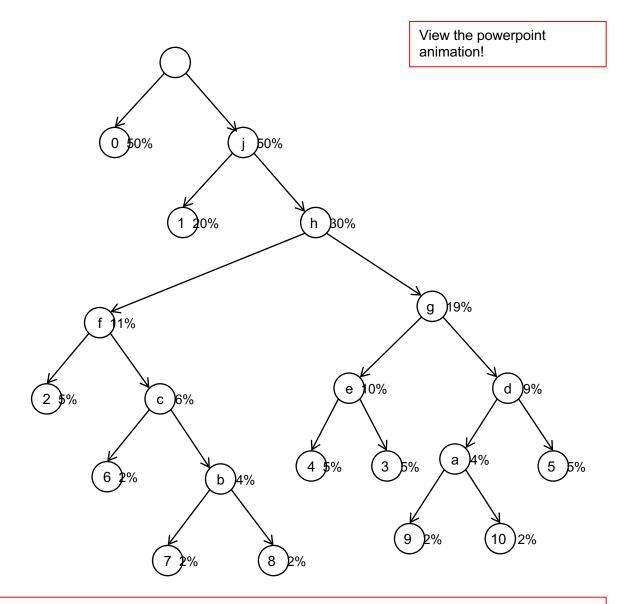
#### Prefix-free codes

Great idea #3:

- Build the tree from the bottom-up, combining nodes with smallest frequencies.
  - Start with a leaf for each symbol, labelled with its frequency.
  - At each step, combine two nodes with smallest frequencies, add a new node as their parent, labelled with the sum of their frequencies.
  - Stop when all nodes are combined into a single tree.

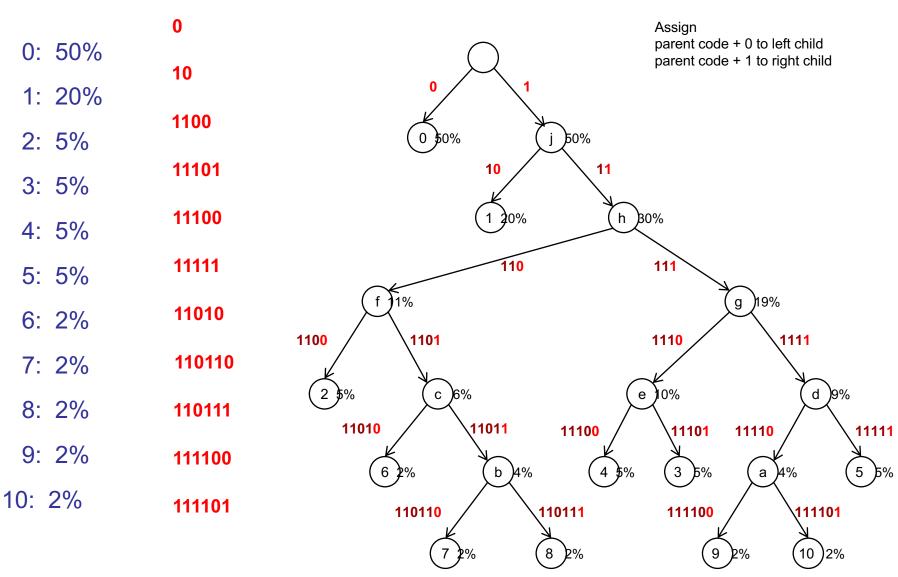
## Example: Building the tree





10<del>: 2%</del>

# Example: Assigning the codes



average code length = (1\*.5)+(2\*.2)+(4\*.05)+(5\*.17)+(6\*.08) = 2.43 bits

#### **Huffman Coding**

- Generates the best set of codes, given frequencies/probabilities on all the symbols.
- Creates an optimal binary tree to construct the codes.

```
Construct a leaf node (singleton tree) for each symbol with the given probability

Put these nodes into a priority queue, with frequency as priority.

(lowest frequency = highest priority)

while there is more than one node in the queue: (i.e. more than one tree)

remove the top two nodes

create a new tree node with these two nodes as children.

node frequency = sum of frequencies of the two nodes

add new node to the queue

final node is root of tree.
```

Traverse tree to assign codes: if node has code c, assign c0 to left child, c1 to right child

- This is a "greedy" algorithm can always choose the nodes that lead to best code.
- See video on YouTube: Text compression with Huffman coding

## **Huffman Coding**

To decode, we need a table of the codes used.

- If we label the edges of the tree with 0's and 1's, as added at each level, we get a *trie* which can be used like a scanner to split the coded string/file into separate codes to be decoded.
- Example: Use above tree to decode: 010011010010

## **Huffman Coding**

- When storing/transmitting a compressed file, we need to include the tree for decompressing.
  - Can reduce efficiency of coding.

- Or, use a standard frequency table, not based on the particular file, for code.
  - E.g. use known frequencies of letters in English text.