Quant II

Lab 11: Interference

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Outline

- Interference
 - Interference with known structure
 - General interference
 - Random network
- Contagion

- One of the pioneering works in this field is Manski (1993).
- A linear-in-means model:

$$Y_i = \alpha + \beta \frac{\sum_{j \in P} Y_j}{n_i} + \gamma X_i + \delta \frac{\sum_{j \in P} X_j}{n_i} + \varepsilon_i.$$

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- ullet In addition, $arepsilon_i$ may not be independent to each other due to homophily.
- Many econometric works are based on this framework (e.g. Bramoullé et al., 2009; Graham, 2014).
- The model can be arbitrarily complicated: dynamics, spatial autoregression, network formation, etc.

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- The outcome-based approach provides a conceptual benchmark.
- When the treatment of others matters: interference.
- When the outcome of others matters: contagion.
- Homophily is often an important source of confounding.
- Challenge: how could we ensure the correctness of the outcome model?

- The outcome-based approach provides a conceptual benchmark.
- When the treatment of others matters: interference.
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- Homophily is often an important source of confounding.
- Challenge: how could we ensure the correctness of the outcome model?
- We can defend the model via structural approaches.
- Or we can switch to the design-based perspective.

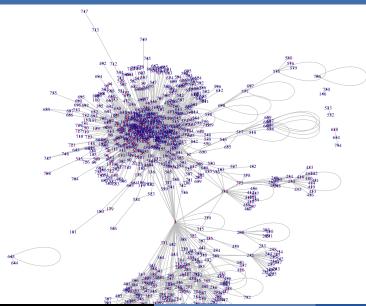
- We assume that the treatment is randomly assigned.
- We possess the knowledge of the "social network" among individuals.
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- Partial interference: all units in the same stratum are connected, but no connection between strata.
- Aronow and Samii (2017): with the network we can construct "exposure mapping."
- The network is actually a moderator: $D_i \mapsto W_i$.

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- The network allows us to draw the DAG.
- Then everything is identifiable.
- van de Laan (2014) and Ogburn et al. (2018): a general framework to deal with spillover effects in dynamic social networks.
- The more challenging part is inference.
- We cannot assume that everyone is connected to everyone else.
- Then there is only one observation, N = 1.
- We have to assume that the spillover is somehow "local."



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```
## dir_ind1 isol_dir ind1
## 2437.561 -1128.116 2717.595
## dir_ind1 isol_dir ind1
## 65653393 3837374 24041666
```

- But knowing the network is often a very strong assumption.
- Egami (2019): sensitivity analysis for the network's misspecification.
- Recent works proceed under the framework of "general interference."
- There are two questions we are interested in:
 - Is it still possible to estimate the ATE?
 - How can we estimate the interference effect?

- For the first question, the answer is yes under some conditions (Aronow, Hudgen and Savje, 2019; Chin, 2017).
- We require the average "perturbation" from changing the treatment status of one unit to be small.
- Notice that the ATE is no longer well-defined, so the limit is actually EATE:

$$\tau^* = \frac{1}{N} \sum_{i=1}^{N} \tau_i = \frac{1}{N} \sum_{i=1}^{N} \left[Y_i(1, \mathbf{Z}_{-i}) - Y_i(0, \mathbf{Z}_{-i}) \right]$$

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- For the second question, there is rapid progress in recent years.
- Aronow, Samii and Wang (2020): As the design is known, we can aggregate the individualistic effects in arbitrary ways.
- In spatial experiments, it is natural to do it by distance.
- Just draw circles at each distance *d* and apply the IPW estimator.
- Inference relies on Stein's method.

- Wang (2020): the same idea works in TSCS dataset under the assumption of sequential ignorability.
- Researchers have to trade off two sources of confounding: fixed effects vs. interference.
- Papadogeorgou et al. (2020): modeling treatment point process as a stochastic intervention strategy.
- They examine the effect of airstrike in Iraq on rebellions.

Within-unit interference

- Interference is also a big problem in TSCS data analysis.
- It is not surprising that the treatment in period t-1 affects the outcome in period t.
- Then the assumption behind the two-way fixed effects model will be violated (no carryover).
- What can we do?

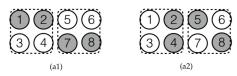
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- What can we do?
- If we are fine with abandoning the unit fixed effects: just estimate a MSM.
- Or we have to add more variables into the regression and hope the model is correct.
- A special case is staggered adoption (Strezhnev, 2019; Liu, Wang and Xu, 2020).

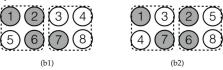
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- All these approaches assume that there is a fixed network and the intervention is at random.
- Another possibility is that the assignment is pre-specified but the network is randomly generated.
- Li et al. (2019)



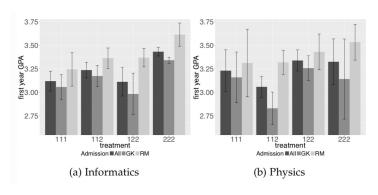
(a) The first type of interference with a fixed network and random external interventions. (a1) and (a2) are two possible realizations of random external interventions (colors of the units).



(b) The second type of interference with fixed attributes of all units and a random network. (b1) and (b2) are two possible realizations of random networks (dashed circles).

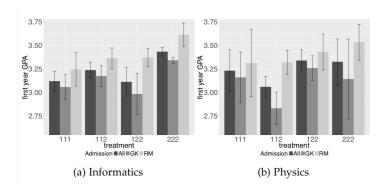
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- Does living with IMO medalists boost your GPA?
- Notice that this is interference not contagion.
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- Does living with IMO medalists boost your GPA?
- Notice that this is interference not contagion.
- A design-based approach to understand peer effect in dorms.
- Two assumption on "local interference:"
 - Partial interference
 - Only attributes matter, not identities
- They propose a Horvitz-Thompson estimator, and prove that it is equivalent to a regression with interaction.



• They also discuss the optimal assignment.

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- Let champions play with champions...

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Network formation

- A relevant question is whether interference affects the network's structure.
- There is a large literature on network formation in social network analysis.
- A familiar approach is to fit a two-way fixed effects model:

$$Y_{ij} = \mu + \alpha_i + \zeta_j + \beta X_{ij} + \varepsilon_{ij}$$

- You can further add the time dimension into the model.
- No design-based approaches yet.

• The peril of peer effects (Angrist, 2011)

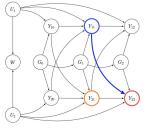
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- Imai and Jiang (2020) presents it in a meadiatio framework



	C	C^{P}	Placebo Test
No Bias	Y_{21}, U_2, G_2	$Y_{20}, Y_{10}, U_2, G_2, G_1$	Accept
Contextual Confounding	Y_{21}, U_2	Y_{20}, Y_{10}, U_2	Reject
Homophily Bias	Y_{21}, G_2, G_1	$Y_{20}, Y_{10}, G_2, G_1, G_0$	Reject
Both	Y_{21}, Y_{20}	Y_{20}, Y_{10}	Reject

(a) Example of Placebo Test

(b) Control and Placebo Sets

Suggested Readings

- For an overview of the interference lecture: Aronow, Peter; Dean Eckles, Cyrus Samii & Stephanie Zonszein. (2020). "Spillover Effects in Experimental Data." In James Druckman & Donald Green, Eds. Advances in Experimental Political Science. Cambridge: Cambridge University Press
- also its reference.