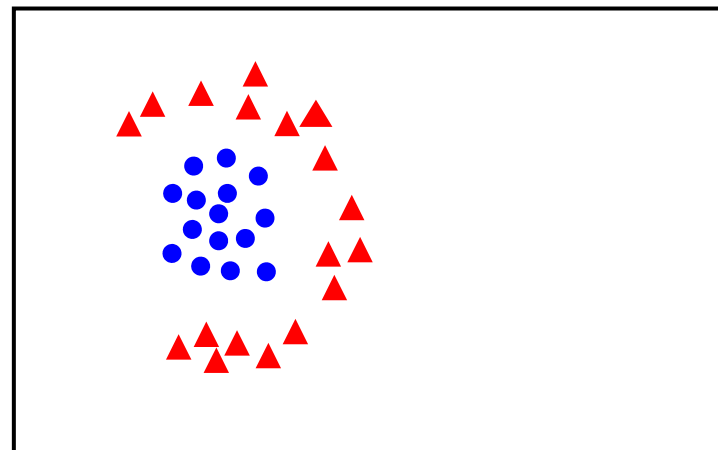
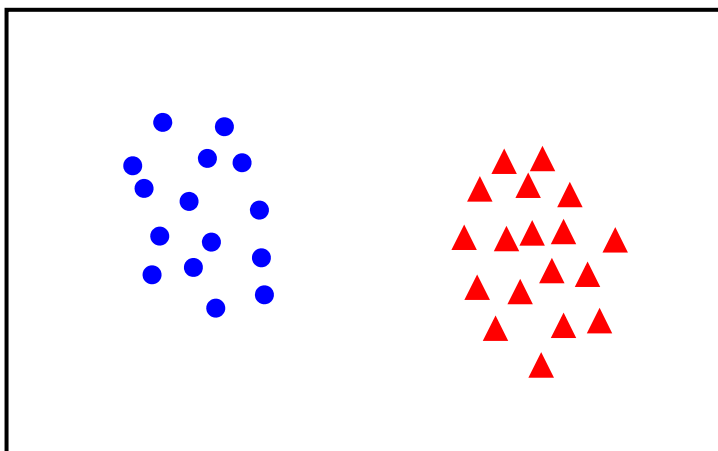


Binary Classification

Given training data (\mathbf{x}_i, y_i) for $i = 1 \dots N$, with $\mathbf{x}_i \in \mathbb{R}^d$ and $y_i \in \{-1, 1\}$, learn a classifier $f(\mathbf{x})$ such that

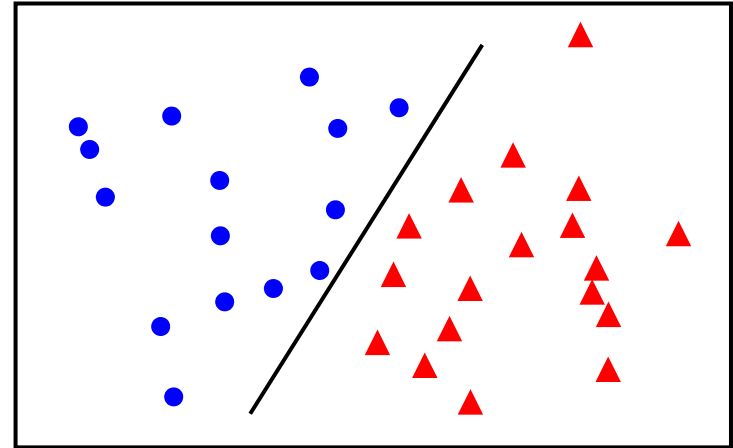
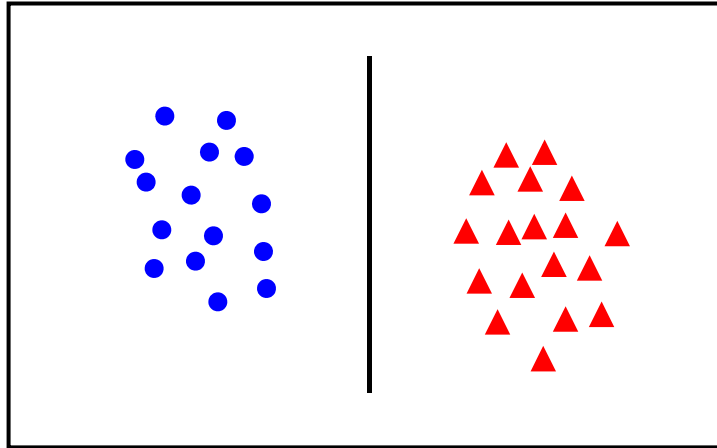
$$f(\mathbf{x}_i) \begin{cases} \geq 0 & y_i = +1 \\ < 0 & y_i = -1 \end{cases}$$

i.e. $y_i f(\mathbf{x}_i) > 0$ for a correct classification.

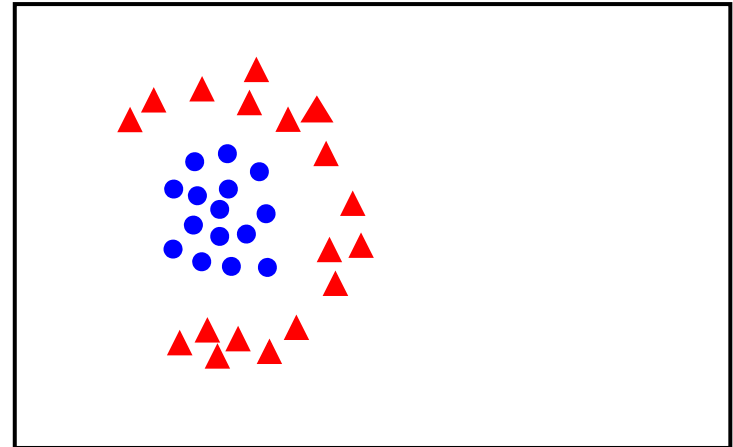
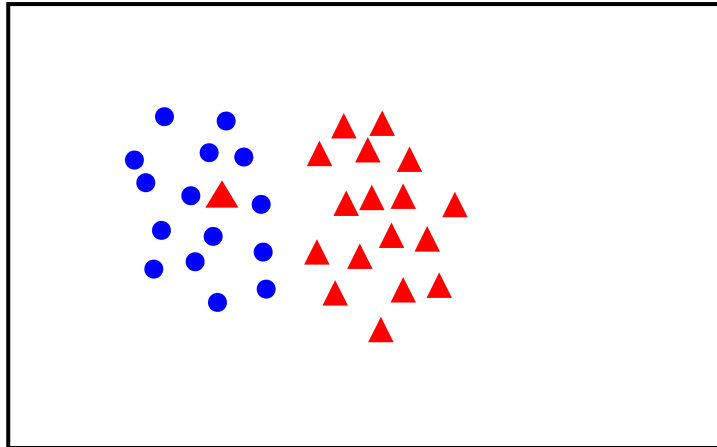


Linear separability

linearly
separable



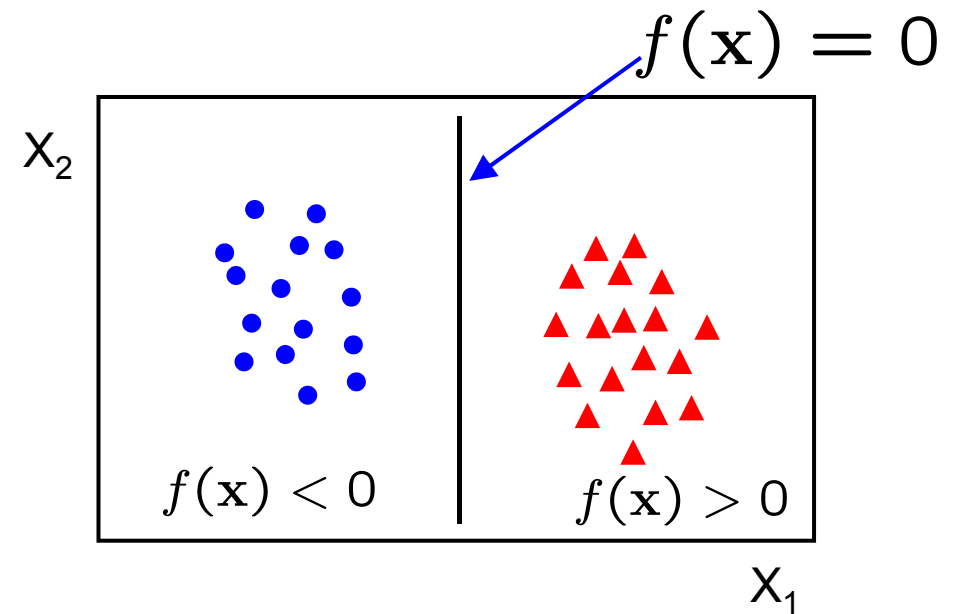
not
linearly
separable



Linear classifiers

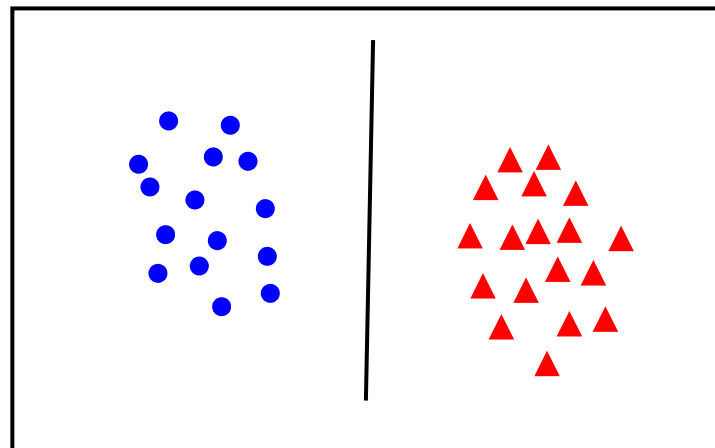
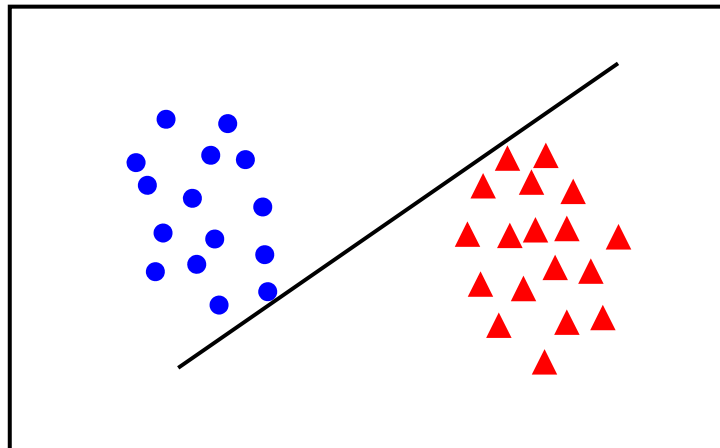
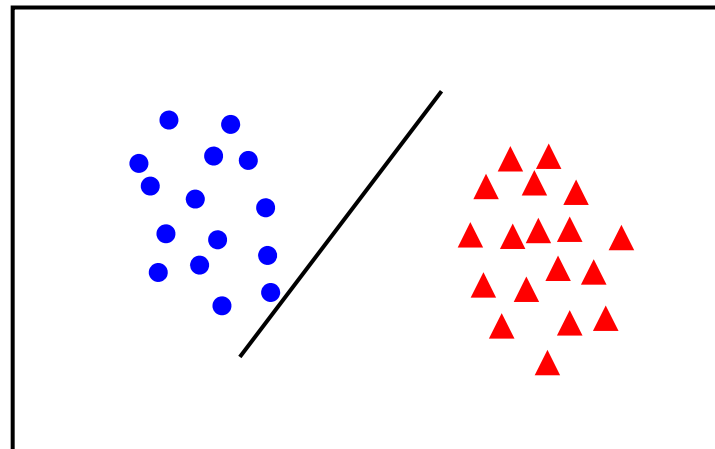
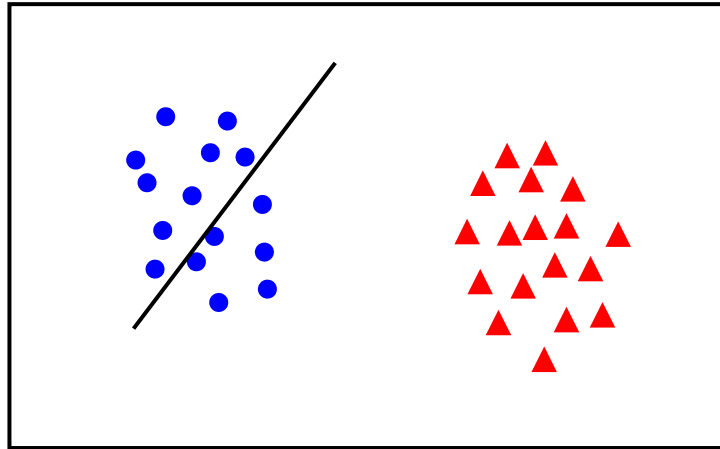
A linear classifier has the form

$$f(\mathbf{x}) = \mathbf{w}^\top \mathbf{x} + b$$



- in 2D the discriminant is a line
- \mathbf{W} is the **normal** to the line, and b the **bias**
- \mathbf{W} is known as the **weight vector**

What is the best w ?



- **maximum margin** solution: most stable under perturbations of the inputs

Support Vector Machine

linearly separable data

